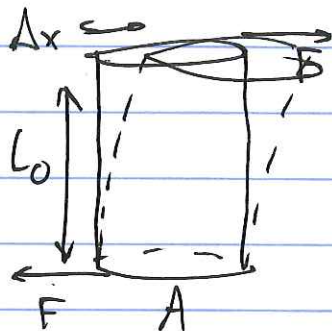


## \* Fluids (statics)

- no resistance to deformation (ideal fluid)
- yields to shear forces: shear modulus is zero



$$\frac{F}{A} = S \frac{\Delta x}{L_0}$$

$$F=0 \rightarrow S=0$$

no force  $F$  required for any  $\Delta x$

Examples: liquids, gases, glasses

## \* Two quantities that describe the static fluid

1) Pressure  $P$

2) Density  $\rho$

\* Density:  $\rho = \frac{M}{V} = \frac{\text{mass}}{\text{volume}}$  in units  $\frac{\text{kg}}{\text{m}^3}$

$$\text{H}_2\text{O}: 1000 \text{ kg/m}^3 = 1 \text{ kg/dm}^3 = 1 \text{ g/cm}^3$$

definition liter

float  $\left\{ \begin{array}{l} \text{sink} \\ \text{air: } 1.29 \text{ kg/m}^3 \\ \text{blood: } 1060 \text{ kg/m}^3 \\ \text{ice: } 920 \text{ kg/m}^3 \end{array} \right.$

object < liquid: float  
object > liquid: sink

neutron star:  $5 \times 10^{17} \text{ kg/m}^3 \sim$  inside nucleus of an atom

$$\text{s.g.} = \text{specific gravity} = \frac{\rho}{\rho_{\text{H}_2\text{O}}}$$

$$\text{ice: s.g.} = \frac{920 \text{ kg/m}^3}{1000 \text{ kg/m}^3} = 0.920$$

$$\text{blood: s.g.} = 1.060$$

s.g.  $< 1$  : object float on water

$$\times \text{ Pressure: } P = \frac{F}{A} = \frac{\text{force}}{\text{area}} \text{ in units } \frac{\text{N}}{\text{m}^2} = \text{Pa}$$

Blaise Pascal: - first mechanical calculator  
(1623-1662) - hydraulic presses

$$\begin{aligned} \text{Other units of pressure: } 1 \text{ atm} &= 101.3 \text{ kPa} \quad \text{bar} \\ &= 1013 \times 10^5 \text{ Pa} \\ &\quad \pm 0.07 \times 10^5 \text{ Pa} \\ &\quad \text{weather} \end{aligned}$$

$$\begin{aligned} 1 \text{ atm} &= 14.7 \text{ lbs/in}^2 \text{ (psi)} \rightarrow \text{psia} = \\ &= 760 \text{ Torr} = 760 \text{ mm Hg} \end{aligned}$$

Alternate definitions of density:

$$\text{s.g.} = \text{specific gravity} = \frac{\rho}{\rho_{\text{H}_2\text{O}}} \rightarrow \text{ice has s.g.} = 0.926$$

An object will float if  $\rho_{\text{object}} < \rho_{\text{liquid}} \rightarrow \text{ice floats in water}$

\* Pressure:

$$P = \frac{F}{A} = \frac{\text{force}}{\text{area}} \text{ in units } \frac{\text{N}}{\text{m}^2} = \text{Pa, Pascal}$$

Blaise Pascal, 1623-1662, French math/phys/phil/inventor

- first mechanical calculator
- hydraulic press

Other units of pressure:  $1 \text{ atm} = 101.3 \text{ kPa}$

$$1 \text{ atm} = 14.7 \text{ lbs/in}^2 \text{ (psi)}$$

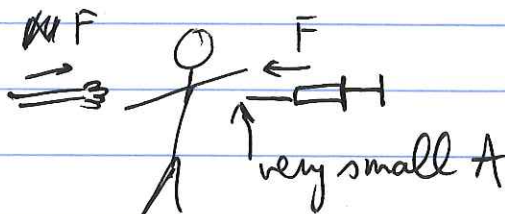
$$= 760 \text{ Torr} = 760 \text{ mm Hg}$$

$$= 1.013 \text{ (bar)}$$

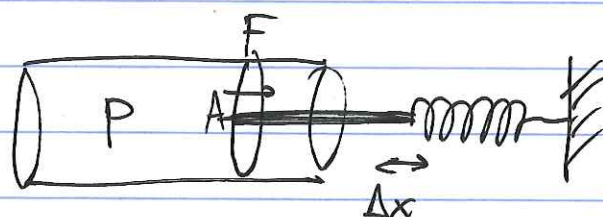
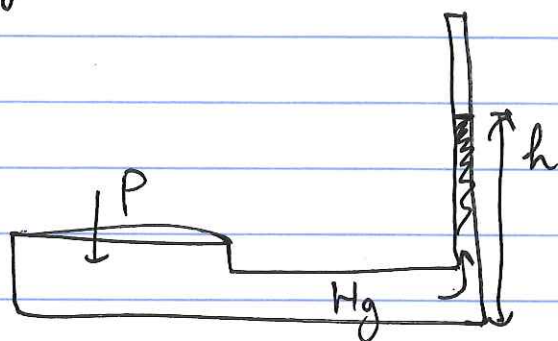
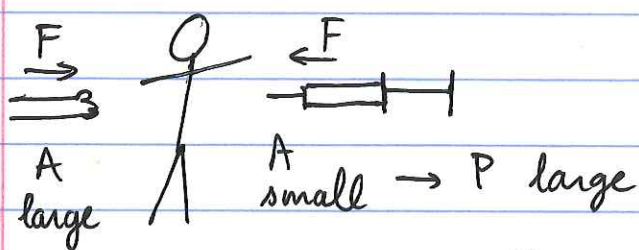
$$= 1.013 \times 10^5 \text{ Pa} \pm 0.07 \times 10^5 \text{ Pa}$$

weather

A smaller area with the same force  $\rightarrow$  larger pressure



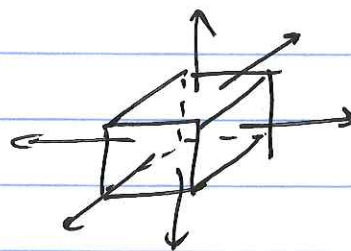
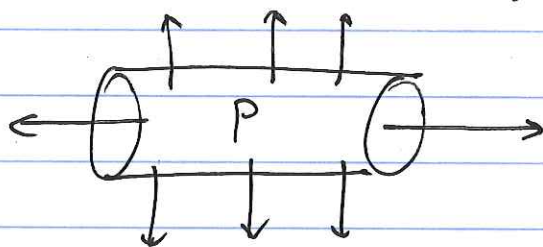




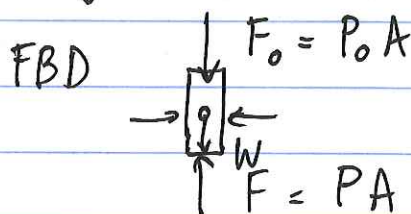
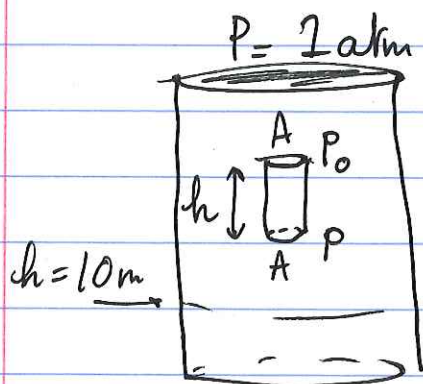
$$F = P \cdot A = k \Delta x$$

$$P = \frac{k \Delta x}{A}$$

\* Force due to pressure is always in the perpendicular direction to the surface



\* Fluids under gravity : pressure will increase with depth



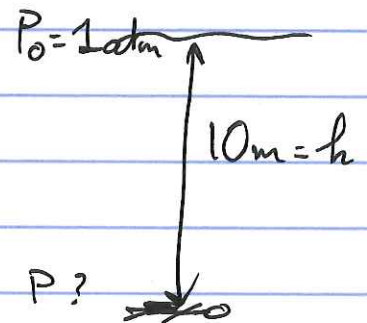
$$W = mg = \rho V g = \rho A h g$$

$$F_{\text{net}} = 0 = P A - P_0 A - \rho A h g = 0$$

$$\rightarrow \underline{P = P_0 + \rho g h}$$

What's the pressure when you are 10m under water?

$$\underset{\substack{\uparrow \\ 10\text{m}}}{P} = \underset{\substack{\uparrow \\ P_0}}{P_0} + \rho g h$$



$$= 10^5 \text{ Pa} + (1000 \text{ kg/m}^3)(10 \text{ m/s}^2) \cdot P?$$

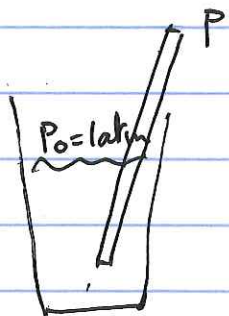
$$= 10^5 \text{ Pa} + 10^5 \text{ Pa} = \underline{2 \times 10^5 \text{ Pa}}$$

$$760 \text{ mm Hg} = 0.76 \text{ m Hg}$$

$$\rho_{\text{Hg}} = 13.6 \times \rho_{\text{H}_2\text{O}}$$

What is the additional force on the eardrum,  $A = 1 \text{ cm}^2$ ?

$$F = P \cdot A = (10^5 \text{ Pa}) \left( \underset{10^{-4} \text{ m}^2}{0.0001 \text{ m}^2} \right) = \underset{10 \text{ N}}{10 \text{ Pa} \cdot \text{m}^2}$$



$$\rho g h = (1000 \text{ kg/m}^3)(10 \text{ m/s}^2)(0.1 \text{ m})$$

$$= \underline{1000 \text{ Pa}}$$

\* Pascal's principle:

Pressure everywhere at same depth will be the same.

