

# Particle nature of EM radiation

- Planck's constant:  $h$

The units of  $h$  are units of angular momentum.

$$E_\gamma = h\nu$$

Units of  $h$ :

$$[h] = \frac{[E]}{[\nu]} = \frac{[ML^2T^{-2}]}{[T^{-1}]} = [ML^2T^{-1}]$$

$$[h] = \underset{\uparrow}{L} \cdot \underset{\uparrow}{[MLT^{-1}]} = [r] \cdot [p] = \underset{\uparrow}{[L]}$$

Length      Momentum

Angular momentum

**Example:**

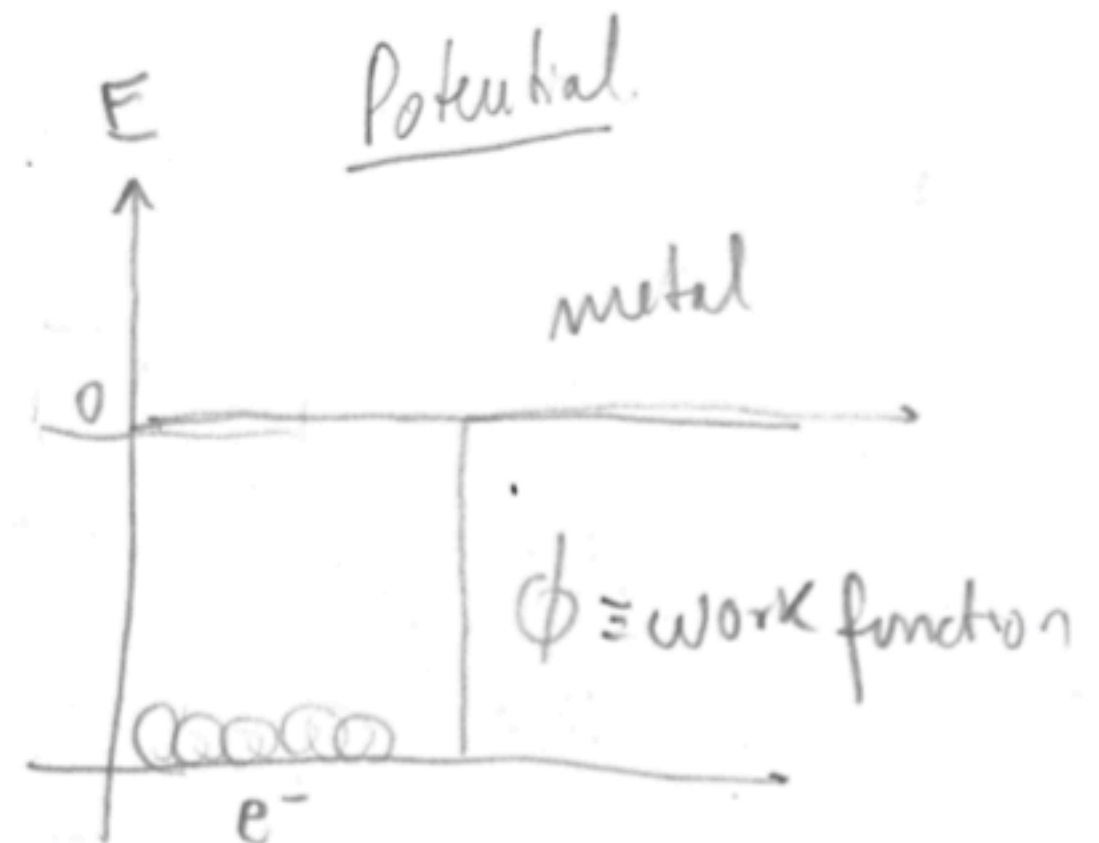
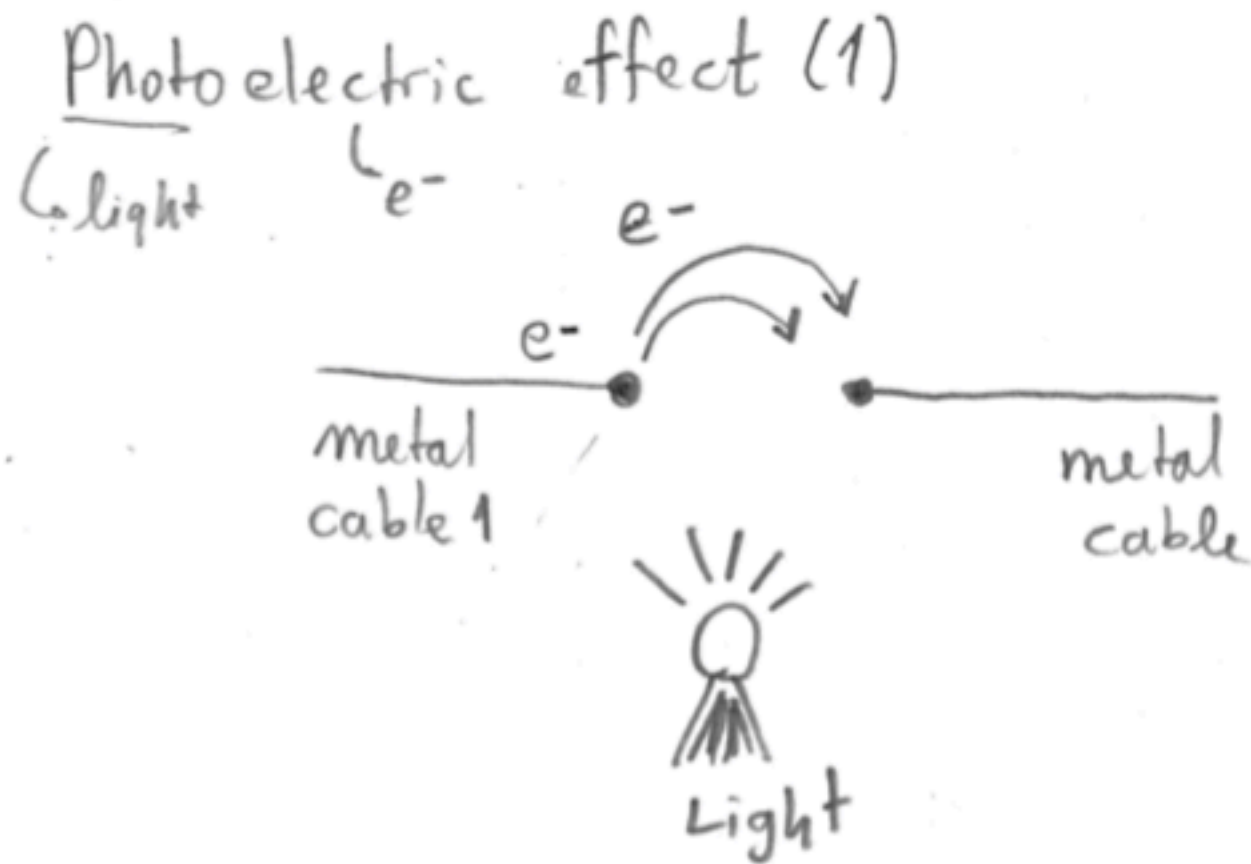
Spin 1/2 particle

$$|\vec{S}| = \frac{1}{2} \hbar$$

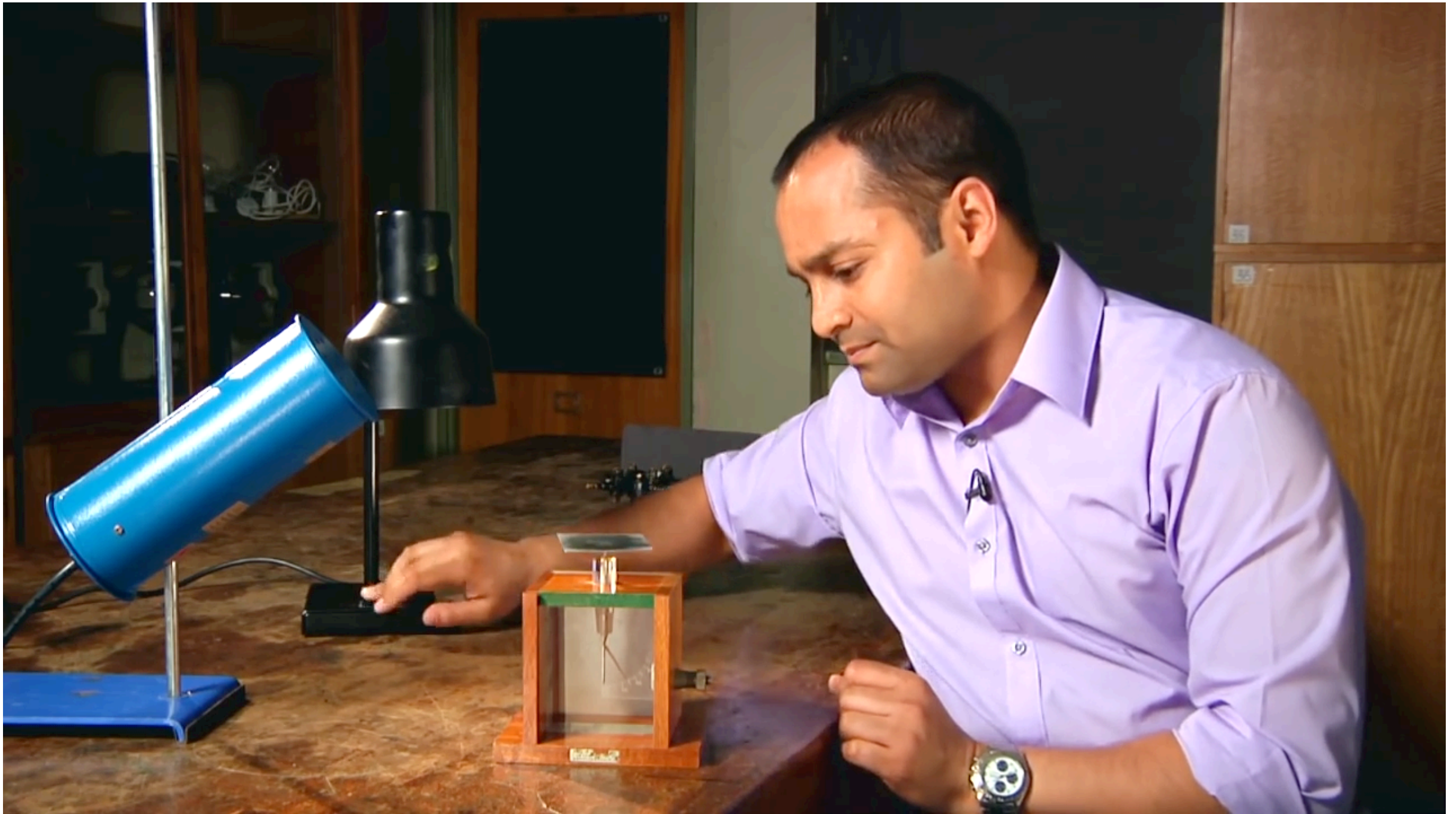
# The Photoelectric Effect

It is a process by which  $e^-$  can be removed from a metal surface.

- **1887** - H. Hertz discovers the Photoelectric Effect by irradiating metal plates with light.
- Irradiated polished plates emit  $e^-$  called photo-electrons.



# The Photoelectric Effect

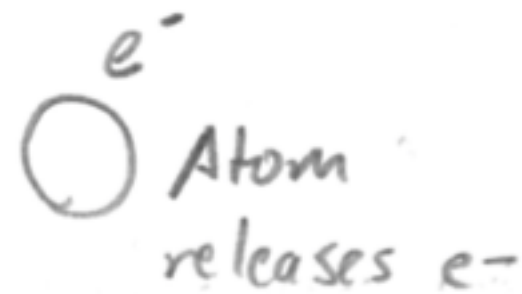


Video: <https://www.youtube.com/watch?v=v-1zjdUTu0o>

# The Photoelectric Effect

- **Why does the photoelectric effect occurs?**

Classical (wave)  
view:



$\Rightarrow$  Should happen  
for all  $\lambda$   
any

- **Did experiments agree? No.**

Photoelectric effect occurs:

Only for some  $\lambda$   
For other  $\lambda \rightarrow$  no  $e^-$  jump

# The Photoelectric Effect

- **Einsteins' view:** photons come in packets of energy.

Einstein: Beam of light  $\nu$

Photons  $\gamma$   $E_\gamma = h\nu$

$h \equiv$  Planck's constant  $= 6.63 \times 10^{-34} \text{ J}\cdot\text{s}$

$$E_\gamma = h \frac{c}{\lambda} = \frac{2\pi\hbar c}{\lambda}$$

$$\hbar = \frac{h}{2\pi}$$

$$\text{fm} = 10^{-15} \text{ m}$$

$$\hbar c = 200 \text{ MeV}\cdot\text{fm} \rightarrow \text{fermi}$$

$$\hbar c = (197.33)$$

- **Einsteins' prediction:**

$$E_{e^-} = \frac{1}{2}mv^2 = E_\gamma - \phi = h\nu - \phi \quad \left. \vphantom{E_{e^-} = \frac{1}{2}mv^2 = E_\gamma - \phi = h\nu - \phi} \right\} \text{Einstein's prediction}$$

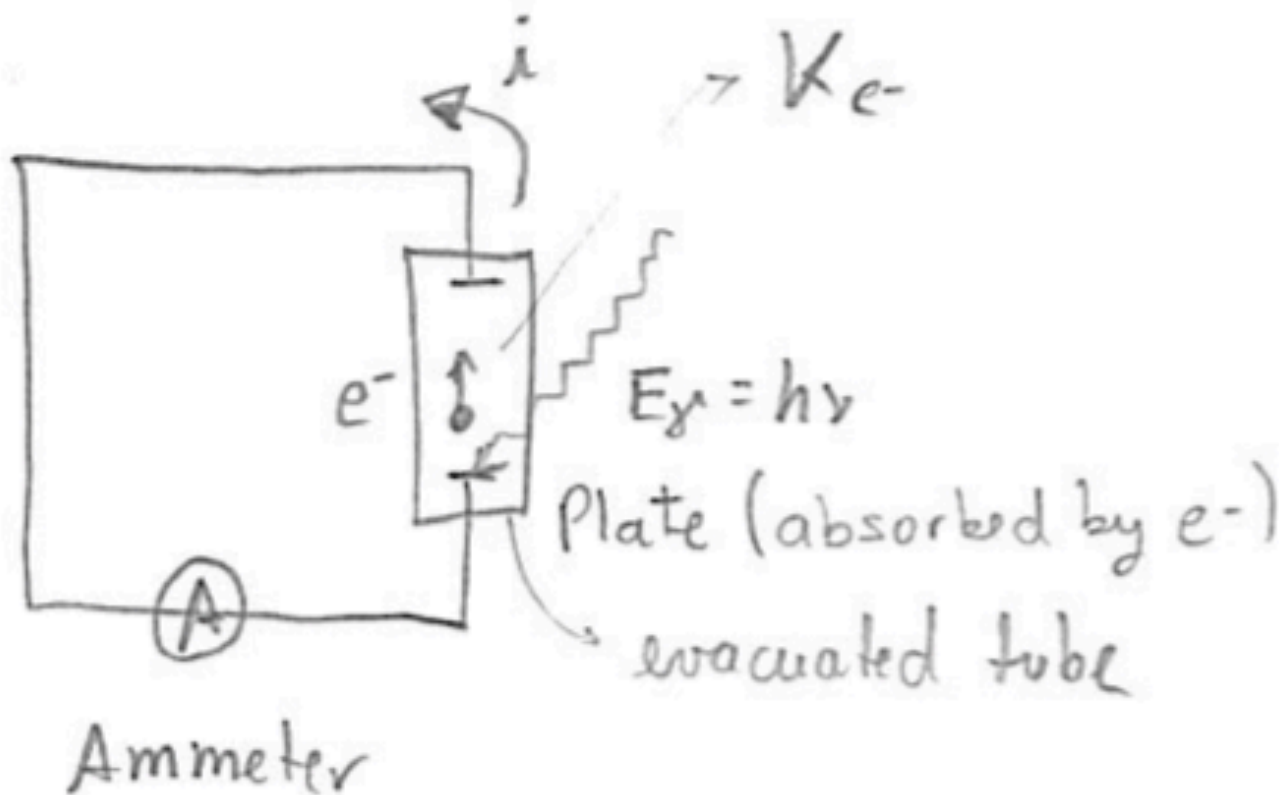
$\underbrace{\hspace{1cm}}$     $\underbrace{\hspace{1cm}}$     $\underbrace{\hspace{1cm}}$   
 Leftover    $E$  given    $E$  needed  
 energy   to  $e^-$    to liberate  $e^-$



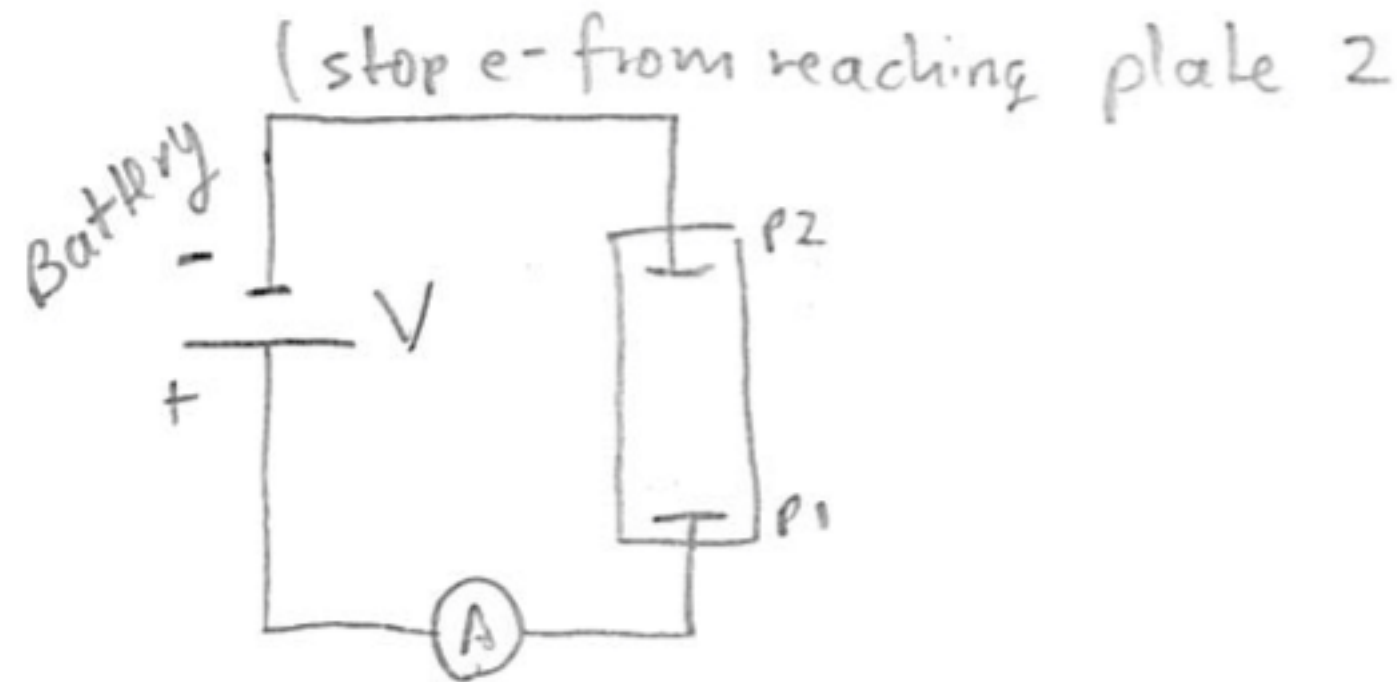
# The Photoelectric Effect

- **1915** - Millikan's experiment:

**Instance 1** (no battery)



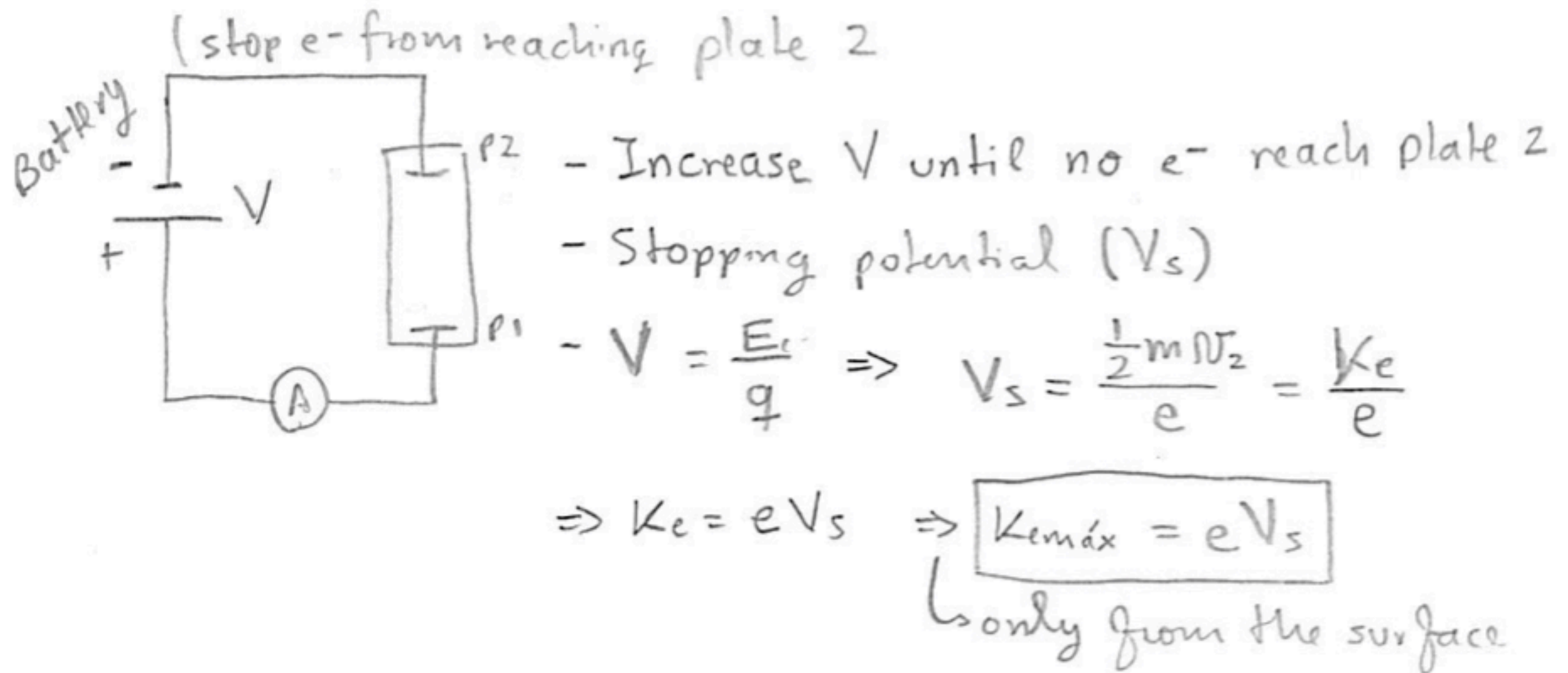
**Instance 2** (battery added)



- There is a threshold frequency above which there is electric current.
- Energy to remove  $e^-$  from the metal plates depends on the metal, crystalline structure on the surface of the plates.

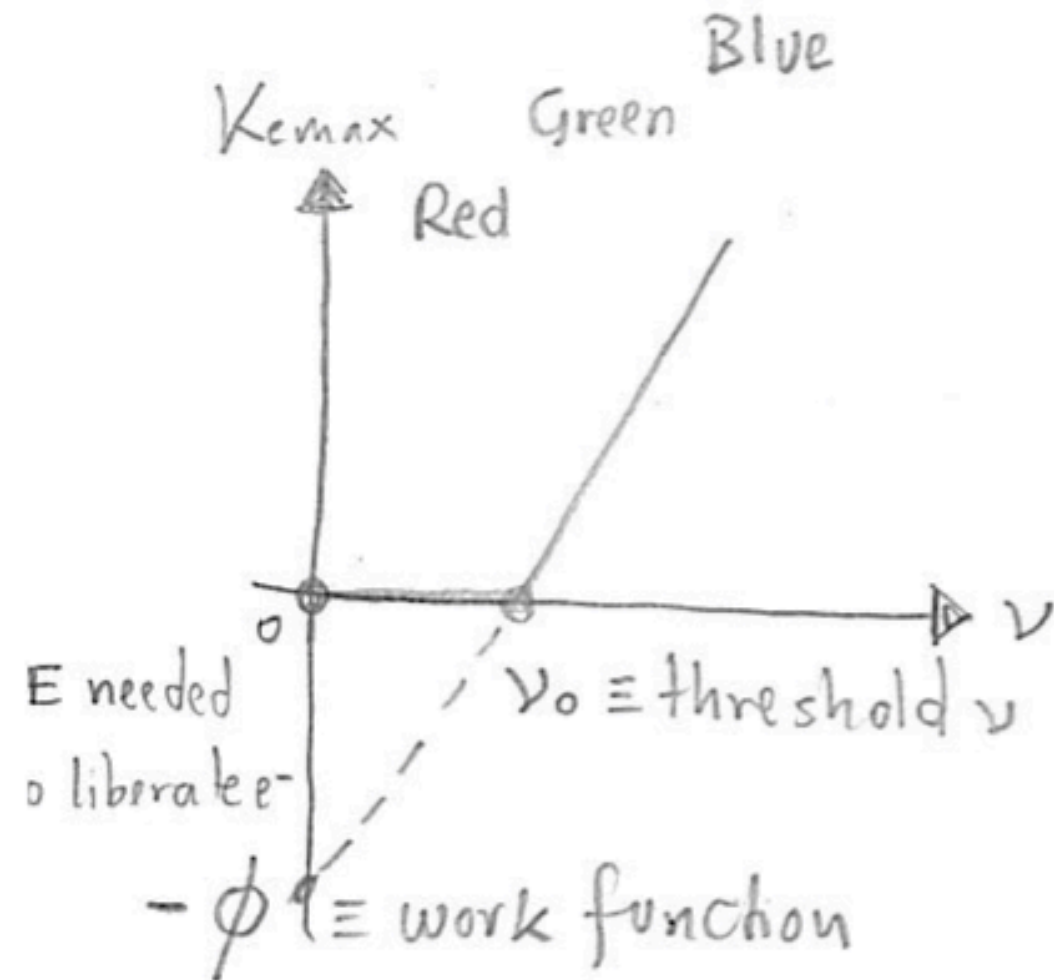
# The Photoelectric Effect

- **1915** - Millikan's experiment:



# The Photoelectric Effect

- 1915 - Millikan's experiment:



$$E_{e^-} = \frac{1}{2}mv^2 = E_{\gamma} - \phi = h\nu - \phi \quad \left. \begin{array}{l} \text{Einstein's} \\ \text{prediction} \end{array} \right\}$$

$$\Rightarrow \underbrace{K_{\max}}_{\text{Leftover energy for } e^- \text{ after liberation}} = \underbrace{h\nu}_{\text{E given to } e^- \text{ by } \gamma} - \underbrace{\phi}_{\text{E needed to liberate } e^-}$$

$$0 = h\nu_0 - \phi$$

$$\nu_0 = \frac{\phi}{h}$$

$$\Rightarrow \boxed{\phi = \nu_0 h}$$

$$\boxed{K_{\max} = h(\nu - \nu_0)}$$

- Higher Intensity
- More  $\gamma$  do not  $\uparrow K_{\max}$
  - 1  $\gamma$  absorbed by 1  $e^-$
  - Light exists as quanta



# The Photoelectric Effect

- **1915** - Millikan's experiment conclusions:

- Millikan (1915) verifies Einstein's prediction.

-  $h$  is measured to better than 1% of its currently accepted value

$h$  is the slope of this linear eq:

$$K_{e\max} = h\nu - \phi$$

- Magnitude of the current (# of photo-e-) is proportional to light intensity.
- Energy of photo-e- is independent of light intensity
- Energy of photo-e- increases linearly with the frequency of the light.

**It is NOT easy to understand the above with waves.**

# Light duality

- **1905** - Einstein proposes light's wave/particle duality.  
Light is made of wave-packets, bundles of energy.  
Did not say explicitly that light is a particle.  
It comes in discrete packets of energy -> **photons**  
(Lewis proposes the name photon in the 1920s)

## Discovery of photons

- **Properties of photons:**
  - Photons are packets of energy.
  - Photons are the smallest pieces of light.
  - Energy = constant times a colour.
  - Charge = 0, Rest mass = 0, Spin = 1 (Right and Left)
  - Light speed  $c$ ,  $E=pc$ , inability of experience time-space