

Physics 107: Physics for Life-Sciences

Midterm Exam: October 19, 2015

This test is administered under the rules and regulations of the honor code of the College of William & Mary.

Name: _____

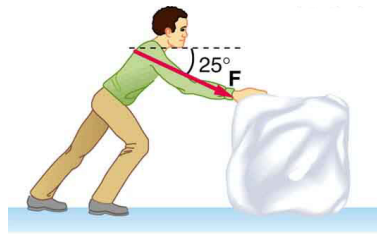
Signature: _____

Instructions:

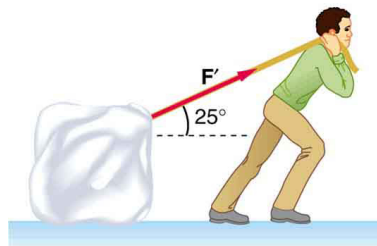
- This is a closed book, closed notes test.
- Calculators are NOT needed and NOT allowed. Devices with wireless connections are NOT allowed.
- Start your work from the fundamental equations on the formula sheet, and derive any additional expressions that you may need.
- Circle your answer for each part of each problem.
- Clearly mark out any work that you wish the grader to disregard. Do not waste your time erasing.
- Your work will be graded based on your ability to write down a logical and organized solution grounded in the correct assessment of the physics of a situation. No credit will be given for an answer that is not justified by a logical solution or where that justification is not organized or readable. Partial credit will be given up to the point where your solution departs from a correct analysis of the physics involved for any given part of a problem.

Question	Points	Score
1	10	
2	5	
3	5	
4	15	
5	20	
6	20	
Total:	75	

1. A contestant *a* in the winter games pushes a block of ice across a frozen lake with his arms at an angle of 25° below the horizontal. A second contestant *b* pulls an identical block of ice with a rope over his shoulder at an angle of 25° above the horizontal. Both contestants are shown in the figure below.



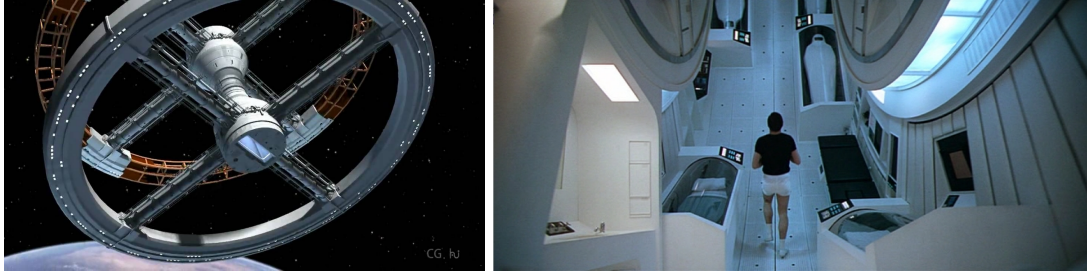
(a)



(b)

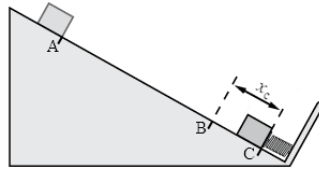
- (a) (5 points) Which contestant must exert a larger force F to move the block with a constant velocity?
- ☐ Contestant *a* has to exert a larger force.
 - ☐ Contestant *b* has to exert a larger force.
 - ☐ Both contestants have to exert the same force.
 - ☐ Unable to determine without additional information.
- (b) (5 points) Explain in words the reason for your answer above.
2. (5 points) An object moves in a circular path at a constant speed. Compare the direction of the object's velocity and acceleration vectors.
- ☐ Both vectors point in the same direction.
 - ☐ The vectors point in opposite directions.
 - ☐ The vectors are perpendicular to each other.
 - ☐ The question is meaningless since one of the vectors is zero.
 - ☐ The question is meaningless since the relative orientation of the two vectors will change.
3. (5 points) Two marbles, one twice as heavy as the other, are dropped from rest to the ground from the roof of a building. Ignore any air resistance. Just before hitting the ground, the heavier marble has a kinetic energy that is...
- ☐ ...equal to the kinetic energy of the lighter marble.
 - ☐ ...twice the kinetic energy of the lighter marble.
 - ☐ ...half of the kinetic energy of the lighter marble.
 - ☐ ...four times the kinetic energy of the lighter marble.
 - ☐ ...impossible to determine without additional information.

4. A rotating space station is said to create *artificial gravity* – a loosely-defined term used for an acceleration that would be crudely similar to gravity. The outer wall of the rotating space station would become a floor for the astronauts, and centripetal acceleration supplied by the floor would allow astronauts to exercise and maintain muscle and bone strength more naturally than in non-rotating space environments. An example of such a setup is *Space Station V* from the movie *2001: A Space Odyssey* as shown below.



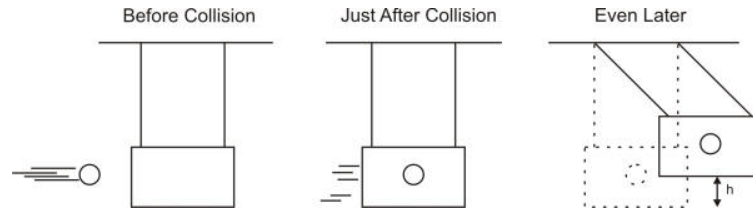
- (a) (5 points) If the space station is 500 m in diameter, what angular velocity (in radians per second) would produce an artificial gravity similar to that on Earth inside the outer wall of the station? You may approximate the magnitude of the Earth's gravitational acceleration g as 10.0 m/s^2 .
- (b) (5 points) What is the period of revolution of the space station? You may use $2\pi \approx 6.4$.
- (c) (5 points) An astronaut standing inside the space station drops a ball to the floor. Describe the motion of the ball as seen by a non-rotating observer outside the space station. What will be the acceleration of the ball for that outside observer?

5. The spring driven ball launcher in a pinball machine launches a 100 g metal ball by compressing the spring by 10 cm. The pinball machine's surface is tilted at an angle of 30° with the horizontal. We want to determine the spring constant k such that we can launch the ball and reach the highest point A, a distance of 1 m away from C, as measured along the tilted playing surface. Assume that frictional effects are negligible. You may approximate the magnitude of the gravitational acceleration g as 10.0 m/s^2 .



- (a) (5 points) What is the mechanical energy (kinetic and potential energy) when the ball reaches the highest point A and is momentarily stationary there?
- (b) (5 points) What is the mechanical energy (kinetic and potential energy) when the spring in the launcher is fully compressed at point C, immediately before launching the ball?
- (c) (5 points) What is the value for the spring constant k such that the ball reaches the highest point A?
- (d) (5 points) What is the speed of the ball as it leaves the launcher at point B?

6. You have been hired by the W&M Police Department to examine their new pistols. They have asked you to determine the velocity of the bullets when they leave the handgun. To test this you fire a standard $m_1 = 2.0 \text{ g}$ bullet toward a wooden block hanging from a rope (called a *ballistic pendulum*). When the bullet hits the block it embeds itself in the wood. You observe that the block swings upward after the collision. When you do your experiment you note that the block swings to a height of $h = 0.20 \text{ m}$ above its original hanging position. You measure the mass $m_1 + m_2$ of the block with the bullet embedded to be exactly 1.000 kg . You may approximate the magnitude of the gravitational acceleration g as 10.0 m/s^2 .



(a) (5 points) What is the potential energy of the block and bullet when it is at its highest position?

(b) (5 points) What is the speed of the block just after the bullet hits the block?

(c) (5 points) What is the speed of the bullet before the collision?

(d) (5 points) How much energy is converted into other energies (*e.g.* heat) in this inelastic collision?

Possibly useful relations (feel free to detach this page):

$$\vec{v}_{avg} = \Delta \vec{x} / \Delta t$$

$$\vec{a}_{avg} = \Delta \vec{v} / \Delta t$$

$$x = x_0 + v_0 t + \frac{1}{2} a t^2$$

$$v = v_0 + a t$$

$$v_{avg} = \frac{v_0 + v}{2}$$

$$v^2 = v_0^2 + 2a(x - x_0)$$

$$\vec{F}_{net} = m \vec{a}$$

$$\vec{F}_{BA} = -\vec{F}_{AB}$$

$$W = F d \cos \theta$$

$$W_{net} = -\Delta PE = \Delta KE$$

$$KE = \frac{1}{2} m v^2$$

$$PE_k = \frac{1}{2} k x^2$$

$$PE_g = mgh$$

$$KE_i + PE_i + W_{nc} = KE_f + PE_f$$

$$P = \frac{W}{\Delta t}$$

$$\text{Eff} = \frac{W_{out}}{E_{in}}$$

$$\cos \theta = \text{adjacent/hypotenuse}$$

$$\sin \theta = \text{opposite/hypotenuse}$$

$$\tan \theta = \sin \theta / \cos \theta$$

$$\sin 30^\circ = \cos 60^\circ = \frac{1}{2}$$

$$\cos 30^\circ = \sin 60^\circ = \frac{\sqrt{3}}{2}$$

$$\tan 45^\circ = 1$$

$$R = \frac{v_0^2}{g} \sin 2\theta$$

$$h = \frac{v_0^2}{2g} \sin^2 \theta$$

$$0 \leq f_s \leq \mu_s N$$

$$f_k = \mu_k N$$

$$\frac{F}{A} = Y \frac{\Delta L}{L}$$

$$F_k = -kx$$

$$\vec{W} = m \vec{g}$$

$$\vec{g} = 9.80 \text{ m/s}^2 \text{ downward}$$

$$F_G = G \frac{mM}{r^2}$$

$$G = 6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2$$

$$\vec{I} = \vec{F}_{avg} \Delta t$$

$$\vec{p} = m \vec{v}$$

$$\vec{F}_{net} = \frac{\Delta \vec{p}}{\Delta t}$$

$$v_1 - v_2 = v'_2 - v'_1$$

$$\theta = \frac{s}{r}$$

$$v = r\omega$$

$$f = \frac{1}{T} \text{ and } \omega = 2\pi f = \frac{2\pi}{T}$$

$$a_c = \frac{v^2}{r} = r\omega^2$$

$$F_c = m \frac{v^2}{r} = mr\omega^2$$

$$1 \text{ cal} = 4.186 \text{ J and } 1 \text{ Cal} = 1000 \text{ cal}$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$