

1.) Explanation of Implementation

- **DFS**
 - **Recursive Implementation**
 - start at S
 - loop through the neighbors of the current node adding each neighbor to the path
 - check if the neighbor had already been visited
 - if not, recursive call the function with the neighbor as the start
 - check if start is the goal
 - if true return
 - if there are no more neighbors that haven't been visited then go back up a recursive level and pop the most recent node off the path
 - **Stack**
 - start at S
 - loop through stack popping on each iteration
 - if the node just popped is the goal return
 - else loop through neighbors for the node popped
 - add those to the stack
 - if no neighbors for node that haven't been visited pop most recent node off of path
- **BFS**
 - **Recursion**
 - start at S
 - check if start contains any entries
 - loop through the nodes in start
 - if node is goal get path by retracing through parent list and return
 - else loop through neighbors of the current node adding each new node to the next level
 - also add new node as an entry to the parents list with a pointer to its parent
 - recursive call function with next level as the start
 - **Queue**
 - start at S
 - loop through queue popping the first entry in every iteration
 - check if node had been visited
 - check if node is goal
 - if node is goal make path by retracing path through parents list
 - reverse path from parents list so that it is the right way
 - else loop through the neighbors of the current node and add them to the queue
- **UCS**
 - **Undirected**
 - start at S
 - get neighbors of S
 - loop through the neighbors getting their weighted edges and adding them to the priority queue
 - loop through the queue
 - pull highest priority
 - check if node is goal
 - if node is goal loop through the queue pulling the highest priority and comparing the cost to the cost to get to the goal
 - if cost is equal add to a list
 - loop through the list and find each nodes parent in the visited nodes starting at S
 - add G if not already in the path

- return
- else get the neighbors for the current node and add them along with the total cost to get to them into the priority queue
- **Directed**
 - start at S
 - get neighbors of S
 - loop through the neighbors getting their weighted edges and adding them to the priority queue
 - loop through the queue
 - pull highest priority
 - check if node is goal
 - create path by retracing through the parents list
 - reverse path so that it is the right way
 - return
 - else get the neighbors for the current node and add them along with the total cost to get to them into the priority queue
 - add the neighbor as an entry into the parents list with a pointer to its parent
- **get_neighbors()**
 - loops through the neighbors of the node and returns a list containing the neighbors to the node
- **get_weight_of_edge()**
 - returns the weight of the edge between two nodes in the graph
- **PriorityQueue**
 - uses heapq to create a priority queue using a heap
 - is_empty() returns true if the queue is empty and false otherwise
 - insert_with_priority() pushes the edge along with its weight onto the heap
 - pull_highest_priority() returns the lowest priority element in the heap multiplied by -1 because in the UCS algorithm the lower the number the higher the priority

2.) Results

- **BFS**
 - **Undirected**
 - States Expanded: ['S', 'D', 'E', 'P', 'B', 'C', 'H', 'R', 'Q', 'A', 'F', 'G']
 - Path Returned: ['S', 'D', 'C', 'F', 'G']
 - *out put as list/matrix and recursion/queue was the same
 - **Directed**
 - States Expanded: ['S', 'D', 'E', 'P', 'B', 'C', 'H', 'R', 'Q', 'A', 'F', 'G']
 - Path Returned: ['S', 'E', 'R', 'F', 'G']
 - *out put was same for list/matrix and recursion/queue
- **DFS**
 - **Undirected**
 - States Expanded: ['S', 'D', 'B', 'A', 'C', 'F', 'G']
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- **UCS**
 - **Undirected**
 - States Expanded: ['S', 'P', 'D', 'B', 'H', 'E', 'A', 'R', 'C', 'Q', 'F', 'G']
 - Path Returned: ['S', 'D', 'E', 'R', 'F', 'G']
 - *Output was the same for list/matrix

- **Directed**

- States Expanded: ['S', 'P', 'D', 'B', 'E', 'A', 'R', 'F', 'C', 'G']
- Path Returned: ['S', 'D', 'E', 'R', 'F', 'G']
- *Output was the same for list/matrix

3.) **Imported modules**

- heapq