Ec141, Spring 2020

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Problem Set 1

<u>Due:</u> February 7th, 2020 (note this is prior to the final day to add/drop classes for the Spring 2018 semester)

Problem sets are due at 5PM in the GSIs mailbox. You may work in groups, but each student should turn in their own write-up (including a narrated/commented and executed Jupyter Notebook). Please use markdown boxes within your Jupyter notebook for narrative answers to the questions below.

1 The distribution of total factor productivity

The file semiconductor_firms.out contains several thousand firm-by-year observations for a sample of publicly traded semiconductor firms (NAICS 4-digit code 3344) drawn from the S&P Capital IQ - Compustat database. The following firm attributes, measured from 1998 to 2014 inclusive, are included:

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gvkey - Compustat firm identification code
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conm - firm name

year – calendar year

Y – total real sales by the firm (in millions of 2009 US\$)

K – capital stock (in millions of 2009 US\$)

L – employees (in thousands)

M – materials expenditures (in millions of 2009 US\$)

VA - total real valued added by the firm (in millions of 2009 US\$)

w - annual wage rate (in 2009 US\$)

i – real investment (in millions of 2009 US\$)

naics_4digits - NAICS four digit sector code for the firm

In this problem set you will use this dataset to study the distribution of productivity across firms. A nice introduction to economic research in this area is provided by Syverson (2011).

Preparing and exploring the dataset

1. How many firm-year observations are in the dataset?

- 2. How many distinct firms are in the dataset?
- 3. In 2014 what was the aggregate total sales across all semiconductor firms in the dataset?
- 4. How many employees did these firms employ in total?
- 5. In 2014 compute the average, standard deviation and 5th, 25th, 50th, 75th and 95th percentiles of total sales, capital stock, employees, materials, and investment across all firms in your dataset. Display this information in an easy-to-read table.
- 6. Write a few sentences summarizing your dataset.

Profit maximization

Assume that in each period t output, Y_t , is produced using capital, K_t , labor, L_t , and materials, M_t , according to the production technology

$$Y_t = A_t K_t^{1-\alpha-\beta} L_t^{\alpha} M_t^{\beta}, \tag{1}$$

where A_t is a factor neutral shifter or total factor productivity. Let R_t and W_t be the prevailing rental rate for capital and wage rate for labor. Assume that firms maximize profits – taking their output price, P_t , as fixed (i.e., perfect competition):

$$\max_{k_t, l_t, m_t} P A_t k_t^{1-\alpha-\beta} l_t^{\alpha} m_t^{\beta} - R_t k_t - W_t l_t - m_t.$$

Let K_t , L_t and M_t denote the profit-maximizing input choices made by the firm. Show that the firm's first order conditions for labor and materials imply that

$$\alpha = \frac{W_t L_t}{Y_t}, \ \beta = \frac{M_t}{Y_t}.$$

Measuring productivity

Note that \mathbf{Y} in the dataset corresponds to P_tY_t in the theoretical model; our theory is about physical units of output, Y_t , but what we observe in the financial filings of firms is generally total sales, P_tY_t . It is this latter quantity which is recorded as \mathbf{Y} in the dataset. This discrepancy between data and theory has numerous implications which we will gloss over for the time being, but return to later in the course.

1. Construct a measure of the firm's wage bill each period, W_tL_t , using the formula

wage bill =
$$\frac{(L \times 1,000) \times w}{1,000,000}.$$

Explain the reasoning underlying this formula.

2. Let i index firms and t years. Consider the following estimate of firm i's elasticity of output with respect to labor:

$$\hat{\alpha}_i = \frac{1}{T_i} \sum_{t} \frac{\text{wage bill}_{it}}{\mathbf{Y}_{it}}$$

where the summation is over all years firm i is in the dataset and T_i denotes the total number of years firm i is in the dataset. Similarly estimate firm i's elasticity of output with respect to materials as:

$$\hat{\beta}_i = \frac{1}{T_i} \sum_{t} \frac{\mathbf{M}_{it}}{\mathbf{Y}_{it}}.$$

Explain the reasoning underlying these elasticity measures.

- 3. Compute the average, standard deviation and 5th, 25th, 50th, 75th and 95th percentiles of $\hat{\alpha}_i$ and $\hat{\beta}_i$ across all firms in your dataset. Display this information in a table.
- 4. Let $\hat{\alpha}$ and $\hat{\beta}$ be the *median* firm-specific elasticity estimates. Compute these.
- 5. Construct the following measure of productivity for each firm-year in your dataset:

$$exttt{TFPR}_{it} = rac{ exttt{Y}_{it}}{ exttt{K}_{it}^{1-\hat{lpha}-\hat{eta}} extst{L}_{it}^{\hat{lpha}} exttt{M}_{it}^{\hat{eta}}}.$$

How does this measure relate to A_{it} – total factor productivity – as defined in the theoretical model?

6. In 2014 compute the average, standard deviation and 5th, 25th, 50th, 75th and 95th percentiles of $TFPR_{it}$ across all firms in your dataset. Display this information in a table. Are the productivity differences across firms larger or smaller than you expected?

Productivity decomposition

1. Let $S_t = Y_t / \mathbb{E}[Y_t]$ and show that

$$\mathbb{E}\left[S_{t}A_{t}\right] = \mathbb{E}\left[S_{t}\right]\mathbb{E}\left[A_{t}\right] + \mathbb{C}\left(S_{t}, A_{t}\right)$$

$$= \mathbb{E}\left[A_{t}\right] + \left[\frac{\mathbb{C}\left(S_{t}, A_{t}\right)}{\mathbb{V}\left(A_{t}\right)}\right]\mathbb{V}\left(A_{t}\right)$$

$$= \mathbb{E}\left[A_{t}\right] + \rho_{t}\mathbb{V}\left(A_{t}\right)$$

Discuss how this expression might be used to understand industry-level change in productivity over time.

- 2. Equate A_t with TFPR_{it} and S_i with $Y_{it}/\frac{1}{n}\sum_{i=1}^{N}\sum_{t=1}^{T_i}Y_{it}$; here nequals the total number of firm-year observations in the dataset. Compute the sample analogs of $\mathbb{E}\left[A_t\right]$, ρ_t and $\mathbb{V}\left(A_t\right)$ for each year from 1998 to 2014.
- 3. Use your calculations above to discuss the evolution of productivity in the semi-conductor industry from 1998 to 2014. Support your answer with plots and/or tables.

References

Syverson, C. (2011). What determines productivity. *Journal of Economic Literature*, 49(2), 326 – 365.