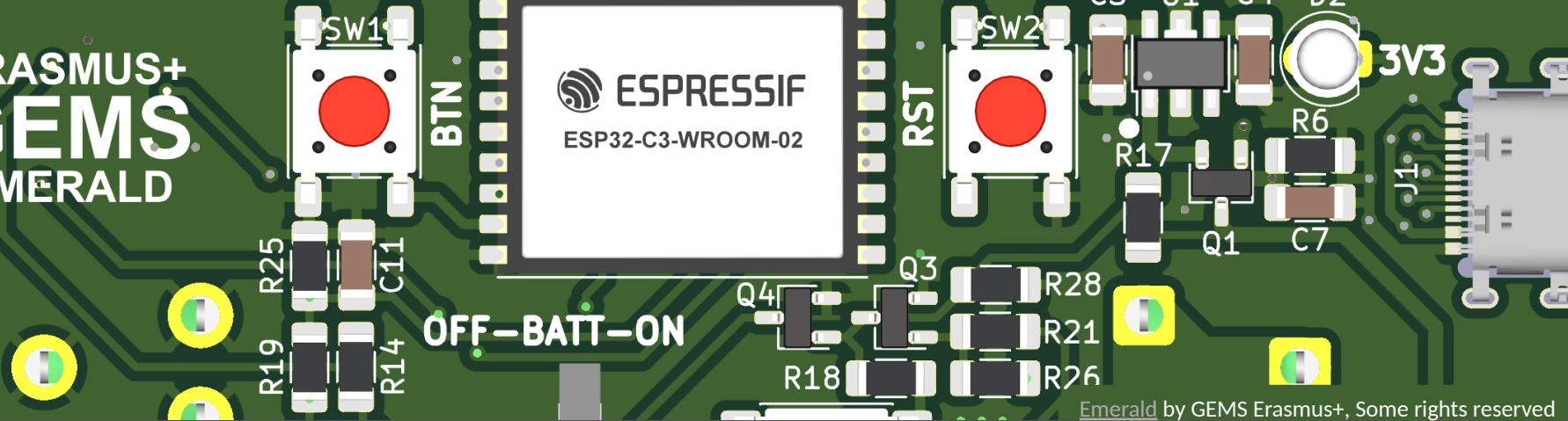


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# Mobile robot with differential drive

Building Robots: System Integration

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# About

1 Mobile robot

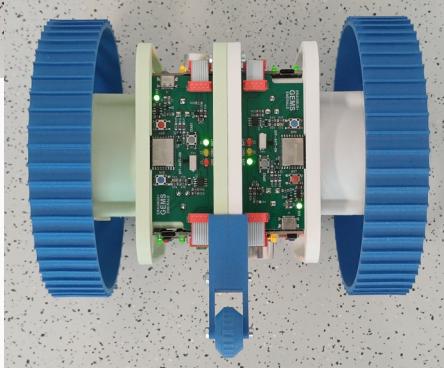
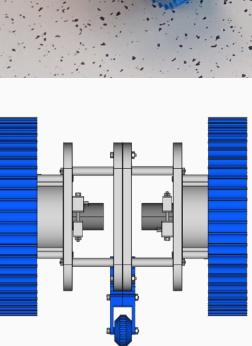
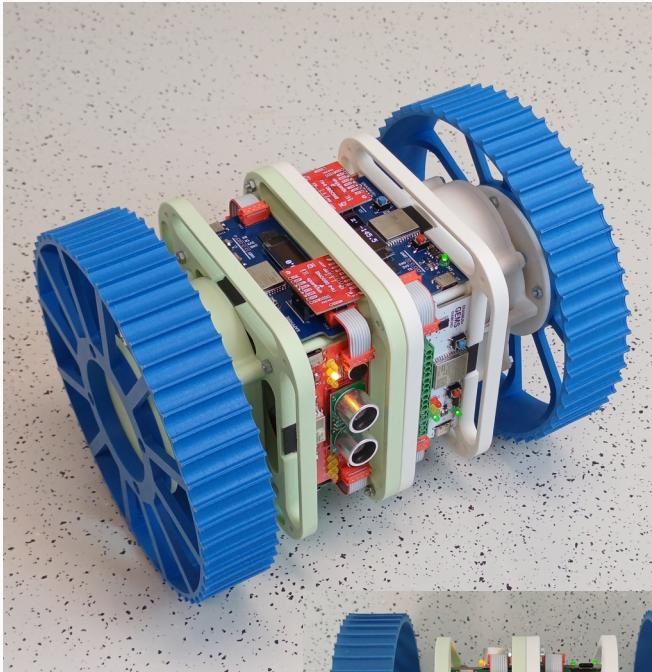
2 Structure

3 Forward kinematics

4 Inverse kinematics

# Mobile robot

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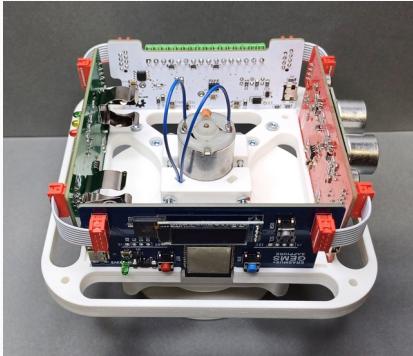
# Robot type

- 1 Mobile robot → movement  
(to different location)
- 2 Wheels → ground → ~flat
- 3 2 drive wheels → Differential drive  
(+ support → 3 point contact)

# Structure

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# GEMS Mobile Robot

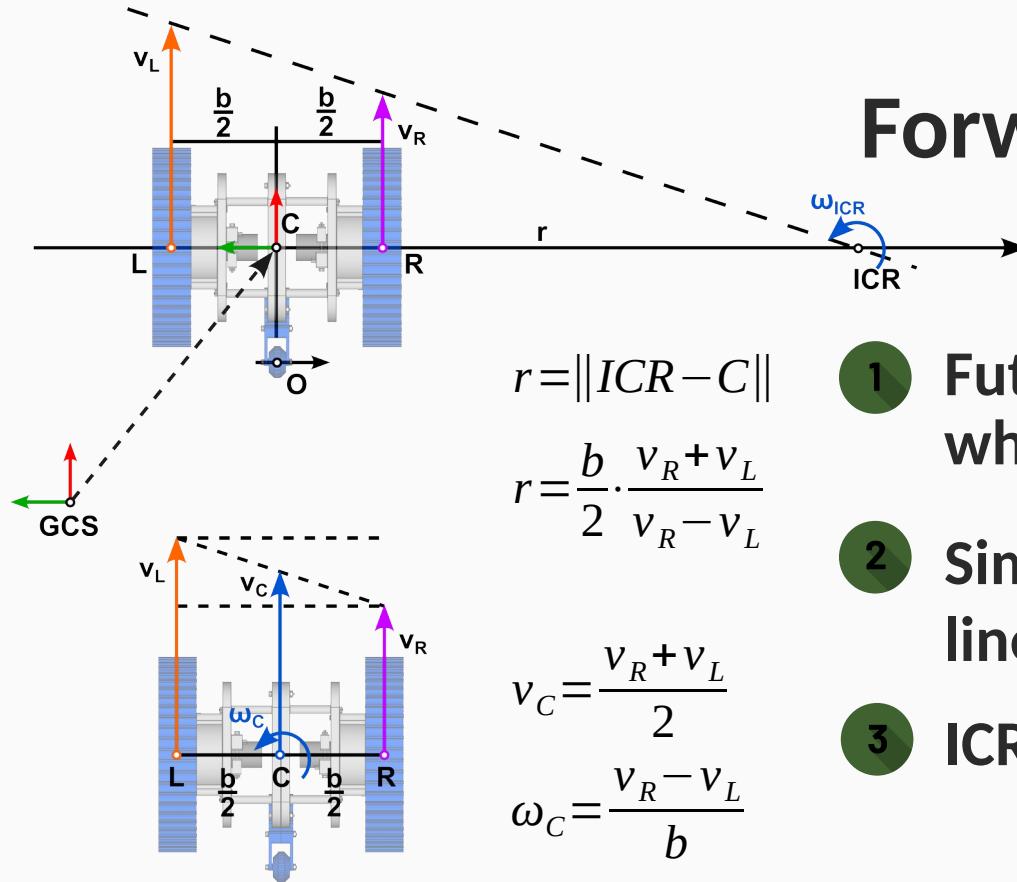


- 1 Modular: PCB modules → servo motor → Mobile Robot
- 2 Educational → slow and robust (big 3D printed wheels)
- 3 Autonomy → Emerald PCB module with battery

# Kinematics

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# Forward kinematics



$$r = \|ICR - C\|$$

$$r = \frac{b}{2} \cdot \frac{v_R + v_L}{v_R - v_L}$$

$$v_C = \frac{v_R + v_L}{2}$$

$$\omega_C = \frac{v_R - v_L}{b}$$

1 Future position derived from wheel speeds

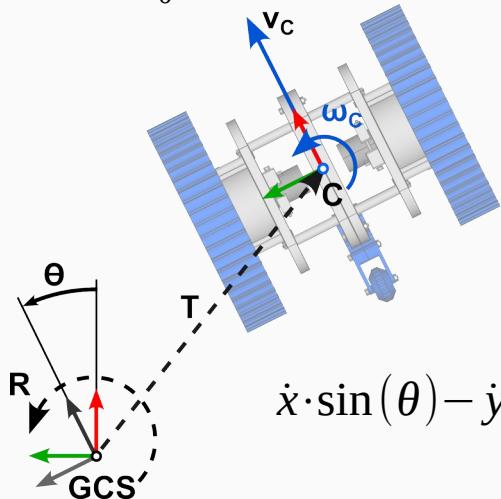
2 Simple  $\rightarrow$  similar triangles linear and rotational speed

3 ICR - Instant center of rotation

$$x(t) = \int_0^t v_c(t) \cdot \cos(\theta(t)) dt$$

$$y(t) = \int_0^t v_c(t) \cdot \sin(\theta(t)) dt$$

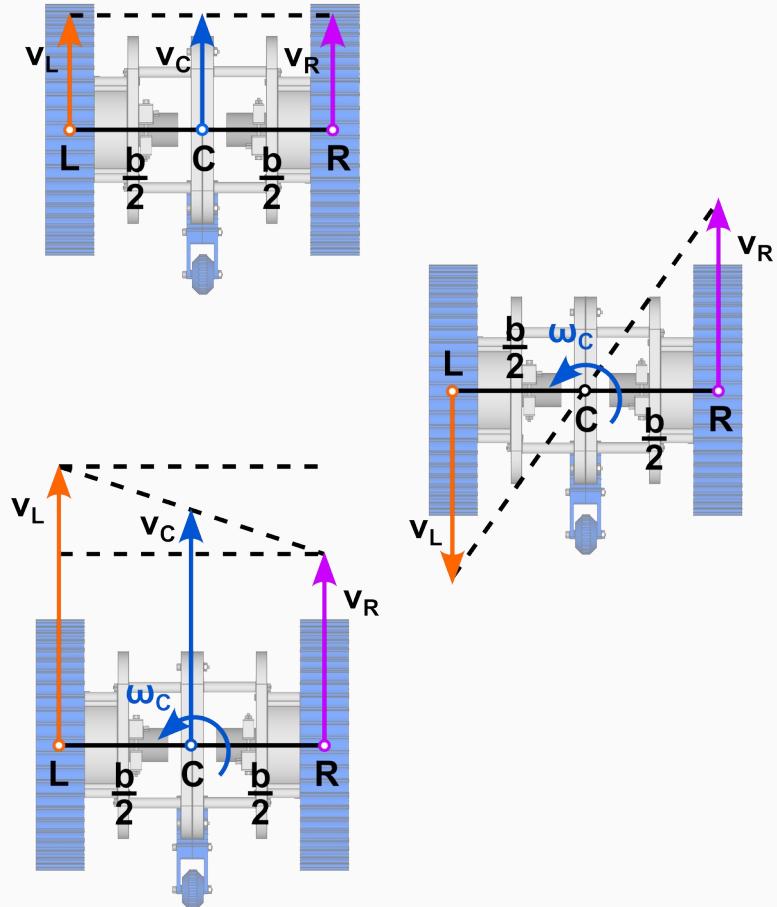
$$\theta(t) = \int_0^t \omega_c(t) dt$$



$$\dot{x} \cdot \sin(\theta) - \dot{y} \cdot \cos(\theta) = 0$$

# Forward kinematics

- 1 Non-holonomic system: cannot move freely in all directions
- 2 Assumptions: flat and no slip
- 3 Integration → Future position

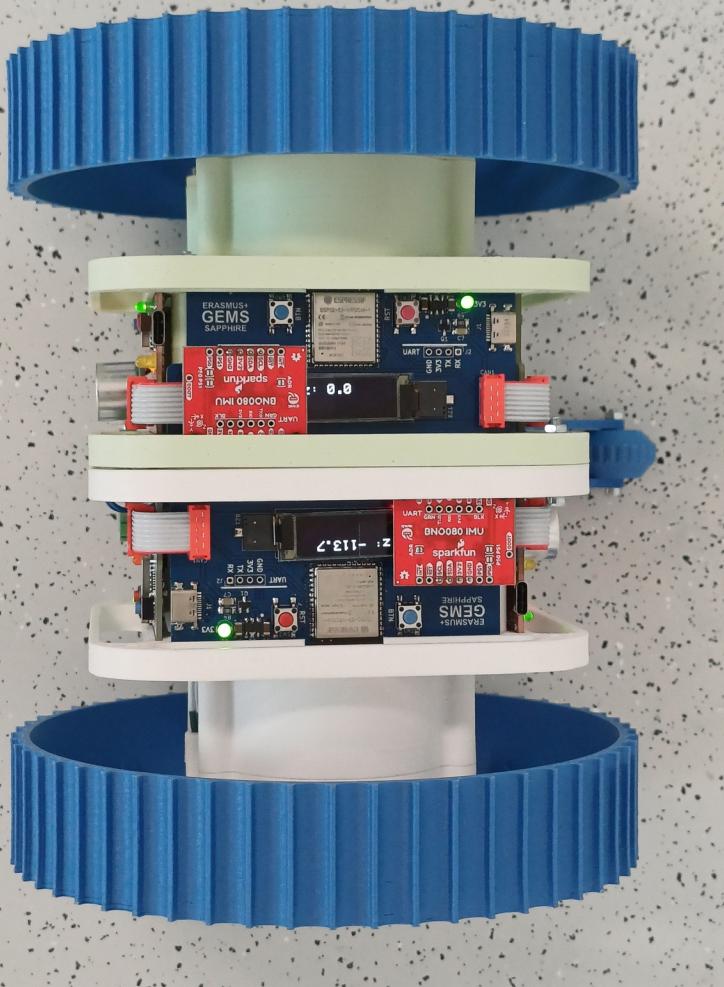


# Inverse kinematics

- 1 Wheel speeds derived from the robot's desired position change
- 2 Non-holonomic system: cannot move freely in all directions
- 3 Difficult → Simplification

# Task

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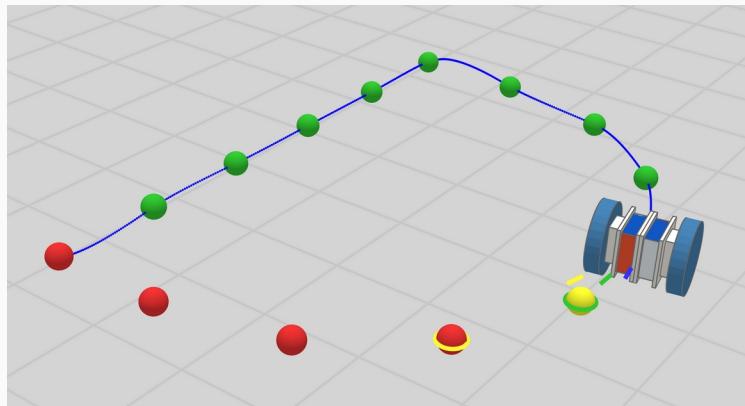
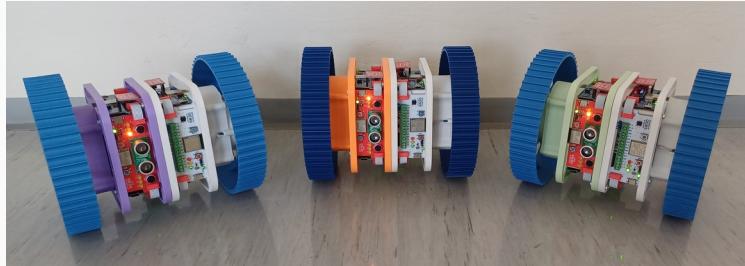
# Forward kinematics

## Arduino program

- 1 Target: ESP32C3/S3  
reusable function
- 2 Input: L and R motor speed, robot  
geometry from CAD (Github)
- 3 Output: translation speed, rotation  
speed and path radius

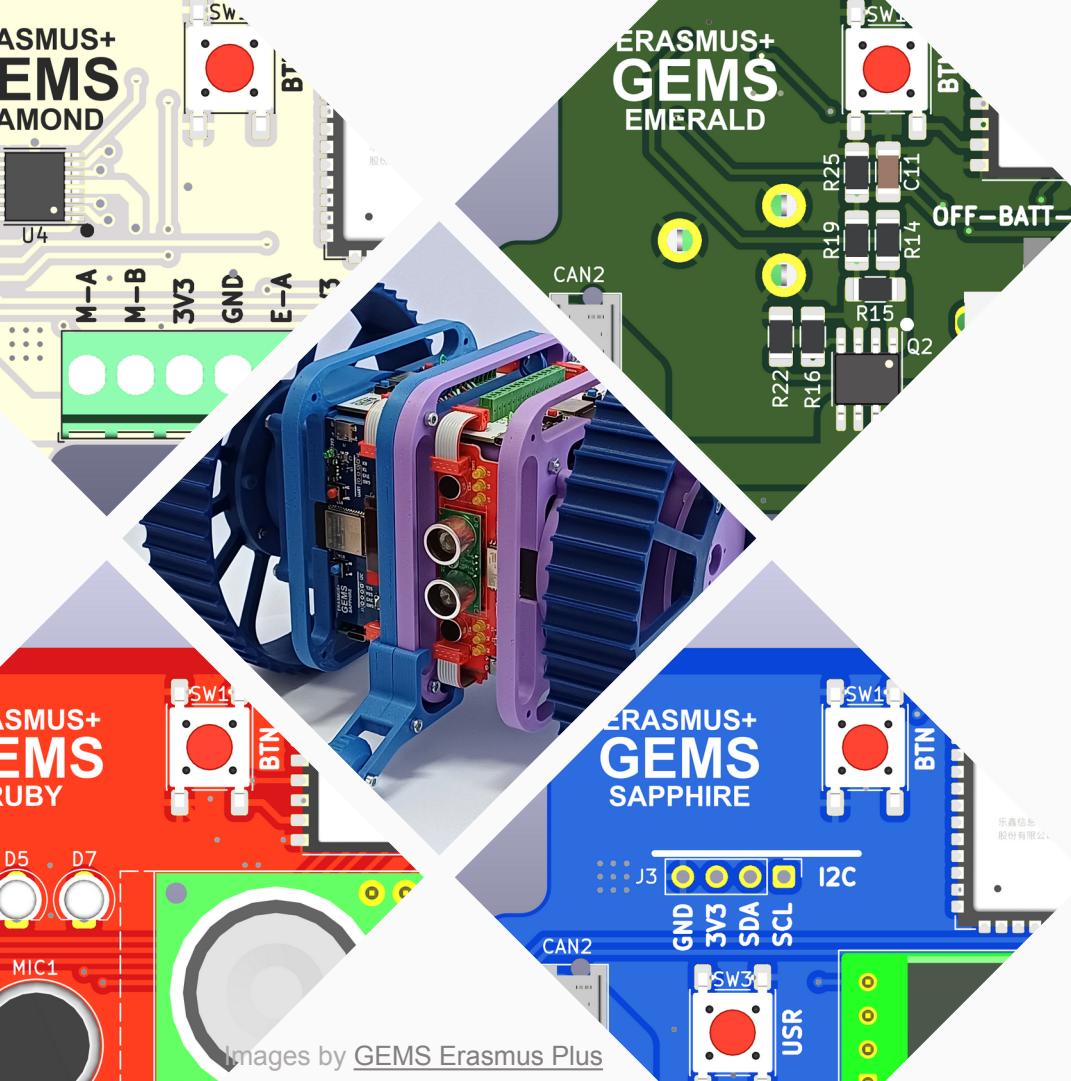
# Conclusion

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# Mobile robot with differential drive

- 1 Simple configuration
- 2 Mechanical connections → change robot characteristics
- 3 Kinematics → control



# Thank you for watching!

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