

Time Warp Simulation on Multi-core Processors and Clusters

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Abstract

Acknowledgments

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Chapter 1

Introduction

1.1 Motivation and Plan of Study

Many systems can be described by events that occur in discrete time intervals such as communication networks, digital logic circuits, transportation systems, or disease outbreak. To gain a better understanding of these systems, researchers develop models of the systems and perform simulations on computing platforms. These *Discrete Event Simulations* (DESs) can take a long time to simulate large, complex systems by sequentially processing events and has led researchers to design parallel algorithms to run simulations on parallel computing platforms. The field of study that deals with parallel algorithms to speed up discrete event simulations is called Parallel Discrete Event Simulation (PDES).

Parallel algorithms can be written for shared memory architectures, clusters, or any other type of system that supports hardware concurrency. Furthermore, communication between concurrent workers in the system can be achieved through shared data structures or through explicit messages that are passed among workers.

Some time warp systems are designed for only shared memory multiprocessors and use shared memory for communication. These systems minimize communication latencies and allow very fast, simple algorithm because everything can run in a single address space and use shared data structures but are still limited in computational power, memory size, and memory bandwidth.

Other time warp systems are completely based on a message passing system that can be scaled to any

number of processor cores on any number of machines. However, the time it takes to exchange messages with message passing is usually higher due to message copying, temporary buffering, and network latencies.

The WARPED2 simulation kernel, which is a reimplement of the original WARPED simulation kernel, is an entirely different approach which uses shared memory between *worker threads* in a single process to eliminate communication overheads, but uses message passing between processes to allow the system to scale to larger sizes. A dedicated *manager thread* handles all message passing communication between processes. Figure 1.1 illustrates the communication model that is used in WARPED2.

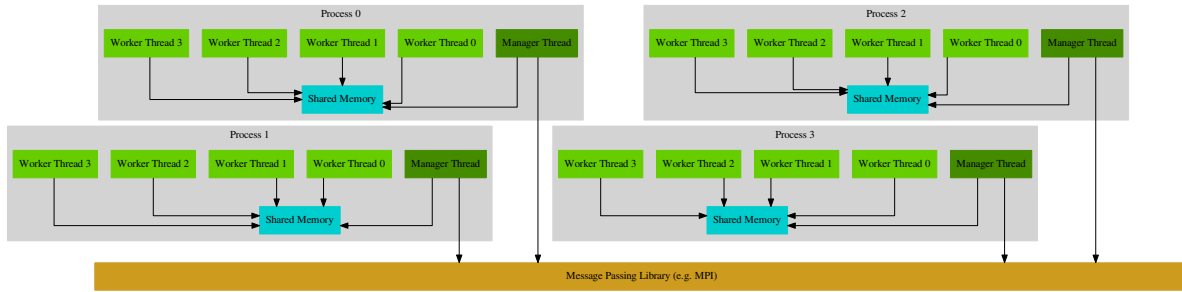


Figure 1.1: Communication Model of WARPED2

This communication model not only allows for high scalability and reduced communication overhead within processes, but allow the simulation to follow the critical path better since the worker threads can share a scheduling data structure to process events from. Less scheduling data structures creates a bottleneck since multiple worker threads cannot access them simultaneously without race conditions. On the other hand, more scheduling data structures allows more concurrency but spreads out the critical path of execution, allowing more rollbacks.

To further reduce any communication overheads in both message passing and shared memory communication, partitioning the work between processes can have a significant impact. Partitioning the work between processes in a parallel discrete event simulation can be achieved by partitioning the logical processes

The combination of shared memory and message passing communication does create some complications in the implementation of a time warp system. GVT and termination detection algorithms are usually designed for either shared memory or message passing but not both. Using a single message passing algo-

rithm between worker threads and processes would mean that some kind of message passing scheme would have to be implemented for worker threads to communicate. This scheme would still use shared memory for message communication but would still have the overheads of using explicit messages. On the contrarary, it is possible to have a single shared memory algorithm that extends to distributed memory systems but would require shared virtual memory. A shared virtual memory system would still have to transparently use message passing to achieve synchronization. For these reasons, the GVT and termination algorithms developed for WARPED2 include a message passing base algorithm and a shared memory subalgorithm.

Using shared memory introduces a whole new set of problems that must be

1.2 Thesis Overview

The remainder of this thesis is organized as follows:

Chapter 2 contains some background information on parallel simulation and parallel computing that is used in this thesis.

Chapter 3 reviews several of the prominent parallel simulation kernels that use the Time Warp synchronization protocol. The software architecture and target compute platforms for each is described.

Chapter 4 introduces the software architecture and modeling API for the WARPED2 simulation kernel.

Chapter 5 gives an overview of the studies carried out in the remainder of the text, motivations for the studies, and the hardware architectures and simulation models used in the studies.

Chapter 6 describes the pending event set data structures used within the WARPED2 kernel and provides some preliminary results in finding the best configurations for various models.

Chapter 7 talks about partitioning.

Chapter 8 descibes various GVT and termination detection algorithms that have been used explains the algorithms used in WARPED2. This chapter also provides some preliminary results in determining the best configurations for these algorithms.

Chapter 9 analyzes techniques for managing memory efficiently. This includes state saving techniques, fossil collection, and GVT period. Some preliminary results are also shown for various configurations.

Chapter 11 summarizes the preliminary results from preceding chapters by putting them all together.

Finally, Chapter 12 contains some concluding remarks and suggestions for future research.

Chapter 2

Background

This chapter describes some of the basics of Parallel Discrete Event Simulation (PDES) with a focus on the Time Warp mechanism. Then a brief overview of message passing and shared memory communication models and their strengths and weaknesses are compared. Lastly, the big.LITTLE platform is introduced and some different scheduling/switching mechanisms are described.

2.1 Discrete Event Simulation

Discrete Event Simulation (DES) is a method of modeling the execution of a physical system with a sequence of events that occur at discrete time intervals. A Discrete Event Simulation typically contains three main data structures

State variables: A set of variables that describe the current state of the system.

Simulation Clock: A clock to measure the progress of the simulation and determine the order of event processing.

Pending Event Set: A set of future events that are waiting to be processed.

A *Simulation Model* describes a physical system by a set of *Logical Processes* (LP's). Each LP corresponds to a physical process that is part of the physical system. The LP's interact with timestamped events that

dictate the simulation time that the event should be processed. With each event that occurs, and only when an event occurs, the state of the system is updated.

In a *Sequential* Discrete Event Simulation only one event is processed at a time. All pending events are kept in a single list which is sorted by timestamp. The next event to be processed is always the one with lowest timestamp. Each successive event updates the state of the system, advances the simulation clock, and possibly produces new future events. This is clearly not very efficient for large simulations. This method can be improved by realizing that events for different LP's are independant and will only affect the state for a single LP.

2.2 Parallel Discrete Event Simulation

Parallel Discrete Event Simulation (PDES) is a method running a discrete event simulation on a parallel computer which could be a shared-memory multiprocessor, a distributed memory system such as cluster or NUMA system, or a combination of both. In a parallel discrete event simulation the state of the system is usually split among the logical processes so that each one contains a portion of system's state without any sharing of state variables [3]. In addition to each logical process having it's own separate state, the logical processes also have seperate simulation clocks and pending event sets. Event's from different LP's can then be processed concurrently without the need to worry about sharing state variables and the model can be viewed as concurrent processes operating independantly which contribute to the overall progression of the simulation. This has the potential to increase performance significantly; However, it is possible that events at a receiving LP can be received and processed out of order, violating causality. These *causality errors* can occur because of the independant nature of the logical processes and because the LP's can be processing events at different rates. Causality errors can produce incorrect changes in state variables and incorrect events to be sent to other LP's. Parallel Discrete Event Simulation techniques can be categorized in terms of how causality errors are handled. *Conservative* approaches use methods to detect when possible causality errors might occur and prevent them from ever occurring. *Optimistic* approaches, on the other hand, allow causality errors to occur but use methods to detect and recover from the errors. Generally, the simulation models can be developed without the knowledge of the underlying simulation mechanism. The simulation mechanism is usually implemented in a self-contained module which provides an API for the models and is

commonly referred to as the *kernel* or *executive*. For the remainder of this text, only optimistic methods will be discussed, specifically the Time Warp mechanism which is the most widely used optimistic mechanism used in practice.

2.2.1 Time Warp

The Time Warp mechanism is an optimistic method of simulation which is based on the virtual time paradigm [4]. *Virtual Time* provides a method of ordering events in distributed systems which are not described by real time such as a simulation. When used for parallel discrete event simulation, Virtual Time is synonymous with simulation time. The current time of an LP's simulation clock in Time Warp is called the *Local Virtual Time* (LVT).

When an a causality error is detected at an LP (next event to be processed is less than the simulation time) the effects of the incorrectly processed event(s) must be undone. The process of undoing the effects is called a *rollback* and the event that triggers a rollback is called a *straggler event*. When a straggler event is detected at an LP, the first step taken during the rollback is to restore the LP's state back to a previous state before the incorrect event(s) were processed. Then the LP must "unsend" the events that were incorrectly sent by sending *negative events* or *anti-messages*. The negative event, when received by the receiving LP will stop the corresponding positive event from being processed or if the corresponding positive message has already been processed at the receiving LP then that LP must also rollback. This processes recursively occurs until all causality errors are corrected. The negative messages are never processed as normal events but serve only to annihilate an generated event produced by an incorrectly processed event (causality error).

Jefferson [4] describes how to support rollbacks with three main data structures:

1. Input Queue
2. Output Queue
3. State Queue

Every LP will have separate input queues, output queues, and a state queues. The input queue contains the unprocessed and processed events for the LP that it belongs to. The input queue must be sorted in timestamp order and the LP's must always process from the lowest unprocessed event. The LVT is always the largest

timestamped processed event and is used to detect a straggler event. The output queue contains the events that have been sent by the LP that it belongs to which will allow the LP to send anti-messages during a rollback. The state queue contains previous states of the LP and allows the proper states to be restored during a rollback.

The *Global Virtual Time* (GVT) of the simulation at a given point during the simulation is the minimum of all unprocessed events and the send times of all events that have been sent but not received [4]. There are numerous algorithms for determining the GVT which will be discussed further in chapter 8. LP's cannot send events that are less than their LVT value and so the GVT acts as a lower bound on how far a rollback can occur. Because no LP's will ever rollback past the GVT value, it is often used to free memory that is no longer needed for the events in the input and output queues and the states in the state queue that have timestamps less than the GVT as well as committing I/O operations that cannot be undone. This process of freeing memory and committing I/O operations is known as *fossil collection*. Fossil collection does not have to be based on the GVT and several other methods of fossil collection have been developed which will also be discussed more in chapter 9.

The need to save the state of the LP's is one of the fundamental overheads in the Time Warp mechanism in terms of both the amount of time it takes to copy the LP's states to save them and the amount of memory that must be used to store them. Because of this, a number of different approaches have been developed to reduce the overhead of state saving such as periodic state saving, incremental state saving, and reverse computation.

2.3 Parallel Systems Architectures

Systems that support parallel processing come in many forms. They can generally be characterized by how processors and memories are grouped together.

2.3.1 Shared Memory Multiprocessor Systems

A shared memory multiprocessor is a system where processors in the system have a common shared address space. The address space can be within a single memory or multiple memories depending on the system.

A **Symmetric Multiprocessor (SMP)** is a type of shared memory multiprocessor system where each processor has uniform access to a single shared memory through a common bus. SMP systems cannot scale very large due to increasing contention as the number of processors increasing and for this reason, they usually have 8 or fewer processors. To increase available bandwidth in the system, each processor usually has one or two levels of private caches as well as a shared cache which act as a way limit the number of memory accesses. Figure 2.1 illustrates what a typical SMP system looks like.

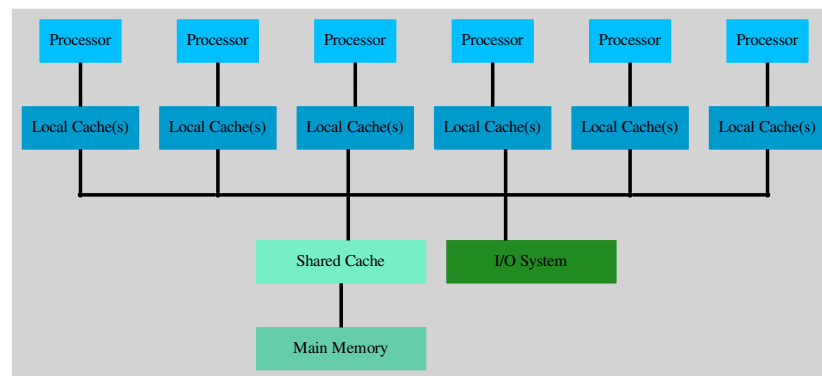


Figure 2.1: SMP System

A **Distributed Shared Memory** system, also known as a Non-Uniform Memory Access (NUMA) has multiple memories that are distributed. In these systems, the memories are still shared between processors, but access to different memories may take different amounts of time. An interconnection network connects processors and memories together with one or more processors per memory. Because memory access times can vary, software on NUMA systems usually try to keep memory accesses local to a processor. However, NUMA systems can scale much larger than SMP systems because contention to single memory does not necessarily increase with an increasing number of processors. Figure 2.2 illustrates what a typical NUMA system might look like.

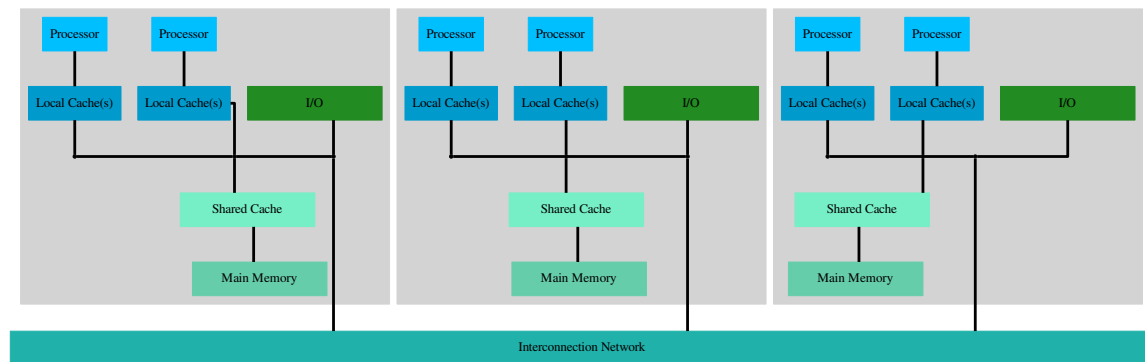


Figure 2.2: NUMA System

2.3.2 Clustered Systems

A **Beowulf Cluster** is a type of cluster which appears to the user as a single machine. A single program is executed by all machines in the cluster and typically use parallel communication software such as MPI or PVM.

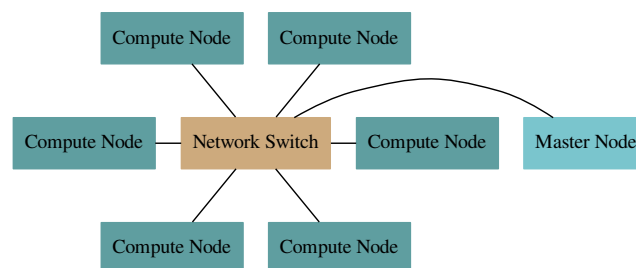


Figure 2.3: Beowulf Cluster

2.4 Parallel Systems Communication

Parallel applications are composed of multiple workers that operate independently in parallel and may have to exchange information. The workers in a parallel application can be a process, thread, or any other type of execution context. Workers can communicate by either sending explicit messages to each other by means

of well defined message formats or by using shared data structures that all workers can access. The former method is known as *message passing* and the latter method is known as *shared memory*. Both communication models are fundamentally different and both have strengths and weaknesses.

2.4.1 Message Passing

In a message passing system, workers are completely isolated in different address spaces and communicate only through serialized messages. The formats of the messages must be defined so that the message can be serialized and deserialized by the sender and the receiver, respectively. Message passing can either be synchronous or asynchronous. With synchronous message passing, the send/receive operations must be done in a specific order so that the sender/receiver workers operate together in a synchronized fashion. The send operation at the sender will block until the message is received at the receiver and the receive operation at the receiver will block until the message is fully received. That means the every worker must follow a predictable communication pattern. Workers cannot continue other operations during communication operations and may slow down the whole system. On the other hand, asynchronous communication allows workers to start send and receive operations and immediately continue without blocking. To allow this, intermediate queues must be used to hold pending operations. The workers do not have to follow a predictable communication pattern in this case because the messages will be queued and can be processed at any time and in any order. The main advantage of message passing in general is that the number of workers can be scaled very efficiently as long as the work is partitioned in the right way. The workers can execute in address spaces on different machines and communicate over a local network. The biggest disadvantage, however, is the high communication latency compared to computation speed. Since workers run in different address spaces the messages must be copied or if the address spaces exist on different machines, they must be propagated through the network. This makes message passing especially hard for fine-grained parallel applications. An illustration of simple message passing is shown in figure 2.4.

Message Passing Interface (MPI)

MPI [5] is an extensive message passing API specification for parallel applications and supports both synchronous and asynchronous forms of communication. MPI is just a standard specification for developers and

MPI users and many current implementations exist. The most widely used implementations used in practice include MPICH and OpenMPI.

2.4.2 Shared Memory

The workers in a parallel application can also share a single address space and communicate through shared data structures. The producer worker will insert data directly into the data structure and the consumer worker will remove the data and use it. This takes much less time to send data than message passing. However, access to the shared data structures must be protected so that multiple workers do not simultaneously access the same data which could cause unpredictable results. Access to the data is enforced using lock synchronization mechanisms such as mutexes or semaphores. Shared memory data structures may suffer from performance if lots of workers contend for the lock at the same time. For this reason, it is very hard to scale systems that use only shared memory as a means of communication. An illustration of a simple shared memory system is show in figure 2.4.

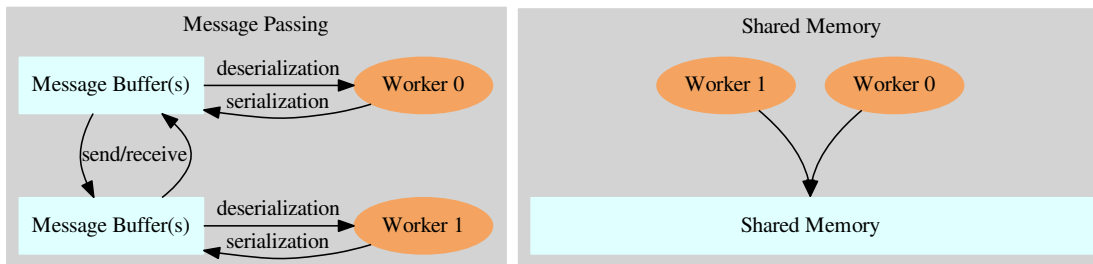


Figure 2.4: Message Passing and Shared Memory Communication

2.5 ARM big.LITTLE

ARM big.LITTLE is a computer architecture design which uses a combination of powerful processor cores that use a lot of power (big) with slower, more power-efficient processor cores (LITTLE). The purpose of this design is to allow good performance when the system load is heavy by running tasks on the big cores while also allowing power savings when the system load is low by running tasks on the LITTLE cores. The

operating system CPU scheduler can make use of the big.LITTLE architecture in multiple ways by using different task allocation and switching policies. The three main methods that are currently being used in practice are cluster switching, CPU migration, and heterogeneous multi-processing. The remainder of this section describes the three methods in more detail.

2.5.1 Cluster Switching

With cluster switching, the LITTLE cores and big cores are grouped into *clusters* with the big cores in one cluster and the LITTLE cores in another cluster. At any point in time, the OS scheduler will only schedule tasks to cores within a single cluster. When the system gains enough load so that a big core is needed, then the OS scheduler must switch to the big cluster and only use the big cores. This is the simplest method but can still waste a lot of power by unnecessarily switching to the big cluster. Furthermore, only half of the cores are available at any time which prohibits the use of full computational capacity. A diagram that illustrates cluster migration is shown in figure 2.5.

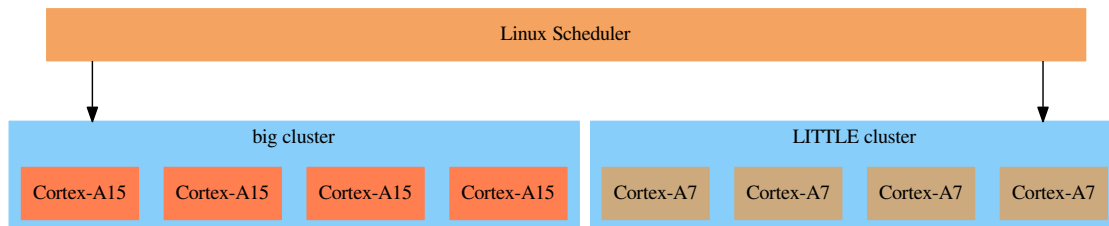


Figure 2.5: Cluster Switching

2.5.2 CPU Migration

CPU migration is the next step up from cluster switching. With CPU migration, each big core is paired with a LITTLE core and the OS treats them as a single virtual core. At any point in time, the OS scheduler will only schedule tasks to only one of the physical cores within each virtual core. The advantage of this approach over cluster switching is that if the load on the system is only large enough so that a single big core is needed then power isn't wasted because only a single big core will be switched on. Like cluster

switching though, only half the of CPU cores are available at a time which still prohibits full computational capacity of the system. A diagram that illustrates cpu migration is shown in figure 2.6.

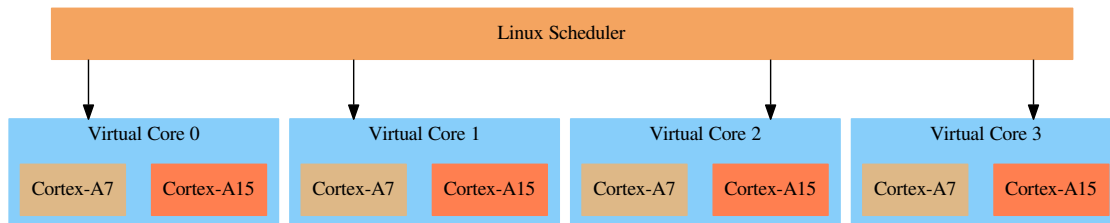


Figure 2.6: CPU Migration

2.5.3 Heterogeneous Multi-Processing (HMP)

Heterogeneous Multi-Processing or Global Task Scheduling (GTS) allows simultaneously scheduling to all CPU cores at the same time. The tasks that have a higher priority or require more processing power will be scheduled to the big cores whereas the tasks with low priority that don't require much processing power, such as background tasks can be scheduled to the LITTLE cores. This is the most complex approach and is hard to implement because the OS scheduler must not treat all cores the same. Policies to allocate tasks must be implemented in the proper manner as well as policies for migration of task to and from the big cores and LITTLE cores. Much research is still in progress to determine the right policies. A diagram that illustrates HMP is shown in figure 2.7.

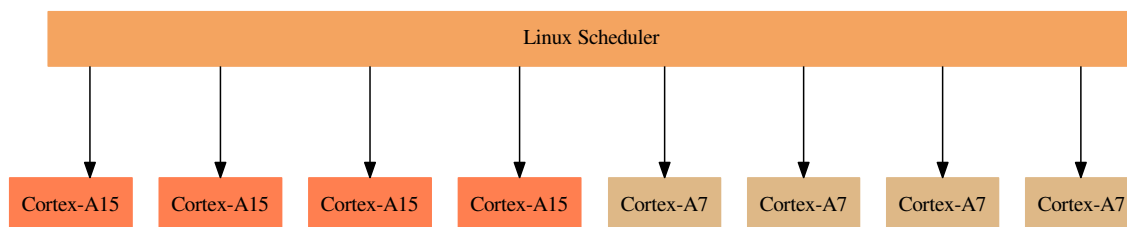


Figure 2.7: Heterogeneous Multi-Processing

Chapter 3

Related Work

This chapter give an overview of some of the most popular Time Warp systems. For each system, the design will be described at a high level. The the data structures and algorithms used will be described further as well as the strengths and weaknesses.

3.1 Georgia Tech Time Warp (GTW)

Georgia Tech Time Warp is a general purpose Time Warp Simulator designed specifically for shared memory multiprocessors. Although GTW is not used any more, it's design has influenced the design of other simulators that are used widely in practice. GTW simulation models run in a single processes, multi-threaded environment and uses only shared memory to communicate between threads that are bound to single processor. The LP's for all models are statically allocated to a single thread so that events for the LP's are processed only on a single processor.

The pending event set is distributed among threads with each having its own data structures. Since the threads can only run on a single processor, the data structures are owned by that processor. The pending event set for each processor consists of three main data structures listed below [1]:

1. The *Message Queue* is a linked list that contains positive messages that are destined for the LP's mapped to the owning processor. Access to the message queue must be synchronized because it can be accessed by tasks running on any processor.

2. The *Cancel Queue* is a linked list that serves exactly the same purpose as the message queue except that it contains only negative messages(anti-messages). Access to this queue must also be synchronized.
3. The *Event Queue* is used to hold unprocessed and processed events and is directly used to schedule events to be processed. The event queue is actually made up of different data structures, one for processed events and one for unprocessed events. The processed events are contained within a doubly linked list and the unprocessed events are contained within a priority queue which can be configured to be either a calendar queue or a skew heap depending on a user configuration.

When messages are sent between LP's, they are inserted directly in the message queue or the cancel queue depending on whether they are positive or negative. Each thread first moves messages from the message queue to the event queue and processes any rollbacks. Then, the messages from the cancel queue are removed and cancellations and any more rollbacks are processed. The smallest event from the event queue is then processed and added to the processed event list. This procedure is repeated over and over again by all processors. Psuedocode for the main event processing loop in GTW is show in figure 1.

Algorithm 1: GTW Main Event Processing Loop [1] [2]

```

while eventQ is not empty do
    move messages from MsgQ to EvQ and process any rollbacks
    remove anti-messages from CanQ, process annihilations and rollbacks
    remove smallest timestamped event E from EvQ
    processe event E

```

To avoid accessing the message queues and cancel queues too often, which is a contention point, GTW also supports batch processing. With batch processing, multiple events will be processed at a time without processing any rollbacks or cancellations.

The partitioning of the LP's among processors must be done in the simulation model during initialization. That means that the model developer must understand some the features of the underlying architecture such as the number of processors, to effectively partition the LP's. Furthermore, the initial partitioning of the LP's is hard to change during the course of the simulation because there are no separte input queues but rather a single message queue to hold all unprocessed events for each processor.

3.2 Clustered Time Warp (CTW)

Clustered Time Warp [6] (CTW) uses a hybrid approach by processing events within a *cluster* of LP's sequentially and using the Time Warp mechanism between the clusters. This design was chosen because it works well for digital logic simulation which tend to have localized computation within a group of LP's. Furthermore, digital logic simulation tends to have low computational granularity and lot's of LP's which can lead to a lot of rollbacks and a large memory footprint in a traditional Time Warp simulator. CTW is implemented for shared memory multiprocessors but only uses shared memory for use with a message passing system. No other shared memory algorithms are used.

Each cluster has a timezone table, an output queue, and a set of LP's which each have an input queue and a state queue. The timezones in the timezone table are divided by timestamps of the events received from LP's on different clusters. Whenever an event is received from a remote cluster, a new timezone is added. Only a single output queue is needed per cluster because anti-messages can only be sent between clusters and not between LP's on the same cluster.

When a straggler event arrives at a cluster, all of the LP's that have processed events that are greater than the timestamp of the straggler will be rolled back. This rollback scheme is called *clustered rollback*. The alternative to clustered rollback is *local rollback*. In a local rollback scheme the straggler event would be inserted into the receiver LP's input queue and the LP will roll back when it is detected. Although clustered rollbacks may cause some LP's to be rolled back unnecessarily leading to slower computation, the approach was chosen for CTW because processed events will not have to be saved which requires less memory.

CTW uses a form of infrequent state savings with the timezone table used to determine the frequency. When an event is about to be processed for an LP, the timezone of the last processed event is looked up and if event that is about to be processed is in a different timezone then the state is saved. This approach in which all LP's save their state every time an event is processed in a new timezone regardless of whether it receives an event from a remote cluster is called *local checkpointing*. This method reduces the state saving frequency more than a *clustered checkpointing* approach in which only the LP that receives an event from a remote cluster saves its state. The local checkpointing approach was chosen for CTW because a larger state saving frequency can increase rollback computation and it can even lead to more memory consumption because more events must be saved for coast forwarding during state restoration.

3.3 Rensselaer's Optimistic Simulation System (ROSS)

ROSS [7] is a general purpose simulator that is capable of running both conservatively and optimistically synchronized parallel simulations as well as sequential simulations. It is most often used for optimistic parallel simulations which is achieved with the time warp mechanism. ROSS started as a reimplementaion of GTW and is still modeled after it but has some enhancements. The same basic event scheduling mechanism is used but ROSS supports different priority queue implementations and different algorithms are used for fossil collection, state saving, and gvt calculation. In addition, ROSS uses processes instead of threads and uses message passing with MPI instead of shared memory for communication among the processes.

Just as in GTW, ROSS maps every LP to a process and each process contains its own pending event set structures. No locks are needed explicitly within each process because there are no shared data structures among processes. The data structures are very similar to those used in GTW but have a different naming convention. The main data structures in ROSS are:

1. The *Event Queue* is analogous to the message queue in GTW. It contains the positive events for all LP's in the corresponding process. In addition, an event queue is used to hold all remote events regardless of whether it is positive or negative. The event queue is implemented as a linked list.
2. The *Cancel Queue* is a linked list which is used to hold negative events for all LP's for the corresponding process. The cancel queue is used in the exact same way as GTW except that no locks are necessary.
3. The *Priority Queue* is analogous to the event queue in GTW and contains events in timestamp order. ROSS also allows the priority queue to be implemented as a calendar queue, heap, splay tree, or avl tree depending on user configuration.

3.4 WARPED

WARPED is the predecessor of WARPED2. The complexity of WARPED became unmanageable over the years which eventually led to its demise and rewrite. WARPED, from its beginnings, has always followed a modular design to allow maximum flexibility for new optimization.

The famous computer scientist David Wheeler used to say "All problems in computer science can be solved by another level of indirection."

Kevlin Hennley's corollary to goes "...except for the problem of too many layers of indirection."

The original WARPED was written for

3.5 Others

3.5.1 The ROME Optimistic Simulator (ROOT-Sim)

ROOT-Sim is another general purpose Time Warp Simulator that uses message passing via MPI [8]. Like WARPED, ROOT-Sim is a more classic Time Warp implementation with each LP having their own input queues, and output queues. What sets ROOT-Sim apart from other time warp simulators is the internal instrumentation tool, Dynamic Memory Logger and Restorer (DyMeLoR) that can optimize memory usage. DyMeLoR can determine whether the simulation models are better fit for copy-state saving or incremental state saving and transparently switch between them during runtime. Another service that ROOT-Sim offers is the Committed and Consistent Global Snapshot (CCGS). After each GVT calculation, ROOT-Sim transparently rebuilds a global snapshot of all LP states. Each LP can access its portion of the global snapshot on every GVT calculation. With this service, a simulation model can implement any custom global snapshot algorithm.

3.5.2 ROSS-MT

ROSS-MT [9] is a multi-threaded version of ROSS which is optimized to use shared memory to communicate among threads. The use of message passing with MPI was completely removed and all events are sent by direct insertion into the event queues. To reduce the added contention on the event queues, they are further divided by possible senders. ROSS-MT also optimizes the free memory lists so that they are more NUMA aware. Instead of allocating memory from the receiver processors free list, it is allocated from the senders free list. Furthermore, a LIFO approach is taken to improve cache reuse.

Chapter 4

The WARPED2 Simulation Kernel

This chapter describes the software architecture of the WARPED2 simulation kernel. The main components are described. The modeling API is also described and an example model is shown to illustrate the API.

4.1 The Software Architecture of WARPED2

The WARPED2 simulation kernel uses a modular design to make it configurable, extendable, and maintainable.

4.1.1 Event Dispatcher

The event dispatcher is at the center of everything and determines how the simulation will be progressed. Warped2 currently supports the event dispatcher to be configured for either sequential simulation or time warp simulation. The sequential event dispatcher just contains a single list of all events because only a single event is processed at a time. The time warp event dispatcher has more complex data structures and multiple components. In either case, the event dispatcher calls methods that are defined by the LP. Since a sequential simulation doesn't really have any real complexity only the time warp event dispatcher will be discussed any further. The time warp components are illustrated in figure 4.1.

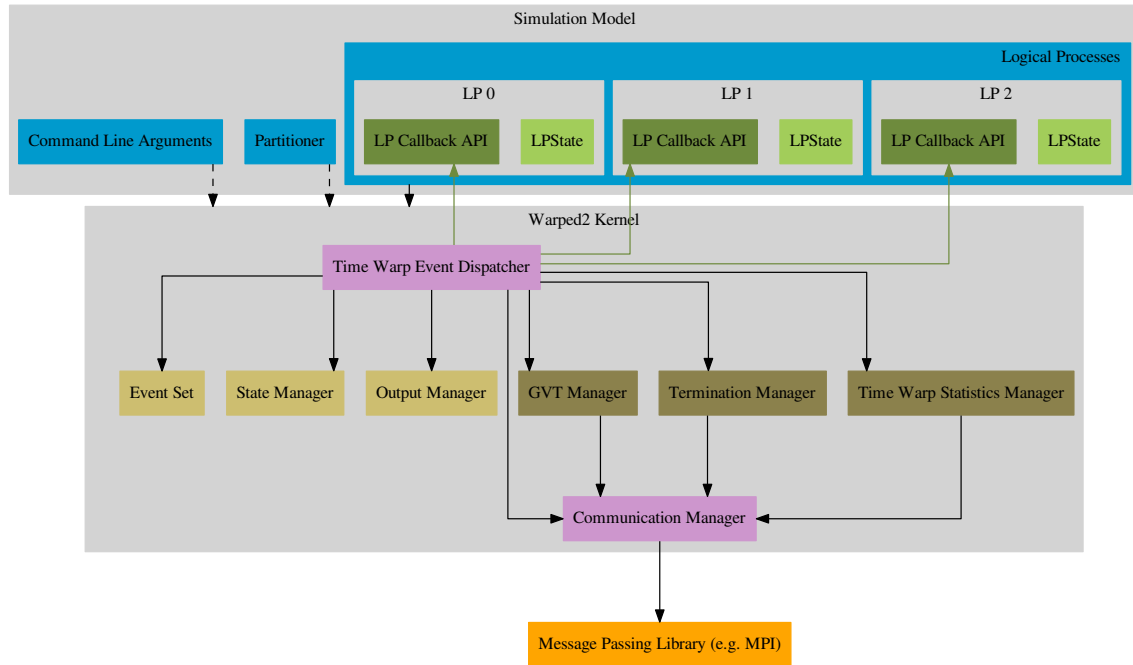


Figure 4.1: Time Warp Components in WARPED2

Each process has its own time warp components that exist in only their own address space. The time warp components can be categorized as either a local time warp component or a global time warp component. The local time warp components are concerned only with the local control mechanism of the individual LP's such as rollbacks and fossil collection whereas the global time warp components are concerned with the global control mechanisms such as GVT, termination detection and statistics counting.

4.1.2 Local Time Warp Components

The Event Set contains the data structures for all of the unprocessed and processed events for the LPs that are local to the process. This is where the events are scheduled for processing. It provides methods for getting the next event, rolling back an LPs input queue, and fossil collecting the processed events for an LP.

The Output Manager contains all of the output queues and implements a cancellation technique. It provides methods for adding an event to an LPs output queue, rollback back an LPs output queue, and fossil

collecting old output events. Currently, WARPED2 only supports aggressive cancellation.

The State Manager contains all of the state queues and implements a technique for saving and restoring states for the LPs. It provides methods for saving the state of an LP, restoring the state of an LP, and fossil collecting old states. Currently, WARPED2 only supports periodic state saving.

4.1.3 Global Time Warp Components

The GVT Manager implements an algorithm for determining the Global Virtual Time of the simulation. A more detailed description of the GVT algorithm used in WARPED2 is given in chapter 8.

The Termination Manager implements an algorithm for determining when all processes become inactive and initiates termination when that occurs. A more detailed description of the termination algorithm used in WARPED2 is given in chapter 8.

The Time Warp Statistics Manager keeps track of all local statistics counts and provides methods to do global reductions on the statistics.

4.1.4 Communication Manager

The communication manager provides an interface between the underlying message passing library and the WARPED2 simulation kernel. Any interprocess communication must go through the communication manager whether the communication processes are on the same machine or different machines.

4.2 The Modeling API of WARPED2

The modeling interface of warped2 is a set of abstract base classes that contain methods that must be implemented in a derived class. The base classes may also contain methods and data members that are available to use by the derived classes. The three main base class types that must be implemented are LogicalProcess, LPState, and Event. Optionally, the user may create a custom partitioner from the Partitioner base class. In the remainder of this section, each class is described in more detail and sample implementations are shown for each.

```
WARPED_DEFINE_LP_STATE_STRUCT(ExampleState) {  
    unsigned int messages_received;  
    ...  
};
```

Listing 4.1: Example WARPED2 State Definition

4.2.1 The LPState Structure

The state of the LP's must be define with the `WARPED_DEFINE_LP_STATE_STRUCT` macro. This is used to ensure that the warped2 kernel can save a copy of the state and restore the state from a pointer to the `LogicalProcess` base class. An intermediate template class is defined which defines the necessary methods to make a copy of the state and to restore the state so that the user does need to explicitly define them. However, if the state contains complex data structures that contains pointers then the default copy constructor and default copy assignment operator will only perform shallow copies. In this case the user must implement a custom copy constructor or a custom copy assignment operator or both. The copy constructor will define the behavior for saving the state whereas the copy assignment operator will define the behavior for restoring the state. Note that the copy assignment operator will most likely not be needed since a shallow copy will usually suffice. A simple example of a LP state that contains just message counts is shown below in listing 4.1.

4.2.2 The Event Class

The event base class is used as the basis for creating model specific events. The user must implement at least two function: `receiverName()` and `timestamp()` so that the name of the receiver and receive time, respectively, can be obtained for each instance of an event. The user must also register all member variables with the serialization API so that a storage order can be defined for events that are sent and received over a network. To do this, the `WARPED_REGISTER_SERIALIZABLE_MEMBERS` macro is provided. All member variable must be passed to this macro as well as `cereal::base_class<warped::Event>(this)` to ensure that all members that are inherited are also serialized. The order that the members are listed is completely arbitrary and does not matter. In addition, the derived event type must be registered using the `WARPED_REGISTER_POLYMORPHIC_SERIALIZABLE_CLASS` macro. A basic example of

```
class ExampleEvent : public warped::Event {
public:

    ...

    const std::string& receiverName() const { return receiver_name_; }
    unsigned int timestamp() const { return time_stamp_; }

    ...

    std::string receiver_name_;
    unsigned int timestamp_;

    ...

    WARPED_REGISTER_SERIALIZABLE_MEMBERS(cereal::base_class<warped::Event>(this
        ),
                                     receiver_name_, timestamp_, ...)
};
WARPED_REGISTER_POLYMORPHIC_SERIALIZABLE_CLASS(ExampleEvent)
```

Listing 4.2: Sample WARPED2 Event Definition

an event implementation is shown below in listing 4.2.

4.2.3 The LogicalProcess class

The most important class definition in the simulation model is the LogicalProcess class. The implementation of the LogicalProcess class defines the callback functions that the warped2 kernel calls and thus defines the behavior of the simulation. The user must include a single LPState implementation as well three method implementations:

1. The `initializeLP` method is called to perform any initializations that must be done prior to the start of the simulation and must return a set of initial events.
2. The `receiveEvent` method is called to perform some computation based on the event that is passed. The implementation of this method interprets the event, updates the state of the LP and returns a set of new events with future timestamps.
3. The `getState` method provides a way for the warped2 kernel to get the current state of the LP.

```
class ExampleLP : public warped::LogicalProcess {
public:

    ...

    warped::LPState& getState() { return this->state_; }

    std::vector<std::shared_ptr<warped::Event> > initializeLP() override {
        this->registerRNG(this->rng_);
        std::vector<std::shared_ptr<warped::Event> > events;
        ...
        return events;
    }

    std::vector<std::shared_ptr<warped::Event>> receiveEvent(const warped::
        Event& event) {
        ++this->state_.messages_received_;
        std::vector<std::shared_ptr<warped::Event> > response_events;
        ...
        return response_events;
    }

    ExampleState state_;
};
```

Listing 4.3: Example WARPED2 LogicalProcess Definition

It is necessary that at least one LP has an initial event that is returned by `initializeLP`, otherwise no events can be received and simulation will terminate immediately. Also note that the it will be called once for *every* LP instance so it is possible that initial events are returned only in some cases. An example of a `LogicalProcess` implementation is shown below in listing 4.3.

4.2.4 The Partitioner class

The `warped2` kernel already provides a round-robin partitioner and a profile-guided partitioner but the user can define their own partitioner that is customized for a specific model. The user must derive from the `Partitioner` base class and implement just a single method which takes a vector of all LP'ss and the number of partitions desired and returns a vector of vectors of LP's. In general, the partitioner should work for any number of partitioners and not impose any constraints because the partition method is called back from the kernel. A simplified version of the kernel's round-robin partitioner is shown in listing 4.4. Note that a model would never have to implement such a general partitioner but is showed just as a simple example.

```
class ExamplePartitioner : public Partitioner {
    std::vector<std::vector<LogicalProcess*>>
    partition(const std::vector<LogicalProcess*>& lps, const unsigned int
        num_partitions) {
        std::vector<std::vector<LogicalProcess*>> parts;
        ...
        return parts;
    }
};
```

Listing 4.4: Example WARPED2 Partitioner Definition

4.2.5 Random Number Generation

If the simulation model uses random number generators, they must all be registered with the warped2 kernel. This is necessary so that the state of the random number generator can be saved and restored in case of rollbacks. The random number generators can be any type as long as they implement the `<<` operator and `>>` operator to allow the kernel to save and restore the internal state of the random number generator. To register the random number generator, the `registerRNG` template function must be used which is a member of the `LogicalProcess` class. All LP's must have separate random number generators and must be registered in the `initializeLP` callback function as shown in listing 4.3.

4.2.6 Command Line Arguments and the Kernel Entry Point

Once all the necessary structures and classes have been defined, the model's main function must be implemented which is where all calls into the kernel are made. First, the model specific command line arguments must be registered with the kernel. This must be done first so that it can be passed to the constructor of a `Simulation` instance. Then all of the LP's and optionally a partitioner must be instantiated and passed to the kernel through the `simulate` method of `Simulation` object. Two versions of the `simulate` methods are available, one for a model with a custom partitioner and one without as listed below:

1. `void simulate(const std::vector<LogicalProcess*>& lps);`
2. `void simulate(const std::vector<LogicalProcess*>& lps,`
`std::unique_ptr<Partitioner> partitioner);`

A sample implementation of a models main function is shown in listing 4.5.

```
int main(int argc, const char **argv) {
    unsigned int num_lps = 10000;

    TCLAP::ValueArg<unsigned int> num_lps_arg("o", "lp-count", "Number_of_lp's"
        , false,
                                     num_lps, "unsigned_int");
    std::vector<TCLAP::Arg*> cmd_line_args = { &num_lps_arg };
    warped::Simulation simulation {"Sample_Simulation", argc, argv,
        cmd_line_args};

    num_lps = num_lps_arg.getValue();
    std::vector<SampleLP> lps;
    for (unsigned int i = 0; i < num_lps; i++) {
        std::string name = std::string("LP_") + std::to_string(i);
        lps.emplace_back(name, 1, i);
    }

    std::vector<warped::LogicalProcess*> lp_pointers;
    for (auto& lp : lps) {
        lp_pointers.push_back(&lp);
    }
    simulation.simulate(lp_pointers);

    return 0;
}
```

Listing 4.5: Sample WARPED2 Main Definition

Chapter 5

Plans of Study

5.1 Implementation Components of WARPED2

5.1.1 Pending Event Set

5.1.2 Partitioning

Partitioning the work between parallel workers is commonly done in distributed systems to increase efficiency and minimize communication. In a parallel discrete event simulation the work can easily be partitioned by partitioning logical process.

Profile-Guided partitioning is a method of partitioning based on profile data collected from a sequential simulation. The profile data forms a weighted graph with vertices representing LPs and edges representing communication channels. The weights of the edges are based on the frequency of communication on the channels. The profile-guided partitioner uses this data and a graph partitioning tool to build partitions that minimize interpartition communication.

5.1.3 GVT and Termination

Another important aspect of a time warp system is GVT and termination detection algorithms. These algorithms are particularly hard to implement in distributed systems efficiently. Most of the common GVT and termination detection algorithms are well suited for either shared memory or message passing but not both. In chapter 8, some popular GVT and termination detection algorithms will be discussed as well as the

algorithms used in WARPED2.

5.1.4 State Saving and Fossil Collection

The state saving and fossil collection techniques in a time warp system can significantly impact the memory requirements of the system and thus are very important and need to be considered. Furthermore, saving the state of and fossil collecting the LPs takes a nonnegligible amount of time. There have been many state saving techniques that have been developed to minimize space and time overheads such as periodic state saving,

These techniques will be discussed in chapter 9.

WARPED2 implements a periodic state saving technique where the state for every LP is saved only every N events.

In chapter 9, the effects of different state saving periods and fossil collection techniques are analyzed to determine the optimal memory/time tradeoff.

5.1.5 Multi-Threading Optimizations

Spinlocks and Atomic Instructions

Most multi-threaded applications use mutexes to protect shared data structures by only allowing a single thread to access the critical section. These mutexes are usually implemented so that if a thread tries to acquire the lock but the lock has already been acquired by another thread, the thread will be put to sleep and try again in the future. If the lock is only held by any thread for a short period of time then the amount of time it takes to put the thread to sleep and wake it back up is usually not necessary.

Instead of using this type of mutex, a spinning mutex or just spinlock can be used. In the case of a spinlock, when the lock is contended, the thread that is trying to acquire the lock will continuously keep trying to acquire it over and over. This works well for small critical sections that are executed quickly as in the case of warped2.

Furthermore, if the critical section only contains a few variables that do not depend on each other in any way, then atomic instructions can be used instead of locks. Atomic instruction can also be used as a basis for lock free data structures.

Thread Caching Malloc (TCMalloc)

TCMalloc is a memory allocator that is optimized for multithreaded applications. The main feature that sets it apart is the use of per-thread set of "free-lists" which are called *thread caches*. The thread caches do not have to be protected by locks since they belong to only a single thread and only the owner thread can access its thread cache.

The central cache is also protected by spinlocks.

5.2 Platforms for Assessment

5.2.1 x86 SMP Nodes and Clusters

5.2.2 ARM big.LITTLE Nodes and Clusters

5.3 Simulation Models used for Assessment

5.3.1 PCS

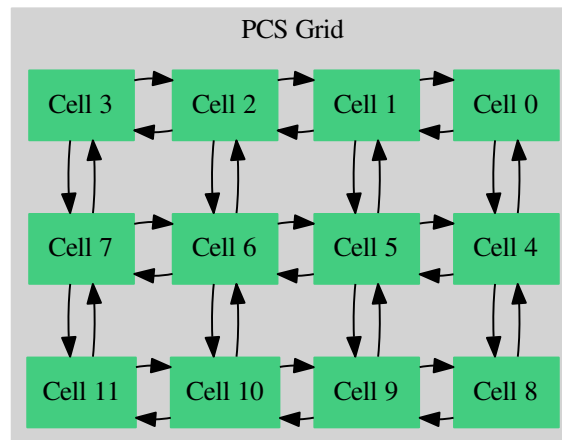


Figure 5.1: PCS Model Logical Processes

State Variables:

- Number of idle channels
- Number of call attempts
- Number of channel blocks
- Number of handoff blocks

5.3.2 Traffic

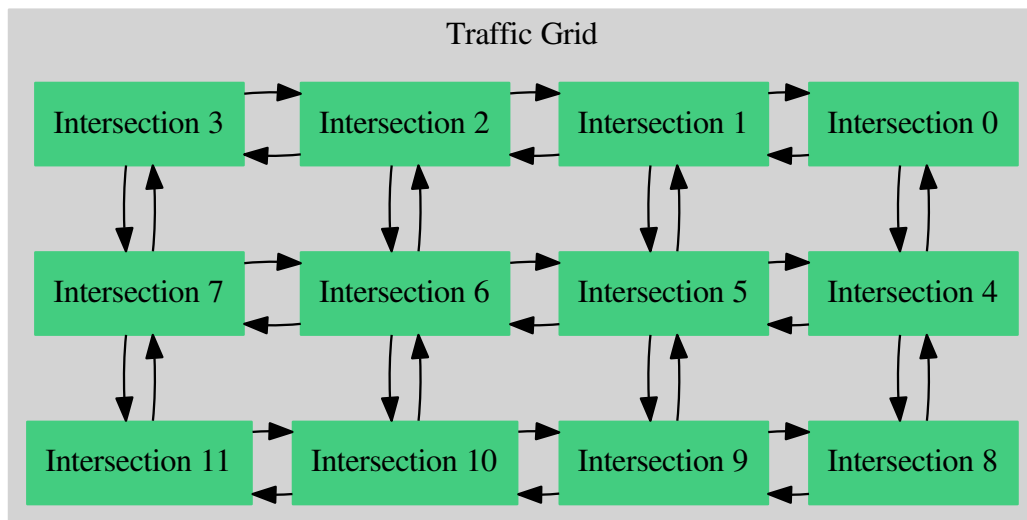


Figure 5.2: Traffic Model Logical Processes

5.3.3 Epidemic

5.3.4 Airport

Chapter 6

WARPED2 Data Structures and Their Organization

6.1 Pending Event Set Data Structures

The pending event set is the set of all unprocessed events. Every process contains a logically separate pending event set for a dedicated set of LPs. Exchanging of events between LPs between processes is funneled through the manager thread of the processes.

Each LP has an unprocessed queue which contains both positive events and anti-messages and remains sorted at all times. The anti-messages are given priority over their positive counterparts to prevent any unnecessary rollbacks and prevent cascading of rollbacks that can cause instability [10]. To avoid any copying, the unprocessed queue only contains pointers to the unprocessed events which are allocated by the simulation model. The worker threads or manager thread send events to LPs by simply inserting the pointers into their unprocessed queue.

A second type of data structure, an *LTSF (Lowest TimeStamp First) Queue*, provides order among events from multiple LPs. At most, a single event from each LP is *scheduled* into a single LTSF queue. Scheduling an event to an LTSF queue means only inserting a pointer into the LTSF data structure with no removal from the unprocessed queue. The pending event set contains one or more LTSF Queue to process events from.

A third type of data structure is also used to keep track of the events that have been scheduled or are

currently being processed and is organized by receiving LP. It is used for two main reasons. First, it provides a way to determine if a smaller event is scheduled for an LP upon the arrival of another event into its unprocessed queue. The new event can be scheduled in place of the already scheduled event if that occurs. Second, it serves to prevent multiple worker threads from processing events from the same LP which could cause out of order committing of events violating the local causality constraint [3].

Figure 6.1 illustrates the pending event set data structures in WARPED2.

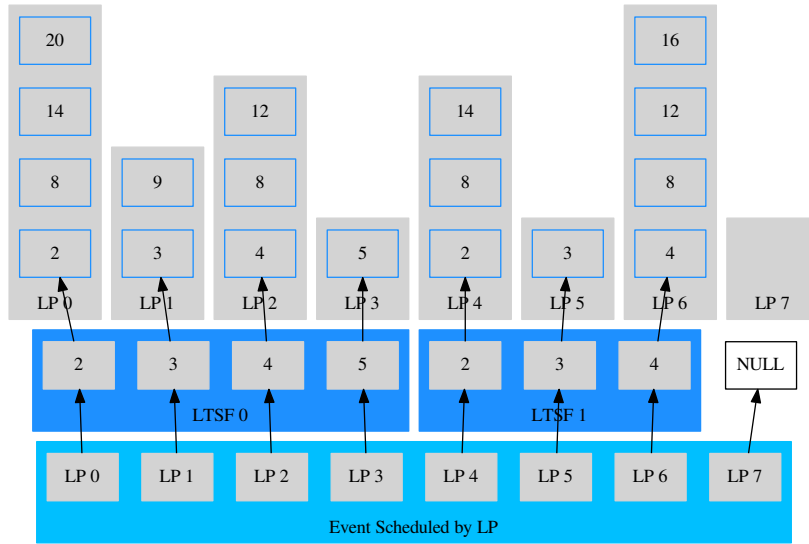


Figure 6.1: WARPED2 Pending Event Set Date Structures

6.2 Processing Events

One or more of the worker threads are assigned to each LTSF Queue to process events from and they all follow the exact same procedure. First, an event is removed from an LTSF queue to be processed but remains in the unprocessed queue until it is processed. The event is then checked to see if it is a straggler, and rolled back if so. An anti-message is also considered a straggler if its positive counterpart was the last processed event since WARPED2 makes the assumption that events cannot be sent out of order. If the event is an anti-message, the positive counterpart is assumed to be in the LPs unprocessed queue after rolling back and is

cancelled out and a new event is scheduled. If the event is positive it is processed normally, the state of the LP is saved, and new events are sent to other LPs. The event is then inserted into the processed queue of the LP and a new event is scheduled if one exists for the LP. Lastly, the data structure that keeps track of scheduled events by LP is updated. To summarize the worker thread processing loop is shown in pseudocode in algorithm 2.

Algorithm 2: WARPED2 Main Event Processing Loop

```

while termination not detected do
SQCRTIT   $e \leftarrow \text{getNextEvent}()$ 
           $lp \leftarrow \text{receiver of } e$ 

          if  $e < \text{last processed event for } lp$  then
            |  $\text{rollback } lp$ 

          if  $e$  is an anti-message then
SQCRTIT  |  $\text{cancel event with } e$ 
          |  $\text{schedule new event for } lp$ 
          | continue

          process event  $e$ 
          save state of  $lp$ 
SQCRTIT  send new events
SQCRTIT  |  $\text{replace scheduled event for } lp$ 

```

When events are sent to an LP that is local to the process, they are directly inserted into the unprocessed queue and checked against the currently scheduled event. If the new event is less than the scheduled event, the scheduled event is replaced. When events are sent to an LP that is not local to the process, they are inserted into a shared data structure called the *remote event queue*. The manager thread removes the events from the remotod event queue, serializes them into messages and sends them to remote processes through the communication manager.

6.2.1 Total Ordering of Events

The time warp system assumes that every event is labeled with a totally ordered clock value based on virtual time [4]. This is important so that causal dependencies are preserved and so that simulation results are deterministic [11]. WARPED2 uses a four tuple scheme which provide a total ordering of events:

1. Receive Time
2. Send Time
3. Sender LP Name
4. Generation

The last three serve as a tie breaker for simultaneous receive times. The send time is necessary to ensure correct causal dependencies. It is analogous to a Lamport logical clock [12] in real time distributed systems but for virtual time systems. The send time works for this as long as LPs only send a single event with the same send time to any individual LP. The sender LP name is necessary to ensure that order is determined between events received with the same receive time and send time from different senders. Without it, it is possible that different results could occur on different runs of the simulation [11]. The generation is necessary for distributed systems to differentiate between the same events which could be resent after rolling back [11]. In WARPED2 it is implemented as a single counter per LP and keeps track of the number of events that have been sent from the LP.

6.2.2 Performance Analysis

6.3 Data Structures to Support Rollback and Cancellation

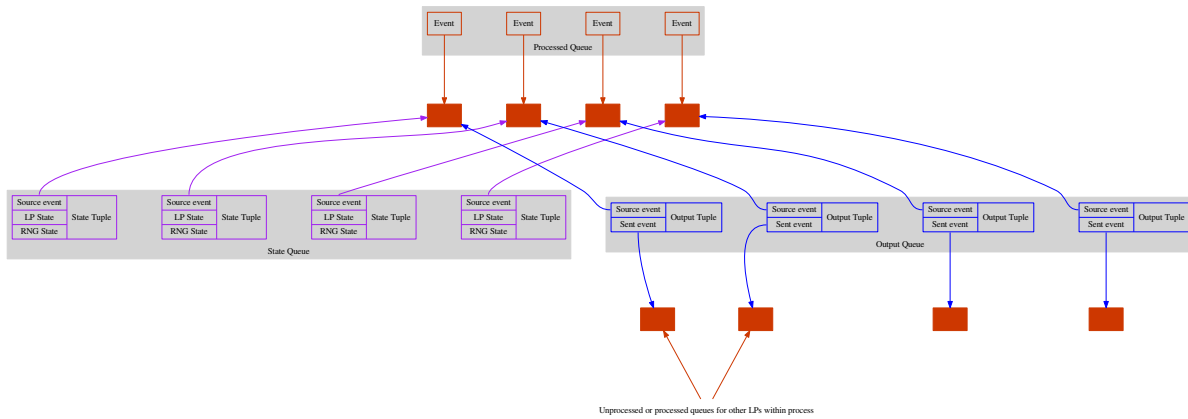


Figure 6.2: Rollback and Cancellation Data Structures in WARPED2

6.4 Protecting Access to Shared Data Structures

6.4.1 Performance Analysis

Chapter 7

Partitioning

7.1 Overview

Partitioning the work in a distributed system is always important to minimize interprocess communication. In parallel discrete event simulation, the work is usually partitioned by the LPs. Each process in the system can then process events from a dedicated subset of LPs.

In a message based system, communication latency is much larger than the frequency of computation. The disparity of communication time and compute time greatly increases the chances of rollbacks occurring in a time warp system. Partitioning can greatly reduce communication between processes, effectively pushing each process closer to a sequential simulation.

In a shared memory system, partitioning can aid reducing the number of simultaneous accesses to shared data structures (e.g. unprocessed queues). Although it may not reduce the total number of accesses to a data structure, it can force worker threads to access the same subset of data structures reducing contention. This can also enhance the number of cache hits by increasing locality.

7.2 Partitioning in WARPED2

Since WARPED2 uses multiple worker threads within multiple processes, two levels of partitioning is done. The first level of partitioning is for allocating LPs to processes and the second level is for allocating LPs to an LTSF queue.

7.2.1 Process Partitioning

7.2.2 LTSF Queue Partitioning

Each process further partitions the LPs by the LTSF Queue that the LPs schedule their events to. It is effectively partitioning among worker threads if each worker thread has its own LTSF Queue and has no effect if a single LTSF is shared among worker threads.

Chapter 8

GVT and Termination Detection

Algorithms that compute the Global Virtual Time (GVT) and detect termination conditions are both examples of algorithms that can be solved by determining the global state of a distributed system. The global state of a system is defined as the combination of all the local states of the processes in the system and all messages in transit. Global state determination algorithms are also commonly used for deadlock detection, garbage collection, debugging, and checkpointing for failure recovery in distributed systems.

8.1 Global Snapshots

Chandy and Lamport [13] described a basic global state algorithm by using *global snapshots* for distributed systems that use only FIFO channels for communication. To start the algorithm, an initiator process records its state and sends a control token out of all outgoing channels. When a process receives a control token, and it hasn't yet recorded its state, the process records its state and sends more control tokens out of all its outgoing channels. The algorithm terminates at each process when it has received a token through all of its incoming channels.

Lai and Yang [14] describe an algorithm for non-FIFO systems which computes a consistent cut by piggybacking a control bit onto basic messages. The control bit is used to indicate whether or not the sending process has recorded its state. The processes can be explained in terms of colors. A process that has not recorded its state is colored white and a process that has recorded its state is red. White processes send

white messages and red processes send red messages. The control bit in the messages indicates the color. All processes are initially white and turn red when a red message arrives. When a red message arrives at a white process, the process must record its state BEFORE actually receiving the message. The snapshot only relies on basic messages and no control tokens are used. This algorithm has several drawbacks. First, it assumes that every process will eventually receive a red message and record its state which is not guaranteed. Second, to ensure transient messages are recorded, the processes must record all incoming and outgoing messages and send them to other processes within the basic messages. That way the transient messages can be calculated by differences in incoming and outgoing messages.

Mattern [15] extended the algorithm by Lai and Yang by adding a separate control token which is used to create two cuts by circulating the control token to every process twice. The control token is used to color the processes instead of the basic messages. This guarantees that every process will eventually record its state because the token is always circulated. Furthermore, processes do not have to keep track of sent and received messages. Instead counters can be used to keep track of the differences in sent and received white messages at each process. The control token can then accumulate the counts. When the white message counts accumulate to zero when the token arrives back at the initiator process, it can be determined that the snapshot is complete. These counters can be *vector counters* or *scalar counters*. Vector counters keep track of messages to/from each process individually whereas scalar counters keep track of just a single count at each process. When the algorithm is complete, only the initiator process can produce a global snapshot so if all processes must use the snapshot, it must be broadcasted to the other processes.

8.2 GVT

Although GVT algorithms can be implemented with the basic global snapshot algorithms described above, it is usually more efficient to build custom solutions on top of the basic algorithms. In a GVT algorithm, the local minimum clock of process is the local state and the basic messages are events that are sent between processes. This section first describes the key ideas that must be considered when developing a GVT algorithm. Then, a few of the classic GVT algorithms and modern GVT algorithms that are commonly used in practice today are described. Finally, the algorithm that is implemented in WARPED2 is described as well as

the reasons for choosing the approach.

GVT algorithms can be synchronous or asynchronous. In a synchronous GVT algorithm, since all other computation will be blocked, event processing will be halted. Synchronous GVT algorithms are usually very simple to implement but halting the event processing can be very costly. On the other hand, asynchronous GVT algorithms calculate GVT concurrently with event processing. For this reason, asynchronous GVT algorithms perform much better than synchronous GVT algorithms but are harder to implement because special cases must be considered.

There are two special cases that must be considered in any GVT algorithms:

Transient Message Problem: is caused by messages(events) that have been sent by the sending process but not yet recieved by the receiving process. If not carefully considered in a GVT algorithm, these *transient messages* can be completely missed which could lead to an erroneous GVT calculation if they contain the minimum timestamp of all other events in the system.

Simultaneous Reporting Problem: is caused because processes can report their local minimum clock at different points in real time. Consideration must be taken into account to ensure that a process does not report its local minimum clock value and then receive an event from a process that has not yet reported its local minimum clock value, completely missing the event.

There are many synchronous and asynchronous GVT algorithms that have been developed over the years that all have some method of either solving these problems.

8.2.1 Asynchronous GVT Algorithms

Message Passing Algorithms

Most of the time warp systems in use today are based on message passing and classically GVT algorithms have been designed for message passing systems. In this section Samadi's and Mattern's message passing algorithms are discussed and in the next section Fujimoto's shared memory GVT algorithms is discussed as well as the Seven O'Clock algorithm which is an extension of Fujimoto's shared memory algorithm extended for distributed memory systems.

Samadi's Algorithm [16] in the most general form uses acknowledgements for all events that have been received. All processes must track all events that have been sent but have not been acknowledged. Furthermore, the received messages must also be tracked so that acknowledgements can be sent. All transient message can then be calculated from the tracked messages. A process initiates the GVT algorithm by broadcasting a start message to all processes. After this start message is received by a process, it is marked(colored) and all acknowledgements sent from a marked process are also marked(colored). All processes then calculate their local minimum by taking the minimum of the unacknowledged received events, the marked acknowledgments sent, and the local simulation clock. Marking the acknowledgements sent after the start of the GVT calculation ensures that the simultaneous reporting problem will not occur.

Mattern's Algorithm [15] for GVT calculation is an extension on his general snapshot algorithm that was described above. The white message counts are used to determine whether transient messages are still in the system. They also serve as the basis for determining when the snapshot is complete which occurs when the accumulated white message count of all processes is zero. To ensure that the simultaneous reporting problem does not occur, red messages received at a white process are recorded and used in the local minimum value. The algorithm is initiated by sending a control token to all processes in some defined order. The token accumulates the white message counters, local minimum clocks, and minimum red message timestamps. When the accumulated count reaches zero and the token is back at the initiator process, the GVT is approximated using the minimum of the accumulated clocks and timestamps.

Other GVT Algorithms that are based on message passing model are usually based on the same ideas from Samadi's algorithm or Mattern's algorithm. Many algorithms are just extensions or variations of the algorithms that aim to optimize it in some particular way.

Shared Memory Algorithms

Fujimoto's Algorithm [2] is a fast GVT algorithm that exploits properties of shared memory architectures. In most shared memory architectures, processors cannot observe memory operations in different orders. For this reason, it is not possible to have transient messages if a shared data structure is used to communicate between tasks running on different processors. Furthermore, a shared flag variable can be

used to initiate the GVT algorithm. However, it is still possible that the flag can be read at different times, so the simultaneous reporting problem can still occur. To solve the simultaneous reporting problem, two things must be done, First, the start flag is checked after sending events and recorded if the sending task has not yet reported its local minimum value and is eventually used when the reporting is done. Second, the start flag must be read into a temporary local variable before obtaining a new event to process.

Seven O’Clock Algorithm [17] is an extension of Fujimoto’s algorithm for distributed memory systems. Although the algorithm can be used in message passing systems, the algorithm does not use any messages and is still uses shared memory ideas. The key idea in the algorithm is that all processors in a distributed system all have a consistent view of wall clock. Hence, the processors can carry out an operation atomically, without having to explicitly interact. The atomicity can be achieved by using cycle level counters which are available on most modern architectures. Unlike Fujimoto’s algorithm though, transient messages can still be missed in the calculation. To solve that problem, each processor must wait a small time interval which is calculated based on the worst round trip time for network transactions.

8.2.2 Synchronous GVT Algorithms

Global Reductions provide a good way to do a synchronous minimum calculation which and is a common way to implement a synchronous GVT algorithm. ROSS implements a synchronous GVT algorithm which uses global reductions [18]. First, to prevent the transient message problem, a global reduction on message counts of each process is performed until it reaches zero which is guaranteed because the reduction acts as a barrier for each process. The message counting is necessary because asynchronous communication is used for sending and receiving events. When the messages count reaches zero a global reduction is performed on the local minimum timestamp of all processes to give a GVT value which is broadcast to all processes. This algorithm is efficient when time warp simulation are run on large supercomputing platforms like the blue gene machine which perform collective operations very quickly.

8.2.3 Warped2 Algorithm

To calculate the GVT in WARPED2, Fujimoto’s shared memory algorithm is used between worker threads and a variation of Mattern’s algorithm with scalar message counters is used between processes. Hence,

Fujimoto's algorithm is a subalgorithm of Mattern's algorithm. The details of the Mattern's algorithm implementation in WARPED2 is detailed below as well as how it is used with Fujimoto's algorithm.

In the WARPED2 implementation, scalar counters are used to keep track of message that are sent that carry the initial color. That means that each process keeps track of the number of sent messages minus the number of received messages to and from all other process as a single counter. The reason that scalar counters are used over vector counters is that vector counters require that communication is stopped after receiving a control token until all known transient messages bound for the receiving process are received. With scalar counters, this is not possible because it is only a single counter. However, it is possible that more than two rounds of the control token will be necessary. This is usually not a problem in practice though since two rounds is usually sufficient. With scalar counters, each process must maintain a counter for both white messages *and* red messages so that counters can be consistent between multiple runs of the algorithm. Moreover, the role of colors must be switched between successive runs.

In the description of the WARPED2 algorithm, the colors will be described as *initial* and *final*. Each process also keeps track of its current color, a minimum timestamp of an event received with the final color, and temporary variables to hold accumulated values from the token. The variables that are maintained at each process and are used in the succeeding discussion are listed below in algorithm 3.

Algorithm 3: Process Variables in WARPED2 Mattern Implementation

ts_{min} : Minimum timestamp of event messages received with final color
color : Current color of the process
color_{initial} : Initial color of all processes
msgcount_{initial} : Messages sent minus messages received with initial color
msgcount_{final} : Messages sent minus messages received with final color
clock_{min} : Temporary variable to hold accumulated minimum clock from all processes
msgcount : Temporary variable to hold accumulated initial color message count from all processes

The event messages that are sent between processes contain the format:

$\langle sender, receiver, mcolor, \dots \rangle$

where *sender* is the id of the sender process, *receiver* is the id of the receiver process, and *mcolor* is the color of the message. The message color is the color of the sending process at the time it is sent. The message count for the current color is also incremented when it is sent. Pseudocode illustrating this procedure is shown in algorithm 4.

Algorithm 4: Event Message Send

```

 $mcolor \leftarrow color$ 
if  $color = color_{initial}$  then
  |  $msgcount_{initial} \leftarrow msgcount_{initial} + 1$ 
else
  |  $msgcount_{final} \leftarrow msgcount_{final} + 1$ 

```

When an event is received by a process the message count for the current color of the process is decremented. If the color carried by the message is the final color in the algorithm, indicating that the sender has already reported a local minimum value, then the timestamp of the event is recorded as ts_{min} . Psuedocode illustrating the receiving procedure is show in algorithm 5.

Algorithm 5: Event Message Receive

```

if  $color_{message} = color_{initial}$  then
  |  $msgcount_{initial} \leftarrow msgcount_{initial} - 1$ 
else
  |  $msgcount_{final} \leftarrow msgcount_{final} - 1$ 
  |  $ts_{min} \leftarrow \min(ts_{min}, ts_{event})$ 

```

The control token that is sent between processes contains the format:

$< sender, receiver, mclock, msend, mcount >$

where $mclock$ is an accumulated minimum of all local minimum clocks at all processes visited by the token, $msend$ is an accumulated minimum of all ts_{min} values at all processes visited by the token, and $mcount$ is an accumulated sum of $msgcount_{final}$ from all processes visited by the token.

In the WARPED2 implementation, the token is passed in logical ring fashion to increasing process ids and is initiated by process with id 0. When the token reaches process $N - 1$, where N is the number of processes in the system, it is sent back to process 0. To start the algorithm, process 0 toggles its color, resets minim values to infinity, stores the initial color message count into a temporary variable $msgcount$, and starts Fujimoto's algorithm. When Fujimoto's algorithm is complete, it will send the token $< 0, 1, lvt_{min}, ts_{min}, msgcount >$ with lvt_{min} being the result of Fujimoto's algorithm. Psuedocode illustrating the start procedure is shown in algorithm 6.

When a token is received at a process that is not the initiator and it still has the initial color then the color

Algorithm 6: Mattern Algorithm Start Procedure

```

if  $color = WHITE$  then
   $color \leftarrow RED$ 
else
   $color \leftarrow WHITE$ 
 $ts_{min} \leftarrow \infty$ 
 $clock_{min} \leftarrow \infty$   $msgcount \leftarrow msgcount_{initial}$ 
 $msgcount_{initial} \leftarrow 0$ 
 $lvt_{min} \leftarrow doFujimoto()$ 
SendToken( $0, 1, lvt_{min}, ts_{min}, msgcount$ )

```

is toggled. Then, the minimum timestamp received from final colored messages, the minimum clock value, and the initial message count for the process are accumulated with the token's value. The initial message count is then reset so it will not be used in the next round and Fujimoto's algorithm is initiated. When Fujimoto's algorithm is completed, the token is sent to the next process with all of the accumulated values including lvt_{min} calculated from Fujimoto's algorithm. This procedure is illustrated in pseudocode shown in algorithm 7.

Algorithm 7: Mattern Control Token Receive Procedure: Non-initiator Node

```

if  $color = color_{initial}$  then
   $ts_{min} \leftarrow \infty$ 
  if  $color = WHITE$  then
     $color \leftarrow RED$ 
  else
     $color \leftarrow WHITE$ 
 $ts_{min} \leftarrow \min(ts_{min}, msend)$ 
 $clock_{min} \leftarrow \min(clock_{min}, mclock)$ 
 $msgcount \leftarrow msgcount_{initial} + msgcount$ 
 $msgcount_{initial} \leftarrow 0$ 
 $lvt_{min} \leftarrow doFujimoto()$ 
SendToken( $i, (i + 1) \bmod N, \min(lvt_{min}, clock_{min}), ts_{min}, msgcount$ )

```

When a token is received at a the initiator process, it can be assumed that a minimum clock value has already been included in the token that is received. If the accumulated message count for the initial color has reached zero, then the GVT can be approximated and the algorithm is terminated. If there are still transient message that were not accounted for, the initiator process initiates a new round until the resulting message

count accumulation is zero when received at the initiator. The GVT is approximated at the initiator by taking the minimum of the accumulated minimum clock values and the accumulated minimum timestamp values and broadcast to the rest of the processes. This procedure is illustrated in the psuedocode in algorithm 8.

Algorithm 8: Mattern Control Token Receive Procedure: Initiator Node

```

if  $mcount = 0$  then
   $gvtApprox \leftarrow \min(mclock, msend)$ 
  SendGVTUpdate()
  if  $color_{initial} = WHITE$  then
     $color_{initial} \leftarrow RED$ 
  else
     $color_{initial} \leftarrow WHITE$ 
   $clock_{min} \leftarrow \infty$ 
else
   $ts_{min} \leftarrow \min(ts_{min}, msend)$ 
   $msgcount \leftarrow msgcount_{initial} + mcount$ 
   $msgcount_{initial} \leftarrow 0$ 
   $lvt_{min} \leftarrow doFujimoto$ 
  SendToken( $i, (i + 1) \bmod N, lvt_{min}, ts_{min}, msgcount$ )
  
```

8.3 Termination Detection

Termination detection, like GVT, is a problem of determining the global state of the system. Termination is a *stable property* of a distributed system, meaning that once termination conditions occur, the system will remain with termination conditions forever until further action is taken.

A process in the system can be in one of two states at any time: active or passive. A process is considered active if some basic computation still remains and passive otherwise. When all processes in the system become passive and no messages are left in transit, then the system should be terminated. The purpose of the termination detection algorithm is to determine when this occurs. A passive process can become active with the arrival of an *activation message*. For parallel discrete event simulation the basic computation is event processing and the activation messages are events. A termination detection for any parallel discrete event simulation must satisfy the following properties:

Safety: Termination will not be detected if any unprocessed event is still present in system including all

local pending event sets and events still in transit.

Liveness: Termination will be detected at some finite amount of time after all events have been processed.

Just like GVT algorithms, termination detection algorithms can be implemented with message passing or shared memory. Termination algorithms vary widely because different systems can define termination conditions in such different ways. Furthermore, termination usually does not affect system performance so correctness is more important than optimization. For these reasons only the termination algorithm that is implemented in WARPED2 will be discussed any further. It is actually two independent algorithms, a message passing algorithm and a shared memory algorithm. In the opposite manner as the GVT algorithm, the shared memory algorithm is actually used to initiate the message passing algorithm.

8.3.1 Shared Memory algorithm

The purpose of the shared memory algorithm is to determine when all of the worker threads in a process become passive (inactive). The algorithm is fairly straightforward and uses just a single shared counter variable to keep track of the number of active worker threads and a boolean array to keep track of which worker threads are active. Worker threads can only read or write to their own status values. The counter is updated atomically to avoid possible race conditions.

The safety property is achieved because there can be no transient messages. If a thread sends an event to an LP that will be processed by another thread and then becomes inactive, false termination cannot be detected because the receiving thread becomes active again after seeing the event. Come back to this, it may not be accurate. The liveness property is achieved because the manager thread periodically checks the active worker thread count so the inactivity of all worker threads will eventually be discovered. If the count is zero, then the message passing algorithm will be initiated between processes.

8.3.2 Message Passing Algorithm

The algorithm that is carried out among processes is an asynchronous message passing algorithm based on Mattern's "sticky flags" algorithm [15]. Just like the GVT algorithm, the token is passed in a logical ring to increasing process ids. However, the initiator process of the algorithm is dynamic. The initiator is the first active process that the token reaches during circulation. For the first circulation, the initiator is process 0.

Each process has two states, one for the actual state and one for the *sticky state*. The sticky state is the state that is actually used in the algorithm. It becomes active when the actual state becomes active but sticks to active when the actual state becomes passive. The sticky state can only changes to passive on the arrival of a token. By using this scheme the token is forced to circulate two times with no process becoming active and ensures the safety property. Without this scheme, a process that has already forwarded the token because it was passive could receive an activation message and then the sender of the activation message could become passive before receiving the token. False termination could then be detected.

The process variable names that are used for the succeeding discussion are listed in algorithm 9.

Algorithm 9: Process Variables in Termination Detection Algorithm

state_{actual} : Indicates the actual state of the process at all times

state_{sticky} : Indicates the state of the process if active, but may stick to active if passive

initiator : Boolean variable indicating process is leader

The termination token that is sent between process has the format:

$\langle sender, receiver, mstate, minitiator \rangle$

where *sender* is the id of the sending process, *receiver* is the id of the receiving process, *mstate* is the partial state of system based on visited processes, and *minitiator* is the process id of the initiator.

The algorithm is started when the initiator process becomes passive which is determined by the shared memory algorithm. When a process receives the token it becomes the initiator but loses its roles as initiator when it sends the token. That way, only a single process can be the initiator. Furthermoe, since the token always stops at an active process, the token is always guarenteed to start again when it becomes passive which also guarentees the liveness property. When the token is received back at the initiator with a passive state, then termination is signaled to all processes. The procedure is illustrated in algorithm 10.

It should also be noted that this algorithm is only guarenteed to work if the message order is preserved. If that is not the case, then message counters are necessary to ensure transient activation messages are not missed.

Algorithm 10: Termination Token Receive Procedure

```

initiator  $\leftarrow$  true
if statesticky = PASSIVE and stateprocess = minitiator then
  if mstate = PASSIVE then
    └ Signal termination
  else if statesticky = PASSIVE then
    └ initiator  $\leftarrow$  false
    └ SendToken(mstate, minitiator)
statesticky  $\leftarrow$  stateactual

```

Chapter 9

Memory Management

This chapter will focus on three main topics that are all related to the management of memory. First, state saving techniques will be discussed as well the analysis of state saving in WARPED2. This will include both space and time requirements. Then fossil collection and its overheads are introduced and a comparison of worker thread versus manager thread fossil collection will be examined. Lastly, memory allocation and deallocation and its importance in time warp is presented as well as how it is accomplished in WARPED2.

9.1 State Saving

Copy-state Saving is the classic state saving technique that saves every past state of every LP and requires that the all states are copied and saved into the state queues. This method requires a lot of extra memory and requires a lot of extra computation to copy the states and insert them into the state queue. For this reason, copy-state saving is usually used in conjunction with other technique or not at all.

Periodic State Saving is another state saving technique where the state of each LP is saved only once every N events, where N is a number greater than one. Periodic state saving can significantly reduce the overhead of the time taken to copy the state of the LPs into the state queue. However, due to state history being lost, more processed event have to be saved so that the state of LPs can be restored correctly. These saved events must be reprocessed to restore the state in a process known as *coast forwarding*. During coast forwarding the events are processed normally but only to update the state. The only difference is that no

events are sent during the coast forwarding phase. The downside is that the rollback length is increased due to the loss in state saving. However, periodic state saving is a significant improvement over the base copy-state saving approach since the reduced time in state saving far outweighs the extra rollback time for increased rollback length.

Incremental State Saving is a technique that aims to reduce the amount of memory needed to store past states of the LPs. Instead of saving entire snapshots of the past states, the differences in specific state variables are saved. This method requires that metadata describing which variables are modified for each event. Therefore, this approach works well as long as only a small portion of the state variables change during the forward execution of events.

Reverse Computation is a modern approach to state saving that does not actually save any past states of the LPs. Instead, the *control state* of the forward computation is saved as a set of bits that describe the control flow. By saving the control flow of the forward execution for each event, the state variables that are modified and how they are modified are known and can be reversed. That is, at least, if all state variables are reversible without the need to know the histories of the variables. Also, a reversible random number generator is required. These are both practical requirements, though. The major problem with this approach is the necessity to understand forward and reverse computation precisely in the implementation of the simulation model.

9.1.1 State Saving Experimental Assessment

WARPED2 currently implements only periodic state saving because it works well regardless of the simulation model and it can be implemented transparently in the simulation kernel.

9.2 Fossil Collection

GVT-based Fossil Collection

On-the-fly Fossil Collection

Optimistic Fossil Collection

9.2.1 Fossil Collection Experimental Assessment

9.3 Memory Allocation

9.3.1 Thread-Caching Malloc (TCMalloc)

Chapter 10

Observations with the ARM big.LITTLE Platform

10.1

Chapter 11

Summary of Results

Chapter 12

Conclusions and Suggestions for Future Research

12.1 Summary of Findings

12.2 Detailed Conclusions

12.3 Suggestions for Future Work

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