Extra exercises

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1. Cardano triplets¹

The triplet of integers (a, b, c) where $a, b, c \in \mathbb{N}_0$ bears the name of a Cardano triplet if it satisfies the following condition:

$$\sqrt[3]{a+b\sqrt{c}} + \sqrt[3]{a-b\sqrt{c}} = 1$$

- \bullet e.g. (2,1,5) is a Cardano triplet
- there exists 149 Cardano triplets for which $a\,+\,b\,+\,c\,\leq\,1000$
- how many Cardano triplets exist for which $a+b+c \leq 5000000?$

¹Project Euler - Problem 251 (slimmed down version)