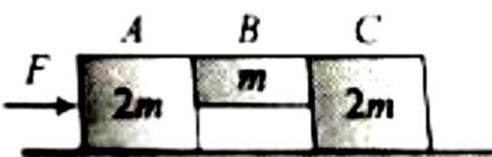


Single Correct Answer Type

| | |
|-------|--|
| 1. | <p>Two cars start off race with velocity 4 m/s and 2 m/s and travel in straight line with uniform accelerations 1 m/s² and 2 m/s² respectively. If they reach the final point at the same instant then the length of the path is</p> <p>a) 30 m b) 32 m c) 20 m d) 24 m</p> |
| Ans. | d |
| Sol.: | |
| 2. | <p>For any arbitrary motion in space, which of the following relations are true:</p> <p>a) $\vec{V}_{average} = \left(\frac{1}{2} (\vec{v}(t_1) + \vec{v}(t_2)) \right)$ b) $\vec{V}_{average} = \frac{[\vec{r}(t_2) - \vec{r}(t_1)]}{(t_2 - t_1)}$ c) $\vec{V}(t) = \vec{v}(0) + \vec{a}(t)$ d) $\vec{r}(t) = \vec{r}(0) + \vec{v}(0)t + \left(\frac{1}{2} \right) \vec{a}t^2$</p> |
| Ans. | b |
| Sol.: | |
| 3. | <p>In a cubical vessel (1m × 1m × 1m) the gas molecules of diameter 1.7×10^{-8} cm are at a temperature of 300 K and a pressure of 10^{-4} mm of mercury. The mean free path of the gas molecule is</p> <p>a) 1 m b) 4 m c) 2.42 m d) 1 cm</p> |
| Ans. | c |
| Sol.: | |
| 4. | <p>The system is pushed by a force F as shown in figure. All surfaces are smooth except between B and C. Friction coefficient between B and C is μ. Minimum value of F to prevent block B from downward slipping is</p>  <p>a) $\left(\frac{3}{2\mu} \right) mg$</p> |

b) $\left(\frac{5}{2\mu}\right)mg$

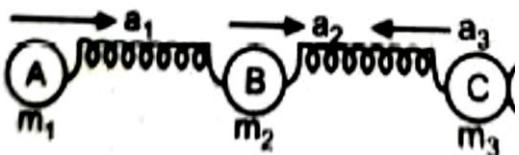
c) $\left(\frac{5}{2}\right)\mu mg$

d) $\left(\frac{3}{2}\right)\mu mg$

Ans. b

Sol.:

5. Shown in the following figure is a system of three particles of mass $m_A = 1\text{kg}$, $m_B = 2\text{kg}$ & $m_C = 4\text{kg}$ connected by two springs. The acceleration of A, B and C at an instant are 1m/sec^2 , 2m/sec^2 and $1/2\text{m/sec}^2$ respectively directed as shown in the figure, then the external force acting on the system is



a) 1 N

b) 7 N

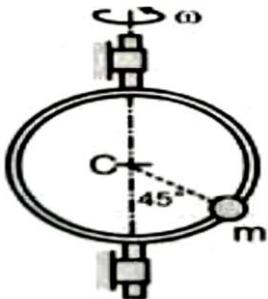
c) 3 N

d) 2 N

Ans. c

Sol.:

6. A small bead of mass $m = 1\text{ kg}$ is carried by a circular hoop having centre at C and radius $r = 1\text{ m}$ which rotates about a fixed vertical axis. The coefficient of friction between bead and hoop is $\mu = 0.5$. The maximum angular speed of the hoop for which the bead does not have relative motion with respect to hoop is



a) $(5\sqrt{2})^{1/2} \text{ rad/s}$

b) $(10\sqrt{2})^{1/2} \text{ rad/s}$

c) $(15\sqrt{2})^{1/2} \text{ rad/s}$

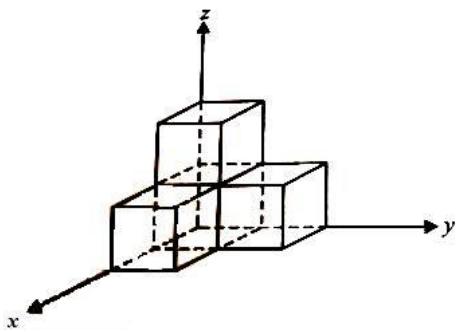
d) $(30\sqrt{2})^{1/2} \text{ rad/s}$

Ans. d

Sol.:

7. Find the center of mass (x, y, z) of the following structure of four identical cubes if

the length of each side of a cube is 1 unit



a) $\frac{3}{4}, \frac{3}{4}, \frac{3}{4}$

b) $\frac{1}{4}, \frac{1}{4}, \frac{1}{4}$

c) $\frac{2}{3}, \frac{2}{3}, \frac{2}{3}$

d) 1, 1, 1

Ans. a

Sol.:

8. The ratio of the weights of a body on the earth's surface to that on the surface of a planet is $\frac{9}{8}$, the mass of the planet is $\frac{1}{18}$ th of that of the earth. If R is the radius of the Earth, what is the radius of a planet? (take the planets to have the same density)

a) $\frac{R}{4}$

b) $\frac{R}{3}$

c) $\frac{R}{9}$

d) $\frac{R}{17}$

Ans. a

Sol.:

9. A uniform rod of length L, has a mass per unit length λ and area of cross section A. The elongation in the rod is l due to its own weight, if it is suspended from the ceiling of a room. The young's modulus of the rod is

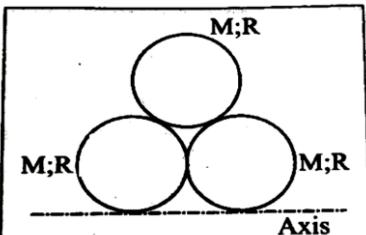
a) $\frac{3\lambda g L^2}{Al}$

b) $\frac{\lambda g L^2}{2Al}$

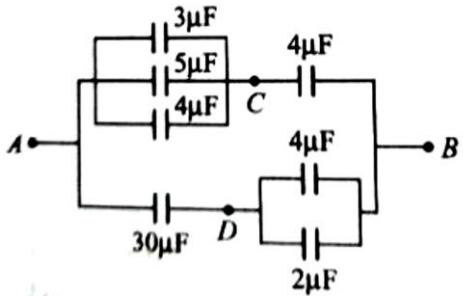
c) $\frac{2\lambda g L}{Al}$

d) $\frac{\lambda g L^2}{Al}$

Ans. b

| | |
|-------|--|
| Sol.: | |
| 10. | A solid sphere of radius R acquires a terminal velocity v_1 when falling (due to gravity) through a viscous liquid having a coefficient of viscosity η . The sphere is broken into 1000 identical solid spheres. If each of these spheres acquires a terminal velocity v_2 , when falling through the same fluid, the ratio $\frac{v_1}{v_2}$ equals to |
| a) | $\frac{1}{27}$ |
| b) | $\frac{1}{10}$ |
| c) | 10 |
| d) | 100 |
| Ans. | d |
| Sol.: | |
| 11. | The efficiency of a Carnot engine operating between the temperatures T_1 and T_2 ($T_1 > T_2$) is η_0 . The temperature of sink is decreased by α K and efficiency is η_1 . The temperature of source is increased by α K and efficiency is η_2 |
| a) | $\eta_1 = \eta_2 = \eta_0$ |
| b) | $\eta_1 > \eta_2 > \eta_0$ |
| c) | $\eta_1 < \eta_2 < \eta_0$ |
| d) | $\eta_1 > \eta_0 > \eta_2$ |
| Ans. | b |
| Sol.: | |
| 12. | There are three rings each of mass M and radius R . What is the moment of inertia about the given axis? |
| |  |
| a) | $MR^2(5 + 2\sqrt{3})$ |
| b) | $MR^2\frac{(15 + 4\sqrt{3})}{2}$ |
| c) | $MR^2\frac{(5 + \sqrt{3})}{2}$ |
| d) | $MR^2(7 + \sqrt{3})$ |
| Ans. | b |
| Sol.: | |
| 13. | A dog while barking delivers about 1mw power. If this power is uniformly distributed over hemispherical area, then the sound level at a distance of 5m is B_1 . If instead of 1 dog, |

| | |
|-------|--|
| | 5 dogs start barking at same time each delivering 1mw power then, the sound level is B_2 . Find, $\frac{B_1}{B_2} = (\text{take } \log(6.37) = 0.8)$ |
| a) | $\frac{68}{75} dB$ |
| b) | $\frac{77}{66} dB$ |
| c) | $\frac{78}{66} dB$ |
| d) | $\frac{62}{71} dB$ |
| Ans. | a |
| Sol.: | |
| 14. | A source of sonic oscillations with frequency $f = 1700\text{Hz}$ and a receiver are located onthe same normal to a wall. Both the source and receiver are stationary, and the wallrecedes from the source with velocity $u = 6.0 \text{ cm/s}$. Find the beat frequency registeredby the receiver. The velocity of sound is equal to $v = 340 \text{ m/s}$ |
| a) | 0.2 Hz |
| b) | 0.6 Hz |
| c) | 0.4 Hz |
| d) | 1.2 Hz |
| Ans. | b |
| Sol.: | |
| 15. | Let a total charge $2Q$ be the distributed in a sphere of radius R , with the charge densityis given by $\rho(r) = kr$, where r is the distance from centre. Two charges A & B of $-Q$ areplaced on diametrically opposite points at equal distance a , from the centre. If A & Bdo not experience any force, then |
| a) | $a = \frac{3R}{2^{1/4}}$ |
| b) | $a = \frac{R}{\sqrt{3}}$ |
| c) | $a = 8^{-1/4}R$ |
| d) | $a = 2^{-1/4}R$ |
| Ans. | c |
| Sol.: | |
| 16. | Several capacitors are connected as shown in figure. If the charge on the $5\mu\text{F}$ capacitoris $120\mu\text{C}$, the potential difference between points A and D is |



- a) 16V
- b) 32V
- c) 64V
- d) 14.2V

Ans. a

Sol.:

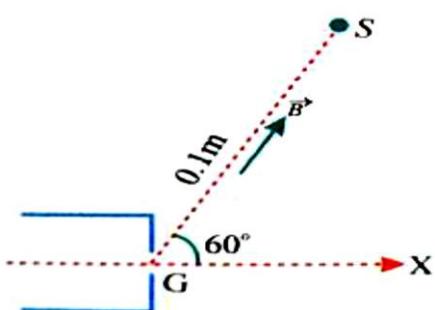
17. An electric motor operating on 50 volt D.C. supply draws a current of 10 amp. If the efficiency of motor is 40%, then the resistance of the winding of the motor is

- a) 1.5Ω
- b) 3Ω
- c) 4.5Ω
- d) 6Ω

Ans. b

Sol.:

18. An electron gun G emits electron of energy 2 keV travelling in the positive X direction. The electrons are required to hit the spot S where GS = 0.1 m, and the line GS makes an angle of 60° with the X-axis as shown in the figure. A uniform magnetic field B parallel to GS exists in the region outside the electron gun. Find the minimum value of B needed to make the electrons hit point S.



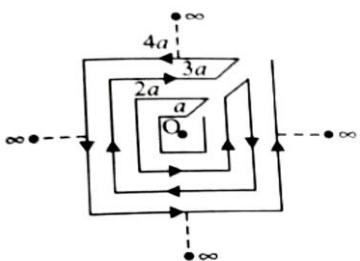
- a) $4.73 \times 10^{-3} T$
- b) $4.73 \times 10^{-2} T$
- c) $2.73 \times 10^{-2} T$
- d) $5.73 \times 10^{-3} T$

Ans. a

Sol.:

19. Determine the magnitude of magnetic field at the centre of the current carrying wire arrangement shown in the figure. The arrangement extends to infinity. The wires joining the successive squares are along the line passing through the centre and the current in

the wires is I.



a) $\frac{\mu_0 I}{\sqrt{2}\pi a}$

b) 0

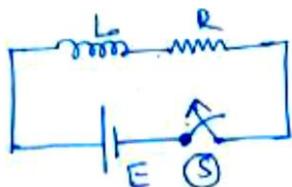
c) $\frac{2\sqrt{2}\mu_0 I}{\pi a} \ln 2$

d) $\frac{4\sqrt{7}\mu_0 I}{\pi a} \ln 2$

Ans. c

Sol.:

20. Consider the LR circuit shown in figure. If the switch S is closed at $t = 0$, then the amount of charge that passes through the battery between $t = 0$ and $t = \frac{L}{R}$ is



a) $\frac{7.3EL}{R^2}$

b) $\frac{EL}{2.7R^2}$

c) $\frac{2.7EL}{R^2}$

d) $\frac{EL}{7.3R^2}$

Ans. b

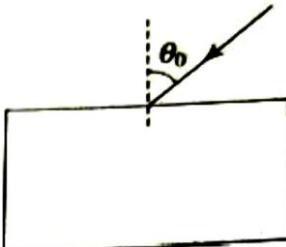
Sol.:

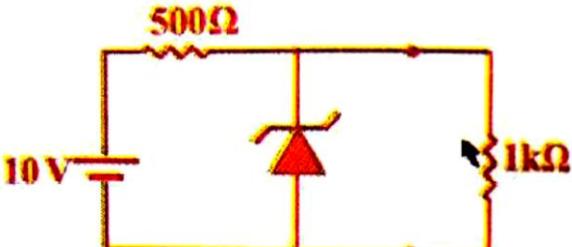
Integer Answer Type

21. A plane electromagnetic wave propagating in the x-direction has a wavelength of 60mm. The electric field is in the y-direction and its maximum magnitude is 99 v/m. The equation for the electric field as a function of x and t is given by $99\sin \pi[10]^{2m}\left(t - \frac{x}{v}\right)$. Find the value of m is

Ans. 5

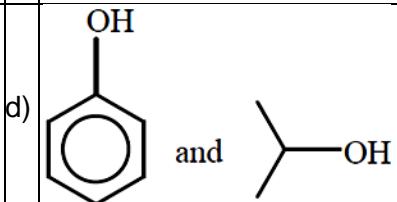
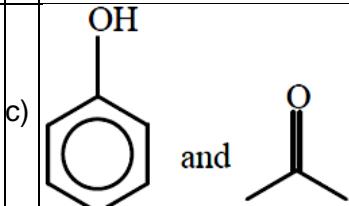
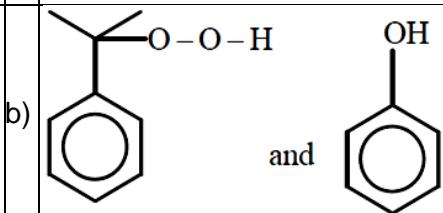
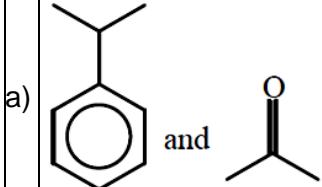
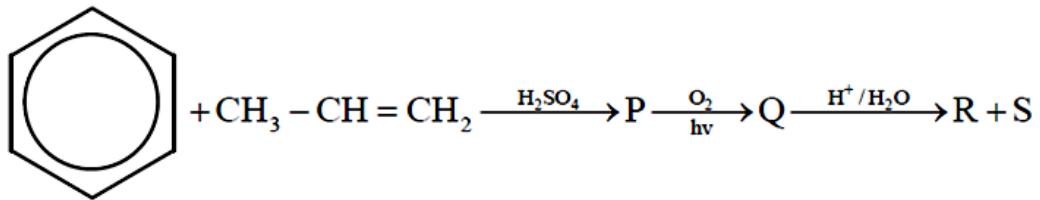
Sol.:

| | |
|------|---|
| : | |
| 22. | A slab of refractive index μ is placed in air and light is incident at maximum angle θ_0 from vertical. The minimum value of μ for which total internal reflection takes place at the vertical surface is $\mu = \sqrt{\frac{4}{K} + \sin^2 \theta_0}$. Then K is |
| |  |
| Ans | 4 |
| Sol. | |
| 23. | A horizontal beam of vertically polarized light of intensity 44 W/m^2 is sent through two polarizing sheets. The polarizing direction of the first is 60° to the vertical, and that of the second is horizontal. The intensity of the light (in W/m^2) transmitted by the pair of sheets is $n/4$ where $n = \underline{\hspace{2cm}}$ |
| Ans | 33 |
| Sol. | |
| 24. | The de Broglie wavelength of neutrons in thermal equilibrium is (Given $m_n = 1.6 \times 10^{-27} \text{ kg}$) (take $\sqrt{T} = 1$) in A° is $7.7 \times x$, then the value of x is |
| Ans | 4 |
| Sol. | |
| 25. | An electron jumps from the fourth orbit to the second orbit of hydrogen atom. Given the Rydberg's constant $R = 10^5 \text{ cm}^{-1}$. The frequency, in Hz, of the emitted radiation will be $\frac{s}{16} \times 10^5$, the value of s is |
| Ans | 9 |
| Sol. | |
| 26. | A container is filled with a radioactive substance for which the half life is 2 days. A week later, when the container is opened, it contains 5g of the substance. Approximately the number of grams of the substances were initially placed in the container is $20N$, the value of N is |
| Ans | 4 |

| | |
|-----------|--|
| Sol. : | |
| 27. | Figure shows the circuit of a simple constant voltage supply using zener diode. The constant voltage available across the zener diode is 5V. The current flowing through the $1\text{ k}\Omega$ load in mA is |
| |  |
| Ans . | 5 |
| Sol. : | |
| 28. | An amplitude modulated wave is modulated to 50 %. If carrier as well as one of the side bands are suppressed then the saving in power is 11.8%. The value of y is |
| Ans . | 8 |
| Sol. : | |
| 29. | A tube of certain diameter and length 48 cm is open at both ends. Its fundamental frequency of resonance is found to be 320 Hz. The velocity of sound in air is 320 m/s. The diameter of the tube (in cm) is $n/3$ where $n = \underline{\hspace{2cm}}$ |
| Ans . | 10 |
| Sol. : | |
| 30. | Interference fringes were produced using light in a double slit experiment. When a mica sheet of uniform thickness and refractive index 1.6 (relative to air) is placed in the path of light from one of the slits, the central fringe moves through some distance. This distance is equal to the width of 30 interference bands if light of wavelength 4800 \AA is used. The thickness of mica is $12x \times 10^{-6}\text{ m}$ then the value of x is |
| Ans . | 2 |
| Sol. : | |

Single Correct Answer Type

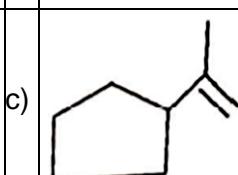
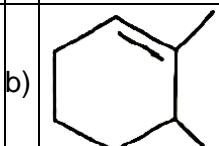
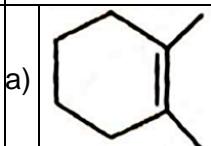
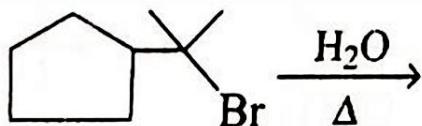
31. Identify R and S:

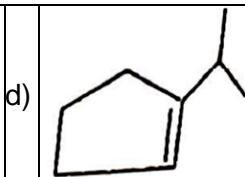


Ans. c

Sol.:

32. Find the major product of the following reaction:





Ans. a

Sol.:

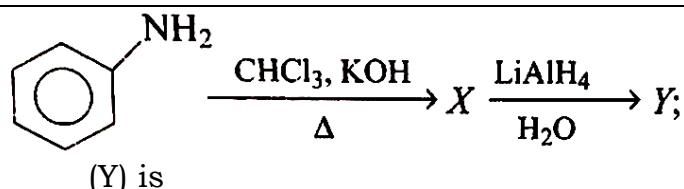
33. Which of the following conditions regarding a chemical process ensures its spontaneity at all temperature?

- a) $\Delta H > 0, \Delta G < 0$
- b) $\Delta H < 0, \Delta S > 0$
- c) $\Delta H < 0, \Delta S < 0$
- d) $\Delta H > 0, \Delta S < 0$

Ans. b

Sol.:

34.



(Y) is

- a) $\text{Ph}-\overset{\text{NH}_2}{\underset{|}{\text{N}}}-\text{CH}_3$
- b) $\text{Ph}-\text{CH}_2-\text{NH}_2$
- c) $\text{Ph}-\overset{\text{O}}{\underset{\parallel}{\text{N}}}-\overset{|}{\text{C}}-\text{NH}_2$
- d) $\text{Ph}-\overset{+}{\text{N}}\equiv\overset{-}{\text{C}}$

Ans. a

Sol.:

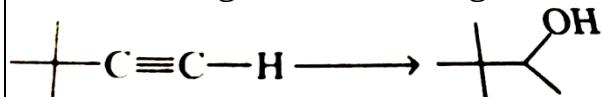
35. Excess of Li and Mg are allowed to react separately with 1 mole of N_2 gas, ratio of gaseous product obtained in complete hydrolysis of both compounds.

- a) 1:2
- b) 2:1
- c) 1:1
- d) 2:3

Ans. c

Sol.:

36. Select the reagent for following transformation:

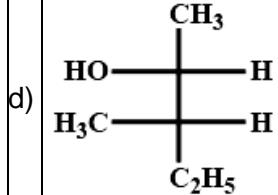
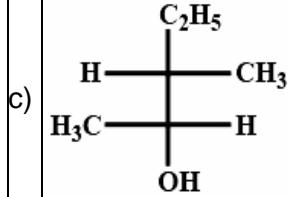
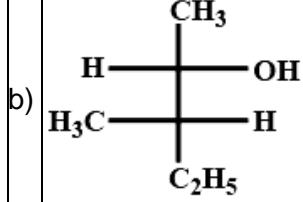
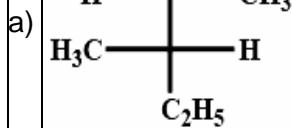
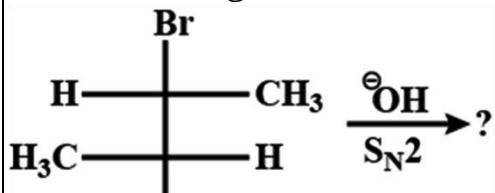


- a) $\text{H}_2\text{-Pd}; \text{HCHO}, \text{H}_2\text{SO}_4$
- b) $\text{H}_2, \text{Pd-BaSO}_4; \text{Hg(OAC)}_2, \text{H}_2\text{O}, \text{NaBH}_4, \text{OH}^-$
- c) $\text{BH}_3, \text{H}_2\text{O}_2, \text{OH}^-; \text{Pd-C}$
- d) $\text{Hg}^{+2}, \text{H}_2\text{SO}_4; \text{H}_2, \text{Pd-BaSO}_4$

Ans. b

| | |
|-------|---|
| Sol.: | |
| 37. | Consider the partial decomposition of A as $2A(g \rightleftharpoons 2B(g) + C(g))$. At equilibrium 700 mL gaseous mixture contains 100 mL of gas C at 10 atm and 300 K. What is the value of K_p for the reaction? |
| a) | $\frac{40}{7}$ |
| b) | $\frac{1}{28}$ |
| c) | $\frac{10}{28}$ |
| d) | $\frac{28}{10}$ |
| Ans. | c |
| Sol.: | |
| 38. | A 0.020 m solution of each of the following compounds is prepared. Which solution would you expect to freeze at -0.1490°C ? K_f (water) = $1.86 \text{ K kg mol}^{-1}$? [Where, py = pyridine (unidentate), en = ethylenediamine (bidentate)] |
| a) | $[\text{Co}(\text{en})_2\text{Cl}_2]\text{Cl}$ |
| b) | $\text{Na}[\text{Co}(\text{EDTA})]$ |
| c) | $[\text{Cr}(\text{py})_5\text{Cl}]\text{Cl}_2$ |
| d) | $[\text{Cr}(\text{NH}_3)_6]\text{Cl}_3$ |
| Ans. | d |
| Sol.: | |
| 39. | Glucose when treated with CH_3OH in presence of dry. HCl gives α - and β -methylglycosides because it contains |
| a) | An aldehydic group |
| b) | $-\text{CH}_2\text{-OH}$ group |
| c) | Give $-\text{OH}$ group |
| d) | None of these |
| Ans. | a |
| Sol.: | |
| 40. | For a first order reaction $\text{A} \rightarrow \text{P}$, the temperature (T) dependent rate constant (k) was found to follow the equation: $\log k = -(2000) \frac{1}{T} + 6.0$. The pre-exponential factor A and the activation energy E_a , respectively are |
| a) | $1.0 \times 10^6 \text{s}^{-1}$ and 9.2 kJ mol^{-1} |
| b) | 6.0 s^{-1} and 16.6 kJ mol^{-1} |
| c) | $1.0 \times 10^6 \text{s}^{-1}$ and 16.6 kJ mol^{-1} |
| d) | $1.0 \times 10^6 \text{s}^{-1}$ and 38.3 kJ mol^{-1} |
| Ans. | D |
| Sol.: | |
| 41. | Select correct for reaction $\text{Na}_2\text{CrO}_4 + \text{H}_2\text{SO}_4 \rightarrow$ |
| a) | It is a redox reaction in which green solution of $[\text{Cr}(\text{H}_2\text{O})_6]^{+3}$ is produced |
| b) | One of the product in reaction has trigonal planar structure |
| c) | Dimeric bridged tetrahedral metal ion is produced |
| d) | Dark blue colour is obtained in reaction |
| Ans. | c |
| Sol.: | |

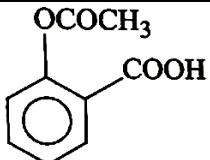
42. In the following reaction the most probable product will be:



Ans. **b**

Sol.:

43.



The compound is used as:

- a) Antiseptic
- b) Antibiotic
- c) Analgesic
- d) Pesticide

Ans. **c**

Sol.:

44. Which of the following sequences is correct for decreasing order of ionic radius?

- a) Se^{2-} , I^- , Br^- , O^{2-} , F^-
- b) I^- , Se^{2-} , O^{2-} , Br^- , F^-
- c) Se^{2-} , I^- , Br^- , F^- , O^{2-}
- d) I^- , Se^{2-} , Br^- , O^{2-} , F^-

Ans. **d**

Sol.:

45. In the below reaction (X) and (Y) are respectively

| | |
|----|--|
| | $\text{H}_3\text{C}-\overset{\text{O}}{\underset{\parallel}{\text{C}}}-\text{OH} + \text{C}_2\text{H}_5\text{OH} \xrightarrow[\text{conc. H}_2\text{SO}_4]{^{18}\text{O}} (\text{X}) \text{H}_3\text{C}-\overset{\text{O}}{\underset{\parallel}{\text{C}}}-\text{OH} + (\text{CH}_3)_3\text{C}-\overset{\text{O}}{\underset{\parallel}{\text{C}}}-\text{OH} \xrightarrow[\text{conc. H}_2\text{SO}_4]{^{18}\text{O}} (\text{Y})$ |
| a) | $\text{CH}_3-\overset{\text{O}}{\underset{\parallel}{\text{C}}}-\overset{^{18}\text{O}}{\text{O}}-\text{C}_2\text{H}_5 \text{ and } \text{CH}_3-\overset{\text{O}}{\underset{\parallel}{\text{C}}}-\text{O}-\overset{\text{CH}_3}{\underset{\mid}{\text{C}}}-\text{CH}_3$ |
| b) | $\text{H}_3\text{C}-\overset{\text{O}}{\underset{\parallel}{\text{C}}}-\overset{^{18}\text{O}}{\text{O}}-\text{C}_2\text{H}_5 \text{ and } \text{H}_3\text{C}-\overset{\text{O}}{\underset{\parallel}{\text{C}}}-\overset{^{18}\text{O}}{\text{O}}-\overset{\text{CH}_3}{\underset{\mid}{\text{C}}}-\text{CH}_3$ |
| c) | $\text{CH}_3-\overset{\text{O}}{\underset{\parallel}{\text{C}}}-\text{O}-\text{C}_2\text{H}_5 \text{ and } \text{H}_3\text{C}-\overset{\text{O}}{\underset{\parallel}{\text{C}}}-\text{O}-\overset{\text{CH}_3}{\underset{\mid}{\text{C}}}-\text{CH}_3$ |
| d) | $\text{CH}_3-\overset{\text{O}}{\underset{\parallel}{\text{C}}}-\text{O}-\text{C}_2\text{H}_5 \text{ and } \text{CH}_3-\overset{\text{O}}{\underset{\parallel}{\text{C}}}-\overset{^{18}\text{O}}{\text{O}}-\overset{\text{CH}_3}{\underset{\mid}{\text{C}}}-\text{CH}_3$ |

Ans. **a**

Sol.:

46. Which one of the following is the most stable conformer?

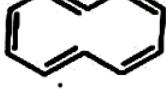
| | |
|----|--|
| a) | |
| b) | |
| c) | |
| d) | |

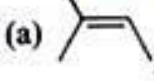
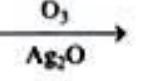
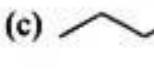
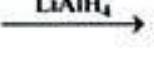
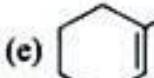
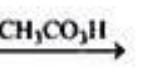
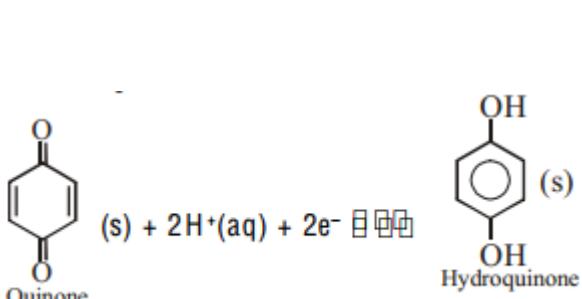
Ans. **c**

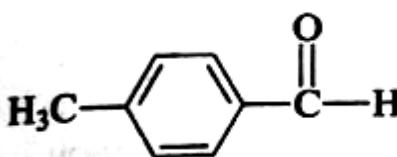
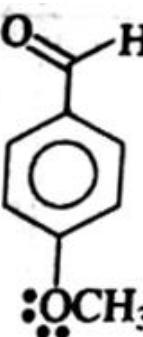
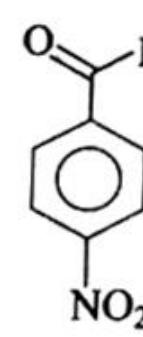
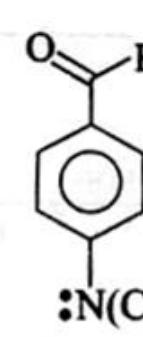
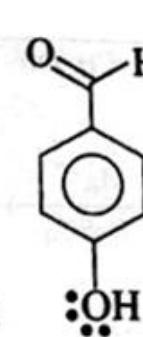
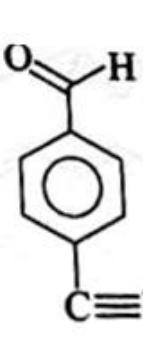
Sol.:

| | |
|-------|---|
| 47. | Which of the following fluoride of Xenon has zero dipole moment? |
| a) | XeF ₂ |
| b) | XF ₆ |
| c) | XeF ₄ |
| d) | None of these |
| Ans. | d |
| Sol.: | |
| 48. | The spin magnetic moment of cobalt in the compound H g[Co(SC N) ₄] is |
| a) | $\sqrt{3}$ |
| b) | $\sqrt{8}$ |
| c) | $\sqrt{15}$ |
| d) | $\sqrt{24}$ |
| Ans. | c |
| Sol.: | |
| 49. | Which of the following is not a planar molecular? |
| a) | H ₂ C = C = CH ₂ |
| b) | H ₂ C = C = C = CH ₂ |
| c) | H ₂ C = C = O |
| d) | NC - HC = CH - CN |
| Ans. | a |
| Sol.: | |
| 50. | The type of hybridization of boron in diborane is |
| a) | sp-hybridization |
| b) | sp ² -hybridization |
| c) | sp ³ -hybridization |
| d) | sp ³ d ² -hybridization |
| Ans. | c |
| Sol.: | |

Integer Answer Type

| | |
|-------|---|
| 51. | Find out number of aromatic compounds or ion from following |
| |  ,  ,  ,  |
| |  ,  ,  ,  |
| Ans. | 5 |
| Sol.: | |
| 52. | What is the minimum pH necessary to cause a precipitate of Pb(OH) ₂ , ($K_{sp} = 1.2 \times 10^{-3}$) to form in a 0.12M PbCl ₂ solution? |
| Ans. | 12 |
| Sol.: | |
| 53. | Ratio of moles of Fe(II) oxidized by equal volumes of equimolar KMnO ₄ and K ₂ Cr ₂ O ₇ |

| | |
|----------------|--|
| | solutions in acidic medium will be $x : y$. Then $x + y = ?$ |
| Ans. 11 | |
| Sol.: | |
| 54. | The energy of a I, II and III energy levels of a certain atom are E , $4E/3$ and $2E$ respectively. A photon of wavelength λ is emitted during a transition from III to I. What will be the wavelength of emission for transition II to I _____? |
| Ans. 3 | |
| Sol.: | |
| 55. | 99% of a first order reaction was complete in 32 minutes when 99.9% of the reaction will complete in _____ min |
| Ans. 48 | |
| Sol.: | |
| 56. | Of the following reactions how many reactions are considered as oxidation reaction |
| | (a)  $\xrightarrow[\text{Ag}_2\text{O}]{\text{O}_2}$ (b)  $\xrightarrow[\Delta]{\text{KMnO}_4\text{OH}}$ (c)  $\xrightarrow{\text{LiAlH}_4}$ (d)  $\xrightarrow[\Delta]{\text{H}_2, \text{Ni}}$ (e)  $\xrightarrow{\text{CH}_3\text{CO}_2\text{H}}$ (f)  $\xrightarrow{\text{NaBH}_4}$ |
| Ans. 3 | |
| Sol.: | |
| 57. | Q quinhydrone electrode is sometimes used to find the pH of a solution. It is based on the following electrode reaction:  $\text{Quinone (s)} + 2\text{H}^+(\text{aq}) + 2\text{e}^- \rightleftharpoons \text{Hydroquinone (s)}$ Its standard electrode potential is 0.70 V. If in a particular solution, the electrode potential is found to be 0.58 V, the pH of the solution is |
| Ans. 2 | |
| Sol.: | |
| 58. | A solution containing 500 gr of a protein per litre is isotonic with a solution continuity 3.42 gr sucrose per litre the molar mass of protein is 5×10^x , hence $x = ?$ |
| Ans. 4 | |
| Sol.: | |
| 59. | The half-life of a reaction is halved as the initial concentration of the reactant is doubled. The order of reaction is |
| Ans. 2 | |

| | |
|-------|--|
| Sol.: | |
| 60. | Examine the structural formula of the following compounds and find out number of compounds which show higher rate of nucleophilic addition than        |
| Ans. | 3 |
| Sol.: | |

Single Correct Answer Type

| | |
|-------|--|
| 61. | The negation of the proposition: "If a number is divisible by 15, then it is divisible by 5 or 3. a) If a number is divisible by 15, then it is not divisible by 5 and 3 b) A number is divisible by 15, and it is not divisible by 5 and 3 c) A number is divisible by 15, then it is not divisible by 5 or 3 d) A number is not divisible by 15 or it is not divisible by 5 and 3 |
| Ans. | b |
| Sol.: | |
| 62. | A particle starts to travel from a point P on the curve $C_1 : z - 3 - 4i = 5$, where $ z $ is maximum. From P, the particle moves through an angle $\tan^{-1} \frac{3}{4}$ in anticlockwise direction on $ z - 3 - 4i = 5$ and reaches at point Q. From Q, it comes down parallel to imaginary axis by 2 units and reaches at point R. Complex number corresponding to point R in the Argand plane is a) $(3+5i)$ b) $(3+7i)$ c) $(3+8i)$ d) $(3+9i)$ |
| Ans. | b |
| Sol.: | |
| 63. | Let p and q be roots of the equation $x^2 - 2x + A = 0$ and let r and s be the roots of the equation $x^2 - 18x + B = 0$. If $p < q < r < s$ are in arithmetic progression. Then the values of A and B respectively are. a) $-5, 67$ b) $-3, 77$ c) $67, -5$ |

| | |
|-------|---|
| | d) 77, -3 |
| Ans. | b |
| Sol.: | |
| 64. | $f(\theta) = \begin{vmatrix} 1 + \sin^2 \theta & \cos^2 \theta & 4\sin 2\theta \\ \sin^2 \theta & 1 + \cos^2 \theta & 4\sin 2\theta \\ \sin^2 \theta & \cos^2 \theta & 1 + 4\sin 2\theta \end{vmatrix}$, then |
| a) | $f(\theta) = k$ must have solution if $k \in [-6, 6]$ |
| b) | $\lim_{\theta \rightarrow \infty} \frac{f(\theta)}{\theta}$ is equal to 1 |
| c) | $\lim_{\theta \rightarrow 0} \frac{8 - f'(\theta)}{\theta^2}$ is equal to 16 |
| d) | $\lim_{\theta \rightarrow \infty} \frac{f'(\theta)}{\theta}$ is equal to 1 |
| Ans. | c |
| Sol.: | |
| 65. | The number of values of k , for which the system equations $(k+1)x + 8y = 4k, kx + (k+3)y = 3k - 1$ has no solution, is |
| a) | 1 |
| b) | 2 |
| c) | 3 |
| d) | Infinite |
| Ans. | c |
| Sol.: | |
| 66. | The number of ways of forming an arrangement of 5 letters from the letters of the word "IITJEE" is |
| a) | 60 |
| b) | 96 |
| c) | 120 |
| d) | 180 |
| Ans. | d |
| Sol.: | |
| 67. | The coefficient of x^5 in the expansion of $(x^2 - x - 2)^5$ is |
| a) | -83 |
| b) | -82 |
| c) | -86 |
| d) | -81 |
| Ans. | d |
| Sol.: | |
| 68. | If $a_1, a_2, a_3, \dots, a_{4001}$ are terms of an AP such that $\frac{1}{a_1 a_2} + \frac{1}{a_2 a_3} + \dots + \frac{1}{a_{4000} a_{4001}} = 10$ and $a_2 + a_{4000} = 50$ then $ a_1 - a_{4001} $ is equal to |
| a) | 20 |
| b) | 30 |
| c) | 40 |
| d) | 10 |

| | |
|-------|---|
| Ans.b | |
| Sol.: | |
| 69. | The value of $\binom{100}{0}\binom{200}{150} + \binom{100}{1}\binom{200}{151} + \binom{100}{2}\binom{200}{152} + \dots + \binom{100}{50}\binom{200}{200}$ is $\binom{n}{r} = {}^n C_r$ |
| a) | $\binom{300}{50}$ |
| b) | $\binom{100}{50} \times \binom{200}{150}$ |
| c) | $\binom{100}{50}^2$ |
| d) | $\binom{200}{100}^2$ |
| Ans.a | |
| Sol.: | |
| 70. | ABC is an isosceles triangle inscribed in a circle of radius of r, If AB = AC and h is the attitude from A to BC and if 'P' is the perimeter of triangle ABC whose area is Δ , then, $Lt_{h \rightarrow 0} \frac{\Delta}{P^3} =$ |
| a) | $\frac{1}{16r}$ |
| b) | $\frac{1}{32r}$ |
| c) | $\frac{1}{64r}$ |
| d) | $\frac{1}{128r}$ |
| Ans.d | |
| Sol.: | |
| 71. | If $y = \tan^{-1} \left[\frac{3+2\log x}{1-6\log x} \right] + \tan^{-1} \left[\frac{\log \left(\frac{e}{x^2} \right)}{\log(ex^2)} \right]$, then the value of $\frac{d^2y}{dx^2}$ is |
| a) | -1 |
| b) | 1 |
| c) | 0 |
| d) | $\tan^{-1} \{(\log x)^n\}$ |
| Ans.c | |
| Sol.: | |
| 72. | The tangent and normal at the point P(4, 4) to the parabola, $y^2 = 4x$ intersect the x-axis at the points Q and R respectively. Then the circumcentre of the ΔPQR is |
| a) | (2, 0) |
| b) | (2, 1) |
| c) | (1, 0) |
| d) | (1, 2) |

| | |
|-------|--|
| Ans.c | |
| Sol.: | |
| 73. | Let f be a function defined by $f(x) = \begin{cases} \frac{\tan x}{x}, & x \neq 0 \\ 1, & x = 0 \end{cases}$ then f has |
| a) | minimum at $x = 0$ |
| b) | maximum at $x = 0$ |
| c) | minimum at $x = \frac{\pi}{4}$ |
| d) | maximum at $x = \frac{\pi}{4}$ |
| Ans.a | |
| Sol.: | |
| 74. | The integral $\int \frac{3x^{13} + 2x^{11}}{(2x^4 + 3x^2 + 1)^4} dx$ is equal to : (where C is a constant of integration): |
| a) | $\frac{x^4}{(2x^4 + 3x^2 + 1)^3} + C$ |
| b) | $\frac{x^{12}}{6(2x^4 + 3x^2 + 1)^3} + C$ |
| c) | $\frac{x^4}{6(2x^4 + 3x^2 + 1)^3} + C$ |
| d) | $\frac{x^{12}}{(2x^4 + 3x^2 + 1)^3} + C$ |
| Ans.b | |
| Sol.: | |
| 75. | $\int_0^a \ln(\cot a + \tan x) dx$, where $a \in \left(0, \frac{\pi}{2}\right)$ is |
| a) | $a \ln(\sin a)$ |
| b) | $-a \ln(\sin a)$ |
| c) | $-a \ln(\cos a)$ |
| d) | none of these |
| Ans.b | |
| Sol.: | |
| 76. | The area of the region in the xy -plane defined by the inequalities $x - 2y^2 \geq 0$, $1 - x - y \geq 0$ is |
| a) | $\frac{1}{2}$ |
| b) | $\frac{1}{3}$ |
| c) | $\frac{1}{4}$ |
| d) | $\frac{7}{12}$ |
| Ans.d | |

| | |
|--------|---|
| Sol.: | |
| 77. | The solution of the differential equation $2x^3ydy + (1-y^2)(x^2y^2+y^2-1)dx = 0$ [Where c is a constant] |
| a) | $x^2y^2 = (cx+1)(1-y^2)$ |
| b) | $x^2y^2 = (cx+1)(1+y^2)$ |
| c) | $x^2y^2 = (cx-1)(1-y^2)$ |
| d) | none of these |
| Ans. c | |
| Sol.: | |
| 78. | A straight line L through the origin meets the lines $x+y=1$ and $x+y=3$ at P and Q respectively. Through P and Q two straight lines L_1 and L_2 are drawn, parallel to $2x-y=5$ and $3x+y=5$ respectively. Lines L_1 and L_2 intersected at R. Then the locus of R is the line |
| a) | $x+3y+5=0$ |
| b) | $x-3y-5=0$ |
| c) | $x-3y+5=0$ |
| d) | $x+3y-5=0$ |
| Ans. c | |
| Sol.: | |
| 79. | Vertices of a variable triangle are $(3,4);(5\cos\theta,5\sin\theta)$ and $(5\sin\theta,-5\cos\theta)$ where θ is a parameter then the locus of its orthocentre is |
| a) | $\left(\frac{x-3}{5}\right)^2 + \left(\frac{y-4}{5}\right)^2 = 1$ |
| b) | $(x+y-7)^2 + (x-y+1)^2 = 100$ |
| c) | $(x-3)^2 + (y-4)^2 = 200$ |
| d) | $(x-y-7)^2 + (x+y+1)^2 = 10$ |
| Ans. b | |
| Sol.: | |
| 80. | From a point R(5,8) two tangents RP and RQ are drawn to a given circle S = 0 whose radius is 5. If circumcentre of the triangle PQR is (2,3), then the equation of circle S = 0 is |
| a) | $x^2 + y^2 + 2x + 4y - 20 = 0$ |
| b) | $x^2 + y^2 + x + 2y - 10 = 0$ |
| c) | $x^2 + y^2 - x - 2y - 20 = 0$ |
| d) | $x^2 + y^2 - 4x - 6y - 21 = 0$ |
| Ans. a | |
| Sol.: | |

Integer Answer Type

| | |
|--------|--|
| 81. | Locus of the mid points of the chords of the hyperbola $x^2 - y^2 = a^2$ that touch the parabola $y^2 = 4ax$ is $\lambda y^2 (x-a) = x^3 \mu$, $\lambda, \mu \in \mathbb{R}^+$ then $\frac{\lambda}{\mu}$ is _____. |
| Ans. 1 | |
| Sol.: | |

| | |
|--------|--|
| 82. | If the curves $\frac{x^2}{4} + y^2 = 1$ and $\frac{x^2}{a^2} + y^2 = 1$ for suitable value of a cut on four concyclic points, then find the radius of the smallest circle passing through these 4 points |
| Ans.1 | |
| Sol.: | |
| 83. | Consider the planes $S_1 : 2x - y + z = 5$, $S_2 : x + 2y - z = 4$ having normals N_1 and N_2 respectively. $P(2, -1, 0)$ and $Q(1, 1, -1)$ are points on S_1 and S_2 respectively. Let L_1 be the line passing through P and parallel to N_1 , L_2 be the line passing through Q and parallel to N_2 . The shortest distance between L_1 and L_2 is λ then $\sqrt{35}\lambda$ is _____ |
| Ans.2 | |
| Sol.: | |
| 84. | \vec{a} and \vec{b} are non zero non-collinear vectors such that $ \vec{a} =2$, $\vec{a} \cdot \vec{b}=1$ and angle between \vec{a} and \vec{b} is $\frac{\pi}{3}$. If \vec{r} is any vector satisfying $\vec{r} \cdot \vec{a}=2$, $\vec{r} \cdot \vec{b}=8$, $(\vec{r} + 2\vec{a} - 10\vec{b}) \cdot (\vec{a} \times \vec{b})=6$ and is equal $\vec{r} + 2\vec{a} - 10\vec{b} = \lambda(\vec{a} \times \vec{b})$ then $\lambda =$ |
| Ans.2 | |
| Sol.: | |
| 85. | The position vectors of the vertices A, B, C of a tetrahedron ABCD are $\hat{i} + \hat{j} + \hat{k}$, \hat{i} and $3\hat{i}$ respectively and the altitude from the vertex D to the opposite face ABC meets the face at E. If the length of the edge AD is 4 and the volume of the tetrahedron is $\frac{2\sqrt{2}}{3}$, then the length of DE is |
| Ans.2 | |
| Sol.: | |
| 86. | The probability of a bomb hitting a bridge is $\frac{1}{2}$ and two direct hits are needed to destroy it. The least number of bombs required so that the probability of the bridge being destroyed is greater than 0.9 is |
| Ans.7 | |
| Sol.: | |
| 87. | In a knockout tournament 16 equally skilled players namely P_1, P_2, \dots, P_{16} are participating. In each round players are divided in pairs at random and winner from each pair moves in the next round. If P_2 reaches the semifinal, then the probability that P_1 will win the tournament is $\frac{\lambda}{\mu}$ (where λ, μ are co prime numbers), find $\lambda + \mu$. |
| Ans.21 | |
| Sol.: | |
| 88. | The number of solutions of the equation $4^{\sin 2x + 2\cos^2 x} + 4^{1+2\sin^2 x - \sin 2x} = 65$ in $\left[0, \frac{\pi}{2}\right]$ is |
| Ans.1 | |
| Sol.: | |
| 89. | ABC is a triangular park with $AB = AC = 100$ cm. A clock tower is situated at |

| | |
|-------|--|
| | the midpoint of BC. The angles of elevation of the top of the tower at A and B are $\text{Cot}^{-1}3.2$ and $\text{Cosec}^{-1}2.6$. The height of the tower is ____ mt. |
| Ans. | 25 |
| Sol.: | |
| 90. | 90 students take mathematics, 72 take science in class of 120 students. If 10 take neither Mathematics nor science then number of students who take both the subjects is |
| Ans. | 52 |
| Sol.: | |