

```
#-----  
  
# Import necessary modules  
  
#-----  
  
import sys  
  
from qiskit import QuantumProgram  
  
import Qconfig  
  
import Basic_gates  
  
import math  
  
from random import randint  
  
import control_unitaries  
  
import xlswriter  
  
#-----  
  
# global variables  
  
#-----  
  
Counts = 0  
  
A = 0  
  
Ran_Quantum_period_finding = 0  
  
global m  
  
m = 0  
  
#-----  
  
# The function to compute GCD using Euclid's method  
  
# Input : Two number to X and Y for which a GCD is to be computed  
  
# Output : GCD of two given numbers  
  
#-----  
  
def gcd(x,y):  
    while y != 0:
```

$(x, y) = (y, x \% y)$

return x

```
#-----  
# The function to construct the unitary based on a  
# Input : Quantum program object, the Circuit name and the quantum register name, and a  
# Output : None. The relevant circuit is made.  
#-----  
  
def cmod(Quantum_program_object,Circuit_name,Quantum_register_name,a):  
    # Get the circuit and the quantum register by name  
    qc = Quantum_program_object.get_circuit(Circuit_name)  
    qr = Quantum_program_object.get_quantum_register(Quantum_register_name)  
  
    # Construct unitary based on a  
    if a == 2:  
        qc.cswap(qr[4],qr[3],qr[2])  
        qc.cswap(qr[4],qr[2],qr[1])  
        qc.cswap(qr[4],qr[1],qr[0])  
    if a == 4 or a == 11 or a == 14:  
        qc.cswap(qr[4],qr[2],qr[0])  
        qc.cswap(qr[4],qr[3],qr[1])  
        qc.cx(qr[4],qr[3])  
        qc.cx(qr[4],qr[2])  
        qc.cx(qr[4],qr[1])  
        qc.cx(qr[4],qr[0])  
    if a == 7:
```

```
qc.cswap(qr[4],qr[1],qr[0])
qc.cswap(qr[4],qr[2],qr[1])
qc.cswap(qr[4],qr[3],qr[2])
qc.cx(qr[4],qr[3])
qc.cx(qr[4],qr[2])
qc.cx(qr[4],qr[1])
qc.cx(qr[4],qr[0])
```

```
if a == 8:
```

```
    qc.cswap(qr[4],qr[1],qr[0])
    qc.cswap(qr[4],qr[2],qr[1])
    qc.cswap(qr[4],qr[3],qr[2])
```

```
if a == 13:
```

```
    qc.cswap(qr[4],qr[3],qr[2])
    qc.cswap(qr[4],qr[2],qr[1])
    qc.cswap(qr[4],qr[1],qr[0])
    qc.cx(qr[4],qr[3])
    qc.cx(qr[4],qr[2])
    qc.cx(qr[4],qr[1])
    qc.cx(qr[4],qr[0])
```

```
#-----
```

```
# The function to compute QFT
```

```
# Input : Circuit, quantum bits, and number of quantum bits
```

```
# Output : None. Circuit is created and saved
```

```
#-----
```

```
def
```

```
qft(Quantum_program_object,Circuit_name,Quantum_register_name,Smallest_Quantum_register_number,Size_of_QFT):
```

```
# Get the circuit and the quantum register by name
```

```
qc = Quantum_program_object.get_circuit(Circuit_name)
```

```
qr = Quantum_program_object.get_quantum_register(Quantum_register_name)
```

```
s = Smallest_Quantum_register_number
```

```
for j in range(Size_of_QFT):
```

```
    for k in range(j):
```

```
        qc.cu1(math.pi/float(2**(j-k)), qr[s+j], qr[s+k])
```

```
    qc.h(qr[s+j])
```

```
#-----
```

```
# The function to find period using the Quantum computer
```

```
# Input : a and N for which the period is to be computed.
```

```
# Output : period r of the function  $a^x \bmod N$ 
```

```
#-----
```

```
def period(a,N):
```

```
    global Ran_Quantum_period_finding
```

```
    Ran_Quantum_period_finding = 1
```

```
# Create the first QuantumProgram object instance.
```

```
qp = QuantumProgram()
```

```
#qp.set_api(Qconfig.APIToken, Qconfig.config["url"])
```

```
# TO DO : generalize the number of qubits and give proper security against rogue input.
```

```
# Create the first Quantum Register called "qr" with 12 qubits
```

```
qr = qp.create_quantum_register('qr', 5)
```

```
# Create your first Classical Register called "cr" with 12 bits
```

```
cr = qp.create_classical_register('cr', 3)
```

```
# Create the first Quantum Circuit called "qc" involving your Quantum Register "qr"
```

```
# and the Classical Register "cr"
```

```
qc = qp.create_circuit('Period_Finding', [qr], [cr])
```

```
# Get the circuit and the registers by name
```

```
Shor1 = qp.get_circuit('Period_Finding')
```

```
Q_reg = qp.get_quantum_register('qr')
```

```
C_reg = qp.get_classical_register('cr')
```

```
# Create the circuit for period finding
```

```
# Initialize qr[0] to  $|1\rangle$ 
```

```
Shor1.x(Q_reg[0])
```

```
# Step one : apply  $a^{**4} \bmod 15$ 
```

```
Shor1.h(Q_reg[4])
```

```
# Controlled Identity on the remaining 4 qubits. Which is equivalent to doing nothing
```

```
Shor1.h(Q_reg[4])
```

```
Shor1.measure(Q_reg[4], C_reg[0])
```

```
# Reinitialize to  $|0\rangle$ 
```

```
Shor1.reset(Q_reg[4])
```

```
# Step two : apply  $a^{**2} \bmod 15$ 
```

```
Shor1.h(Q_reg[4])
```

```
# Controlled unitary. Apply  $a \bmod 15$  twice.
```

```

for k in range(2):

    cmod(qp,'Period_Finding','qr',a)

    if C_reg[0] == 1 :

        Shor1.u1(pi/2.0,Q_reg[4])

        Shor1.h(Q_reg[4])

        Shor1.measure(Q_reg[4],C_reg[1])

# Reinitialize to |0>

Shor1.reset(Q_reg[4])


# Step three : apply 11 mod 15

Shor1.h(Q_reg[4])

# Controlled unitary. Apply a mod 15

cmod(qp,'Period_Finding','qr',a)

# Feed forward and measure

if C_reg[1] == 1 :

    Shor1.u1(pi/2.0,Q_reg[4])

if C_reg[0] == 1 :

    Shor1.u1(pi/4.0,Q_reg[4])

    Shor1.h(Q_reg[4])

    Shor1.measure(Q_reg[4],C_reg[2])


# Run the circuit

#qp.set_api(Qconfig.APIToken, Qconfig.config['url']) # set the APIToken and API url

simulate = qp.execute(["Period_Finding"], backend="local_qasm_simulator", shots=1,timeout=500)

simulate.get_counts("Period_Finding")

#print(simulate)

```

```
data = simulate.get_counts("Period_Finding")
```

```
#print(data)
```

```
data = list(data.keys())
```

```
#print(data)
```

```
r = int(data[0])
```

```
#print(r)
```

```
l = gcd(2**3,r)
```

```
#print(l)
```

```
r = int((2**3)/l)
```

```
#print(r)
```

```
return r
```

```
#-----
```

```
# The main function to compute factors
```

```
# Input : The number to be factored, N
```

```
# Output : Factors of the number
```

```
#-----
```

```
def Factorize_N(N):
```

```
    factors = [0,0]
```

```
#-----
```

```
# Step 1 : Determine the number of bits based on N; n = [log2(N)]
```

```
#-----
```

```
    n = math.ceil(math.log(N,2))
```

```
#-----
```

```
# Step 2 : Check if N is even. In that case return 2 and the remaining number as factors
```

```
#-----
```

```
if N % 2 == 0:
```

```
    factors = [2,N/2]
```

```
    return factors
```

```
#-----
```

```
# Step 3 : Check if N is of the form  $P^k$ , where P is some prime factor. In that case return P and k.
```

```
#-----
```

```
# The step has been eliminated for simulation purposes.
```

```
#-----
```

```
# Step 4 : Choose a random number between 2...(N-1).
```

```
#-----
```

```
while True:
```

```
    a = randint(2,N-1)
```

```
    global A
```

```
    A = a
```

```
#-----
```

```
# Step 5 : Take GCD of a and N.  $t = \text{GCD}(a,N)$ 
```

```
#-----
```

```
    t = gcd(N,a)
```

```
    if t > 1:
```

```
        factors = [t,N/t]
```

```
        return factors
```

```
#-----
```

```
# Step 6 :  $t = 1$ . Hence, no common period. Find Period using Shor's method
```

```
#-----
```

```
    r = period(a,N)
```

```
    if (r%2 == 0) and (((a**(r/2))+1)%N != 0) and (r != 0) and (r != 8):
```



```
break
```

```
global Counts
```

```
Counts = Counts + 1
```

```
factor_1 = gcd((a**(r/2))+1,N)
```

```
factor_2 = N/factor_1
```

```
factors = [factor_1,factor_2]
```

```
return factors
```

```
#-----
```

```
# Running the Shor's algorithm version 1
```

```
#-----
```

```
#-----
```

```
# Step 0 : Take the input N
```

```
#-----
```

```
factors_list = list()
```

```
A_used = list()
```

```
Ran_QPF = list()
```

```
Total_counts = list()
```

```
if __name__ == '__main__':
```

```
    #global m
```

```
    for m in range(100):
```

```
        N = 15
```

```
        factors_found = Factorize_N(N)
```

```
        factors_list.append(factors_found)
```

```
    #ws.write(row,col,A)
```

```

#ws.write(row,col+1,Counts)

#ws.write(row,col+2,factors[0])

#ws.write(row,col+3,factors[1])

#ws.write(row,col+4,Ran_Quantum_period_finding)

#row = row + 1

#print("The Number being factorized is 15")

#print("Factors are = ",factors)

#print("Number of times the quantum circuit did not give correct period = ",Counts)

#print ("The parameter a used = ", A)

print("Run ", m)

A_used.append(A)

Ran_QPF.append(Ran_Quantum_period_finding)

Total_counts.append(Counts)

Counts = 0

Ran_Quantum_period_finding = 0

```

```

if m == 99:

```

```

    wb = xlswriter.Workbook('log.xlsx')

    ws = wb.add_worksheet('Data')

    row = 0

    col = 0

    ws.write(row,col,'a used for factorizing')

    ws.write(row,col+1,'Number of times the quantum circuit did not give correct period')

    ws.write(row,col+2,'Factor1')

    ws.write(row,col+3,'Factor2')

```

```
ws.write(row,col+4,'Ran_Quantum_period_finding?')
```

```
row = row + 1
```

```
for k in range(100):
```

```
    ws.write(row,col,A_used[k])
```

```
    ws.write(row,col+1,Total_counts[k])
```

```
    ws.write(row,col+2,factors_list[k][0])
```

```
    ws.write(row,col+3,factors_list[k][1])
```

```
    ws.write(row,col+4,Ran_QPF[k])
```

```
    row = row + 1
```

```
wb.close()
```