**Nova Southeastern University**

**College of Computing and Engineering**

**ISEC 620 Applied Cryptography**

**Fall 2020**

**(August 17– December 6, 2020)**

Written Assignment #2

Due Date: October 4, 2020

Instructor: Dr. Junping Sun

1. What is the difference between a block cipher and stream cipher? (10 points)

A **Block** **Cipher** can convert more bits then a **Stream** **Cipher**, this is because a Stream Cipher only converts by one Byte at a time which is 8 Bits. Theoretically since A Block Cipher converts by the block, it can convert 64 bits and up at a time. Decryption is more complex on a Block Cipher compared to a Stream Cipher. Also, the Block Cipher is a Feistel Cipher while the Stream Cipher is a Vernam Cipher. Since a Stream Cipher is less complex it is faster and less resource intensive while the Block Cipher is more cryptographically secure but more resource intensive.

2. What is the difference between diffusion and confusion? (15 points)

**Confusion** aims to protect cryptographic integrity by using substitution. This confuses the key breaker by ensuring the cipher text does not give way to the plaintext. An example of this would be the plain text “ABC” becoming the cipher text “XYZ” This way the assailant should be confused on what the original value of what “XYZ” was if they were able to obtain the cipher text.

**Diffusion** aims to protect cryptographic integrity using permutation through transposition. An example of this would be the plaintext “ABC” becoming the ciphertext “BCA”. This leaves the Ciphertext diffused making it hard for the algorithm cracker to fuse the plaintext back together.

So, Confusion is based off of Substitution while Diffusion is based off of transposition.

3. Which parameters and design choices determine the actual algorithm of a Feistel cipher? (35 points)

When it comes to a **Feistel Cipher** design choice’s the following come into discussion.

**Block Size:** The larger the sizes the more security but slower speeds.

**Key Size:** The larger the sizes the more security but slower speeds.

**Number of Rounds:** More rounds the more security but slower speed.

**How the subkey is generated:** The more complex the more secure but more resource intensive.

**Round function complexity:** The more complex the more secure but more resource intensive.

**The Ability to Cryptanalyze:** When developing an algorithm, and design it in such a way that one can perform a cryptanalysis on it they can then use that data to determine how to make it stronger and more efficient. By making an algorithm less susceptive to a cryptanalysis it arguably limits the learning and development of a strong algorithm.

4. What is the difference between differential and linear cryptanalysis? (10 points)

A **Linear cryptanalysi**s is known as a plaintext attack, in this the attacker gains insight about the algorithm by finding linear relations between bits of the plaintext, the ciphertext, and the key, in a piece by piece format. This is done by decrypting each cipher by trying all possibilities of sub-keys for one round of encryption. Then analyzing the cipher texts random results to derive the key.

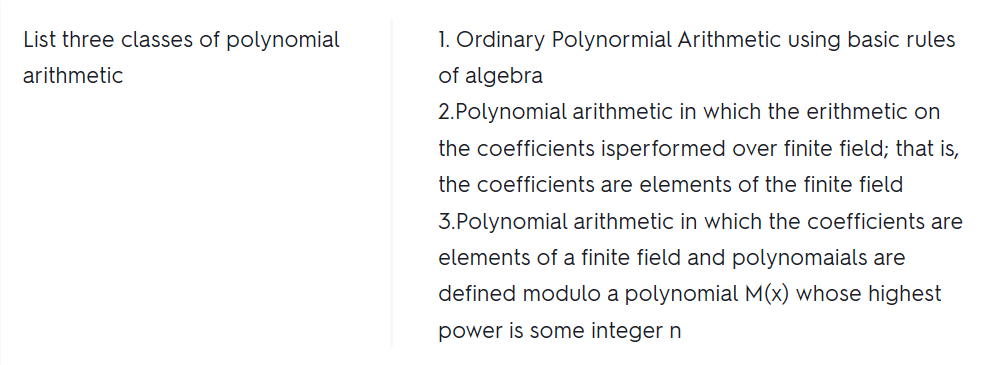
In a **Differential Cryptanalysis**, the attacker puts different inputs to the encryption algorithm and studies the corresponding outputs. This compares the differences and analyzes where similarities and non-random behavior occurs compared to other inputs. This is called differential because it compares the differences between different inputs.

5. List three classes of polynomial arithmetic. (15 points)

**Ordinary Polynomial Arithmetic:** Uses basic rules of algebra.

**Polynomial Arithmetic of Finite Fields:** Arithmetic on coefficients is performed over a finite

field.

**Polynomial Arithmetic with a defined Modulo:** A polynomial M(x) whose highest power is some integer N. 

6. Does the set of residue classes modulo 3 form a group? (10 points)

1. with respect to addition?

No, it will NOT form a group with respect to modular addition.

This can be proven by showing that the inverse element A for 1 can NOT be determined.

**Inverse Addition:**

Example: A=1.

Residue Class of 1 = (… -10, -7, -4, 1, 4, 7, 10 …)

Let’s consider A=1, B= -4, C= -7

Formula: if(A+B) = ((A+C)Mod3) then B = ((C)Mod3)

Simplified: (1-4)=(1-7)mod3? No. they do not equal eachother.

Since, (-3) ≠ ((-6)mod3) , the inverse element A for 1 can NOT be determined making it un-able to form a group in respect to modular addition.

1. with respect to multiplication?

Yes, it WILL form a group with respect to modular multiplication.

**Multiplication:**

Example: A=1.

Residue Class of 1 = (… -10, -7, -4, 1, 4, 7, 10 …)

Let’s consider A=1, B= 4, C= 7

Formula: if(A\*B) = (A\*C)(Mod3) then B = (C)(Mod3)

Simplified: if(1\*4) = ((1\*7)(Mod3) == > 4= 7mod3 is TRUE

**Inverse Multiplication:**

Example: A=1.

Residue Class of 1 = (… -10, -7, -4, 1, 4, 7, 10 …)

Let’s consider A=1, B= 4, C= 7

Formula: if (A-1)(A\*B) = ((A-1)((A\*C))(Mod3) then B = (C)(Mod3)

Simplified: if (1-1)(1\*4) = ((1-1) (1\*7))(Mod3) == > 4= 7mod3 is TRUE

By proving the inverse property is satisfied this shows that residue class of modulo 3 can form a group with respect to modular multiplication.

7. Find integers *x* such that:

1. 5*x* ≡ 4 (mod 3) (5 points)

Means 5x -4 is a multiple of 3.

X=2, 5, 8, 11, 14 … (3N-1).

1. 7*x* ≡ 6 (mod 5) (5 points)

Means 7x-6 is a multiple of 5.

X= 3, 8, 13, 18, 23…(5N-2).

1. 9*x* ≡ 8 (mod 7) (5 points)

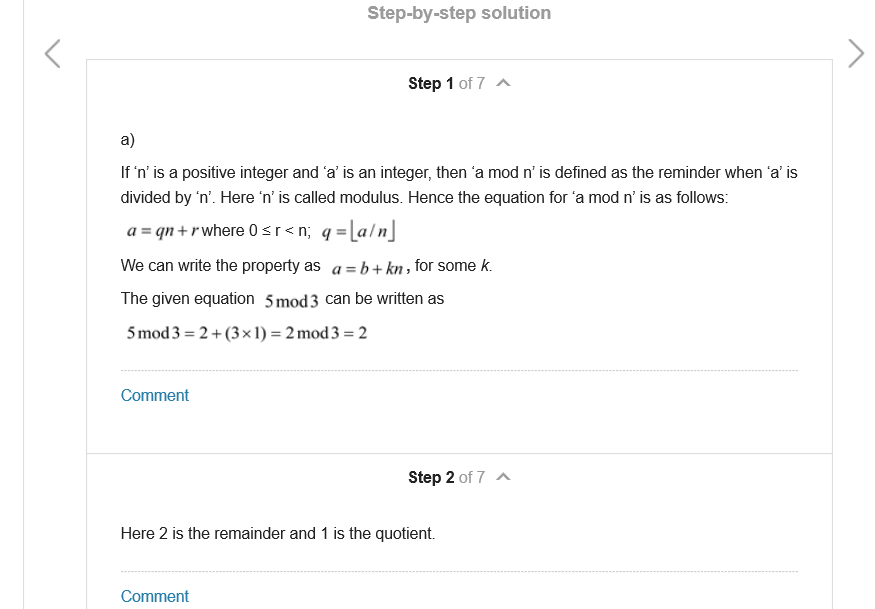
Means 9x-8 is a multiple of 7.

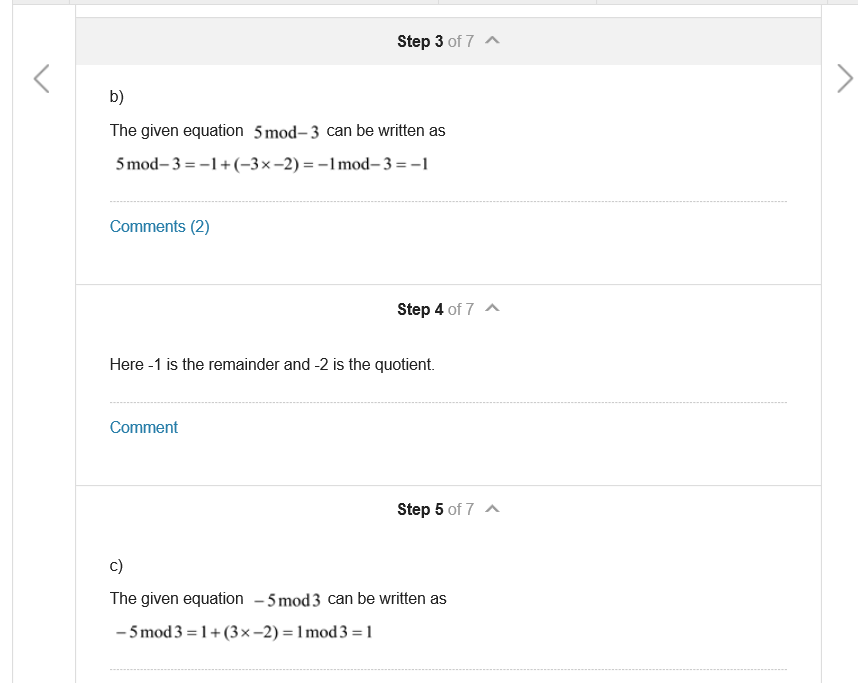
X= 4,11,18,25 …(7N-3).

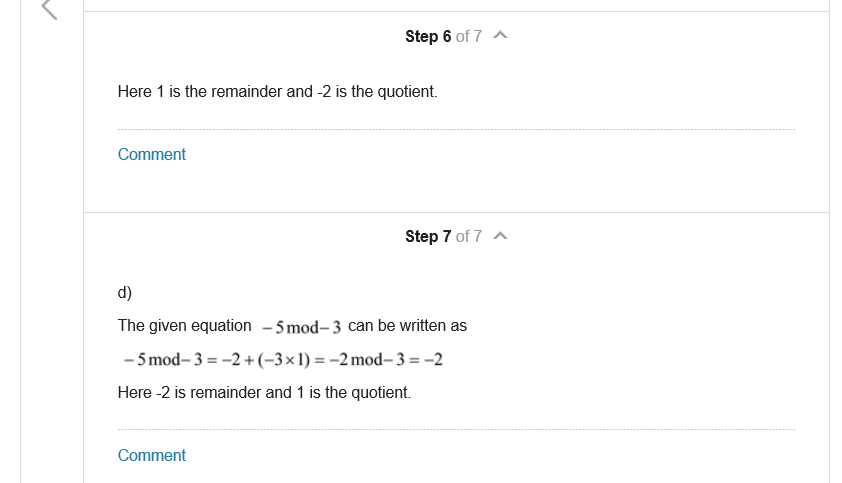
8. In this text we assume that the modulus is a positive integer. But the definition of the expression *a* mod *n* also makes perfect sense if *n* is negative. (20 points)

Determine the following:

1. 5 mod 3
2. 5 mod -3
3. -5 mod 3
4. -5 mod -3





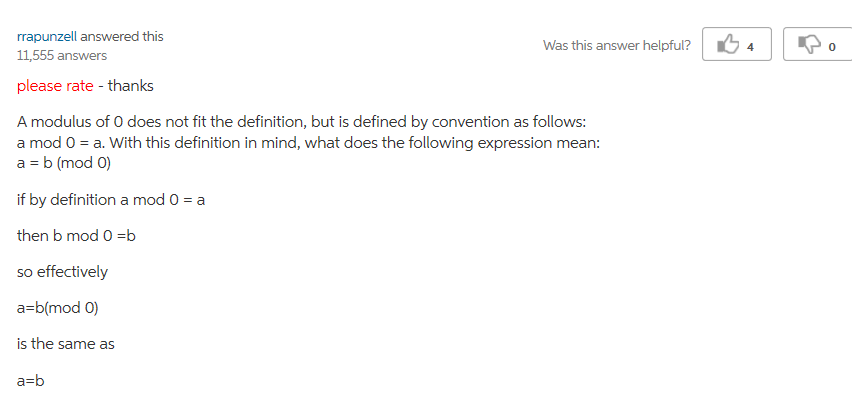


9. A modulus of 0 does not fit the definition, but is defined by convention as follows:

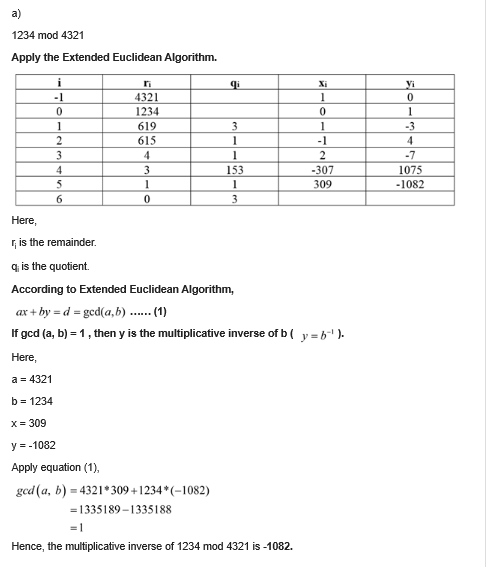
*a* mod 0 = *a*.

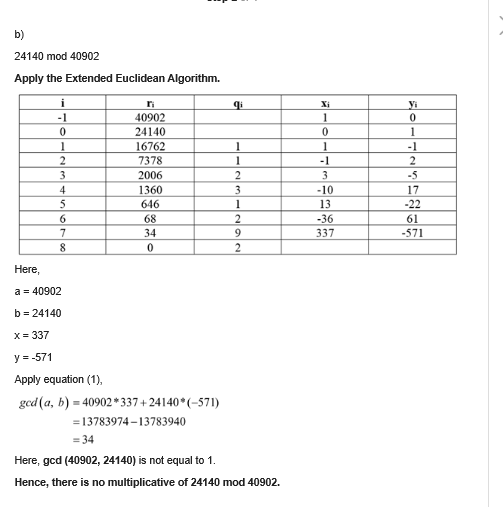
With this definition in mind, what does the following expression mean:

*a* ≡ *b* (mod 0) (10 points)

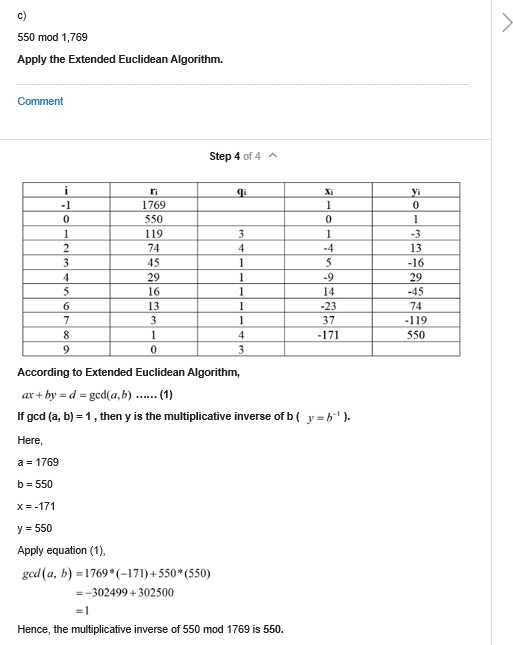


10. Using the extended Euclidean algorithm, and find the multiplicative inverse of

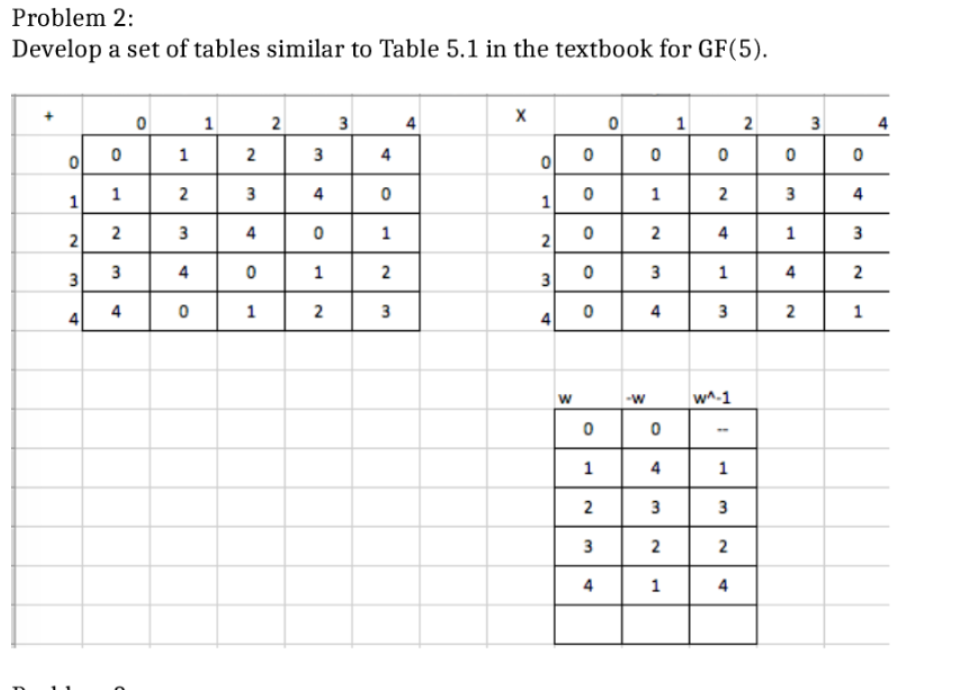
1. 1234 mod 4321 (5 points)
2. 
3. 24140 mod 40902 (5 points)

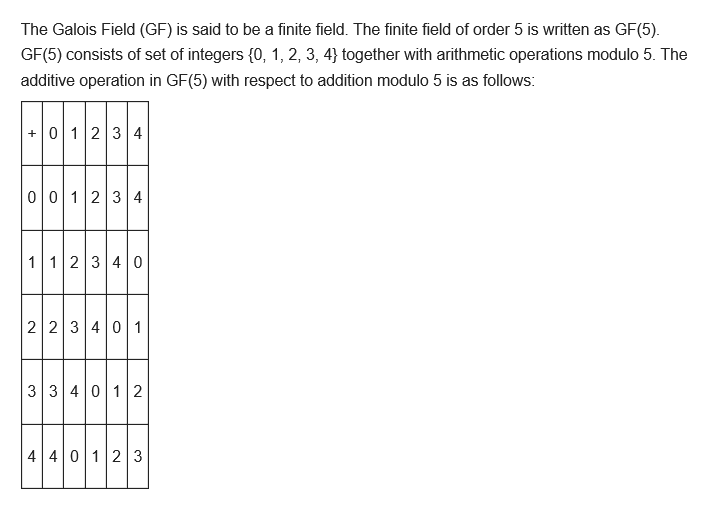


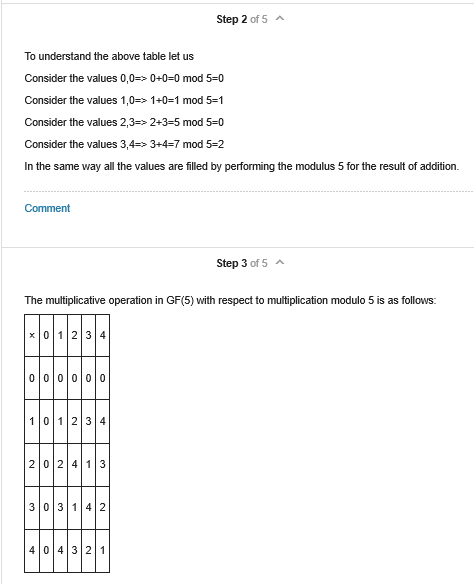
1. 550 mod 1769 (5 points)

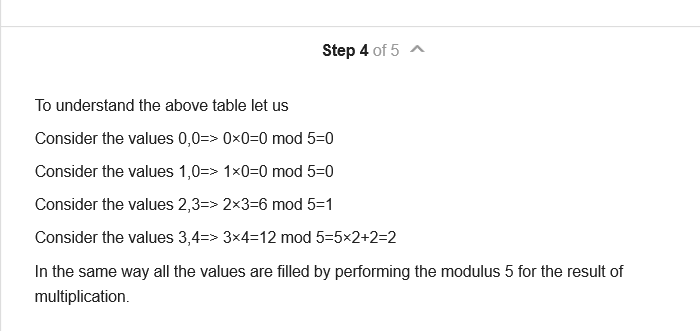


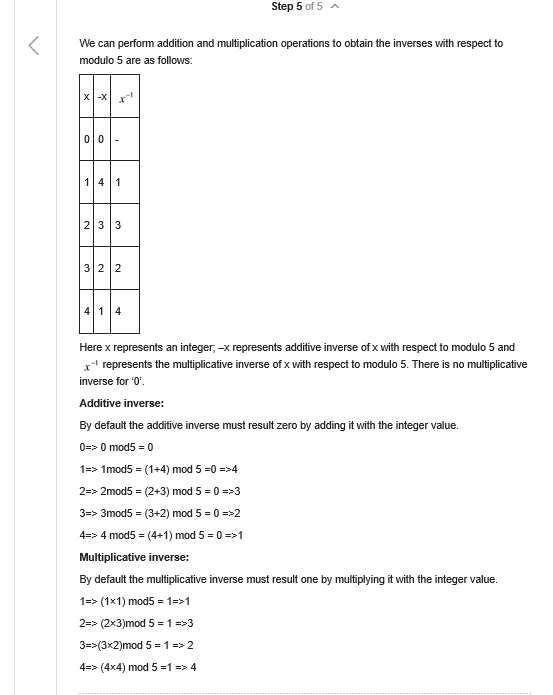
11. Develop a set of tables similar to Table 5.2 for GF(5). (20 points)



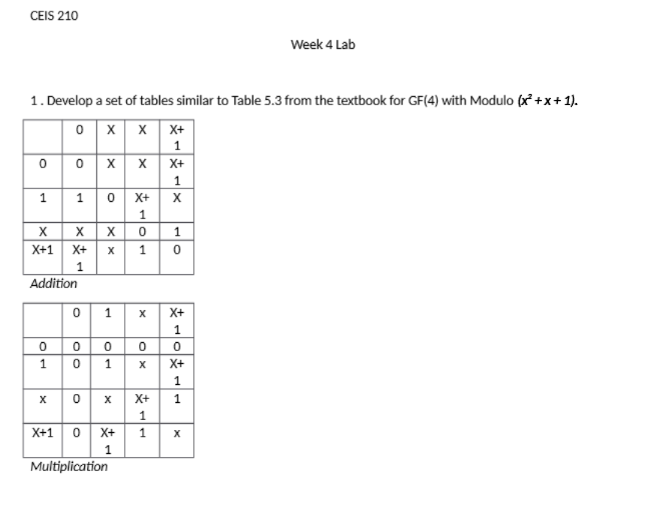


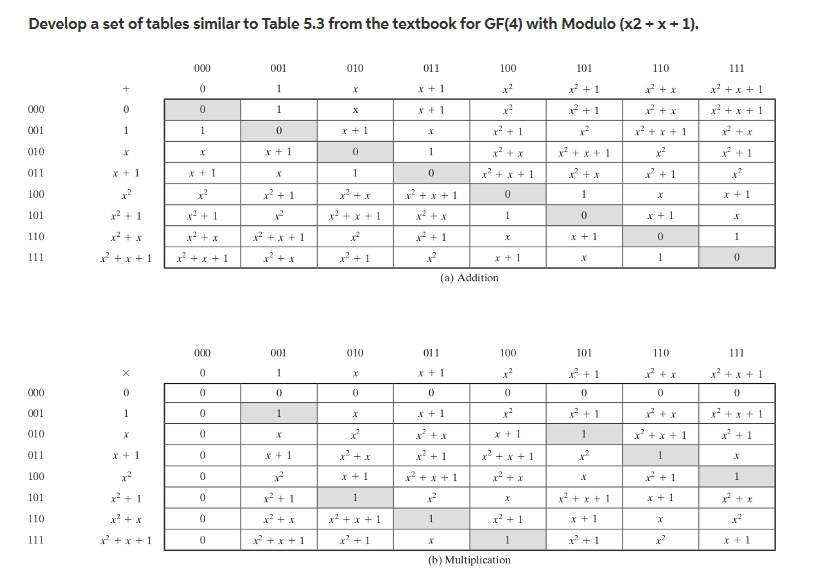






12. Develop a set of tables similar to Table 5.3 for GF(4) with *m*(*x*) = *x*2 + *x* +1 (20 points)





OTHER

