

CS 561: Algorithms & Data Structures

Homework 04

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Preamble: Space here for some notes, before the enumerated problems below. See end of document for example Figures and Tables. While we're at it, here's an example citation from the bibliography: Cormen [1]

- (1) Consider the following alternative greedy algorithms for the activity selection problem discussed in class. For each algorithm, either prove or disprove that it constructs an optimal schedule.
- (a) Choose an activity with shortest duration, discard all conflicting activities and recurse.
 - (b) Choose an activity that starts first, discard all conflicting activities and recurse.

Solutions.

- (a) *Shortest Duration.* Consider Figure (1), showing a collection of “disjoint in time” activities a_1, a_2, a_3, a_4, a_5 , all approximately equal in duration and a special activity a' of noticeably shorter duration . . .

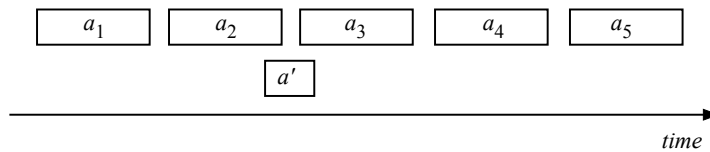


Figure 1: See Problem 1(a). Add more text here for figure caption.

- (b) *Starts First.* Consider Figure (2), showing a collection of activities $a_1, a_2, a_3, a_4, a_5, a'$. The original “Ends First” greedy algorithm would produce the 3-element activity set $\{a_1, a_3, a_4\}$, but the “Starts First” greedy algorithm would produce the single-element activity set $\{a'\}$. Clearly then, the “Starts First” greedy algorithm will not generally produce an optimal schedule.

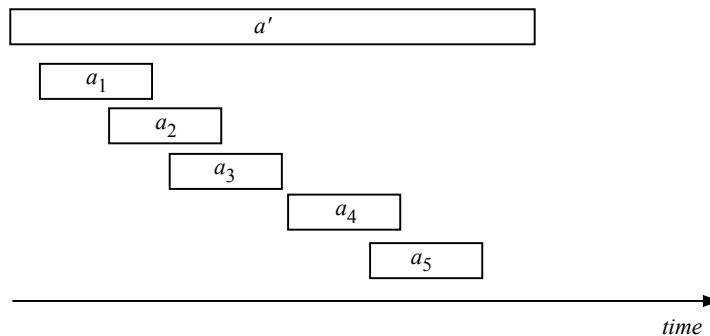


Figure 2: See Problem 1(a). A collection of activities where the “Ends First” greedy algorithm would produce the 3-element activity set $\{a_1, a_3, a_4\}$, but the “Starts First” greedy algorithm would produce the 1-element activity set $\{a'\}$.

(2) Second problem starts here.

(a) Start sub-problem here.

(b) Start sub-problem here.

Solutions.

(a) Solution to 2(a):

(b) Solution to 2(b):

EXAMPLES for use elsewhere ...

$$m(j) = \max \begin{cases} m(x_j) + v_j \\ m(j - 1) \end{cases}$$

(1)

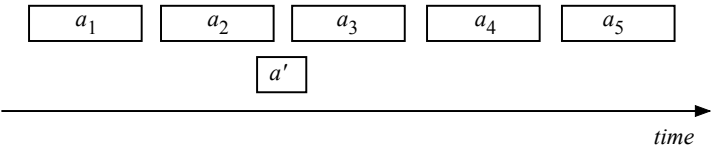
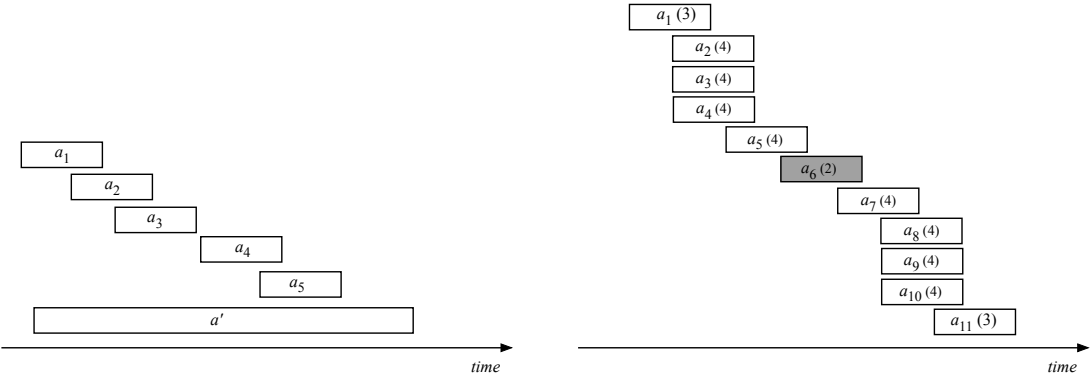


Figure 3: An example figure without subfigures.



(a) Caption for subfigure (a).

(b) Caption for subfigure (b).

Figure 4: Example Figure containining two sub-figures.

r_i/c_j	1	2	1	2
1	0	0	1	0
1	1	0	0	0
2	0	1	0	1
2	0	1	0	1

(a)

r_i/c_j	1	2	1	2
1	0	1	0	0
1	0	0	0	1
2	1	1	0	0
2	0	0	1	1

(b)

Figure 5: Example Figure containing two sub-figures, each containing a Table.

References

[1] Thomas H. Cormen et al. *Introduction to Algorithms*. The MIT Press Ser. MIT Press, 2009. ISBN: 9780262033848.