

Loop-Aware Optimizations in PyPy’s Tracing JIT

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Abstract

One of the nice properties of a tracing JIT is that many of its optimizations are simple requiring one forward pass only. This is not true for loop-invariant code motion which is a very important optimization for code with tight kernels. In this paper we present a scheme for making simple optimizations loop-aware by using a simple pre-processing step on the trace and not changing the optimizations themselves. The scheme can give performance improvements of a factor over two for PyPy’s Python JIT executing simple numerical kernels bringing the performance close to that of compiled C code.

Categories and Subject Descriptors D.3.4 [Programming Languages]: Processors—code generation, incremental compilers, interpreters, run-time environments

General Terms Languages, Performance, Experimentation

Keywords Tracing JIT, Optimization, Loop-Invariant Code Motion

1. Introduction

Reviewer 1 ▶ You often use the word *simple*. While it might make sense to use it, its exact meaning in that context remains unclear. ◀

One of the advantages that tracing JIT compilers have above traditional method-based JITs is that their optimizers are much easier to write. Because a tracing JIT produces only linear pieces of code without control flow joins, many optimization passes on traces can have a very simple structure. They often consist of one forward pass replacing operations by simpler ones or even discarding them as they walk along it. This makes optimization of traces very similar to symbolic execution. Also, many difficult problems in traditional optimizers become tractable if the optimizer does not need to deal with control flow merges.

One disadvantage of this simplicity is that such simple forward-passing optimizers ignore the only bit of control flow they have available, which is the fact that most traces actually represent loops. Making use of this information is necessary to perform optimizations that take the whole loop into account, such as loop-invariant code motion or optimizations that improve across several iterations of the loop. Having to deal with this property of traces complicates

the optimization passes, as a more global view of a trace needs to be considered when optimizing.

In this paper we want to address this problem by proposing a simple scheme that makes it possible to turn optimizations using one forward pass into optimizations that can do loop invariant code motion and similar loop-aware improvements. Using this scheme one does not need to change the underlying optimization much to get these advantages.

The resulting optimizations one gets using this scheme are in no way novel, most of them are well-known loop optimizations. However, the way to implement them is a lot simpler than directly implementing loop-aware optimizations.

2. Background: PyPy

The work described in this paper was done in the context of the PyPy project¹. PyPy is a framework for implementing dynamic languages efficiently [10]. When implementing a language with PyPy, one writes an interpreter for the language in RPython [1]. RPython (“Restricted Python”) is a subset of Python chosen in such a way that it can be efficiently translated to a C-based VM by performing type inference.

Many low-level aspects of the final VM are not contained within the interpreter implementation but are inserted during translation to C. Examples for this are a garbage collector and also a tracing JIT compiler [5].

PyPy’s tracing JIT compiler traces on the level of RPython programs. Thus it actually traces the execution of an interpreter written in RPython, not of the program itself. This makes the details of the object model of the implemented language transparent and optimizable by the tracing JIT. In the context of this paper, this aspect of PyPy’s tracing JIT can be ignored. Instead, it is sufficient to view PyPy’s tracing JIT as a JIT for RPython.

3. Motivation

Reviewer 3 ▶ Don’t break code listings across pages, as at the start of section 3. It makes them very hard to follow. ◀

To motivate the approach we propose here, let’s look at a trivial (unrealistic) trace which corresponds to an infinite loop:

```

L0(i0):                                     1
i1 = i0 + 1                               2
print(i1)                                 3
jump(L0, i0)                              4

```

The first line is a label L_0 with argument i_0 . Every label has a list of arguments. The **print** operation just prints its argument (it is not an operation that PyPy’s tracing JIT really supports, we just use it for this example). The **jump** operation jumps back to the beginning of the trace, listing the new values of the arguments of

the trace. In this case, the new value of i_0 is i_0 , making it a loop-invariant.

Because i_0 is loop-invariant, the addition could be moved out of the loop. However, we want to get this effect using our existing optimization passes without changing them too much. Simple optimizations with one forward pass cannot directly get this effect: They just look at the trace without taking into account that the trace executes many times in a row. Therefore to achieve loop-invariant code motion, we peel one iteration off the loop before running the optimizations. This peeling gives the following trace:

```

L0(i0):
i1 = i0 + 1
print(i1)
jump(L1, i0)

L1(i0):
i2 = i0 + 1
print(i2)
jump(L1, i0)

```

The iteration of the loop that was peeled off (lines 1-4) is called the *preamble*, the loop afterwards (lines 6-9) the *peeled loop*.

Now the optimizer optimizes both of these two iterations of the loop together, disregarding the jump and the label in lines 4-6. Doing this, common subexpression elimination will discover that the two additions are the same, and replace i_2 with i_1 . This leads to the following trace:

```

L0(i0):
i1 = i0 + 1
print(i1)
jump(L1, i0)

L1(i0):
print(i1)
jump(L1, i0)

```

This trace is malformed, because i_1 is used after the label L_1 without being passed there, so we need to add i_1 as an argument to the label and pass it along the jumps:

```

L0(i0):
i1 = i0 + 1
print(i1)
jump(L1, i0, i1)

L1(i0, i1):
print(i1)
jump(L1, i0, i1)

```

The final result is that the loop-invariant code was moved out of the loop into the peeled-off iteration. Thus the addition is only executed in the first iteration, while the result is reused in all further iterations.

This scheme is quite powerful and generalizes to other optimizations than just common subexpression elimination. It allows simple linear optimization passes to perform loop-aware optimizations, such as loop-invariant code motion without changing them at all. All that is needed is to peel off one iteration, then apply simple one-pass optimizations and make sure that the necessary extra arguments are inserted into the label of the loop itself and the jumps afterwards.

This is the key insight of the proposed implementation scheme: Giving an optimization two iterations together at the same time gives the optimization enough context to remove operations from the peeled loop, because it detects that the operation was performed in the preamble already. Thus at runtime these moved operations are only executed once when entering the loop and the results are reused in further iterations.

```

class Base(object):
    pass

class BoxedInteger(Base):
    def __init__(self, intval):
        self.intval = intval

    def add(self, other):
        return other.add__int__(self.intval)

    def add__int__(self, intother):
        return BoxedInteger(intother + self.intval)

    def add__float__(self, floatother):
        floatvalue = floatother + float(self.intval)
        return BoxedFloat(floatvalue)

class BoxedFloat(Base):
    def __init__(self, floatval):
        self.floatval = floatval

    def add(self, other):
        return other.add__float__(self.floatval)

    def add__int__(self, intother):
        floatvalue = float(intother) + self.floatval
        return BoxedFloat(floatvalue)

    def add__float__(self, floatother):
        return BoxedFloat(floatother + self.floatval)

def f(y):
    step = BoxedInteger(-1)
    while True:
        y = y.add(step)

```

Figure 1. An “Interpreter” for a Tiny Dynamic Language Written in RPython

4. Running Example

Reviewer 1 ► *I think the motivation section is great, in particular for readers who are less familiar with compiler/JIT optimizations. However, section 4 starts with “yet another example” – at least this was my impression when reading it. I understand the differences and everything, but still, you might consider to improve the transition between sections 3 and 4.* ◀

For the purpose of this paper, we are going to use a tiny interpreter for a dynamic language with a very simple object model, that just supports an integer and a float type (this example has been taken from a previous paper [3]). The objects support only one operation, `add`, which adds two objects (promoting ints to floats in a mixed addition). The implementation of `add` uses classical Smalltalk-like double-dispatching. The classes can be seen in Figure 1 (written in RPython).

Using these classes to implement arithmetic shows the basic problem of many dynamic language implementations. All the numbers are instances of either `BoxedInteger` or `BoxedFloat`, therefore they consume space on the heap. Performing many arithmetic operations produces lots of garbage quickly, putting pressure on the garbage collector. Using double dispatching to implement the numeric tower needs two method calls per arithmetic operation, which is costly due to the method dispatch.

Let us now consider a simple “interpreter” function `f` that uses the object model (see the bottom of Figure 1). Simply running this function is slow, because there are lots of virtual method calls inside the loop, two for each call to `add`. These method calls need to check the type of the involved objects every iteration. In addition, a lot of

```

L0(p0, p1):
# inside f: y = y.add(step)
guard_class(p1, BoxedInteger)
# inside BoxedInteger.add
i2 = get(p1, intval)
guard_class(p0, BoxedInteger)
# inside BoxedInteger.add__int
i3 = get(p0, intval)
i4 = i2 + i3
p5 = new(BoxedInteger)
# inside BoxedInteger.__init__
set(p5, intval, i4)
jump(L0, p0, p5)

```

Figure 2. An Unoptimized Trace of the Example Interpreter

objects are created when executing that loop, many of these objects are short-lived. The actual computation that is performed by `f` is simply a sequence of float or integer additions (note that `f` does not actually terminate, but it is still instructive to look at the produced traces).

If the function is executed using the tracing JIT, with `y` being a `BoxedInteger`, the produced trace looks like the one of Figure 2 (lines starting with a hash “#” are comments). The trace corresponds to one iteration of the while-loop in `f`.

The operations in the trace are indented corresponding to the stack level of the function that contains the traced operation. The trace is in single-assignment form, meaning that each variable is assigned a value exactly once. The arguments `p0` and `p1` of the loop correspond to the live variables `y` and `step` in the while-loop of the original function.

The label of the loop is `L0` and is used by the jump instruction to identify its jump target.

The operations in the trace correspond to the operations in the RPython program in Figure 1:

- `new` creates a new object.
- `get` reads an attribute of an object.
- `set` writes to an attribute of an object.
- `guard_class` is a precise type check. It typically precedes an (inlined) method call and is followed by the trace of the called method.

Method calls in the trace are preceded by a `guard_class` operation, to check that the class of the receiver is the same as the one that was observed during tracing.² These guards make the trace specific to the situation where `y` is really a `BoxedInteger`. When the trace is turned into machine code and afterwards executed with `BoxedFloat`, the first `guard_class` instruction will fail and execution will continue using the interpreter.

5. Making Trace Optimizations Loop Aware

Reviewer 3 ► *In general, the paper is over-long on generalities and too short on details. For example, the description of the basic technique at the beginning of section 5 is the third time the idea is explained at basically the same level of detail (the others are in section 2 and section 4). In contrast, the optimizations applied rely on a simple type analysis, but this is only briefly alluded to.* ◀

Before a trace is passed to the backend compiling it into machine code it is optimized to achieve better performance. One goal of that is to move operations out of the loop making them executed only once and not every iteration. This we propose to achieve by

²`guard_class` performs a precise class check, not checking for subclasses.

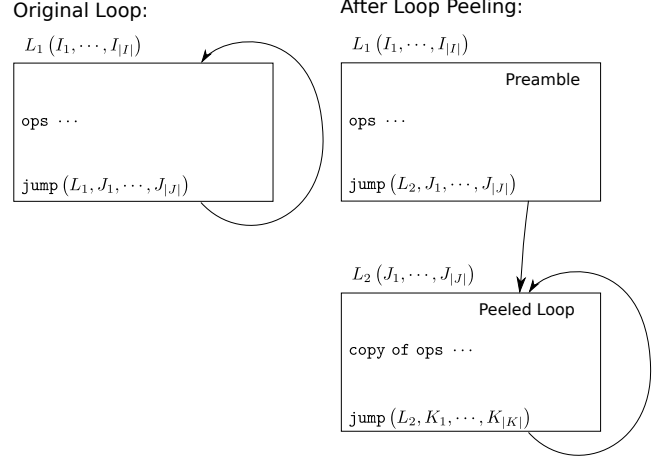


Figure 3. Overview of Loop Peeling

loop peeling. It leaves the loop body intact, but prefixes it with one iteration of the loop. This operation by itself will not achieve anything. But if it is combined with other optimizations it can increase the effectiveness of those optimizations. For many optimization of interest only a few additional details has to be considered when they are combined with loop peeling. These are described below by explaining the loop peeling optimization followed by a set of other optimizations and how they interact with loop peeling.

5.1 Loop Peeling

Loop peeling is achieved by appending an copy of the traced iteration at the end of itself. See Figure 3 for an illustration. The first part (called *preamble*) finishes with a jump the the second part (called the *peeled loop*). The second part finishes with a jump to itself. This way the preamble will be executed only once while the peeled loop will be used for every further iteration. New variable names have to be introduced in the entire copied trace in order to maintain the SSA-property. Note that the peeled loop is not necessary the *first* iteration of the loop execution, it is general enough to correspond to any iteration of the loop. However, the peeled loop can then be optimized using the assumption that a previous iteration has happened.

When applying optimizations to this two-iteration trace some care has to taken as to how the arguments of the two jump operations and the input arguments of the peeled loop are treated. It has to be ensured that the peeled loop stays a proper trace in the sense that the operations within it only operates on variables that are either among its input arguments or produced within the peeled loop. To ensure this we need to introduce a bit of formalism.

The original trace (prior to peeling) consists of three parts. A vector of input variables, $I = (I_1, I_2, \dots, I_{|I|})$, a list of non-jump operations and a single jump operation. The jump operation contains a vector of jump variables, $J = (J_1, J_2, \dots, J_{|J|})$, that are passed as the input variables of the target loop. After loop peeling there will be a second copy of this trace with input variables equal to the jump arguments of the preamble, J , and jump arguments K . Figure 3 illustrates the general case. The running example in Figure 2 has $I = (p_0, p_1)$ and $J = (p_0, p_5)$. The result of applying loop peeling to it is shown in Figure 4 with $K = (p_0, p_9)$.

To construct the second copy of the trace (the peeled loop) from the first (the preamble) we need a function m , mapping the variables of the preamble onto the variables of the peeled loop. This function is constructed during the copying. It is initialized by

```

L0(p0, p1):
# inside f: y = y.add(step)
guard_class(p1, BoxedInteger)
# inside BoxedInteger.add
i2 = get(p1, intval)
guard_class(p0, BoxedInteger)
# inside BoxedInteger.add__int
i3 = get(p0, intval)
i4 = i2 + i3
p5 = new(BoxedInteger)
# inside BoxedInteger.__init__
set(p5, intval, i4)
jump(L1, p0, p5)

L1(p0, p5):
# inside f: y = y.add(step)
guard_class(p5, BoxedInteger)
# inside BoxedInteger.add
i6 = get(p5, intval)
guard_class(p0, BoxedInteger)
# inside BoxedInteger.add__int
i7 = get(p0, intval)
i8 = i6 + i7
p9 = new(BoxedInteger)
# inside BoxedInteger.__init__
set(p9, intval, i8)
jump(L1, p0, p9)

```

Figure 4. A peeled trace of the Example Interpreter

mapping the input arguments, I , to the jump arguments J ,

$$m(I_i) = J_i \text{ for } i = 1, 2, \dots, |I|. \quad (1)$$

In the example that means:

$$\begin{aligned} m(p_0) &= p_0 \\ m(p_1) &= p_5 \end{aligned} \quad (2)$$

Each operation in the trace is copied in order. To copy an operation $v = \text{op}(A_1, A_2, \dots, A_{|A|})$ a new variable, \hat{v} is introduced. The copied operation will return \hat{v} using

$$\hat{v} = \text{op}(m(A_1), m(A_2), \dots, m(A_{|A|})). \quad (3)$$

Before the next operation is copied, m is extend by assigning $m(v) = \hat{v}$. For the example above, that will extend m with

$$\begin{aligned} m(i_2) &= i_6 \\ m(i_3) &= i_7 \\ m(i_4) &= i_8 \\ m(p_5) &= p_9 \end{aligned} \quad (4)$$

6. Interaction of Optimizations with Loop Peeling

6.1 Redundant Guard Removal

No special concerns needs to be taken when implementing redundant guard removal together with loop peeling. The guards from the preamble might make the guards of the peeled loop redundant and thus removed. Therefore one effect of combining redundant guard removal with loop peeling is that loop-invariant guards are moved out of the loop. The peeled loop of the example reduces to

```

L1(p0, p5):
# inside f: y = y.add(step)
# inside BoxedInteger.add
i6 = get(p5, intval)
# inside BoxedInteger.add__int
i7 = get(p0, intval)
i8 = i6 + i7
p9 = new(BoxedInteger)
# inside BoxedInteger.__init__
set(p9, intval, i8)
jump(L1, p0, p9)

```

The guard on p_5 on line 17 of Figure 4 can be removed since p_5 is allocated on line 10 with a known class. The guard on p_0 on line 20 can be removed since it is identical to the guard on line 6.

Note that the guard on p_5 is removed even though p_5 is not loop invariant, which shows that loop invariant code motion is not the only effect of loop peeling. Loop peeling can also remove guards that are implied by the guards of the previous iteration.

6.2 Common Subexpression Elimination and Heap Optimizations

If a pure operation appears more than once in the trace with the same input arguments, it only needs be executed the first time and then the result can be reused for all other appearances. PyPy’s optimizers can also remove repeated heap reads if the intermediate operations cannot have changed their value³.

When that is combined with loop peeling, the single execution of the operation is placed in the preamble. That is, loop invariant pure operations and heap reads are moved out of the loop.

Consider the `get` operation on line 22 of Figure 4. The result of this operation can be deduced to be i_3 from the `get` operation on line 8. The optimization will thus remove line 22 from the trace and replace i_7 with i_3 . Afterwards the trace is no longer in the correct form, because the argument i_3 is not passed along the loop arguments. It thus needs to be added there.

The trace from Figure 4 will therefore be optimized to:

```

L0(p0, p1):
# inside f: y = y.add(step)
guard_class(p1, BoxedInteger)
# inside BoxedInteger.add
i2 = get(p1, intval)
guard_class(p0, BoxedInteger)
# inside BoxedInteger.add__int
i3 = get(p0, intval)
i4 = i2 + i3
p5 = new(BoxedInteger)
# inside BoxedInteger.__init__
set(p5, intval, i4)
jump(L1, p0, p5, i3)

L1(p0, p5, i3):
# inside f: y = y.add(step)
guard_class(p5, BoxedInteger)
# inside BoxedInteger.add
i6 = get(p5, intval)
guard_class(p0, BoxedInteger)
# inside BoxedInteger.add__int
i8 = i4 + i3
p9 = new(BoxedInteger)
# inside BoxedInteger.__init__
set(p9, intval, i8)
jump(L1, p0, p9, i3)

```

After loop peeling and redundant operation removal the peeled loop will typically no longer be in SSA form but operate on variables that are the result of operations in the preamble. The solution is to extend the input arguments, J , with those variables. This will also extend the jump arguments of the preamble, which is also J . Implicitly that also extends the jump arguments of the peeled loop, K , since they are the image of J under m . For the example I has to be replaced by \hat{I} which is formed by appending i_3 to I . At the same time K has to be replaced by \hat{K} which is formed by appending $m(i_3) = i_7$ to K . The variable i_7 will then be replaced by i_3 by the heap caching optimization as it has removed the variable i_7 .

In general what is needed is to keep track of which variables from the preamble are reused in the peeled loop. By constructing a

³ We perform a simple type-based alias analysis to know which writes can affect which reads. In addition writes on newly allocated objects can never change the value of old existing ones.

vector, H , of such variables, the input and jump arguments can be updated using

$$\hat{J} = (J_1, J_2, \dots, J_{|J|}, H_1, H_2, \dots, H_{|H|}) \quad (5)$$

and

$$\hat{K} = (K_1, K_2, \dots, K_{|J|}, m(H_1), m(H_2), \dots, m(H_{|H|})). \quad (6)$$

In the optimized trace I is replaced by \hat{I} and K by \hat{K} .

6.3 Allocation Removals

PyPy’s allocation removal optimization [3] makes it possible to identify objects that are allocated within the loop but never escape it. That is, no outside object ever gets a reference to them. This is performed by processing the operations in order and optimistically removing every new operation. Later on if it is discovered that a reference to the object escapes the loop, the new operation is inserted at this point. All operations (get, set and guard) on the removed objects are also removed and the optimizer needs to keep track of the value of all used attributes of the object.

Consider again the original unoptimized trace of Figure 4. Line 10 contains the first allocation. It is removed and p_5 is marked as allocation-removed. This means that it refers to an object that has not yet been (and might never be) allocated. Line 12 sets the `intval` attribute of p_5 . This operation is also removed and the optimizer registers that the attribute `intval` of p_5 is i_4 .

When the optimizer reaches line 13 it needs to construct the arguments of the `jump` operation, which contains the reference to the allocation-removed object in p_5 . This can be achieved by exploding p_5 into the attributes of the allocation-removed object. In this case there is only one such attribute and its value is i_4 , which means that p_5 is replaced with i_4 in the jump arguments.

In the general case, each allocation-removed object in the jump arguments is exploded into a vector of variables containing the values of all registered attributes⁴. If some of the attributes are themselves references to allocation-removed objects they are recursively exploded to make the vector contain only concrete variables. Some care has to be taken to always place the attributes in the same order when performing this explosion. Notation becomes somewhat simpler if also every concrete variable of the jump arguments is exploded into a vector containing itself. For every variable, J_k , of the original jump arguments, J , let

$$\tilde{J}^{(k)} = \begin{cases} (J_k) & \text{if } J_k \text{ is concrete} \\ H^{(k)} & \text{if } J_k \text{ is allocation-removed} \end{cases}, \quad (7)$$

where $H^{(k)}$ is a vector containing all concrete attributes of J_k . The arguments of the optimized `jump` operation are constructed as the concatenation all the $\tilde{J}^{(k)}$ vectors,

$$\hat{J} = (\tilde{J}^{(1)} \quad \tilde{J}^{(2)} \quad \dots \quad \tilde{J}^{(|J|)}). \quad (8)$$

The arguments of the `jump` operation of the peeled loop, K , is constructed by inlining \hat{J} ,

$$\hat{K} = (m(\hat{J}_1), m(\hat{J}_1), \dots, m(\hat{J}_{|J|})). \quad (9)$$

In the optimized trace I is replaced by \hat{I} and K by \hat{K} . The trace from Figure 2 will be optimized into

```

L0(p0, p1):
# inside f: y = y.add(step)
guard_class(p1, BoxedInteger)
# inside BoxedInteger.add
i2 = get(p1, intval)
guard_class(p0, BoxedInteger)
# inside BoxedInteger.add__int

```

⁴This is sometimes called *scalar replacement*.

```

i3 = get(p0, intval)
i4 = i2 + i3
# inside BoxedInteger.__init__
jump(L1, p0, i4)

L1(p0, i4):
# inside f: y = y.add(step)
# inside BoxedInteger.add
guard_class(p0, BoxedInteger)
# inside BoxedInteger.add__int
i7 = get(p0, intval)
i8 = i4 + i7
# inside BoxedInteger.__init__
jump(L1, p0, i8)

```

If all the optimizations presented above are applied, the resulting optimized peeled loop will consist of a single integer addition only. That is it will become type-specialized to the types of the variables `step` and `y`, and the overhead of using boxed values is removed.

Reviewer 3 ▶ This paper presents an elegant, if simple, technique, and demonstrates that it’s effective in small cases. The worked example is particularly helpful, and would be better if it were worked more thoroughly. Some of the omitted steps are not entirely obvious, and the paper would be improved by making the clearer. In particular, the final program presented on the bottom of page 5, first column, still has memory access, boxing, and type checks, which the paper then claims can be removed. There’s enough space to show this. ◀

7. Benchmarks

Reviewer 2 ▶ A nit: Section 7 says that loop peeling never makes runtime performance worse, but generating more code can potentially slow performance. I assume that non-numeric benchmarks show no slowdown in practice, and that might be worth noting. ◀

Reviewer 2 ▶ Section 7 also mentions performance improvements for a Prolog interpreter. Consider adding a brief explanation of the benefit, since that example stands out as a non-numeric (I assume) performance improvement. ◀

Reviewer 3 ▶ Providing source code for the benchmarks measured are needed for others to reproduce and build on your results. I believe this should be the minimum standard for publishing measurements such as these. ◀

Reviewer 3 ▶ I would have liked to have benchmark results for some larger applications. When is this optimization effective on a large scale, if ever? ◀

Reviewer 4 ▶ It isn’t clear from the paper, but a reader might conclude that the bulk of the time savings are from removing boxing/unboxing operations. ◀

Reviewer 4 ▶ The benchmark results appear quite impressive – especially the comparison with GCC – but without additional information, I have no idea what is being compared. Are these results from the same sizes of integers and/or floating point results? ◀

Reviewer 4 ▶ This paper is relatively short, and could be significantly improved with a couple of pages of additional information about the details of the benchmarks – both on the Python and on the C side. ◀

The loop peeling optimization was implemented in the PyPy framework in about 450 lines of RPython code. That means that the JIT-compilers generated for all interpreters implemented within PyPy now can take advantage of it. Benchmarks have been executed for a few different interpreters and we see improvements in several cases. The ideal loop for this optimization is short and contains numerical calculations with no failing guards and no external calls. Larger loops involving many operations on complex objects typically benefit less from it. Loop peeling never makes runtime performance worse, in the worst case the peeled loop is exactly the

	CPython	PyPy no LP	PyPy	It's input argument, y , while in C, there are three different implementations.
FFT(1024, 32768)	469.07	20.83 +- 0.02	12.73 +- 0.01	• conv3 : one-dimensional convolution with fixed kernel-size 3.
FFT(1024,32768)	-	-	-	• conv5 : one-dimensional convolution with fixed kernel-size 5.
FFT(1048576, 2)	58.93	4.12 +- 0.01	2.05 +- 0.00	• conv3x3 : two-dimensional convolution with kernel of fixed size 3×3 using a custom class to represent two-dimensional arrays.
FFT(1048576,2)	-	-	-	• dilate3x3 : two-dimensional dilation with kernel of fixed size 3×3 . This is similar to convolution but instead of summing over the elements, the maximum is taken. That places a external call to a max function within the loop that prevents some of the optimizations.
LU(100, 4096)	1974.14	32.22 +- 0.14	13.39 +- 0.03	• sobel : a low-level video-processing algorithm used to locate edges in an image. It calculates the gradient magnitude using Sobel derivatives.
LU(100,4096)	-	-	-	
LU(1000, 2)	955.31	14.98 +- 0.22	5.99 +- 0.21	
LU(1000,2)	-	-	-	
MonteCarlo(268435456)	618.89	20.60 +- 0.05	15.33 +- 0.08	
SOR(100, 32768)	1458.12	8.24 +- 0.00	2.66 +- 0.00	
SOR(100,32768)	-	-	-	
SOR(1000, 256)	1210.45	6.48 +- 0.00	2.10 +- 0.00	
SOR(1000,256)	-	-	-	
SparseMatMult(1000, 5000, 262144)	371.66	24.25 +- 0.04	16.52 +- 0.04	
SparseMatMult(1000,5000,262144)	-	-	-	
SparseMatMult(100000, 1000000, 1024)	236.93	17.01 +- 0.01	8.75 +- 0.08	
SparseMatMult(100000,1000000,1024)	-	-	-	
conv3(100, nil)	-	-	-	
conv3(1000, nil)	-	-	-	
conv3(1e5)	-	-	-	
conv3(1e6)	-	-	-	
conv3(array(1e5))	50.14	1.09 +- 0.01	0.49 +- 0.01	
conv3(array(1e6))	49.20	1.13 +- 0.02	0.51 +- 0.00	
conv3x3(1000)	-	-	-	
conv3x3(1000, 1000)	-	-	-	
conv3x3(1000000, 3)	-	-	-	
conv3x3(3)	-	-	-	
conv3x3(Array2D(1000000x3))	139.81	0.70 +- 0.00	0.21 +- 0.00	
conv3x3(Array2D(1000x1000))	138.95	0.70 +- 0.00	0.20 +- 0.00	
conv5(100, nil)	-	-	-	
conv5(1000, nil)	-	-	-	
conv5(1e5)	-	-	-	
conv5(1e6)	-	-	-	
conv5(array(1e5))	74.65	1.22 +- 0.00	0.64 +- 0.00	
conv5(array(1e6))	77.94	1.26 +- 0.00	0.68 +- 0.00	
dilate3x3(1000)	-	-	-	
dilate3x3(1000, 1000)	-	-	-	
dilate3x3(Array2D(1000x1000))	137.52	4.35 +- 0.01	3.91 +- 0.00	
sobel(Array2D(1000x1000))	104.02	0.49 +- 0.00	0.21 +- 0.00	
sobel_magnitude(1000, 1000)	-	-	-	
sqrt(Fix16)	463.46	5.12 +- 0.00	2.96 +- 0.00	
sqrt(float)	14.99	1.37 +- 0.00	0.89 +- 0.00	
sqrt(int)	13.91	3.22 +- 0.02	2.65 +- 0.00	

Figure 5. Benchmark Results in Seconds. Arrays of length 10^5 and 10^6 and matrixes of size 1000×1000 and 1000000×3 are used. The one used in each benchmark is indicated in the leftmost column. For the matrixes, only the number of rows are specified.

same as the preamble. Therefore we chose to present benchmarks of small numeric kernels where loop peeling can show its use.

7.1 Python

The Python interpreter of the PyPy framework is a complete Python version 2.7 compatible interpreter. A set of numerical calculations were implemented in both Python and in C and their runtimes are compared in Figure 7. The benchmarks are

- **sqrt**: approximates the square root of y as x_∞ with $x_0 = y/2$ and $x_k = (x_{k-1} + y/x_{k-1})/2$. There are three different versions of this benchmark where x_k is represented with different type of objects: int's, float's and Fix16's. The latter, Fix16, is a custom class that implements fixpoint arithmetic with 16 bits precision. In Python there is only a single implementation of the benchmark that gets specialized depending on the class of

We can observe that PyPy (even without loop peeling) is orders of magnitude faster than either CPython or Psyco. This is due to the JIT compilation advantages and optimizations we discussed in previous work [3, 4]. The geometric mean of the speedup of loop peeling is 70%, which makes benchmark times comparable with native-compiled C code. We attribute the performance gap to C code to the relative immaturity of PyPy's JIT assembler backend as well as missing optimizations, like instruction scheduling.

Other interesting interpreters that are helped greatly by this optimization are for example our Prolog interpreter written in RPython, as well as numerical kernel used for array manipulation. The exact extent is out of scope for this paper.

8. Related Work

Reviewer 1 ▶ First sentence of the related work section is kind of unfortunate. It is unclear what the reference at the end of the sentence is good for. To support the meaning of the entire sentence? Or is it just a reference to the standard loop invariant code motion techniques? The contribution of your paper seems much smaller than in the former case compared to the latter one. While I have not checked the content of the book, I believe the latter is

the correct interpretation. You should remove this opportunity for misinterpretation. ◀

The effect of combining a one pass optimization with loop peeling gives completely standard loop invariant code motion optimizations [8]. We do not claim any novelty in the effect, but think that our implementation scheme is a very simple one.

Reviewer 3 ▶ *The discussion of LuaJIT is unsatisfying. It's not clear to me from that one quote that Mike is doing the same thing. It might be worth including LuaJIT in the benchmarks, and/or examining the actual implementation of LuaJIT.* ◀

Mike Pall, the author of LuaJIT⁵ seems to have developed the described technique independently. There are no papers about LuaJIT but the author of it writes on a mailing list: “The LOOP pass does synthetic unrolling of the recorded IR, combining copy-substitution with redundancy elimination to achieve code hoisting. The unrolled and copy-substituted instructions are simply fed back into the compiler pipeline, which allows reuse of all optimizations for redundancy elimination. Loop recurrences are detected on-the-fly and a minimized set of PHIs is generated.” [9]

Both the Hotpath VM [7] and SPUR [2] implements loop-invariant code motion directly, by explicitly marking as loop-invariant all variables that stay the same along all looping paths and then moving all pure computation that depends only on these variables out of the loop. SPUR can also hoist loads out of the loop if nothing in the loop can ever write to the memory location. It can also move allocations out of the loop, but does not replace the object by its attributes. This saves only the allocation, not the access to the object attributes.

The type specialization described by Gal *et al.* [6] can be seen as doing a similar optimization (again by manually implementing it) than the one described in Section 6.3: The effect of both is that type checks are fully done before a loop is even entered.

9. Conclusions

In this paper we have studied loop invariant code motion during trace compilation. We claim that loop peeling is a very convenient solution here since it fits well with other trace optimizations and does not require large changes to them. This approach improves the effect of standard optimizations such as redundant guard removal, common subexpression elimination and allocation removal. The most prominent effect is that they all become loop invariant code motion optimizations.

By using several benchmarks we show that the proposed algorithm can significantly improve the run time of small loops containing numerical calculations.

The current approach still has some limitations which we plan to address in the future. In particular loop peeling works poorly in combination with trace trees or trace stitching. The side exits attached guards that fail often currently have to jump to the preamble which makes loops with several equally common paths less efficient than they could be.

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⁵<http://luajit.org/>