

### 3. Basics of Classical Computer

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Turing machine

Circuit model

Two computation model

## Turing machine

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# Definition of Turing machine

## Components of a Turing machine



# Definition of Turing machine

## Operation of a Turing Machine

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## Definition 1

A partial function  $f : A^* \rightarrow A$  is computable if there exists a Turing machine  $M$  such that  $\delta_M = f$ . In this case, we say that  $f$  is computed by  $M$ .

## Church-Turing thesis

The class of functions computable by a Turing machine corresponds exactly to the class of functions which we would naturally regard as being computable by an algorithm.



## Halting problem

Does turing machine  $M$  halt for given input  $x$ ?

→ *We can't compute halting problem by any turing machine!*

\* Proof: (귀류법) Halting 문제를 풀 수 있는 TM HALT가 존재한다고 가정하자.



## Circuit model

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## Theorem 2

*Circuit model can solve every type of boolean function.*

$$f : \{0, 1\}^n \rightarrow \{0, 1\}^m$$

## Two computation model

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## Definition 3 (uniform circuit family)

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Can circuit model solve halting problem?

- M. A. Nielsen and I. L. Chuang, Quantum Computation and Quantum Information
- Lecture notes for QU511: Quantum Computing (Fall 2024)