# Garden of Eden

William B. Jackson

February 5, 2014

# 1 Abstract

Garden of Eden is an exercise in procedural generation of lifelike worlds. It randomly generates a forest scene of realistically shaped and proportioned asymmetric trees on top of a basic topographical map. This map is then rendered in 3D, with support for user navigation. The end result of this project is a sort of game, though without any goal, narrative, or creative purpose. It is simply a static rendering of a natural environment, open for exploration, closed to manipulation exploring how users find visual pleasure and meaning in virtual environments. The passive interaction of the user is vital to this simulation, as it reflects how one would observe a natural environment; by forcing the user into the same perspective from which they view actual natural environments, Garden of Eden explores the concept of natural, the distinction between real and virtual, and the user's sense of place. All packages are offered open source, with detailed documentation, for users wishing to create their own arboreal experience.

# 2 Related Work

A significant body of work relating to natural feature generation exists in the video game industry. Minecraft[12], for example, uses advanced terrain and feature generation techniques to procedurally create such natural features as mountain ranges, cave systems, chasms, coasts, and flora biomes, as well as artifical features such as temples, villages, and mine shafts. It achieves truely impressive scenes using simplified graphics, resulting in a stylised look rather than striving for verisimillitude. Another game worth mentioning in this context is Proteus[7], a small-scale "game of audio-visual exploration and discovery" that allows users to explore a highly-stylized generated island. There are many other games that use feature generation techniques, either as the creative force of the game world or to fill in between created features; I mention these two primarily because, through both gameplay and simple, yet awesome, natural scenery, they served as inspiration for this project.

The father of fractals, ? ] proposed using fractal Brownian Montion, a function that uses concepts from brownian motion with a degree of randomness and fractal constants to produce a natural terrain floor.

? ] uses manual seeding of feature curves combined with the diffusion equation to generate feature-based, eroded terrain in a single step. The algorithm propsed requires more manual input than the midpoint displacement algorithm used, and is thus less desirable for the purposes of Garden of Eden. A similar algorithm could be implemented, however, that randomly places feature curves to achieve a more striking, feature-based landscape.

(author?) [2] discusses detailed visual aspects of tree generation, specifically the maple tree, assuming a realistic skeleton is available. Thus, he mostly describes some of the finer visual details in modeling trees, such as branch continuity and bark texture modeling. Some of his methods have been considered as extensions, though the nature of his work was detailed enough to be out of scope to the current project.

? ] draws from an array of previous work to develop a sophisticated and well-researched model for the visual depiction of trees. His paper displayed the variability of the model with pictures of trees of several species. This accuracy was a combination of modeling a large number of growth affectors as well as

extensive research and observation of trees to obtain a reliable set of constants, many of which I will use in the parameter variation ranomization section.

# 3 Terrain

# 3.1 Midpoint Displacement

The classic method of generating terrain maps is by using a fractal Brownian Motion function[?]. The function is fairly complex in theory; it can be approximated, however, with an algorithm called the midpoint displacement algorithm. The midpoint displacement algorithm, also known as the diamond-square algorithm, is an easy way to generate surface height maps for terrain. the algorithm is as follows[8]:

```
Loop while quadrilateral side is at least 1

// Square step
For each discrete square of given quadrilateral side length
    Get midpoint of square
    Calculate random offset as a random number in a specified range times a scale
    Midpoint becomes average of square's corners plus random offset

// Diamond step
For each discrete diamond defined by the square step's calculated midpoints
    Get midpoint of diamond
    Calculate random offset as a random number in a specified range times a scale
    Midpoint becomes average of diamond's corners plus random offset

Decrease scale by a constant fraction
Half quadrilateral side
```

The algorithm is works well to generate fractal surfaces, and allows for a decent amount of control over the percieved "roughness" of the resultant surface in how one defines the scale factor. However, it is fairly slow, and there are also well-documented artifacts, notably for steeper surfaces. These factors can be mitigated somewhat with careful selection of constants, discussed below.

### 3.2 Feature Extraction

### 3.3 Gaussian Filter

# 4 Trees

# 4.1 L-Systems

An L-System, as defined in [14] describes a recursive substitution system to build increasingly complex strings. A system consists of an initial value or set of values, and a series of rules used to recursively replace sections of the initial set. The set consists of productions, or operations that, when combined with a rule, represent a certain kind of predictable growth. Productions can, for example, represent a single branching structure, or trunk growth. As such, L-Systems are an excellent way to represent the growth of trees, as they give a simple "seed" rules by which it can branch in a biologically feasable way into a much larger system. As L-Systems consist of self-replacement rules, they tend to form fractal systems, which are "self-similar" at different levels of detail. In an L-System, this self-similarity at smaller levels of detail comes from the recursion depth, which replaces productions at small levels with smaller versions of the designs seen at a larger scale.

#### 4.1.1 Productions

A production defines a particular recursive structure. In combination with its replacement rule, it acts similarly to a replacement function; a single production can be replaced by a set of other productions, including itself, leading to interesting fractal shapes. In this project, a production does not represent any physical shape, and is not drawn graphically; instead, it's replacement rule can contain graphical information, allowing a production to represent a specific physical occurance. A production can, for example, represent a bijunction branching, or a bending of a branch due to biological influences, or the thickening of the trunk due to age.

### 4.1.2 Parametric L-Systems

A parametric L-System contains parametric productions, or, more simply, producitons that take parameters. Production rules change to accomidate parameter logic, matching, for example, only if a production has a "time" greater than 5. In this way, productions representing specific growth actions can have significantly different geometry while still having the same basic structure. A branch production, for example, might take an angle parameter, which would make larger branches diverge less dramatically than twigs.

The below L-System can serve as an example, and is used as the L-System module's tester in ./test/lsys\\_console.html.

```
\begin{array}{llll} \omega & : \ \mathsf{B(2)A(4,4)} \\ p_1 & : \ \mathsf{A(x,y)} & : \ y \ \leq \ 3 \ \to \ \mathsf{A(x*2, x+y)} \\ p_2 & : \ \mathsf{A(x,y)} & : \ y \ > \ 3 \ \to \ \mathsf{B(x)A(x/y, 0)} \\ p_3 & : \ \mathsf{B(x)} & : \ x \ < \ 1 \ \to \ \mathsf{C} \\ p_4 & : \ \mathsf{B(x)} & : \ x \ \geq \ 1 \ \to \ \mathsf{B(x-1)} \end{array}
```

In this example,  $\omega$  gives the initial productions with parametric values. The rules have changed both to check the values of the parameters, and replace accordingly, and to modify the parameters in the replacement step. In this way, the productions will have different parameters at each level of recursion, reflecting changing growth at more depth.

#### 4.1.3 Turtle Graphics

As stated before, productions give no graphical information as to how a tree is drawn. Thus, in addition to productions, an L-System must implement a system of graphical information. In order to create branching structures, LOGO-style turtle graphics are used to draw on the HTML5 canvas. Invented as a simple graphics drawer for educational purposes, turtle graphics consist of a set of commands that direct the movement of a "turtle", or a drawing point. In 3D space, three dimensions of orientation are controlled by issuing commands with a specified radial change; drawing occurs by moving the turtle forward. The turtle commands implemented are as follows:

The above commands are included in production replacement rules, and basically define what a production draws. In this way, a production might be used not just to define where a branch or other such growth action occurs, but also to draw the branch upon its replacement with turtle graphics commands. The amount of turtle graphics commands required to draw an appropriately detailed tree is incredibly large; the exact "turtle string", or set of commands, used to draw one tree is printed to the console in ./test/tree.html.

# 4.2 Biological Considerations

As with most graphical projects, the generation of trees must strike a balance between emulating actual biological methods and using efficient computational design. In this section, I will discuss some of the biological phenomenon modeled in the creation of trees, how they were modeled, and the effect that they have on tree growth.

Command	Symbol	Argument	Description
_F	F	time	Moves turtle forward by specified time value
			(turtle rate is constant), drawing a line (a
			cylinder primitive) from its previous location
			to its new one.
_f	f	time	Moves turtle forward by specified time value,
			drawing no line between positions.
_pitch	&	radians	Rotate turtle about its own x-axis by specified
			amount of radians.
_yaw	+	radians	Rotate turtle about its own y-axis by specified
			amount of radians.
_roll	/	radians	Rotate turtle about its own z-axis by specified
			amount of radians.
_set	!	width	Sets the drawn line (3D cylinder) to the spec-
			ified width (diameter).
_push	[	none	Pushes current turtle position and orientation
			into a stack of previous states.
_pop	]	none	Pops current turtle position and orientation
			from a stack of previous states, resetting its
			current state to the new one.

Table 1: Turtle Commands

## 4.2.1 Discussion of Assumptions

Some assumptions were made to simplify and speed up the generation of tree structures:

- 1. All branches are straight. In reality, a tree branch is frequently curved, often noticeably. However, this project uses straight branches exclusively, as it allows for the rendering of a branch with a single, simple, cylindrical primitive. Future work could use warped line segments to represent a branch, extruded to a width specified by the turtle.
- 2. All trees in this project are of a similar age, growing at a similar speed. In a real forest, the actual ages of the trees tend to vary, even while the "age of the forest" grows roughly together. Furthermore, due to a multitude of growth factors, trees of similar age might grow at drastically different speeds. The end result is that in a real forest, trees might be noticeably different in size. This project will not seek to emulate that, though it will result in a fairly noticeable visual artefact. Future extensions to the Forest module might consider tree age in the planting and growth steps.
- 3. "Twigs", or branches of an arbitrarily small size, are not to be rendered. While this is possible for users of the software package, as it involves merely increasing the depth to which the L-System is run, it results in an exponentially larger amount of primitives and a noticeably laggier simulation.
- 4. In this project, to limit the number of specific L-Systems that must be constructed, only a single, archetypal tree species will be constructed. An extension where multiple species are generated is discussed at the end.
- 5. Trees in nature show allometric growth with regards to the ratio of trunk diameter to tree height[3]. This effect is seen over many years; extremely old trees are often notably fat, a result of increasing trunk diameter growth relative to height growth. This project, however, will maintain a constant ratio of trunk width growth to height growth. Such isometric growth is a fair approximation for most younger trees, and simplifies the growth calculation.

### 4.2.2 Bijunctions

A cursory glance out the window will reveal that the vast majority of branching junctions split the root branch into two smaller branches. The reasons for this will not be discussed in this paper, however, for visual integrity, this rule will be maintained. A *branching junction* here is defined as any place, usually represented in the L-System as a single production, where a single branch divides and deviates into a set of smaller child branches. Such a junction that splits into exactly two smaller branches will be defined as a *bijunction*.

The included L-System TernaryTree uses a single branching junction, modeled with the production A(), to represent a *trijunction*, defined as a branching junction that splits into exactly three children[14]. There are benefits to using trijunctions. A trijunction is the smallest possible branching junction that fills a volumetric space, where a bijunction instead is isolated to a single plane. Thus, trijunctions rapidly result in a "fuller" looking tree, where bijunctions frequently have the effect of looking planar, or "flat". Trijunctions also allow the branch count to grow cubically, thus requiring shallower recursion to "fill out" a decent-looking tree. This allows for more flexibility in tree appearance: as the L-System used for TernaryTree and RandomTree grows the size of the tree while constructing branches, a tree with trijunctions will appear more detailed at a smaller sizes.

Thus, careful consideration must be taken to "filling out" a bijunction-exclusive tree. One approach is to use *pseudo-trijunctions*, a branching junction consisting of two stacked bijunctions. These junctions, where a single branch will split off immediately before a branch fork, are fairly common in nature, and allow for trijunction behavior without violating the bijunction rule. For further discussion of the methods used to fill out a bijunction tree, see the below section on Probabilistic L-Systems.

# 4.2.3 Growth Density

A commonly measured property of forests are the density of tree growth. As larger trees tend to block sunlight from trees growing beneath them, in general, the older a forest is, the further spaced its trees. Furthermore, as there is a "sweet spot" of growth away from an older tree where light isn't blocked and roots aren't in conflict over nutrients in the soil, trees, especially of a similar age, tend to be spaced fairly evenly. To reflect this, many system models of forests break the area up into a grid of forest "patches", with the side of the grid roughly corresponding to the size of the oldest tree's canopy[?]. This is because a largest tree in the patch, called a *canopy tree*, consumes most of the light and nutrient resources of the patch. To be sure, other, smaller trees might grow in the same patch, but they must compete directly with the more dominant tree.

# 4.3 Randomization

In nature, the growth and configuration of trees is a result of both biology and environment, and modeling tree geometry should consider their affects. This paper will not seek to exactly model the growth details, though it will consider some of them in the design of randomization algorithms. For this paper, it is sufficient to say that some growth factors are internal to the tree's genetics, information physically encoded and manifesting in commonalities between trees of the same species, whereas some are external to the tree, resulting in commonalities between trees of different species in the same growth conditions[15]. Internal information is reasonably represented by the L-System, which specifies deterministic growth patterns for a specific tree. Taken alone, other influence, trees generated by a single L-System display little variation, to the point of being identical. I suggest that the codified rules of L-Systems be considered a heuristic for genetic patters of tree growth.

The tree's local environment also plays a large hand in growth and configuration. As described in the above section, such factors external to the tree as Tropism, Growth Density, and Elevation affect the presence of trees, the rate of growth, branching, and the general tendency to grow in a specific direction. Weather can affect the tree, too: heavy snow might bow a mighty branch, or a bolt of lightning might split a trunk. Temperature patterns can affect the growth in subtle ways, as well.

The process described below are an imitation of the above factors, seeking to replicate with selective randomness what a perfectly deterministic, physical system would otherwise be able to reproduce. To the degree that they are based on actual growth and environmental factors, they will be justified; many, however, are simply heuristic hacks that result in a realistic geometry.

#### 4.3.1 Parameter variation

The L-System described by TernaryTree uses fixed constants for growth and branch diversion to achieve a realistic, but static, tree. RandomTree addresses this problem in part by variation of parameters[14]. This method involves finding appropriate ranges for the defined constants in the L-System and randomly adjusting them at each replacement step. Thus the majority of the work in this step is finding acceptable ranges for values.

A range of 20% is found to be good for growth constants. Thus, the branch elongation constant L\_R can be randomly assigned to within 20% of its value carried over from TernaryTree, or (0.856, 1.284). Similarly, as the tree is assumed to grow isometrically, the width growth constant V\_R is randomly assigned to within 20% of its initial value, or (1.3856, 2.0784).

### 4.3.2 Probabilistic L-Systems

Thus far, L-Systems depicted have had replacement rules that match evenly to all of the productions defined. This results in static branching structure, as the geometry is deterministic and limited in configuration. However, using a Rule's condition parameter, productions can be replaced randomly with one of a set of options. The condition parameter could, for example, switch the branching style as recursion depth increases, leading to a different configuration for branches than what is used for the trunk.

Using a provided random value from Javascript's built-in Math.random(), condition can also be replaced probabilistically. This can be used to represent several styles of branching. For example, while trees only ever bijunct, trijunction-like branches can occur by closely stacking bijunctions. This style of branching can thus be interspersed randomly with the usual bijunction style.

The L-System used to create the trees in Garden of Eden use this style of probabilistic branching. The branching production, 'A', can be any of the following styles:

- Normal bijunction: Branch continues along current vector, with another branch splitting off at a small acute angle.
- Fork bijunction: Branch splits into two, with both diverging at a small acute angle from the previous vector.
- Pseudo-trijunction: One branch from a fork trijunction is moved down the parent branch, resulting in a normal bijunction stacked below a fork bijunction. See figure 1.

# 4.3.3 Density Management

To manage the spacing of trees in the generated forest, forest system models will be adapted, with some extra logic to make them appropriate for a visual output. As discussed above, forest gap models break forests up into tree grids, corresponding roughly to the area of affect of the canopy trees[?]. The grids operate under a set of assumptions[3], some which must be reconsidered for a visual output:

- 1. The forest is abstracted as a composite of many small patches of land, where each can have a different age and successional stage.
- 2. Patches are horizontally homogeneous, meaning the tree position within a patch is not considered.
- 3. The leaves of each tree are located in an indefinitely thin layer at the top of the stem.
- 4. There are no interaction between patches.

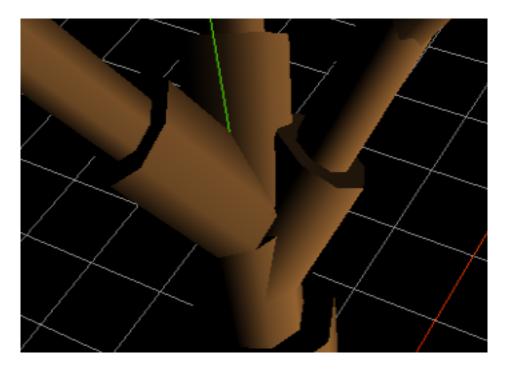


Figure 1: The result of a pseudo-trijunction production

Obviously, assumption #2 must be violated for a visual output: horizontal position in the patch is exactly what we do care about when attempting to manage the density of the forest. As the position of trees in the patch doesn't matter, we can conclude that the position of the canopy trees in the patch doesn't matter, and can be assigned randomly. Furthermore, I will make the assumption that only a single tree in each patch is canopy-tree-sized. Assumption #4 suggests a few problems in the system, which will be addressed at the end of the section.

Thus, we begin the algorithm by following assumption #1, dividing the terrain area up into patches. The size of these patches is the subject of disagreement, ranging from the order of  $10m^2$ [?] to  $1km^2$ [3]. I will assume that the former is true: the size of a patch is dictated by the canopy size of the canopy trees. This size is dictated by size and height of a tree, which is roughly correlated with the age of the tree. The L-System used to generate the trees in this project uses recursion depth as a rough stand-in for tree age; thus, the value assigned as the max recursion depth will be used to dictate the size of a patch. We can use this value, along with maximal values for branch length and branching angle, to set an upper bound on the size of the canopy. The equation governing the maximum canopy size is:

$$\max_{\alpha} = 2DL \sin(\alpha)$$

Where D is the maximum recursion depth of the L-System, L is the maximum length of a branch, and  $\alpha$  is the maximum branching angle. I will assume that the root system of the tree behaves similarly to the branch system, allowing the canopy to singly govern the size of the patch. Thus, the algorithm will begin by dividing the terrain into patches of size  $\max_{\text{canopy}}$ . Following my discussion of assumption #2, a tree which will be rendered to maximum depth, thus making it a canopy tree, will be placed randomly in each patch. From here, smaller trees could be seeded; this will be discussed in the section on extensions. This implementation allows the details of forest generation, specifically any constants relating to how the forest is created, to be dictated entirely by the trees used in the forest, which prevents the user from having to supply additional detail about forest construction and allows for a very clean implementation of the Forest module.

A major problem with this algorithm is suggested by assumption #4: there is nothing preventing two trees from existing close to their shared border, thus growing unrealistically close together, or even colliding. A possible solution to this bug will be discussed in the aforementioned section on extensions; for now, however, I leave this visual error up to chance.

# 5 Implementation

# 5.1 Top Level

Garden of Eden requires a decent amount of set up, especially for the use of Three.js, the details of which will not be included in this document. A skybox is set up (find citation!!), providing the user with a realistic backdrop. The modules are then called; first, the terrain is constructed and then generated. The L-System object, predefined in lsys\_rules.js, is constructed, then used in turn to construct a Forest object. The Forest is then constructed, generating each of the trees using the provided L-System and adding their corresponding Three.js objects to the scene for rendering. The top level also sets up pointer lock controls, allowing the user standard FPS controls, as well as a downward-facing raycaster used for floor detecting and camera height maintenance.

# 5.2 Terrain Implementation

The terrain algorithm begins by calling the build() method, which uses the midpoint displacement algorithm to generate a height map. It then runs this height map through a Gaussian filter in order to smooth out the low-amplitude, high-frequency terrain noise that would be a nuisance to the user. Then, it uses this data to construct a Three.js plane, which is then returned as the scene's floor.

# 5.3 terrain\_gen.js

- Terrain(size\_degree, resolution): The terrain constructor takes as argument size\_degree, a scalar exponent value that is used to determine the size of the terrain. The terrain generated is  $2^{size_degree} + 1$  units on each side, which ensures that the diamond-square algorithm can find even, perfect quadrilaterals on each iteration. The resolution, which defaults to 1, determines how many vertices per unit the terrain generates.
- build(): Initializes construction of the terrain, using built-in values for all parameters and returning a Three.js object representing the generated floor. Top-level function.
- mpd(): Midpoint displacement algorithm. Implemented as described, the method returns an array of arrays of float values representing the generated height at each vertex of the Three.js plane. Largely controlled by built-in constants; for more information, see section on terrain generation.
- smooth(): Uses a Gaussian filter to smooth out low-amplitude, high-frequency noise that would cause the user to jostle vertically as they moved around the map. The parameters of the actual filter are fixed.

## 5.4 Tree Implementation

The creation of a tree begins by creating a rule set for the L-System. A few of these are defined in ./js/app/lsys\_rules.js, which can be used as an example for users wishing to create their own L-Systems. This rule set is used to create an L-System object, which will be used to generate the tree's geometry. A turtle must also be constructed, and must be given a set of three.js objects in order to draw to the HTML5 canvas. Then, by calling the L-System object's build() method, the L-System will recursively construct a tree, storing it in its own property public variable. This is then passed into the turtle object's run() method, which will draw the constructed L-System as a single hierarchical object onto the HTML5 canvas.

#### 5.4.1 turtle\_graphics.js

The turtle graphics module consists of a turtle object, Turtle, a set of turtle commands to control drawing, and a run method, which, given a list of turtle commands, executes them in order from the current position.

- Turtle (scene, material, radius): Turtle object constructor. Creates the turtle drawer, initializing it at the world origin oriented in the +z direction. Turtle properties are as follows:
  - 1. rate: Defaults to 1. Rate at which turtle travels when moving forward, multiplied by the forward command's time parameter to get the total distance traveled.
  - 2. width: "Width" of the drawn line. Defaults to 0.25, can be passed in as an argument. Actual value is the radius of the cylinder primitive created by the turtle.
  - scene: Three.js scene. Must be passed in. Graphics drawn in run() are added to this as a single, hierarchical object.
  - 4. material: Three.js material. Must be passed in. Defines the material of the drawn cylinder lines.
- Turtle commands: The turtle commands (\_F(), \_f(), \_pitch(), \_yaw(), \_roll(), \_push(), \_pop(), and \_set()) are all methods that specify commands to some turtle object. To use, they are attached to a Turtle.Action object along with the value of their argument, and then passed as a list as the argument to run(). Each one specifies a action relative to the turtle drawer's current position and orientation. Details of the actions are given in table 1. In general, the rotation actions work by multiplying a specific rotation matrix to the turtle object's internal orientation matrix. The use of a rotation matrix allows for relative transforms, as opposed to Euler coordinates, which require specific ordering of rotations which can lead to errors. The forward movement controls drawing; it does this by creating a cylinder of the current width and given distance (the actual given is a time parameter, which is multiplied by the turtle's rate to get the cylinder's length) and moving it such that it begins at the turtle's starting position and is oriented in the same direction of the turtle. Then, the turtle's position is incremented by the given distance. \_push() and \_pop() save the turtle's state in a basic object and store or retrieve it from an internal stack.
- run(): The run commands executes a given turtle string. Looping through the string in order, it run's the function's built-in call() function, specifying this as the calling object and Turtle.Action.args as the arguments. This binds the current turtle object to the action, allowing the turtle command to affect the turtle object's internal variables.

#### 5.4.2 lsys.js

lsys.js gives the object used to describe and create an L-System of arbitrary productions and rule set. Relevant object, including LSystem.Production and LSystem.RuleSet, are defined, and the engine to run recursion to a specific depth is included in a method of the base LSystem object. The L-System requires both a rule set and an initial value to run, both of which are described below.

- LSystem: Object containing the L-System and it's rule set. The only argument is rule\_table, the rule set for the L-System.
- LSystem.Production: Object containing production information. Productions, with the added information of their rule sets, represent a specific type of growth, but are not actually drawn by the turtle graphics wrapper. Production arguments are as follows:
  - 1. id: ID of the production, similar to function name. For example, in the production A(1,4), the id is "A".

- 2. args: List of argument values. This is only assigned for initial values; the inject function is used to dynamically assign these values, as the resultant value is usually some function of the previous value, defined in the rule set.
- 3. inject\_args: Function used to dynamically assign arguments from within the rule set. Arguments after the replacement step are usually a function of their previous values; the width of branches, for example, might decrease by a constant scale at each level of branching. The function must take args, the previous production's arguments, and consts, a dictionary of constants defined in the rule set. It must then assign this.args to a list of the argument values.
- LSystem.RuleSet and LSystem.Rule: RuleSet and Rule are used to define the logic of the L-System. RuleSet describes the entire rule system, whereas Rule defines a single rule for a specific production and condition. The arguments for the RuleSet constructor are as follows:
  - 1. consts: Dictionary of defined constants, such as width reduction ratios, used in calculating the argument values at replacement.
  - 2. initial: Initial production list values for the system.
  - 3. rules: List of rule objects for this system. See lsys\_rule.js and its below explanation for more details on LSystem.RuleSet construction.

The arguments for the Rule constructor are as follows:

- 1. id: ID corresponding to the production this rule affects.
- condition: Condition function to the parametric term. Function takes as argument the production object and returns a boolean. Allows the rule to match on the value of the production's parameter.
- 3. output: List of production and turtle action objects to replace the matched production with upon recursion.

More details about the construction of a RuleSet can be seen in the documentation for lsys\_rule.js.

- build(): Launcher function for the recursive L-System construction. Calls internal recursion function on each element in the initial system; thus, it requires that the system variable is set to a list of initial values. The internal recursion runs for a single object in the system list, matching it to the rule set and replacing it with the appropriate output string. It then recursively calls itself on each element of the output array, to a specified MAX\_DEPTH value. Optional argument debug is a boolean that toggles printing of the constructed system after construction.
- checkRule(): Function that checks a given element of the system against the system's rule set, returning the appropriate output. Does a linear search through the list of rules, halting when a match occurs. Matches require that both the rule id and the production id match, as well as the rule's condition function returning a true. The rule's output is then cloned to avoid problems with Javascript's singleton objects affecting subsequent production values. The arguments are then injected using the production's provided inject\_args function, which allows dynamic evaluation of the arguments based on the previous production. The output is then returned. If no match is found, the initial production is returned unchanged.
- printSystem(): Used for debugging. Pretty prints the current value of the L-System's system variable, in form id(args...). Used when the debug flag is turned on in build().

#### 5.4.3 lsys\_rule.js

lsys\_rule.js provides a convenient package of L-System rules used in *The Algorithmic Beauty of Plants*. The rules found in it are used to create the trees in the final Garden of Eden project, but can also serve as examples to users wishing to generate their own L-Systems. The structure for a rule set is given in the above description of LSystem.RuleSet.

- HondaTree: Creates an object that inherits from LSystem.RuleSet. Description of a Honda L-System comes from SOURCE WEE. The tree is of a constant height, but branches with increasing detail at higher levels of recursion. Defined constants allow for a decent amount of variation on what is otherwise a visually highly symmetrical tree.
- TernaryTree: Creates an object that inherits from LSystem.RuleSet. Description of a Ternary L-System comes from SOURCE WEE. By using L-System rules that match to turtle commands, this tree actually grows both larger and more detailed at higher levels of recursion, which more closely resembles the growth of a tree. There is only one branching rule, which erroneously uses a trijunction at each branching node. The generated tree is visually quite complex, but has some symmetrical artefacts visible from specific angles. Varying constants allows for a large amount of variation on this tree structure.

# 5.5 Forest Implementation

# 6 Runtime

- 6.1 LList Algorithm
- 6.1.1 Profile
- 6.1.2 Asymptotic Behavior
- 6.2 Tree Search Algorithm
- 6.2.1 Profile
- 6.2.2 Asymptotic Behavior
- 6.3 Three.js Considerations

# 7 Extensions

# 7.1 Tree Rendering

Currently, there is a significant user experience issue in the time it takes to properly render out a forest of trees. The current solution ignores this, expecting the user to patiently wait several minutes for the trees to render into a forest. Extensions to address this issue, either by speeding up the processs or by circumventing the issue, are proposed below.

#### 7.1.1 Pre-Rendering

Pre-Rendering involves setting the project up with a basic framework to allow for database storage of tree primatives. This solution would save generated tree structures, allowing a user to simply access the database upon reaching the page instead of running the full generation cycle for a forest.

Several problems arise with this solution. First, data tends to be lost when serializing a Javascript object to JSON. Thus, a special serialization process would need to be created in order to store the Three.js graphical primitives. Furthermore, as the objects would be created out of environmental context, growth affectors such as global and local tropism would not be able to affect the geometry of the trees produced.

The benefits of the solution, however, are significant. The user wait time would likely be negligable, allowing the experience to being amost immediately upon accessing the site. For today's impatient users, this is extremely important. Additionally, the addition of a database could open up extensions such as saving particularly nice generated forests.

### 7.1.2 Background Rendering

Javascript does not support threading; however, several worker queue libraries exist that could allow for the creation of trees to happen asynchronously to the creation of the Three.js scene. The user would open the page to a freshly generated, but empty, terrain; as they explore, fully-grown trees would appear around them as the workers finish. The appearing affect would be somewhat jarring, but this could be artistically mitigated with clever visual distraction, such as thick fog with increasing visibility as trees appear. See also the below section on Growth Time Emulation, which could be used in conjunction with this acceleration process.

#### 7.1.3 Tree API

While Javascript does not allow local threading, it has significant asynchronization support in AJAX. To take advantage of this, a tree API could be written. This would have an effect similar to Background Rendering, except that it would utilize default Javascript functionality. Furthermore, there is nothing forcing the API server to use a language that doesn't support threading; the generation could be written in a much faster language, outputting carefully serialized Three.js objects as an asynchronous HTTP JSON response. Global forest data could also be supported by being included as a parameter to the AJAX request to the API.

# 7.2 Graphical Primitives

The current primitive used by the turtle graphics wrapper is a basic cylinder, of diameter specified by Turtle.\_set() and length specified by Turtle.\_F() and the turtle's speed. This results in a very noticeably blocky tree, where each branch has a discontinuous shift in diameter. Obviously, trees in nature to not display such structure; thus, using a different graphical primitive would result in a much more realistic-looking tree.

#### 7.2.1 Tapered Cylinder

To create a tapered cylinder, the turtle's forward draw command would need to take in to account two Turtle.\_set() commands, using them in conjunction with Three.js's cylinder pyramid to make a conical frustum. By matching the diameter of the top of one branch with the diameter of the bottom of the next, the branches of the tree would blend together, resulting in the continuous look found in nature.

To do this, a new turtle command would need to be implemented. Turtle.\_Ft() would work similarly to Turtle.\_F(), except that it would use a conic frustum. The below row expands on Table 1.

Command	Symbol	Argument	Description
_Ft	Ft	time, width	Moves turtle forward by specified time value.
			Draws line as a conic frustum beginning with
			the turtle's current diameter and ending at the
			specified diameter. Also sets the turtle's diam-
			eter to the specified diameter.

Table 2: Turtle Taper Command

#### 7.2.2 Extruded Line

Another option for smoothing the discontinuities is using Three.js is to use the extruded shape feature of Three.js, using a THREE.CurvePath to represent a path. There are several benefits to this option. Extruded paths support tapering lines by default, which would allow a branch to be represented as a simple, light-weight path. A collection of paths might be able to be extruded in a single step, which could improve rendering time. Visually, this would be a very good option, as the extrusion process would smooth the branch joints, which currently are merely the intersection of cylinder primitives and are discontinuous. Using an extruded line might also allow for branch bending; as discussed in Section 4.2.1, branches are currently assumed to be perfectly straight, whereas real branches are usually curved to some degree. Representing branches as paths would allow for the manipulation of these paths, resulting in a extruded branch with a visually more accurately curved shape.

The process of creating these paths, however, might be a little difficult. It might be useful, as with the tapered cylinder, to implement another turtle command that takes as an argument a tapering constant. Post-processing of the turtle command list might also generate data to feed to the extruded shape constructor, adding a large list traversal but allowing the user to implement it without using an L-System constructed with extrusion rules. The details of this implementation, however, will be left for future consideration.

# 7.3 Tropism

# 7.4 Path Traveling

A significant design consideration when making this project is the unique interactive experience, especially with regards to modern video games. If this project is to be considered a game, then the "objective" is not anything tangible, creative, or destructive; instead, I wish to effect a whimsical sense of exploration, reminiscent of childlike play in nature. The user is not in control of their environment; in many ways, I hope that this lack of agency inspires a sense of curious awe.

To this end, I would consider removing, or at least limiting, the user's ability to navigate the world. The current hosted version significantly limits user navigation speed and disables jumping, attempting to "slow down" the experience and force the user to focus on the scene instead of navigation concerns and the thrill of speed. An interesting extension, however, would be using path-finding algorithms to control, or at least guide, user navigation.

One possible implementation would be to bias the user movement with a pathfinding algorithm, allowing user control only as slight deviations from the path. Thus user would thus be allowed a small amount of control over their exploration, but would ultimately be pulled towards the calculated path. Alternatively, movement controls could be disabled completely, allowing the user only to look around as they are led on a walk around the forest.

Several pathfinding algorithms exist for consideration. Dijkstra's algorithm, for example, or its extension A\*, are designed to find the shortest path in a graph, which can be used to calculate a path around obstacles. However, these algorithms are designed to find a shortest path; in this case, as the journey is more important than the destination, I propose an alternative algorithm, based on Namco's Pac-Man[13]. As the user travels, a random "target point" shall be calculated. Then, the player is moved steadily towards that point, using weighted-vector calculations. This weighted vector would tend to point directly toward the target point, but would be deflected by nearby trees. The action can be thought of as similar to a charged particle moving towards a strong attractor, but repulsed by nearby point charges. The user would thus move to the most open areas that lead towards the target point; this has an appealing element of realism to it, as people tend to travel through forest following perceived "paths", which are usually locations of most negative space between trees. When the user arrives at or near the target point, a new target point will be calculated, forcing the user into perpetual motion.

### 7.5 Erosion Emulation

Erosion emulation[10] is a process by which generated terrain can gain the appearance of natural weathering. Currently, terrain is passed through a Gaussian filter, a low-pass filter that smooths over small-scale bumps while preserving larger features. This is visually effective at removing terrain noise, which is annoying to the user whose height changes with respect to the terrain, causing a "bumpy" oscillation of the camera; however, it is not naturally justified. Erosion emulation would be more effective: a natural low-pass filter, it would smooth over annoying terrain noise while giving the scene a cool sense of natural age.

# 7.6 Tree Species

Currently, only a single, achetypal tree is being created by the specified L-System. Obviously, the forests usually consist of different species of trees growing together. This could easily be implemented by including a set of L-System rules, each representing a different tree species. The species could be randomly selected upon the Forest's seeding step, or, if a dominant species is desired, such as is found in a pine forest, probability could be assigned to each species. A more sophisticated selection algorithm could take in to consideration biological advantage for resource aquisition; for example, a tree predisposed to grow taller might be better at capturing light. Careful consideration when constructing the L-System ruleset should be taken if specific species are desired, but a significant body of literature exists discussing the topological details of different tree species.

# 7.7 Texturing

Current, Garden of Eden almost entirely uses solid colors for a very simple look. The use of some basic textures would make the rendered scene look nicer and more realistic.

#### 7.7.1 Bark

A basic, brown bark texture would be a significant visual improvement over the current solid mesh. This texture could come from images of real trees, which might result in very realistic bark; however, the texture should be wrappable in order to avoid seam artefacts. Thus, a bark generation method[2] might be preferable. The proposed method uses sawtooth waves and coloration to achieve a decently-realistic bark look that is wrappable in all directions.

# **7.7.2** Bump Map

Currently, branches are represented as straight, smooth cylinders. Branches in nature, however, are twisted, gnarled, and scarred. This effect can be achieved with a bump map texture, which could be generated with the bark texture to produce the appropriate visual. This could also be used to simulate burls and broken branches, which could be generated along with the actual branches in the L-System, to be rendered out by the texture engine.

## 7.8 Growth Time Emulation

The L-System used for the trees in Garden of Eden has replacement rules for both productions and turtle commands; in other words, it affects both branching junctions and the length and width of the rendered branches. Thus, the branches grow with time, offering a rough correlation between depth of recursion and age of the tree. This extension seeks to expand on this correlation, growing the trees in a process that actually represents time, or the age of the tree in question. A single level of recursion, for example, might represent a year of growth. This would open up a lot of different avenues of forest growth representation. Growth events, mentioned below, become possible. The working assumption that all trees are of a roughly evuivalent age could also be broken: the seeding and growth step could occur in parallel, resulting in a forest of trees and their sapling progeny.

This extension would require a significant rewrite of the Forest module and a specially written L-System ruleset. The Forest module, with the backgrounded workflow described above, would need to combine the seeding and growing steps. This could involve a significant amount of IPC, which Javascript does not easily support. It therefore might work better in conjunction with the Tree API setup, which could provide solid backgrounding support as well as the IPC required for growth time emulation.

# 7.9 Density Management

There are a few problems with the current density management implementation, which will be addressed in detail below. There exists a non-deterministic (due to the use of random placement) bug where trees placed might be too close, or even in contact with, trees in adjacent patches. Furthermore, the algorithm used easily and logically supports the addition of younger trees to fill out the patch.

### 7.9.1 Seedlings

The current density management system lends itself well to extension with regards to adding new, younger trees to a given patch. The process should take in to consideration the distance from the canopy tree, as the dominant tree in the patch should get most of the resources, and preventing young trees from growing too close to the canopy tree would prevent tree collisions from occurring. I propose modeling the patch as a particle system, with the canopy tree as a source of repulsion, and deriving a probability of elimination from the inverse square law thus derived. A constant amount of seedlings would be placed randomly in the patch, perhaps as a part of a growth time emulation step. Then, using the above inverse square law, the seedlings would be filtered on their derived probability. This would make the density manager follow the gap models on which it is based much more accurately, in addition to improving the realism of the generated forest by breaking the same-age assumption.

#### 7.9.2 Placement Error

The aforementioned placement error arises from breaking the assumption that patches are horizontally homogeneous, and that there are no interactions between patches. This can lead to an error where trees are placed close to a shared border, resulting in collision of the trees that is either unreasonable or impossible. There are two possible solutions to this problem:

- 1. Edge repulsion: Similar to the seedlings problem, an inverse square law would be used to repulse canopy trees away from the edges of the patch, resulting in a placement distribution strongly biased towards the center of the square. This would combine well with the proposed seedling extension and offer a probabilistic solution, which has been used throughout the problem as a stand-in for natural, deterministic methods.
- 2. Closest pair algorithm: A more direct solution would be to use a closest pair algorithm[17] to obtain a list of trees that violate visual or natural closeness constraints, then filtering said list to remove collisions. The below algorithm is a linear solution to the problem:

```
Gaussian-Density-Management(density)
  // Proximity detection step
  Create a grid where each square is half the distance between trees, calculated
     from the density
  Seed grid with first tree by mapping the tree's location to the grid and adding
     it to that spot
  For every subsequent tree t_dest,
     Map tree location to grid
     If there are any trees mapped to that location or any of its compass neighbors,
     For each neighboring tree t_src,
```

Calculate the Euclidean distance between  $t\_src$  and  $t\_dest$  Construct a pair of  $t\_src$  and  $t\_dest$ , including the calculated distance Add pair to a list of pairs

```
// Filter step
For each pair in the pair list
    MAP DISTANCE TO NORMAL CURVE TO GET PROBABILITY??
    FILTER USING THAT PROBABILITY??
```

The algorithm fits well with the current density management system in that it partitions the terrain plane into a grid, though of a different size than the patches used to place canopy trees. However, it is a somewhat hacky solution, as it only fixes the bug as it occurs, instead of finding a more natural solution to prevent it.

#### 7.10 Growth Events

Growth events are defined generally as any effectively instantaneous event that dramatically affects tree growth. Growth events could include, but are not limited to, weather affects such as wind damage or lightning, disease, or damage from other trees. These effects are a random, singular event that can significantly change the visual appearance and factors affecting the growth of a tree, and that don't necessarily have global affects. These events could be randomly simulated in the aforementioned growth time emulation, with a random event affecting a single, random tree at a specific interval. The result might range from truncated branches to split trunks, even complete removal of the tree. They would, however, have to occur during the L-System recursion, and would require significant rewriting of the recursion structures to handle outside affectors.

# References

- [1] James Arvo, David Kirk, and Apollo Computer. Modeling plants with environment-sensitive automata. In *In Proceedings of Ausgraph88*, pages 27–33, 1988.
- [2] Jules Bloomenthal. Modeling the mighty maple. SIGGRAPH Comput. Graph., 19(3):305–311, July 1985.
- [3] Harald Bugmann. A review of forest gap models. Climatic Change, 51(3-4):259–305, 2001.
- [4] Phillippe de Reffye, Claude Edelin, Jean Françon, Marc Jaeger, and Claude Puech. Plant models faithful to botanical structure and development. SIGGRAPH Comput. Graph., 22(4):151–158, June 1988.
- [5] Alain Fournier, Don Fussell, and Loren Carpenter. Computer rendering of stochastic models. *Commun. ACM*, 25(6):371–384, June 1982.
- [6] Houssam Hnaidi, Eric Gurin, Samir Akkouche, Adrien Peytavie, and Eric Galin. Feature based terrain generation using diffusion equation. Computer Graphics Forum, 29(7):2179–2186, 2010.
- [7] Ed Key and David Kanaga. http://www.visitproteus.com/.
- [8] Paul Martz (martz@frii.com). Generating random fractal terrain. Game Programmer, 1996, 1997.
- [9] B. Mandelbrot and J. Van Ness. Fractional brownian motions, fractional noises and applications. SIAM Review, 10(4):422-437, 1968.

- [10] F. K. Musgrave, C. E. Kolb, and R. S. Mace. The synthesis and rendering of eroded fractal terrains. SIGGRAPH Comput. Graph., 23(3):41–50, July 1989.
- [11] Teong Joo Ong, Ryan Saunders, John Keyser, and John J. Leggett. Terrain generation using genetic algorithms. In *Proceedings of the 7th Annual Conference on Genetic and Evolutionary Computation*, GECCO '05, pages 1463–1470, New York, NY, USA, 2005. ACM.
- [12] Markus Persson and Notch Software AB. https://www.minecraft.net/.
- [13] Jamey Pittman. The pac-man dossier. http://home.comcast.net/jpittman2/pacman/pacmandossier.html, June 2011.
- [14] Przemyslaw Prusinkiewicz and Aristid Lindenmayer. *The Algorithmic Beauty of Plants*. Springer-Verlag, 2nd edition, 1996.
- [15] Michael G. Ryan and Barbara J. Yoder. Hydraulic limits to tree height and tree growth. *BioScience*, 47(4):pp. 235–242, 1997.
- [16] Akio Takenaka. A simulation model of tree architecture development based on growth response to local light environment. *Journal of Plant Research*, 107(3):321–330, 1994.
- [17] Mark Sandland <Kramii>. Re: Find all points within a certain distance of each other? http://programmers.stackexchange.com/a/129909, May 2014.
- [18] Naokazu Yokoya, Kazuhiko Yamamoto, and Noboru Funakubo. Fractal-based analysis and interpolation of 3d natural surface shapes and their application to terrain modeling. *Computer Vision, Graphics, and Image Processing*, 46(3):284 302, 1989.