

# Machine Learning with Python

Wenbin Guo Bioinformatics IDP, UCLA

> wbguo@ucla.edu 2023 Spring



## Notation of the slides

Code or Pseudo-Code chunk starts with ">", e.g.
 ▶ print("Hello world!")

Link is underlined

Important terminology is in **bold** font

## Agenda

- Day 1: Introduction to machine learning
  - Some key concepts in machine learning
  - Jupyter notebook and some packages usage
- Day 2: Supervised learning
  - Classification
  - Regression
  - Regularization
- Day 3: Unsupervised learning
  - Dimension reduction
  - Clustering















# Day 2: Supervised learning

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## Overview

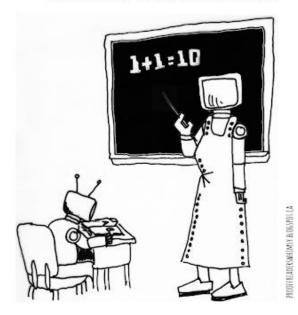
#### Time

• 3-hour workshop (45min + 45min + 30min + practice/Q&A)

### **Topics**

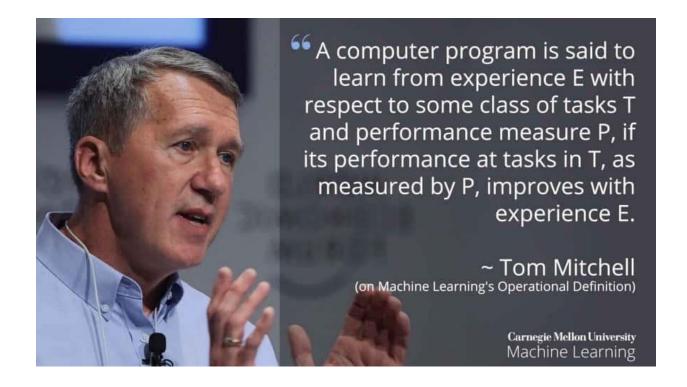
- ☐ Classification algorithms
- ☐ Performance measure
- ☐ Overfitting & underfitting
- Examples and practices

#### SUPERVISED MACHINE LEARNING



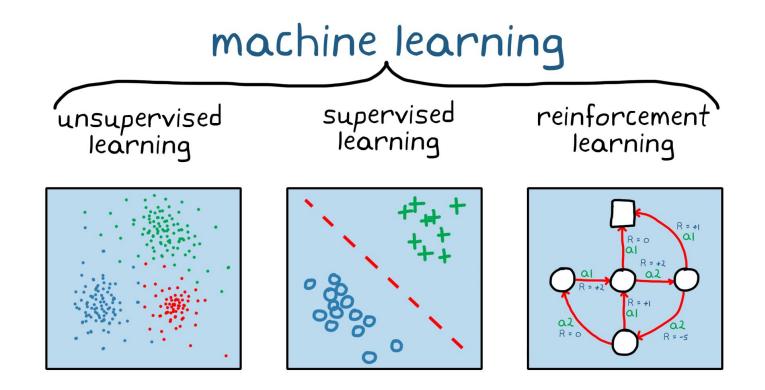
Key concepts in machine learning:

☐ What's machine learning



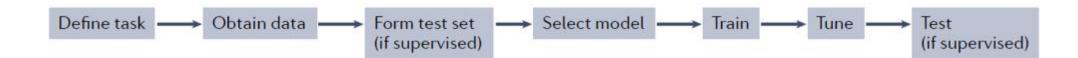
Key concepts in machine learning:

- What's machine learning
- ☐ 3 types of machine learning



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- What's machine learning
- ☐ 3 types of machine learning
- ☐ The big picture of training a machine learning model



Key concepts in machine learning:

- What's machine learning
- ☐ 3 types of machine learning
- ☐ The big picture of training a machine learning model

#### More details about:

- ☐ Training/test set
- ☐ Loss function
- □ Overfitting/underfitting
- ☐ Hyperparameters tunning
- ☐ Cross validation
- ☐ Challenges in machine learning

Key concepts in machine learning:

- What's machine learning
- ☐ 3 types of machine learning
- ☐ The big picture of training a machine learning model

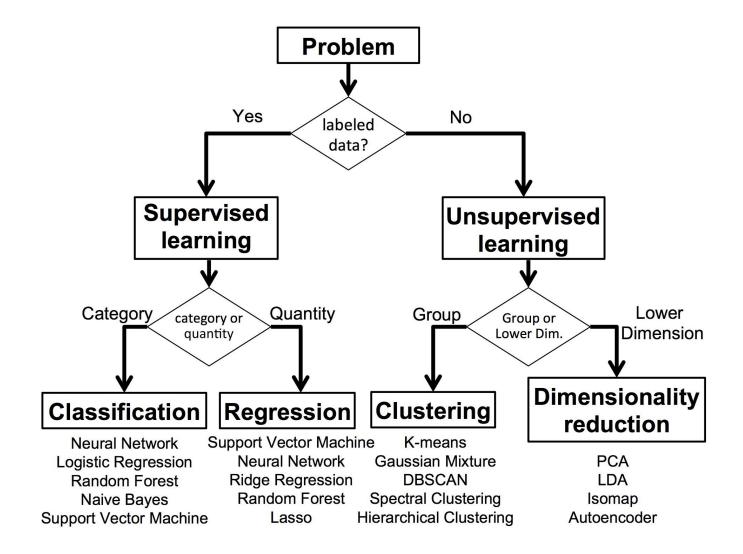
More details about:

- ☐ Training/test set
- ☐ Loss function
- □ Overfitting/underfitting
- ☐ Hyperparameters tunning
- ☐ Cross validation
- ☐ Challenges in machine learning

Practice:

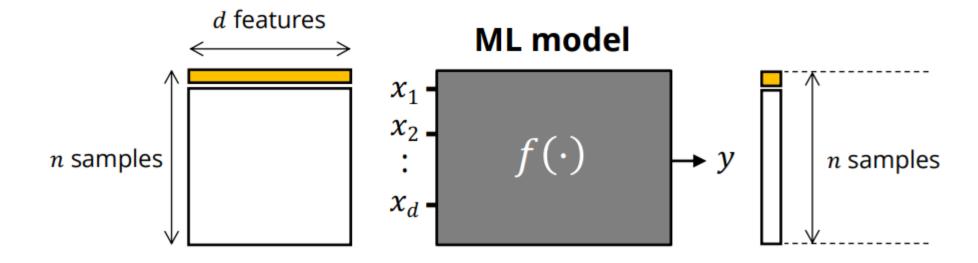
- ☐ Jupyter notebook usage
- ☐ Some useful libraries
- ☐ A supervised learning example

# Types of machine learning



# Supervised learning

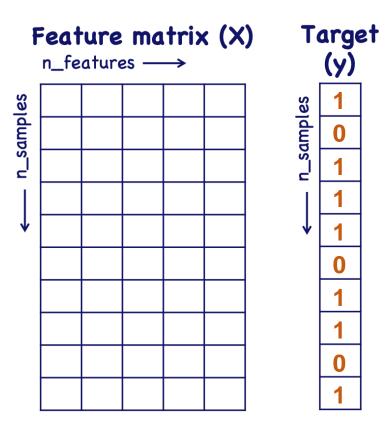
- Training data with n samples of features x and labels y
- Learn a function class f(x) to describe y based on x



# Different choice of f() for classification tasks

- Logistic regression
- K-nearest neighbor
- Naïve bayes
- Support vector machine
- Decision trees
- Random forest
- Adaboost
- Gradient boosting (XGBoost)
- Neural network

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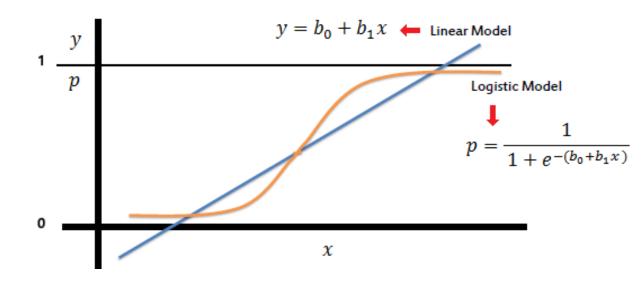
$$\hat{y} = f(x)$$

Model

$$\hat{p} = h_{oldsymbol{ heta}}\left(\mathbf{x}
ight) = \sigma\left(\mathbf{x}^{\intercal}oldsymbol{ heta}
ight)$$

$$\sigma\left(t
ight)=rac{1}{1+\exp(-t)}$$

$$\hat{y} = egin{cases} 0 & ext{if } \hat{p} < 0.5 \ 1 & ext{if } \hat{p} \geq 0.5 \end{cases}$$

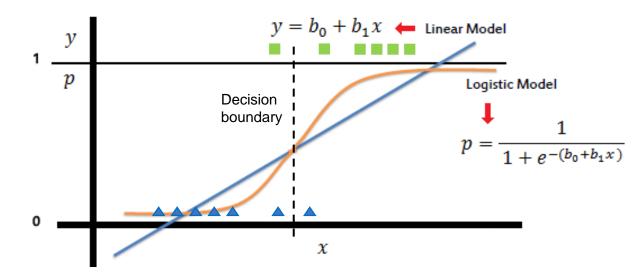


Model

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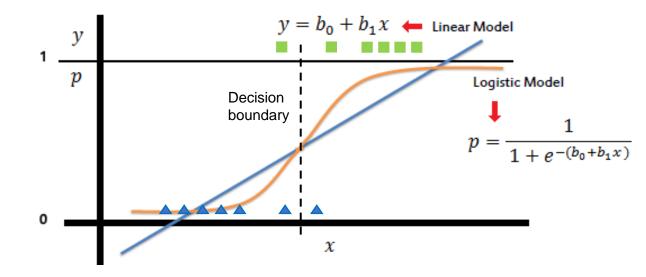


Model

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Loss function:

Equation 4-16. Cost function of a single training instance

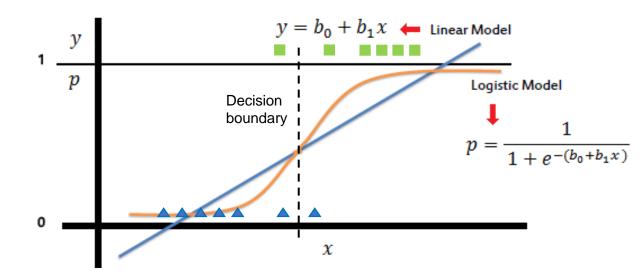
$$c(oldsymbol{ heta}) = egin{cases} -\log(\hat{p}) & ext{if } y=1 \ -\log(1-\hat{p}) & ext{if } y=0 \end{cases}$$

Model

$$\hat{p} = h_{oldsymbol{ heta}}\left(\mathbf{x}
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#### Loss function:

Equation 4-16. Cost function of a single training instance

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ight.$$

Equation 4-17. Logistic Regression cost function (log loss)

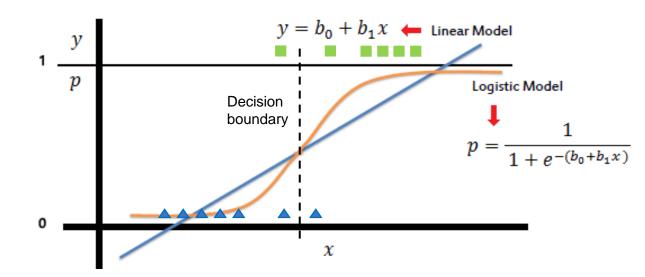
$$J(oldsymbol{ heta}) = -rac{1}{m} \sum_{i=1}^m \left[ y^{(i)} logig(\hat{p}^{(i)}ig) + \left(1 - y^{(i)}
ight) logig(1 - \hat{p}^{(i)}ig) 
ight]$$

Model

$$\hat{p} = h_{oldsymbol{ heta}}\left(\mathbf{x}
ight) = \sigma\left(\mathbf{x}^{\intercal}oldsymbol{ heta}
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$$\sigma\left(t
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$$\hat{y} = egin{cases} 0 & ext{if } \hat{p} < 0.5 \ 1 & ext{if } \hat{p} \geq 0.5 \end{cases}$$



Loss function (generalize to multi-class):

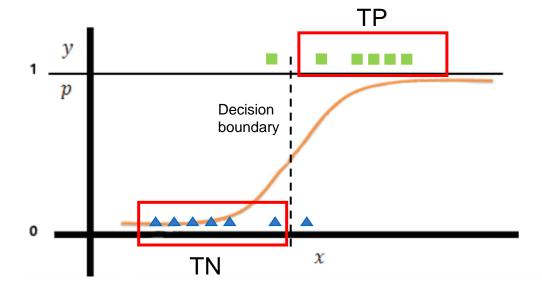
Equation 4-22. Cross entropy cost function

$$J(oldsymbol{\Theta}) = -rac{1}{m} \sum_{i=1}^m \sum_{k=1}^K y_k^{(i)} \log \Bigl( \hat{p}_k^{(i)} \Bigr)$$

## Performance measure

• Accuracy (TP + TN) (TP + FP + TN + FN)

Q: Is accuracy always a good measure?

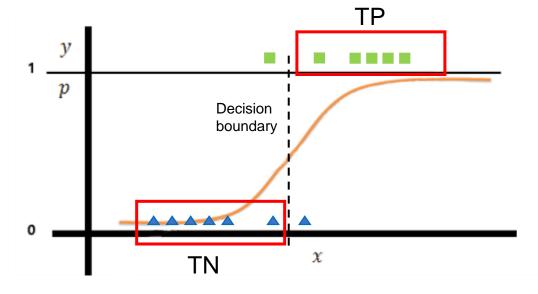


## Performance measure

• Accuracy  $\frac{(TP + TN)}{(TP + FP + TN + FN)}$ 

Q: Is accuracy always a good measure?

Be cautious with skewed dataset !!!

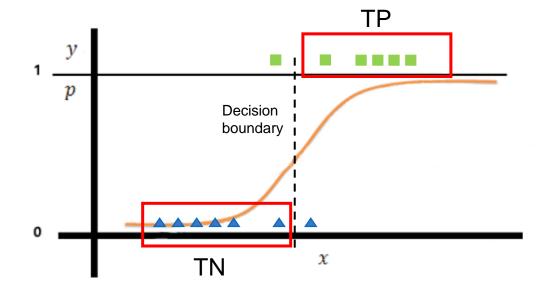


## Performance measure

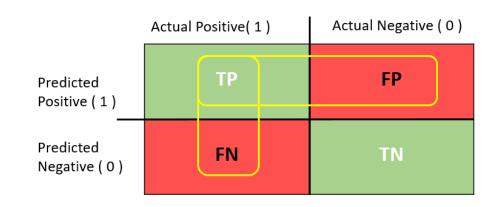
Accuracy

Q: Is accuracy always a good measure?

Be cautious with skewed dataset !!!



#### Confusion matrix

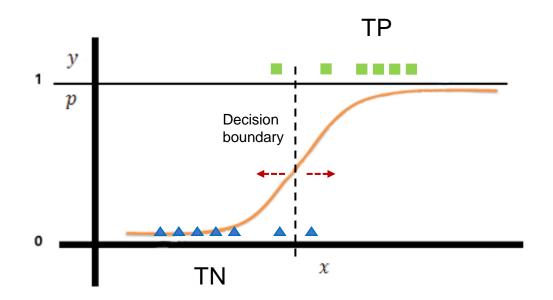


$$ext{precision} = rac{TP}{TP + FP}$$
  $ext{recall} = rac{TP}{TP + FN}$ 

$$F_1 = rac{2}{rac{1}{ ext{precision}} + rac{1}{ ext{recall}}}$$

# Performance measure (varying threshold)

Precision-recall tradeoff



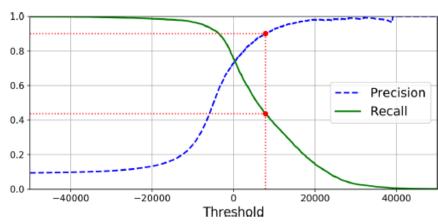
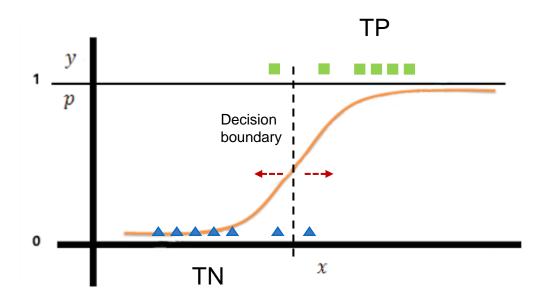


Figure 3-4. Precision and recall versus the decision threshold

# Performance measure (varying threshold)

Precision-recall tradeoff



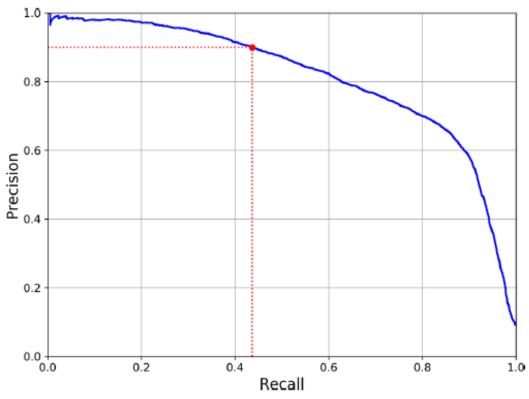


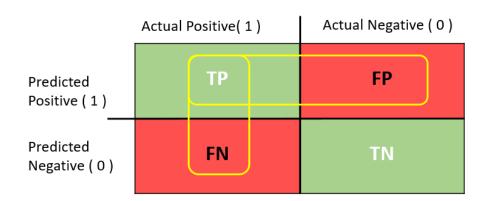
Figure 3-5. Precision versus recall

PR-ROC

# Performance measure (varying threshold)

#### ROC curve & AUC

- Receiver Operating Characteristic curve
- Aera under curve



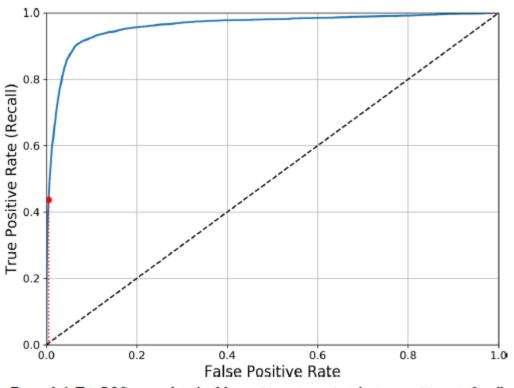


Figure 3-6. This ROC curve plots the false positive rate against the true positive rate for all possible thresholds; the red circle highlights the chosen ratio (at 43.68% recall)

<u>True positive rate</u> (TPR), TP/(TP+FN)

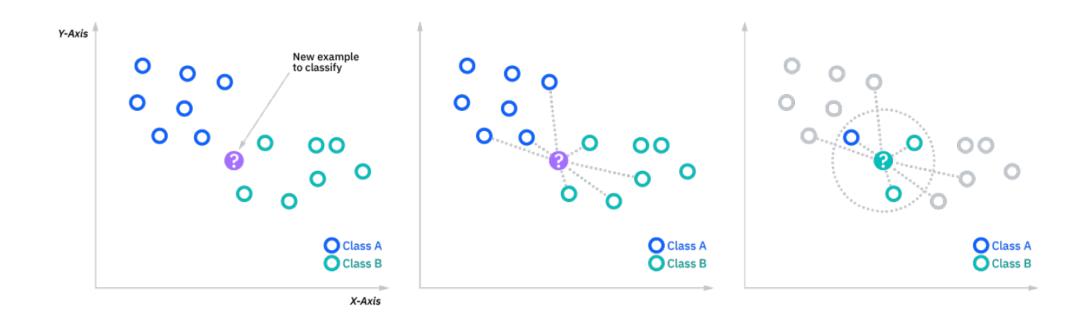
<u>False positive rate</u> (FPR), FP/(FP+TN)

# Summary

- Logistic regression algorithm
- Cross-entropy loss for classification
- Performance measure
  - Accuracy
  - Confusion matrix
  - Precision, recall, and the tradeoff between them
  - ROC, AUC

# K-nearest neighbor (KNN)

An instance based-learning algorithm



## **KNN**

- An instance based-learning algorithm
- Key: distance metrics
  - Euclidean distance (L2 norm)

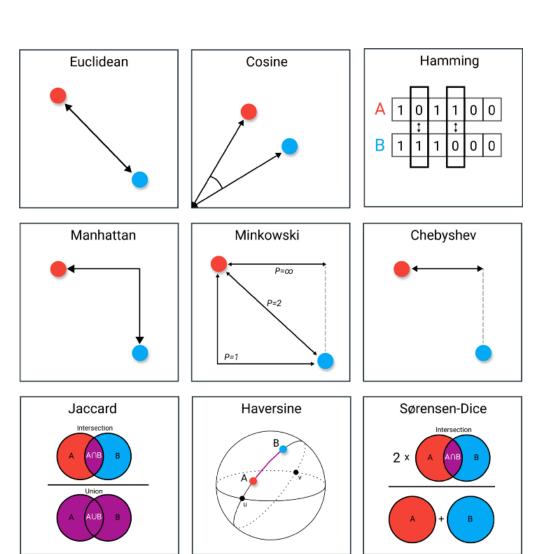
$$D(x,y) = \sqrt{\sum_{i=1}^{n} (x_i - y_i)^2}$$

Manhattan distance (L1 norm)

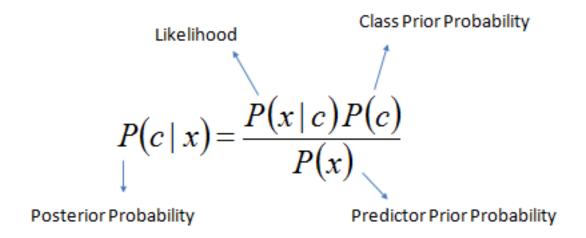
$$D(x,y) = \sum_{i=1}^{k} |x_i - y_i|$$

Minkowski distance (Lp norm)

$$D(x,y) = \left(\sum_{i=1}^{n} |x_i - y_i|^p\right)^{\frac{1}{p}}$$



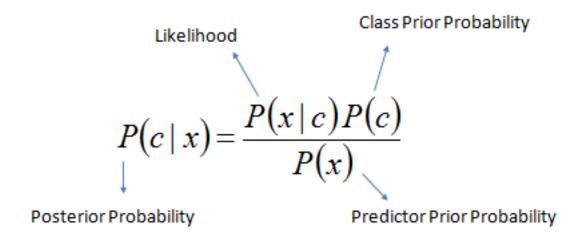
## Naïve bayes



$$P(c \mid X) \propto P(x_1 \mid c) \times P(x_2 \mid c) \times \cdots \times P(x_n \mid c) \times P(c)$$

Q: Why Naïve Bayes is called naïve?

## Naïve bayes

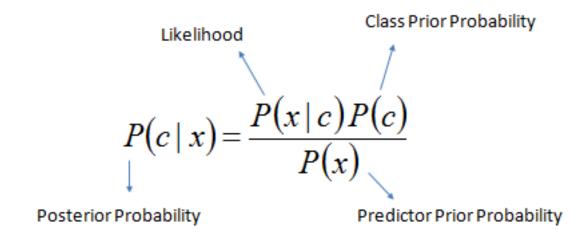


$$P(c \mid X) \propto P(x_1 \mid c) \times P(x_2 \mid c) \times \cdots \times P(x_n \mid c) \times P(c)$$

#### Q: Why Naïve Bayes is called naïve?

it has the assumption that features are *conditionally independent* from each other (condition on class)

# Naïve bayes



$$P(c \mid X) \propto P(x_1 \mid c) \times P(x_2 \mid c) \times \cdots \times P(x_n \mid c) \times P(c)$$

Gaussian Naïve Bayes

$$P(x_i \mid y) = rac{1}{\sqrt{2\pi\sigma_y^2}} \exp\left(-rac{(x_i - \mu_y)^2}{2\sigma_y^2}
ight)$$

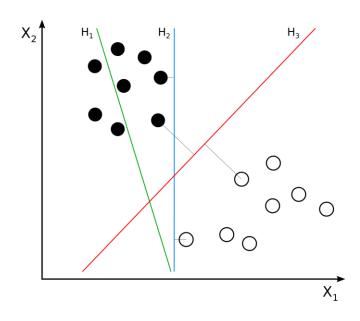
# Support vector machine

#### Decision function

Equation 5-2. Linear SVM classifier prediction

$$\hat{y} = egin{cases} 0 & ext{if } \mathbf{w}^\intercal \mathbf{x} + b < 0, \ 1 & ext{if } \mathbf{w}^\intercal \mathbf{x} + b \geq 0 \end{cases}$$



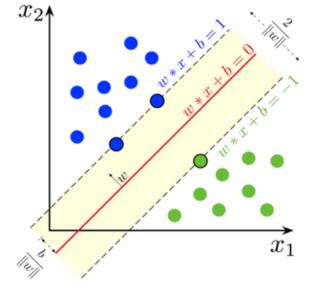


# Support vector machine

### Large margin classification

Equation 5-3. Hard margin linear SVM classifier objective

$$egin{aligned} & \min_{\mathbf{w}, b} & rac{1}{2} \mathbf{w}^\intercal \mathbf{w} \ & ext{subject to} & t^{(i)} \left( \mathbf{w}^\intercal \mathbf{x}^{(i)} + b 
ight) \geq 1 & ext{for } i = 1, 2, \cdots, m \end{aligned}$$



### Support vectors

- The decision boundary is fully determined (or "supported") by the instances located on the edge of the street, these instance are called the support vectors
- Adding more training instances "off the street" will not affect decision boundary

# Support vector machine

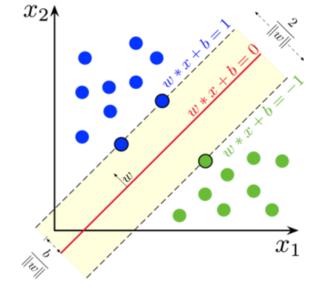
### Large margin classification

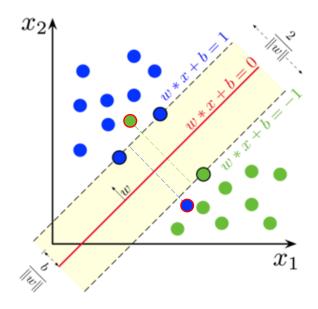
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ight) \geq 1 & ext{for } i = 1, 2, \cdots, m \end{aligned}$$

### Soft-margin classification

$$\begin{split} & \underset{\mathbf{w},b,\zeta}{\text{minimize}} & & \frac{1}{2}\mathbf{w}^{\intercal}\mathbf{w} + C\sum_{i=1}^{m}\zeta^{(i)} \\ & \text{subject to} & & t^{(i)}\left(\mathbf{w}^{\intercal}\mathbf{x}^{(i)} + b\right) \geq 1 - \zeta^{(i)} \quad \text{and} \quad \zeta^{(i)} \geq 0 \quad \text{for } i = 1, 2, \cdots, m \end{split}$$





# Support vector machine (nonlinear)

With polynomial kernel

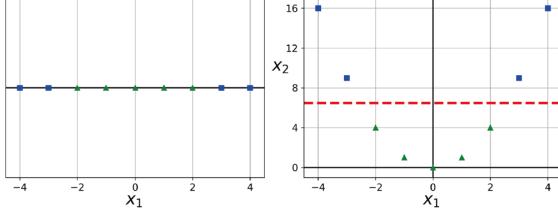


Figure 5-5. Adding features to make a dataset linearly separable

- With similarity measure
  - Gaussian Radial Basis Function (RBF)

$$\phi_{\gamma}\left(\mathbf{x},\ell
ight) = \exp\Bigl(-\gamma{\left\|\mathbf{x}-\ell
ight\|}^2\Bigr)$$

l: a particular landmarkγ: a hyperparameter

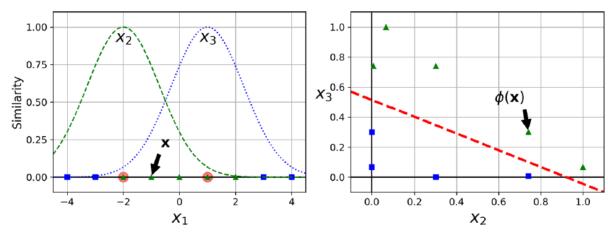


Figure 5-8. Similarity features using the Gaussian RBF

## **Decision trees**

• A white-box algorithm, which is intuitive and its decision is easy to interpret

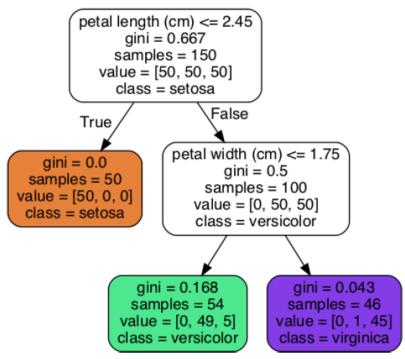
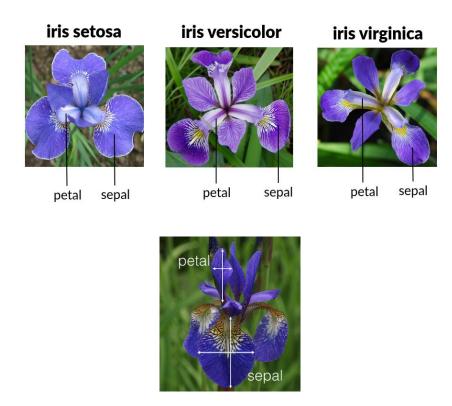


Figure 6-1. Iris Decision Tree



## Decision trees

• A white-box algorithm, which is intuitive and its decision is easy to interpret

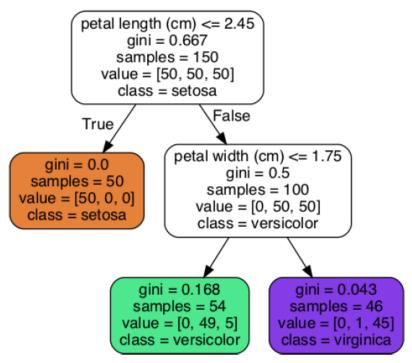


Figure 6-1. Iris Decision Tree

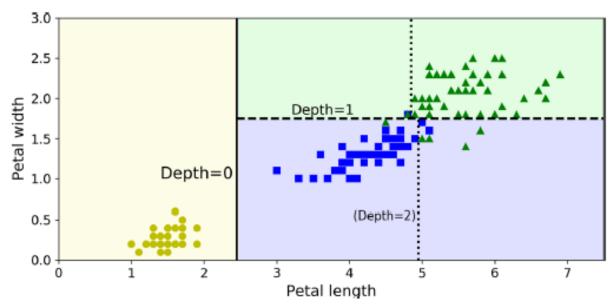


Figure 6-2. Decision Tree decision boundaries

#### Decision trees

A white-box algorithm, which is intuitive and its decision is easy to interpret

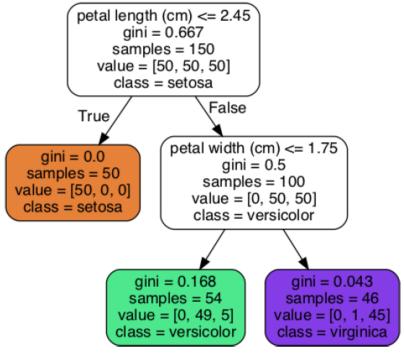


Figure 6-1. Iris Decision Tree

 The algorithm search for a feature k and threshold t that produce a purest subset

Equation 6-2. CART cost function for classification

$$J(k,t_k) = rac{m_{
m left}}{m} G_{
m left} + rac{m_{
m right}}{m} G_{
m right} \ ext{where} \ \begin{cases} G_{
m left/right} & ext{measures the impurity of the left/right subset,} \ m_{
m left/right} & ext{is the number of instances in the left/right subset.} \end{cases}$$

#### **Decision trees**

A white-box algorithm, which is intuitive and its decision is easy to interpret

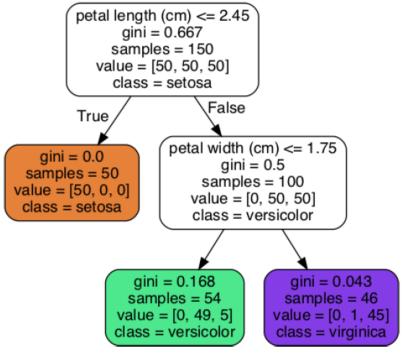


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m left/right} & ext{measures the impurity of the left/right subset,} \ m_{
m left/right} & ext{is the number of instances in the left/right subset.} \end{cases}$$

• Purity measure: Gini index

$$G_i=1-\sum_{k=1}^n {p_{i,k}}^2$$

 $(p_{i,k})$  is the ratio of class k instance in node i)

#### Decision trees limitation

• Instability: sensitive to small variation in training data

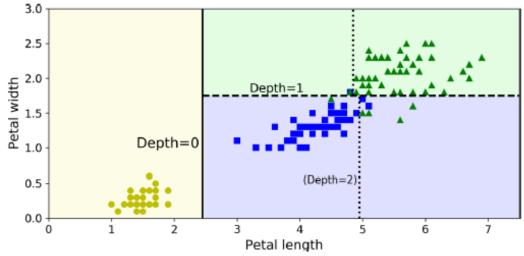


Figure 6-2. Decision Tree decision boundaries

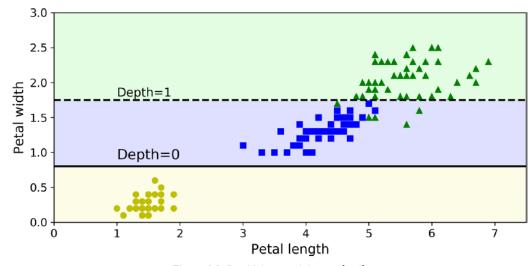
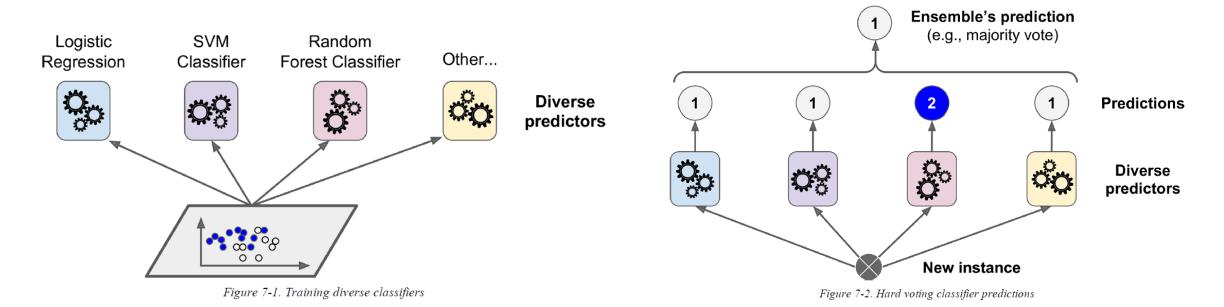


Figure 6-8. Sensitivity to training set details

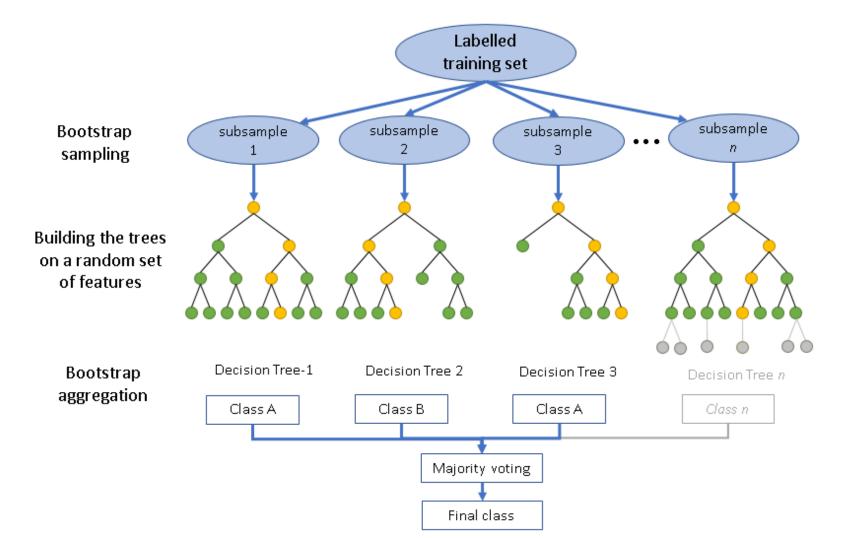
# Ensemble learning – the wisdom of the crowd

Even if each classifier is a *weak learner* (meaning it does only slightly better than random guessing), the ensemble can still be a *strong learner* (achieving high accuracy), provided there are a sufficient number of weak learners and they are sufficiently diverse



#### Random forest

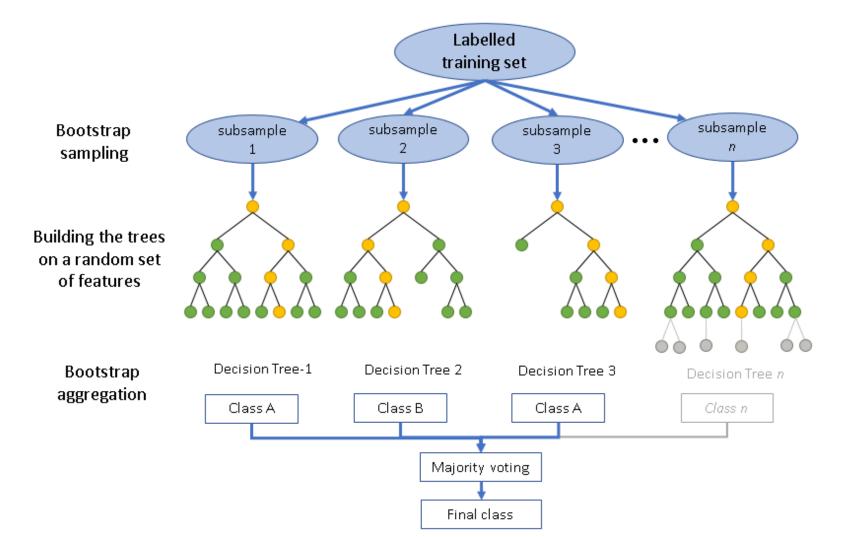
An ensemble of decision trees



Reduce the variance of a single tree

#### Random forest

An ensemble of decision trees



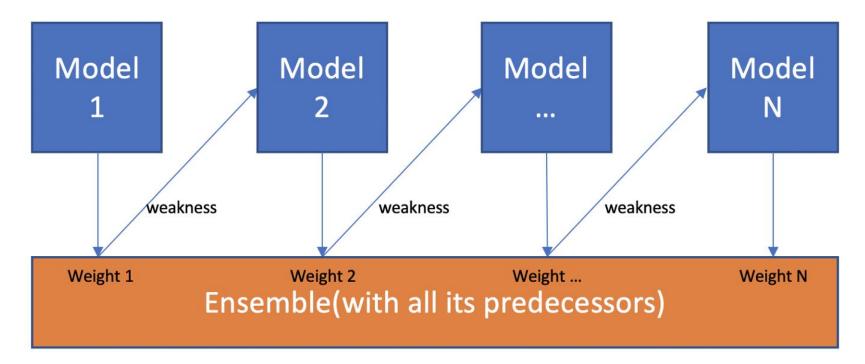
#### Feature importance:

how much the tree nodes that use that feature reduce impurity on average (across all trees in the forest)

# Boosting method:

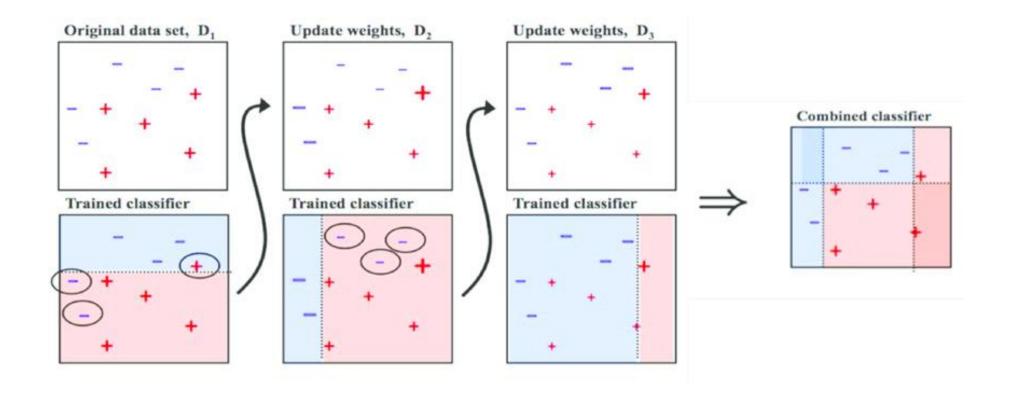
- Combine weak learner to form a strong learner
- Train predictors sequentially, each trying to correct its predecessor

Model 1,2,..., N are individual models (e.g. decision tree)



## Adaboost

 Pay a bit more attention to the training instances that the predecessor underfitted



### Adaboost

#### Core algorithm:

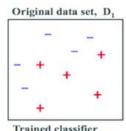
- Initialize with equal weights for each instance i
- > Compute weighted error rate for *j*<sup>th</sup> predictor
- Compute the predictor's weight
- Weight update for instance



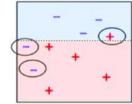
> Repeat until designed number of predictors is reached or perfect predictors is found

 $lpha_j = \eta \log rac{1-r_j}{r}$ 

 To make predictions, computes the predictions of all the predictors and calculate weighted average



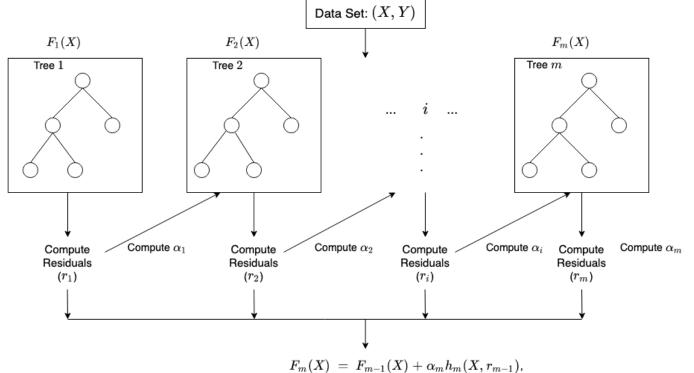




# Gradient boosting

• Fit a new predictor to the residual errors made by the previous

predictor

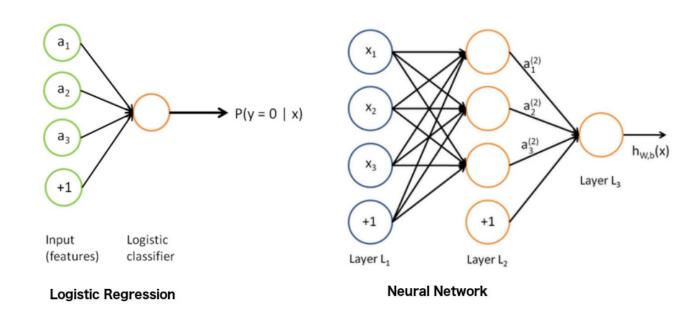


where  $\alpha_i$ , and  $r_i$  are the regularization parameters and residuals computed with the  $i^{th}$  tree respectfully, and  $h_i$  is a function that is trained to predict residuals,  $r_i$  using X for the  $i^{th}$  tree. To compute  $\alpha_i$  we use the residuals

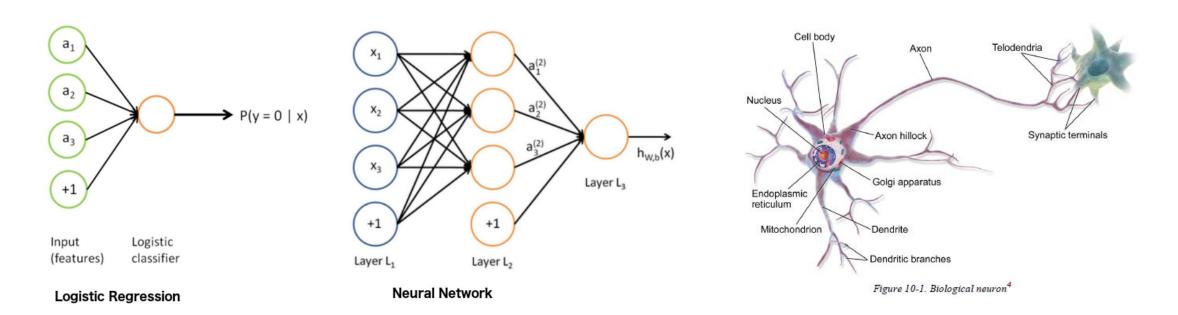
computed, 
$$r_i$$
 and compute the following:  $arg \min_{lpha} = \sum_{i=1}^m L(Y_i, F_{i-1}(X_i) + lpha h_i(X_i, r_{i-1}))$  where

L(Y, F(X)) is a differentiable loss function.

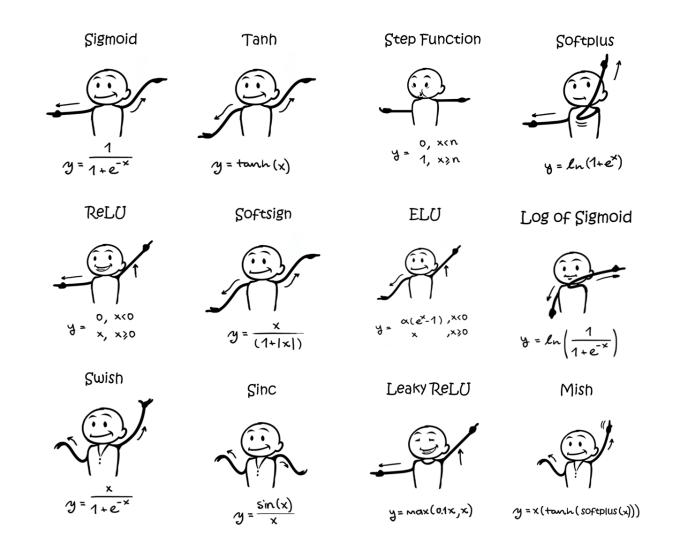
 Logistic regression can be regarded as a single layer of Neural network with sigmoid activation function



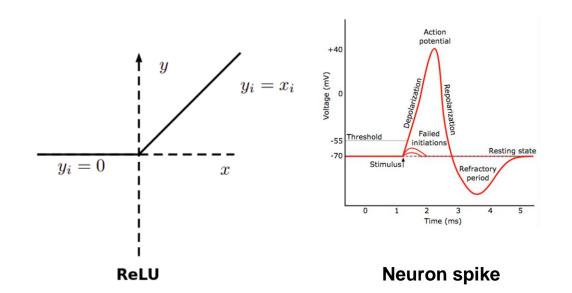
 Logistic regression can be regarded as a single layer of Neural network with sigmoid activation function

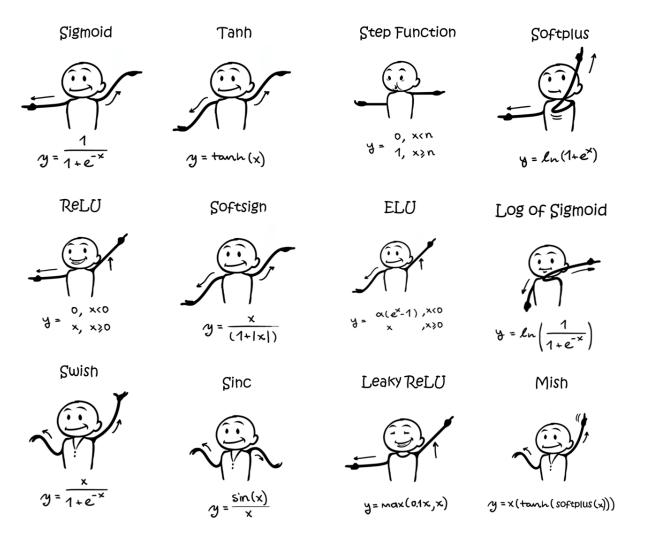


- Activation function
  - What if there is no activation function?

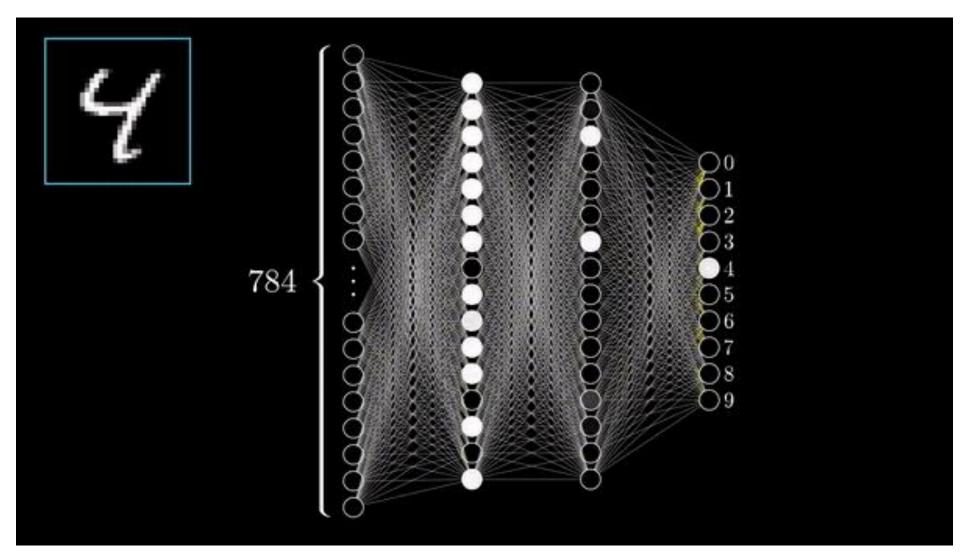


- Activation function
  - ReLU is a good default





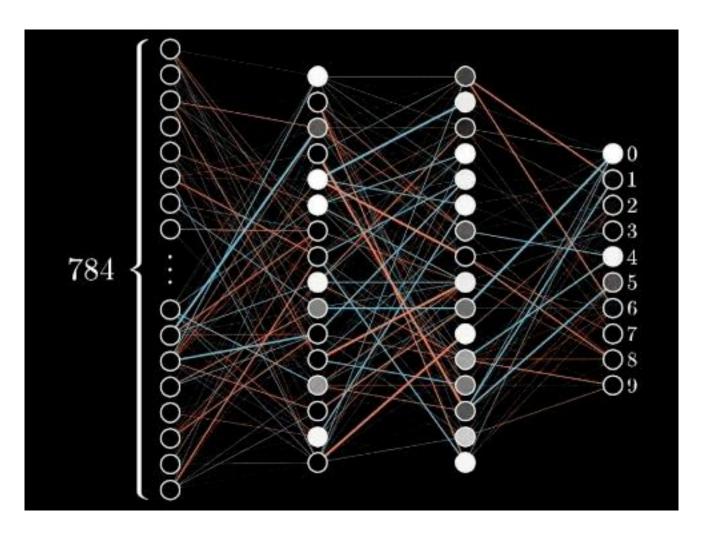
## Neural network example (forward propagation)



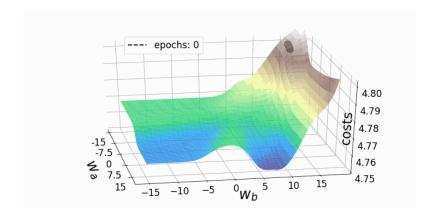
#### **Cross Entropy Loss:**

$$L(\Theta) = -\sum_{i=1}^k y_i \log{(\hat{y}_i)}$$

# Neural network example (back propagation)



$$w_{t+1} = w_t - \alpha \frac{\partial L}{\partial w_t}$$

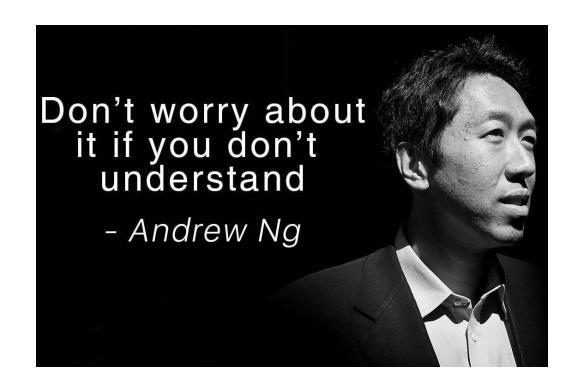


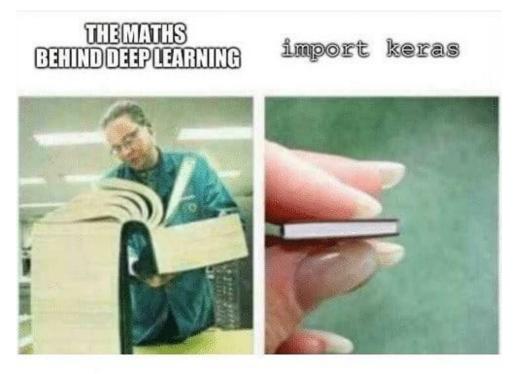
# Summary

Algorithm	Time complexity		Space	Advantage	Limitations
	Training	Testing	complexity		
Logistic Regression	O(n*d)	O(d)	O(d)	Simple, easy to implement and interpret Require less computation Can update easily using SGD	<ul> <li>Need regularization in high dimensional data</li> <li>Cannot handle non-linear problem</li> <li>Sensitive to outliers</li> </ul>
KNN	O(k*n*d)	O(n*d)	O(n*d)	<ul><li>Intuitive, easy to implement</li><li>Less assumption restriction</li><li>No pre-training is needed</li></ul>	<ul> <li>Slow speed with big dataset</li> <li>Don't perform well in imbalanced dataset or high dimensional data</li> <li>May be sensitive to outliers</li> </ul>
Naïve bayes	O(n*d)	O(d)	O(c*d)	Require less computation	Independence assumption may not hold
SVM	O(n^2)	O(n'*d)	O(n*d)	<ul><li>Can handle non-linear problem by kernel tricks</li><li>Generalize well in practice</li></ul>	Don't scale up easily
Decision tree	O(n*log(n)*d)	O(d)	O(td)	<ul><li>Easy to interpret, white box</li><li>Require little data preparation</li><li>Scale well to large datasets</li></ul>	<ul><li>Not robust to small variation</li><li>May overfit</li></ul>
Random forest	O(k*n*log(n)*d)	O(k*d)	O(k*td)	<ul><li>Reduce overfitting, improve accuracy</li><li>Built-in feature importance</li></ul>	Blackbox     A little longer training time

(n: # samples; d: # features; c: # classes; n': # support vectors; k: # trees/neighbors; td: tree depth;)

# Let's do some practice!





Machine learning be like

<sup>&</sup>gt; git clone https://github.com/wbvguo/qcbio-ML\_w\_Python.git

# Q&A