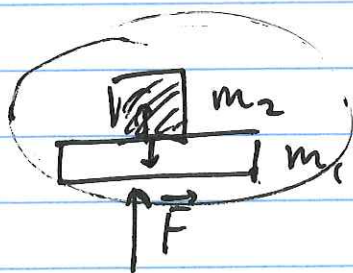


Top Hat

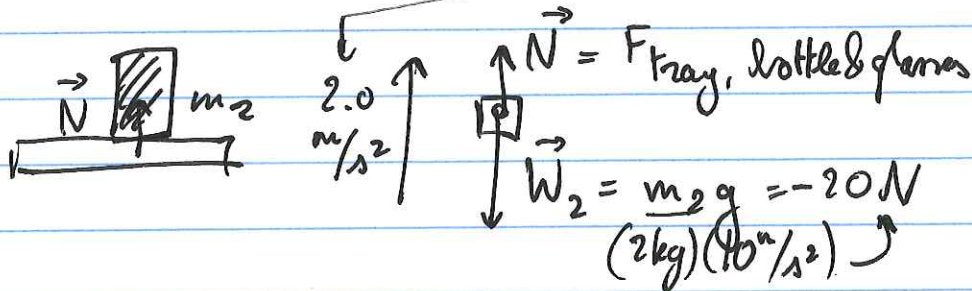


$$\vec{F}_{\text{net}} = \vec{F} + \vec{W}$$

$$F_{\text{net},y} = F - (m_1 + m_2)g$$

$$30\text{N} - (2.5\text{kg})(10\text{m/s}^2) = 30\text{N} - 25\text{N} = 5\text{N}$$

$$\rightarrow a = \frac{F_{\text{net}}}{m} = \frac{5\text{N}}{2.5\text{kg}} = +2\text{m/s}^2$$

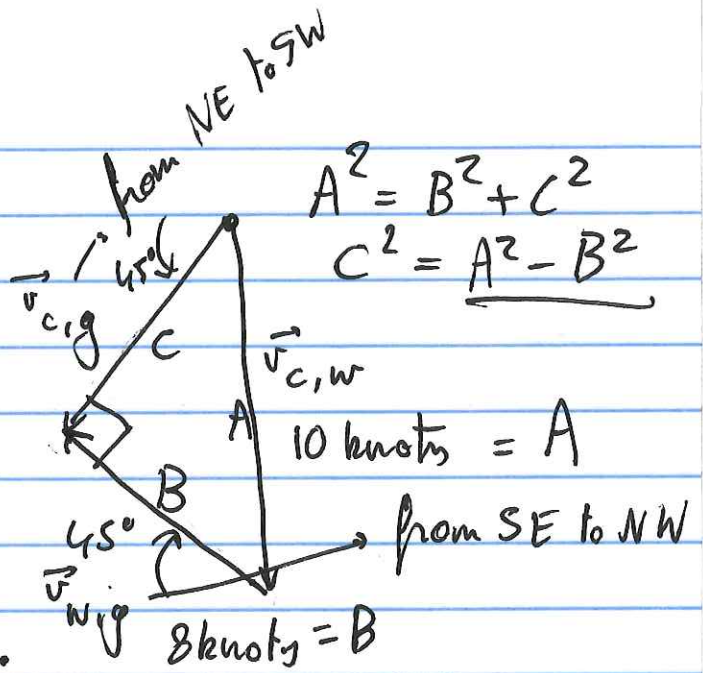
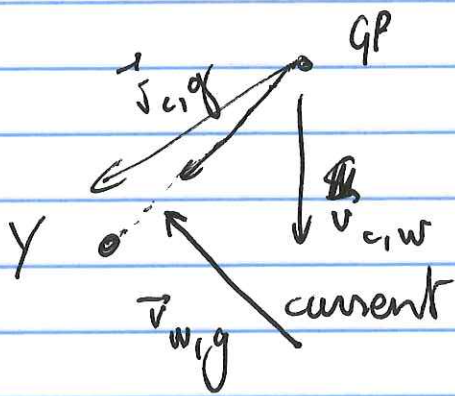
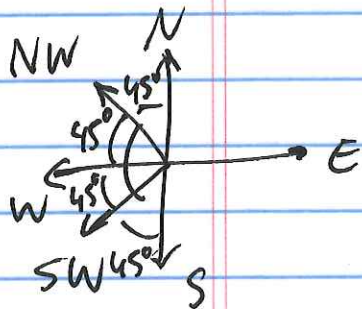


$$m_2 a = F_{\text{tray, bottle}} - 20\text{N}$$

$$2\text{kg} \cdot 2\text{m/s}^2$$

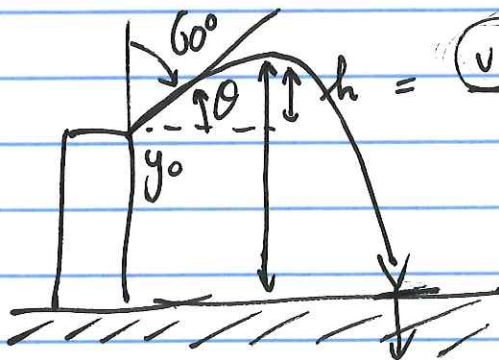
$$4\text{N} \rightarrow F_{\text{tray, bottle}} = 4\text{N} + 20\text{N} = 24\text{N}$$

$$\vec{F}_{\text{bottle, tray}} = -\vec{F}_{\text{tray, bottle}} = -24\text{N}$$



$$|\vec{v}_{c,g}| = \sqrt{10^2 - 8^2} \text{ knots} = \sqrt{100 - 64} \text{ knots} = \sqrt{36} \text{ knots} = 6 \text{ knots}$$

$$6 \text{ knots} = 6 \text{ nm/hour} \rightarrow 2 \text{ nm} \rightarrow \frac{1}{3} \text{ hour}$$



$$h = \frac{v_0^2 \sin^2 \theta}{2g} = 0.2 \text{ m} = \frac{(4 \text{ m/s})^2 (\frac{1}{2})^2}{2(10 \text{ m/s}^2)} + 16.0 \text{ m}$$

$y_0 \rightarrow y_{\text{max}} = 16.2 \text{ m}$

$$v_{0,y} = v_0 \sin \theta = 4 \text{ m/s} \cdot \sin 30^\circ = 2 \text{ m/s}$$

$$y = 0 = y_0 + \underbrace{v_{0,y}}_{2 \text{ m/s}} t - \frac{1}{2} g t^2 \quad \text{only } y\text{-components}$$

$$\hookrightarrow 0 = 16 + 2t - 5t^2 \rightarrow t = \frac{-2 \pm \sqrt{4 + 320}}{2(-5)}$$

$$v_y = v_{0,y} - g t = 2 \text{ m/s} - 20 \text{ m/s} = -18 \text{ m/s}$$

$$= \begin{cases} -1.8 \text{ s} \\ +2.0 \text{ s} \end{cases}$$

$$h = \frac{v_o^2 \sin^2 60^\circ}{2g} = \frac{(4 \text{ m/s})^2 \left(\frac{\sqrt{3}}{2}\right)^2}{2g} = 0.6 \text{ m}$$

$$\hookrightarrow y_{\text{max}} = 16.0 \text{ m} + 0.6 \text{ m} = \underline{16.6 \text{ m}}$$

$$v_{y0,y} = 4 \text{ m/s} \sin 60^\circ = 4 \cdot \frac{\sqrt{3}}{2} \text{ m/s}$$

$$\underline{2\sqrt{3} \text{ m/s}}$$

$$y=0 = 16.0 \text{ m} + 2\sqrt{3} \text{ m/s} t - 5 \text{ m/s}^2 t^2$$

$$\hookrightarrow t = \frac{-2\sqrt{3} \text{ m/s} \pm \sqrt{\dots}}{2(-5 \text{ m/s}^2)}$$

$$\underline{v_y = v_{0,y} - gt}$$

$$\cancel{v_y^2} = v_{0,y}^2 - 2g(y - y_0)$$

$$v_{ay}^2 = (2\sqrt{3})^2 - (20)(16 \text{ m}) \rightarrow \sqrt{\dots}$$



\* Gravitational force in circular motion

$$\underline{a_c} = r\omega^2 \rightarrow F_c = F_g = G \frac{M_1 M_2}{r^2} = m a_c$$

$$F_g = G \frac{M_{\text{Earth}} m_W}{r_E^2} \rightarrow a_c = \frac{F_g}{m_W}$$

$$r_E = 6380 \text{ km}$$

$$M_E = 5.98 \times 10^{24} \text{ kg}$$

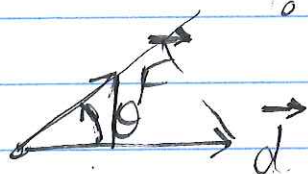
$$G = 6.673 \times 10^{-11} \frac{\text{N m}^2}{\text{kg}^2}$$

$$a_c = G \frac{M_{\text{Earth}}}{(r_E^2)} = \underline{9.80 \text{ m/s}^2}$$

$$\vec{W} = m \vec{g}$$

# Work & Energy

Work = force times distance of motion parallel to the direction of the force



$$W = |\vec{F}| \cdot |\vec{d}| \cdot \cos \theta$$

$$d_F = |\vec{d}| \cos \theta$$

$$\rightarrow W = |\vec{F}| d_F = F d \cos \theta$$

$$W = d F_d = F d \cos \theta$$

$$F_d = F \cos \theta$$

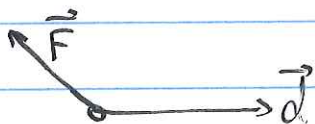
$$0 < \theta < 90^\circ \rightarrow \cos \theta > 0 \rightarrow W > 0$$

add energy

$$\theta = 90^\circ \rightarrow \cos \theta = 0 \rightarrow W = 0$$



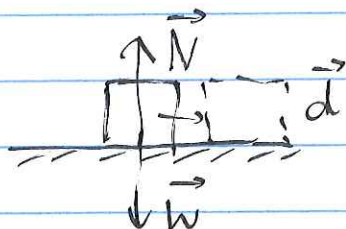
$$\theta > 90^\circ$$



$$\rightarrow W < 0$$

lose energy

$$\vec{F} \perp \vec{d}$$



$$\vec{N} \perp \vec{d}$$

$$\rightarrow W_N = 0$$

