

PHYS 107 - Week 12 - Wednesday

* Laminar flow versus turbulence

Video Laminar Flow

laminar flow: no mixing, streamlined
↓

turbulent flow: eddies, swirls, caused by - swift flow
- obstacles, corners

Where is the transition? How do we know when flow will be turbulent or laminar?

Define Reynolds number $N_R = \frac{2 \rho v r}{\eta}$ (for tube of radius r)
(units: none)

If $N_R > 3000$: turbulent
If $N_R < 2000$: laminar
in between: ill-determined, unstable

Flow will be more turbulent when:

- density higher
- velocity higher
- characteristic length scale larger
- viscosity smaller

Scaling up or down: if N_R is the same for a scaled up or scaled down version of geometry, system, then the flow will behave similarly

Example: At what speed will blood flow turn turbulent in an artery that has $r = 2 \text{ mm}$?

$$\rho = 1030 \text{ kg/m}^3, \eta = 2.08 \times 10^{-3} \text{ Pa}\cdot\text{s}$$

$$N_R = 3000 \text{ if } v = \frac{N_R \eta}{2 \rho r} = 3.0 \text{ m/s}$$

Note that the calculated blood flow is 1.9 m/s in pulmonary artery. Obstruction of half diameter \rightarrow turbulence!

* Generally $N_R = \frac{\rho v L}{\eta}$ where $L =$ characteristic length
 $L = 2r$ for tube or sphere

Example: Tacoma Narrows bridge:

When will a cable of a suspension bridge cause turbulence?
at what wind speed

$$v = \frac{\eta N_R}{\rho L} = \frac{(10^{-3} \text{ Pa}\cdot\text{s})(3000)}{(1.29 \text{ kg/m}^3)(21 \text{ inch})} = 4 \text{ m/s}$$

9 mph

Phenomenon called "vortex shedding" causes the bridge to vibrate "in resonance" (see later).

Video Tacoma Narrows

* Diffusion, random walk, Brownian motion

Brownian motion of nano-particles in water

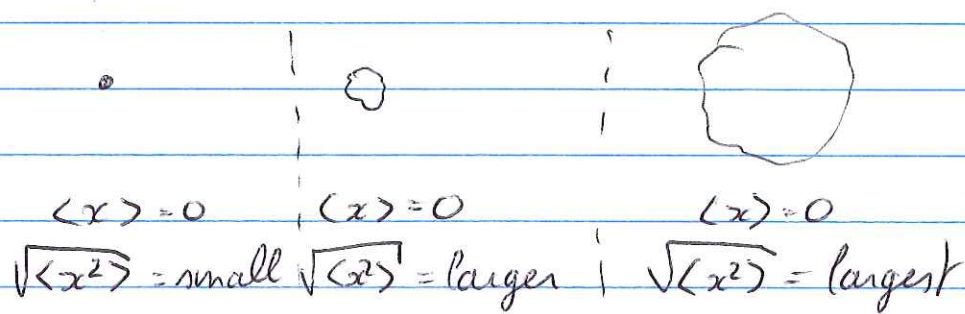
→ water molecules collide with nano-particles → move the nano-particles around

Video Brownian Motion

Position x is a random variable that changes randomly over time, but $\langle x \rangle = \bar{x}$ = average position remains zero.

Root-mean-square $\sqrt{\langle x^2 \rangle} = x_{\text{RMS}}$ is not zero but describes how widely the particles disperse from their original position

* Diffusion of ink on paper



Diffusion law: $x_{\text{RMS}} = \sqrt{2Dt}$ with D = diffusion constant in units $\frac{\text{m}^2}{\text{s}}$

D depends on the molecule and the medium it is in

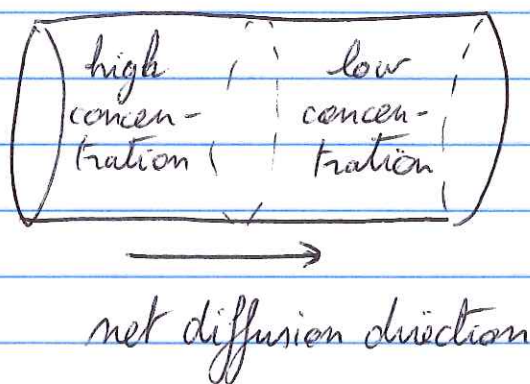
D for O_2 in H_2O	$1.0 \times 10^{-9} \frac{m^2}{s}$
$C_6H_{12}O_6$ in H_2O (glucose)	$0.7 \times 10^{-9} \frac{m^2}{s}$
hemoglobin in H_2O	$0.07 \times 10^{-9} \frac{m^2}{s}$
DNA in H_2O	$0.0013 \times 10^{-9} \frac{m^2}{s}$

larger molecules ^{/diffuse} move more slowly

How far will O_2 diffuse in H_2O during 1 second breathing cycle?

$$x_{RMS} = \sqrt{2Dt} = \sqrt{2(1.0 \times 10^{-9} \frac{m^2}{s})(1s)} = 45 \mu m$$

* Direction of diffusion is isotropic, in all directions



but different concentrations will cause diffusion from high to low, because "there is more to diffuse" on the high side.

* Diffusion defines the size of cells and their time scale

Amoeba : how long does it take for O_2 to diffuse?
500 μm

$$x_{RMS} = \sqrt{2Dt} \rightarrow t = \frac{x_{RMS}^2}{2D} \approx 100s$$

Red blood cell : $t = \frac{x_{RMS}^2}{2D_{hemoglobin}} \approx \underline{0.5s} \rightarrow$ breathing rate
8 μm

Chromosome : $t = \frac{x_{RMS}^2}{2D_{DNA}} \approx 20s$
7 μm

How long would it take for DNA to diffuse through an amoeba?
 $t = 27$ hours

Diffusion determines the short distance travel in cells

For longer distances, cells need active mechanism:
flagella, molecular motors, ATP

* Osmosis : diffusion will happen until the concentrations are equal

If membrane does not allow one type of molecules through
→ pressure builds up

