

Problem 1. Suppose that we have a function $f(x)$ whose values are given by the following table.

x	0.0	0.2	0.4	0.6	0.8	1.0
$f(x)$	1.0	0.9	0.7	0.9	1.0	1.2

Use Simpson's Rule to approximate the value of $\int_0^{0.8} f(x)dx$ with $n = 2$.

$$\begin{aligned} & \frac{1}{3} \Delta x (f(0.0) + 4f(0.4) + f(0.8)) \\ &= \frac{1}{3} 0.4 (1.0 + 4 \cdot 0.7 + 1.0) = \boxed{0.64} \end{aligned}$$

Problem 2. Determine the value of the integral if it exists or else write DIVERGENT.

$$\begin{aligned} & \int_0^1 \frac{1}{\sqrt{x}} dx \\ &= \lim_{t \rightarrow 0^+} \int_t^1 \frac{1}{\sqrt{x}} dx = \lim_{t \rightarrow 0^+} 2\sqrt{x} \Big|_t^1 \\ &= \lim_{t \rightarrow 0^+} (2 - \sqrt{t}) = 2 - \sqrt{0} = \boxed{2} \end{aligned}$$