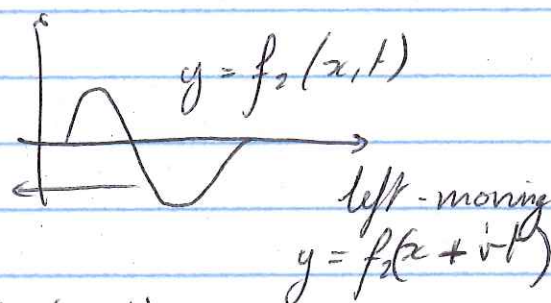
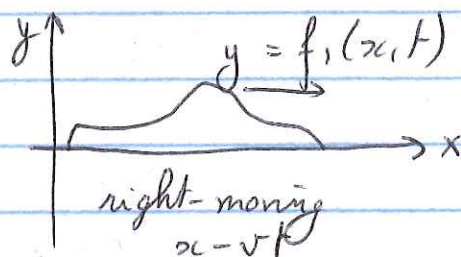


## \* Superposition and interference



$$\textcircled{y} = f_1(x, t) + f_2(x, t)$$

\* Beat ~~notes~~ notes

$$\left. \begin{array}{l} f_1 \approx f_2 \\ y_1 = A \cos(2\pi f_1 t) \quad (x=0) \\ y_2 = A \cos(2\pi f_2 t) \quad (x=0) \end{array} \right\}$$

$$y = y_1 + y_2 = A \cos(2\pi f_1 t) + A \cos(2\pi f_2 t)$$

$$= \textcircled{2A \cos(\pi f_B t)} \cos(2\pi f_{\text{avg}} t)$$

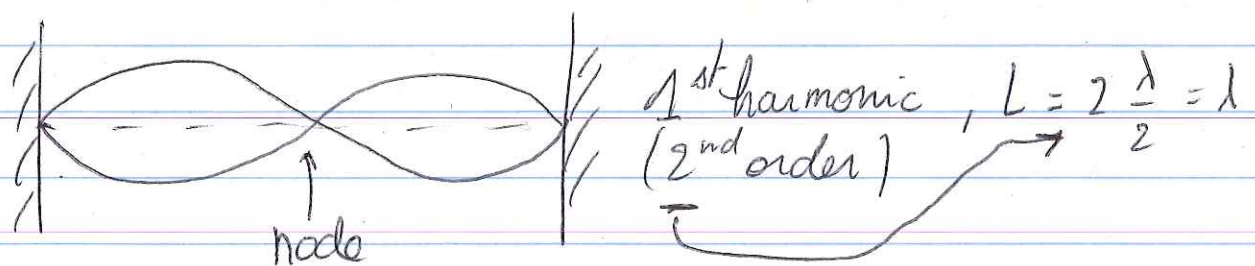
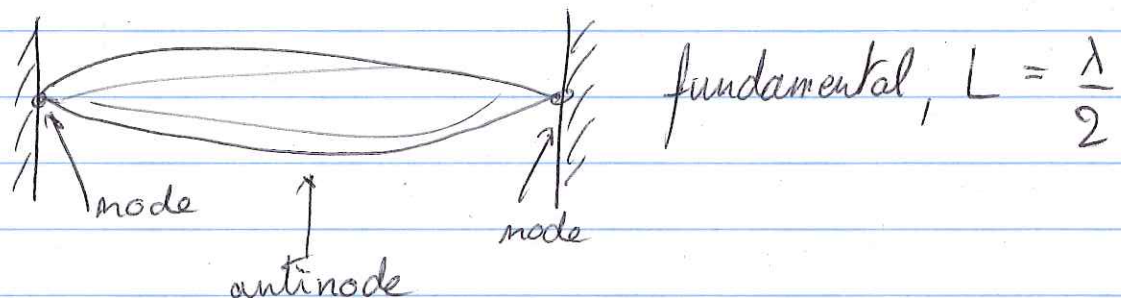
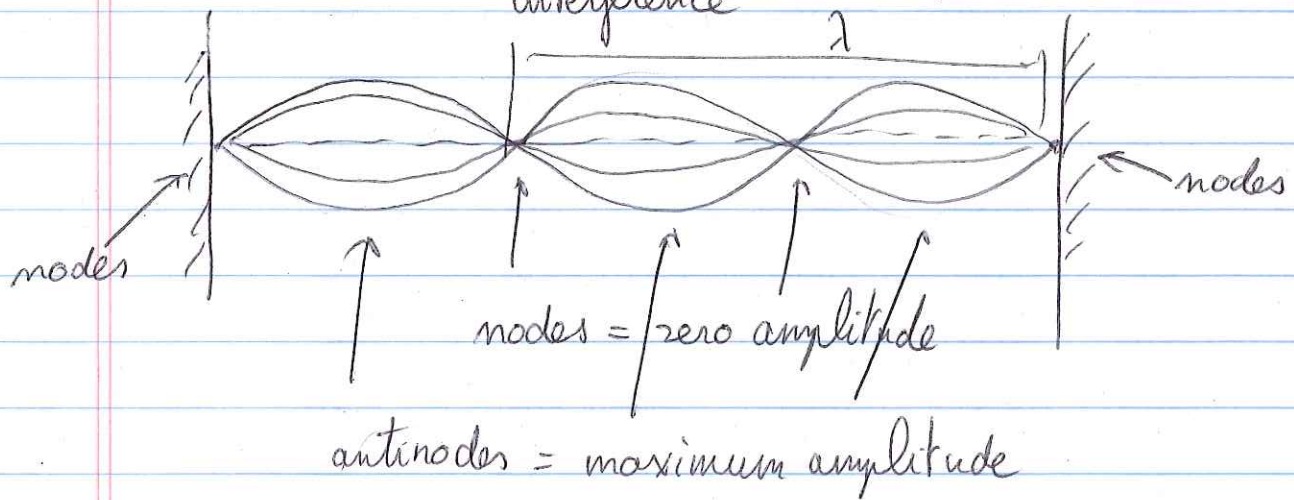
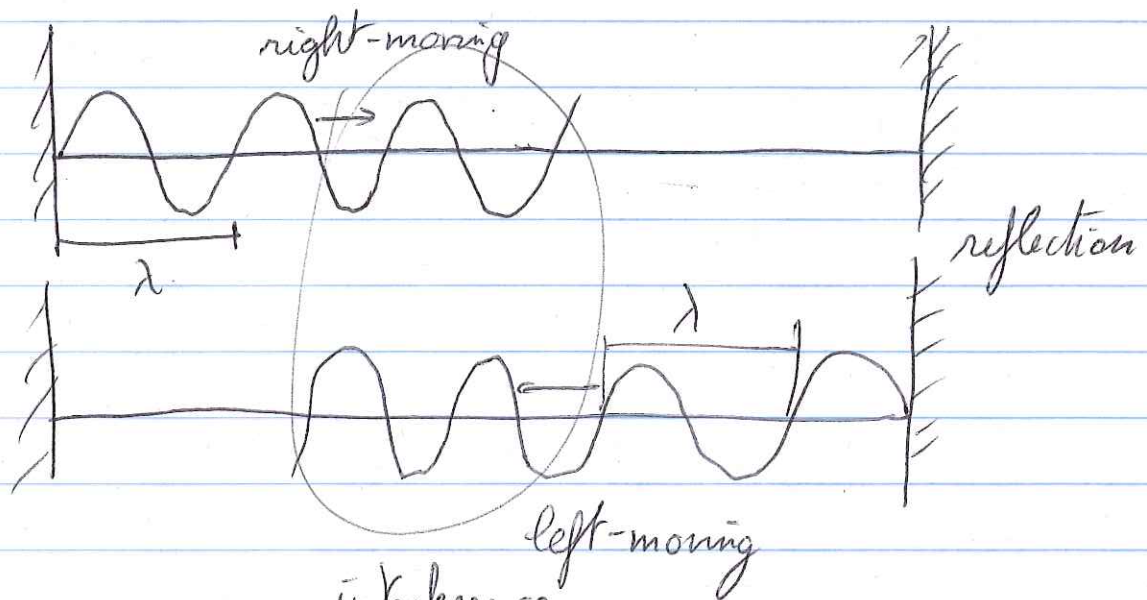
$$f_B = |f_1 - f_2| \ll f_1, f_2$$

$$f_{\text{avg}} = \frac{f_1 + f_2}{2}$$

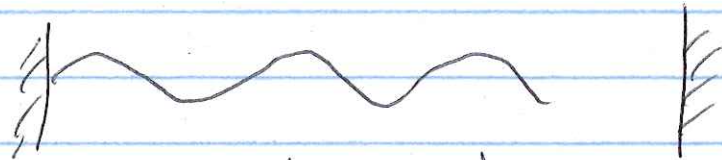
$$\left. \begin{array}{l} f_1 = 440 \text{ Hz} \\ f_2 = 442 \text{ Hz} \end{array} \right\} \rightarrow f_B = |f_1 - f_2| = 2 \text{ Hz} \ll 440 \text{ Hz}$$



# \* Standing waves



$k^{\text{th}}$  harmonic  
( $n^{\text{th}}$  order)  
 $n = k+1$



$$L = n \frac{\lambda}{2}, \quad n = 1, 2, 3, \dots$$

↑  
fundament

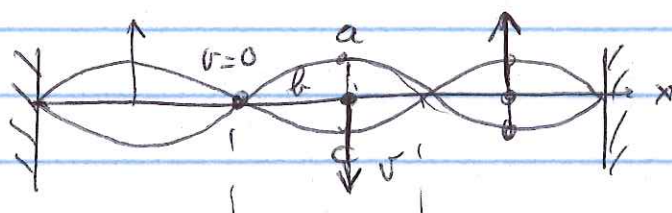
↑  
1<sup>st</sup> harm.

$$\lambda = \frac{2L}{n}$$

If  $v = \text{constant}$ :  $v = \lambda f \rightarrow f = \frac{v}{\lambda} = \frac{nv}{2L}, \quad n = 1, 2, 3, \dots$

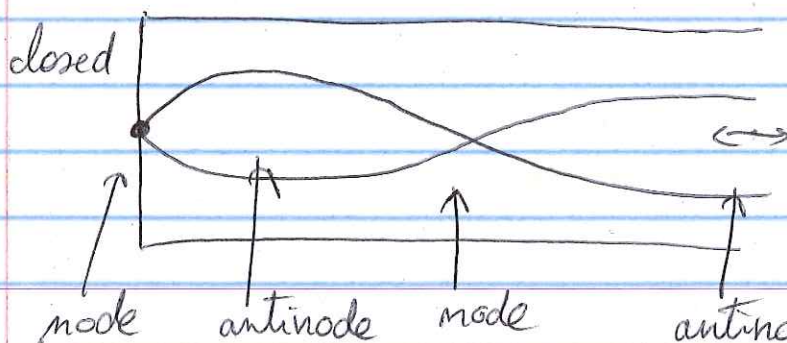
$$f_n = n \frac{v}{2L} = n f_1$$

↑  
fundamental  
frequency



$v$  depends on the position

\* musical instruments



$$f_1 = \frac{v}{4L}$$

large  $L \rightarrow$  low  $f$   
small  $L \rightarrow$  high  $f$



\* Waves transport energy:

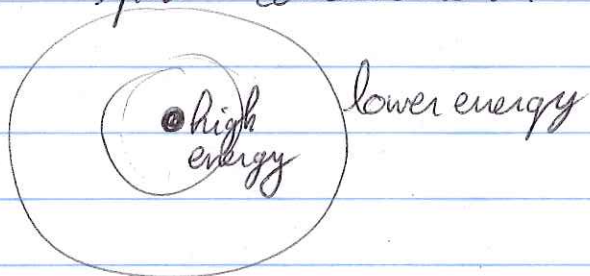
SHM: energy  $\propto A^2$  = amplitude squared

$$E = \frac{1}{2} k A^2$$

effects of waves, determined by energy transported.  
dependon: -  $A \rightarrow E \propto A^2$

- duration: all energy arrives in a short time  $\rightarrow$  Power =  $\frac{\text{energy}}{\text{time}} = \frac{E}{\Delta t}$

- spatial concentration:

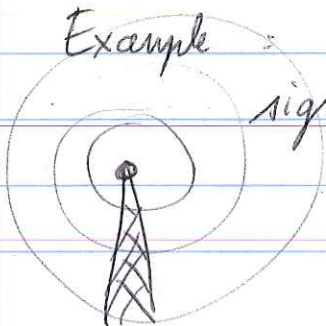


$$I = \text{intensity} = \frac{E/\Delta t}{A} = \frac{\text{power}}{\text{area}} \text{ in units } \frac{W}{m^2}$$

$$\left. \begin{array}{l} A_{\text{circle}} = \pi r^2 \\ A_{\text{sphere}} = 4\pi r^2 \end{array} \right\} A \propto r^2 \rightarrow I \propto \frac{1}{r^2}$$

Example: radio-transmitter emits a 10kW power signal in all directions

$$A_{\text{sphere}} = 4\pi r^2$$



1) what is the intensity at 1 km distance?

$$I = \frac{P}{A} = \frac{10 \text{ kW}}{4\pi(1000 \text{ m})^2} = 8 \times 10^{-4} \frac{\text{W}}{\text{m}^2}$$

2) what is the intensity at 10 km distance?

$$I = \frac{1}{100} (8 \times 10^{-4} \frac{\text{W}}{\text{m}^2}) = 8 \times 10^{-6} \frac{\text{W}}{\text{m}^2}$$

3) what is the power received by an 10 cm x 10 cm antenna at 10 km?

$$P = IA = I \cancel{\text{Area}} (0.1 \text{ m})^2$$

$$P = \cancel{8 \times 10^{-4}} 8 \times 10^{-8} \text{ W} \approx 10^{-7} \text{ W}$$

$0.1 \mu\text{W}$