

$$\begin{aligned}\cos 60^\circ &= \frac{1}{2} \\ \sin 30^\circ &= \frac{1}{2} \\ \cos 45^\circ &= \sin 45^\circ \\ 1 &= \sqrt{2} \\ \tan 45^\circ &= 1\end{aligned}$$

$$\vec{v}_{\text{plane, ground}} = \vec{v}_{\text{plane, air}} + \vec{v}_{\text{air, ground}}$$

$$\begin{aligned}x &: -|\vec{v}_{\text{plane, ground}}| \cos 45^\circ = -|\vec{v}_{\text{plane, air}}| \cos 7^\circ + 45 \text{ m/s} \cos 21^\circ \\ y &: -|\vec{v}_{\text{plane, ground}}| \sin 45^\circ = -|\vec{v}_{\text{plane, air}}| \sin 7^\circ - 45 \text{ m/s} \sin 21^\circ\end{aligned}$$

$$x \rightarrow |\vec{v}_{\text{plane, ground}}| = \frac{1}{\cos 45^\circ} \left(|\vec{v}_{\text{plane, air}}| \cos 7^\circ - 45 \text{ m/s} \cos 21^\circ \right)$$

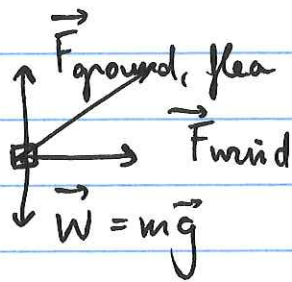
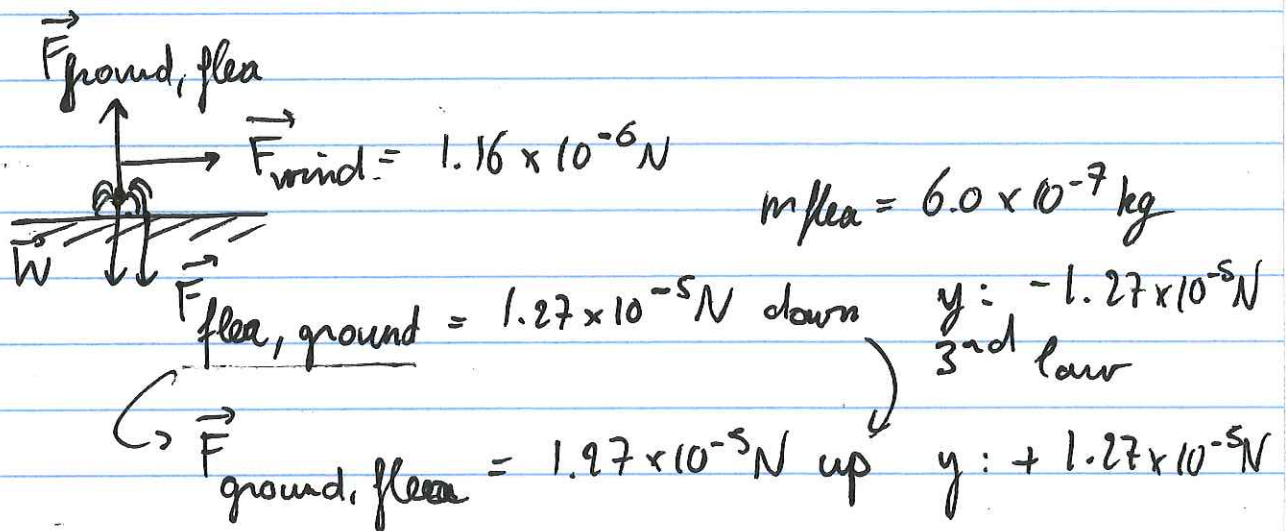
$$y \rightarrow + \frac{\sin 45^\circ}{\cos 45^\circ} \left(|\vec{v}_{\text{plane, air}}| \cos 7^\circ - 45 \text{ m/s} \cos 21^\circ \right) = 1 + |\vec{v}_{\text{plane, air}}| \sin 7^\circ + 45 \text{ m/s} \sin 21^\circ$$

$$|\vec{v}_{\text{plane, air}}| (\cos 7^\circ - \sin 7^\circ) = 45 \text{ m/s} (\sin 21^\circ + \cos 21^\circ)$$

$$|\vec{v}_{\text{plane, air}}| = 45 \text{ m/s} \frac{\sin 21^\circ + \cos 21^\circ}{\cos 7^\circ - \sin 7^\circ} = 66.8 \text{ m/s}$$

$$\begin{aligned}|\vec{v}_{\text{plane, ground}}| &= \frac{1}{\cos 45^\circ} \left(66.8 \text{ m/s} \cos 7^\circ - 45 \text{ m/s} \cos 21^\circ \right) \\ &= 34.3 \text{ m/s}\end{aligned}$$

$|\vec{F}|$



$$\vec{F}_{\text{net}} = \vec{F}_{\text{ground, flea}} + \vec{F}_{\text{wind}} + \vec{W}$$

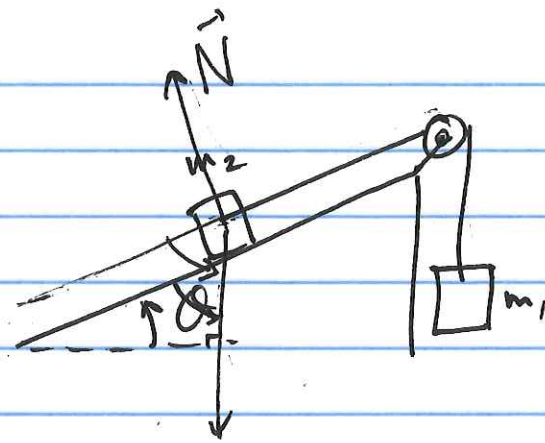
$$\begin{aligned}
 x: F_x &= F_{\text{wind}} = 1.16 \times 10^{-6} \text{ N} \\
 y: F_y &= F_{\text{ground, flea}} - mg = 1.27 \times 10^{-5} \text{ N} - (9.8 \text{ m/s}^2)(6.0 \times 10^{-7} \text{ kg})
 \end{aligned}$$

$$F_x = 1.16 \times 10^{-6} \text{ N}$$

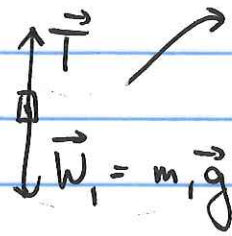
$$F_y = 1.15 \times 10^{-5} \text{ N}$$

$$\rightarrow |\vec{F}| = \sqrt{F_x^2 + F_y^2}$$

$$|\vec{F}| = |m\vec{a}| \rightarrow |\vec{a}| = \frac{|\vec{F}|}{6.0 \times 10^{-7} \text{ kg}} = 11.5 \text{ m/s}^2$$



FBD:



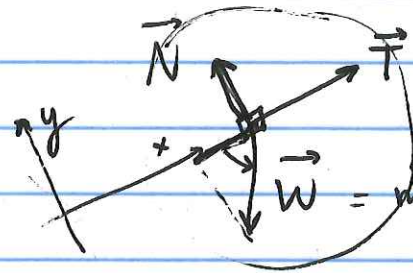
2nd

$$T - m_1 g = 0 \quad \overset{m_1}{\underset{m_1}{\downarrow}} = a_1$$

$$T = m_1 g$$

when is $\vec{a}_2 = 0$?

$$\vec{F}_{\text{net}} = m \vec{a}_2 = 0$$

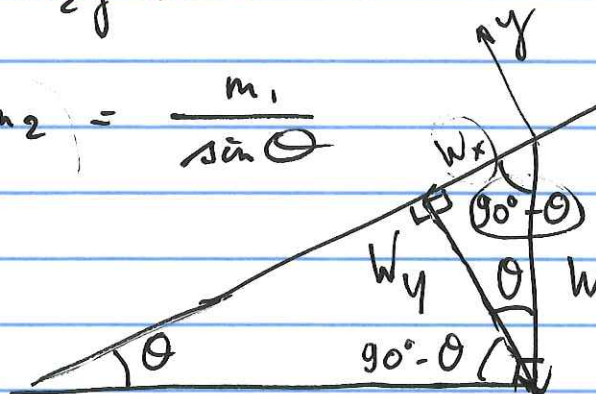
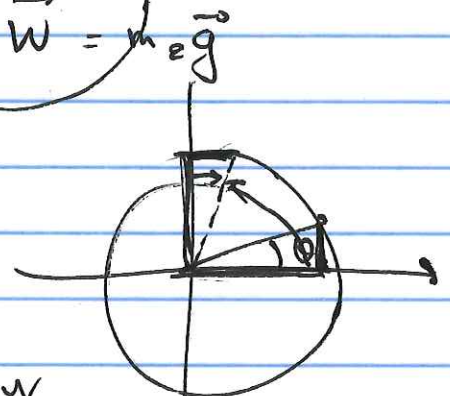


$$x: T - m_2 g \cos(90^\circ - \theta) = 0$$

$$T - m_2 g \sin \theta = 0$$

$$m_1 g - m_2 g \sin \theta = 0$$

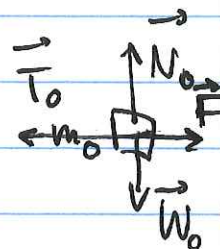
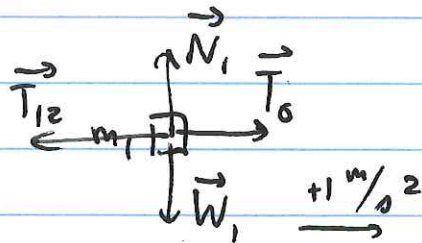
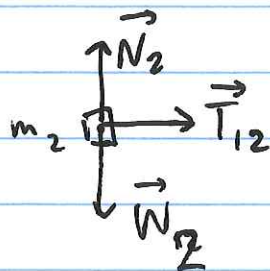
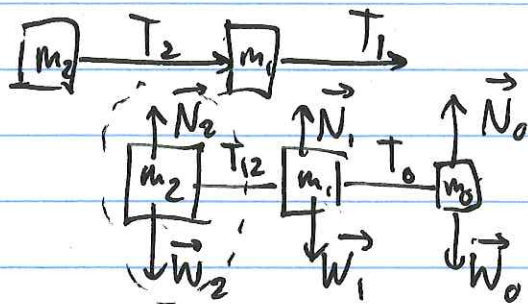
$$\hookrightarrow m_2 = \frac{m_1}{\sin \theta}$$



$$W_y = -W \sin(90^\circ - \theta) = -W \cos \theta$$

$$y: N - W \cos \theta = 0$$

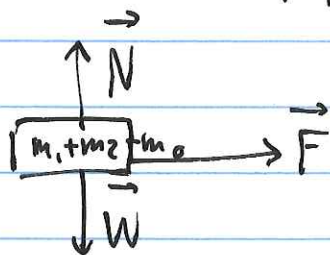
$$\hookrightarrow N = m_1 g \cos \theta$$



$$+1 \text{ m/s}^2 \rightarrow F_{\text{net}, x, 2} = m_2 (+1 \text{ m/s}^2) = \underline{T_{12}}$$

$$F_{\text{net}, x, 1} = m_1 (+1 \text{ m/s}^2) = \underline{T_0 - T_{12}}$$

$$F_{\text{net}, x, 0} = m_0 (+1 \text{ m/s}^2) = \underline{F - T_0}$$



$$\underline{(m_1 + m_2 + m_0) (+1 \text{ m/s}^2) = F}$$

PHYS 107 - Midterm 1

ch2: kinematics
ch3: ballistic motion
ch4: Newton's laws

MC questions : * acceleration at highest point of ballistic trajectory
* velocity given vs. time → calculate acceleration and distance

Q : contact forces between stacked masses

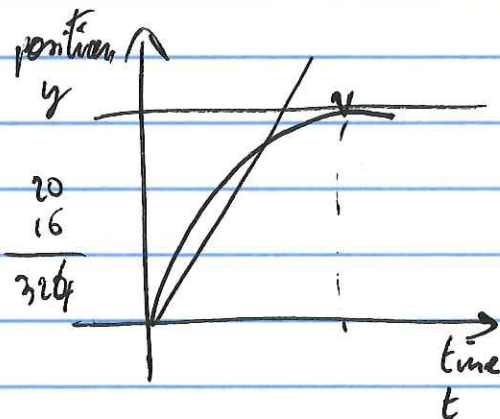
$$16 + 2t - 5t^2 = 0$$

$$t = \frac{-2 \pm \sqrt{4 + 4 \times 5 \times 16}}{-10}$$

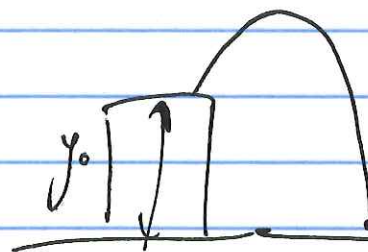
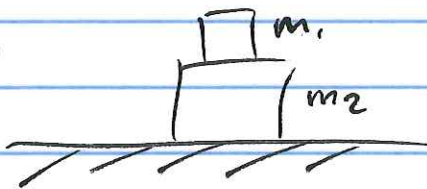
$$1 + 5 \times 18$$

$$\frac{20}{18}$$

$$360$$



$$100 - 64 = 36$$



$$y = 0 = y_0 + v_0 y t - \frac{1}{2} g t^2$$

$$-\frac{1}{2}(10)t^2 + v_0 t \quad y_0 = \frac{1}{2} g t^2 - v_0 \sin \theta t$$

$$h = \frac{v_0^2}{2g} = \frac{v_0^2}{20} \quad \text{then } 20 - 2 = 18m$$

$$-\frac{1}{2} g t^2 = h$$

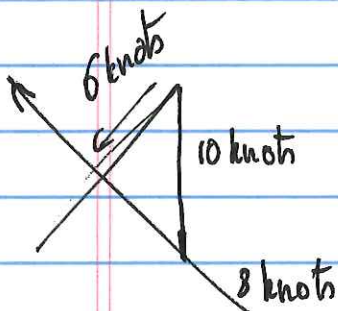
$$h = 20 \rightarrow v_0 = 20$$

$$t = 20$$

$$15 = at^2 + bt = at^2 - 2at^2$$

$$15 = t$$

$$a = \frac{15}{2at^2}$$



$$at^2 + bt = y$$

$$t = x$$

$$2at + b = 0$$

$$b = -2at$$

$$y_0 = 18m \rightarrow t = 2s$$