Chapter DM:II (continued)

II. Cluster Analysis

- □ Cluster Analysis Basics
- □ Hierarchical Cluster Analysis
- □ Iterative Cluster Analysis
- □ Density-Based Cluster Analysis
- Cluster Evaluation
- Constrained Cluster Analysis

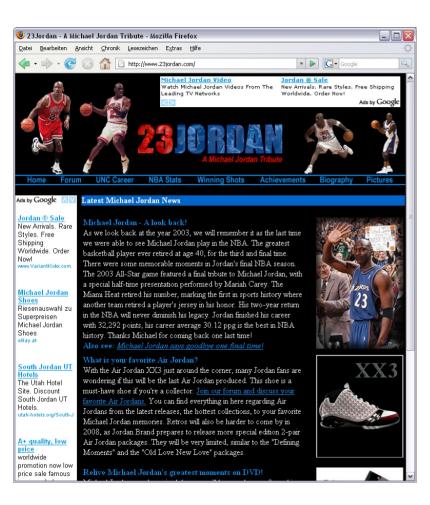
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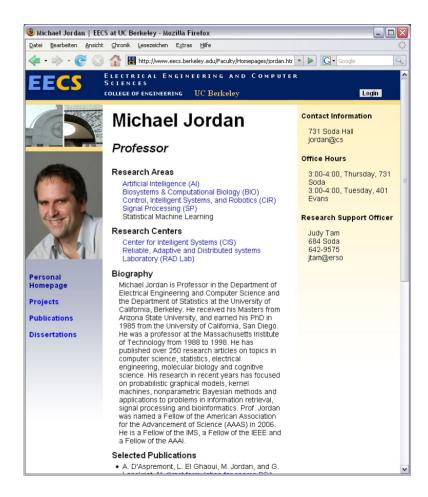
Person Resolution Task



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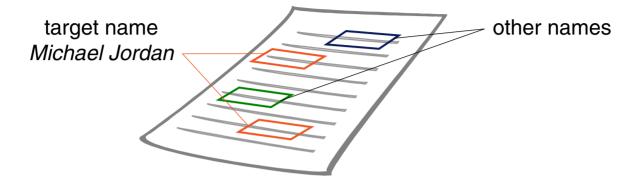
Person Resolution Task





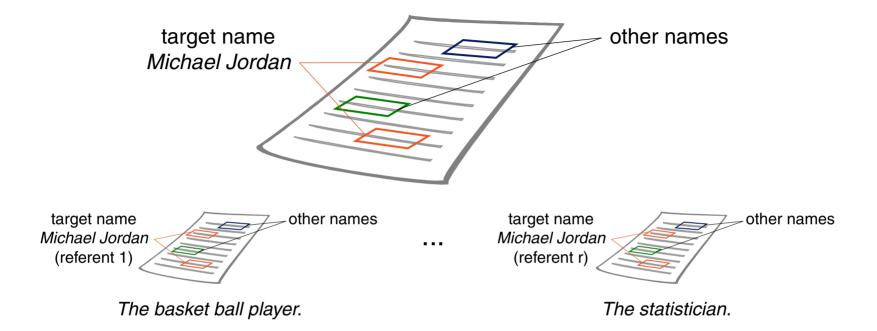
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Person Resolution Task



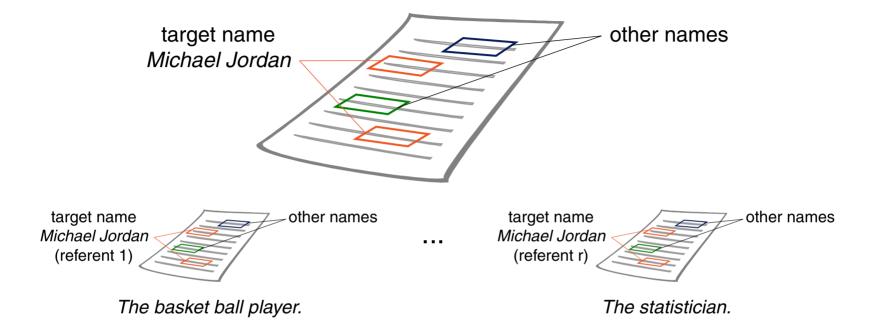
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Person Resolution Task



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Person Resolution Task



Multi-document resolution task:

Names, Target names: $N = \{n_1, \dots, n_l\}, \quad T \subset N$

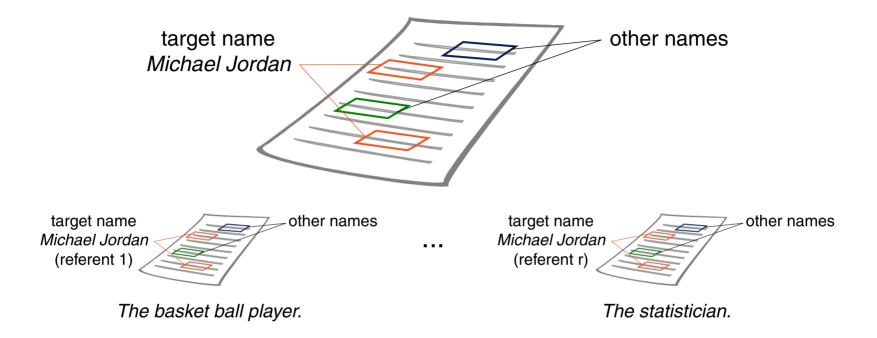
Referents: $R = \{r_1, \dots, r_m\}, \quad \tau : R \to T, \ |R| \gg |T|$

Documents: $D = \{d_1, \dots, d_n\}, \quad \nu : D \to \mathcal{P}(N), \quad |\nu(d_i) \cap T| = 1$

A solution: $\gamma: D \to R$, s.t. $\tau(\gamma(d_i)) \in \nu(d_i)$

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Person Resolution Task



□ Facts about the Spock data mining challenge:

Target names: |T| = 44

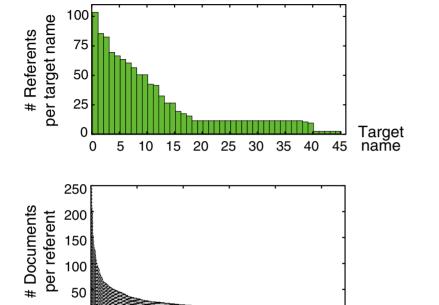
Referents: |R| = 1101

Documents: $|D_{train}| = 27\,000$ (labeled ≈ 2.3 GB)

 $|D_{\textit{test}}| = 75\,000$ (unlabeled ≈ 7.8 GB)

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Person Resolution Task



- □ up to 105 referents for a single target name
- about 25 referents
 on average per target name

 about 23 documents on average per referent

□ Facts about the Spock data mining challenge:

600

Target names: |T| = 44

200

Referents: |R| = 1101

400

Documents: $|D_{train}| = 27\,000$ (labeled ≈ 2.3 GB)

800

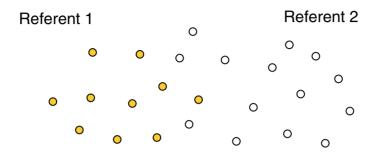
1000

 $|D_{\textit{test}}| = 75\,000$ (unlabeled pprox 7.8 GB)

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Referent

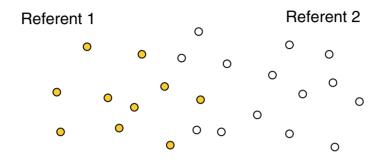
Applied to Multi-Document Resolution



- 1. Model similarities → new and established retrieval models:
 - global and context-based vector space models
 - explicit semantic analysis
 - ontology alignment
- 2. Learn class memberships (supervised) → logistic regression
- 3. Find equivalence classes (unsupervised) → cluster analysis:
 - (a) adaptive graph thinning
 - (b) multiple, density-based cluster analysis
 - (c) clustering selection by expected density maximization

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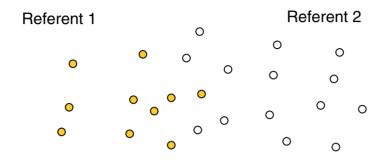
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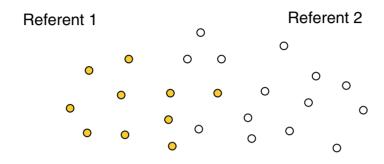
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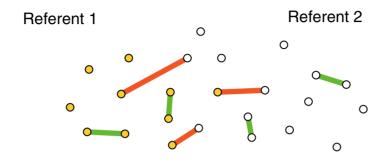
Applied to Multi-Document Resolution



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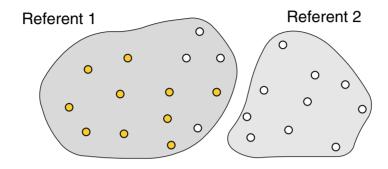
Applied to Multi-Document Resolution



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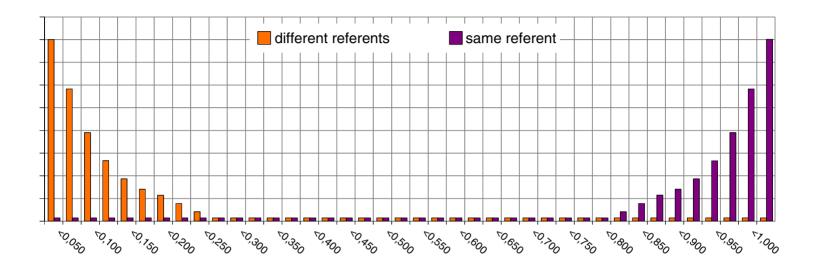
Applied to Multi-Document Resolution



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Idealized Class Membership Distribution over Similarities



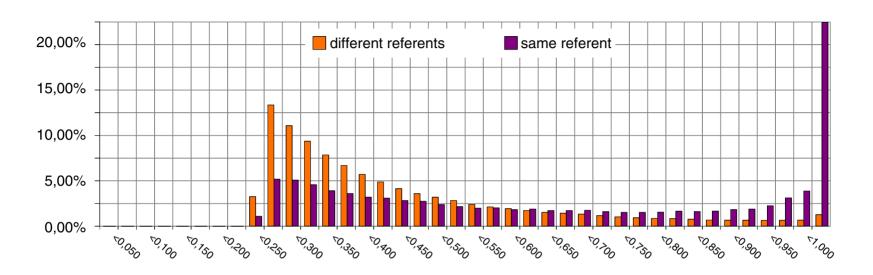
Similarity distributions for document pairs from different referents and same referent.

Logistic regression task:

- □ sample size: 400 000
- \square classes imbalance: non-target class : target class \approx 25:1
- items are drawn uniformly distributed wrt. non-targets and targets
- items are uniformly distributed over the groups of target names

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Membership Distribution under tf-idf Vector Space Model



Model details:

□ corpus size: 25 000 documents

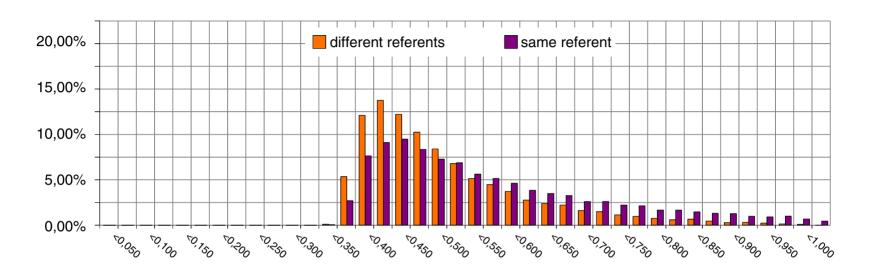
□ dictionary size: 1,2 Mio terms

□ stopwords number: 850

□ stopword volume: 36%

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Membership Distribution under Context-Based Vector Space Model



Model details:

□ corpus size: 25 000 documents

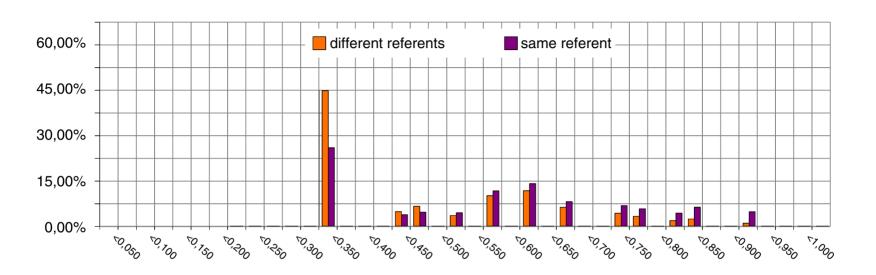
☐ dictionary size: 1,2 Mio terms

□ stopwords number: 850

□ stopword volume: 36%

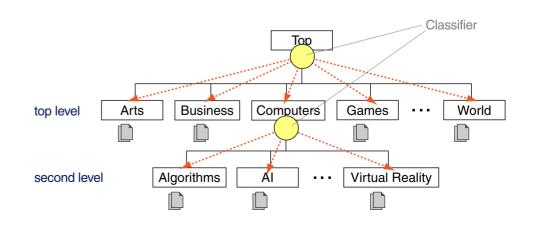
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Membership Distribution under Ontology Alignment Model



Model details:

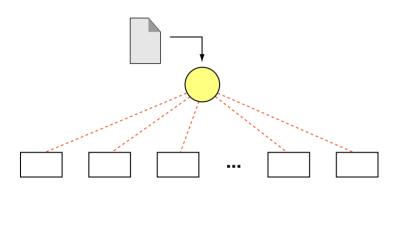
- DMOZ open directory project
- → > 5 million documents
- □ 12 top-level categories
- □ 31 second level categories
- ☐ ML: hierarchical Bayes
- □ training set: 100 000 pages



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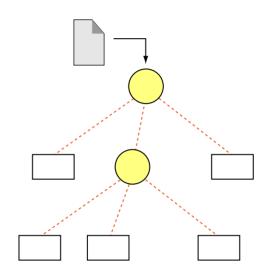
In-Depth: Multi-Class Hierarchical Classification

Flat (big-bang) classification



- + simple realization
- loss of discriminative power with increasing number of categories

Hierarchical (top-down) classification



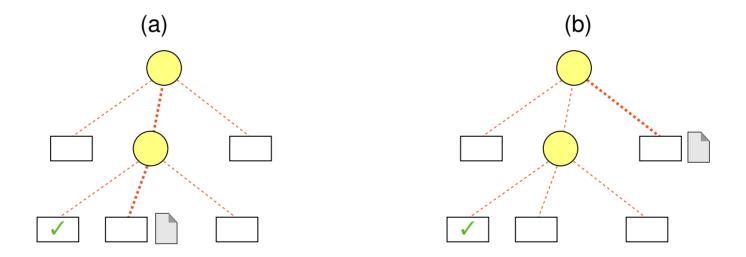
- + specialized classifiers (divide and conquer)
- misclassification at higher levels can never become repaired

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In-Depth: Multi-Class Hierarchical Classification

State of the art of effectiveness analyses:

- 1. independence assumption between categories
- 2. neglection of both hierarchical structure and degree of misclassification



Improvements:

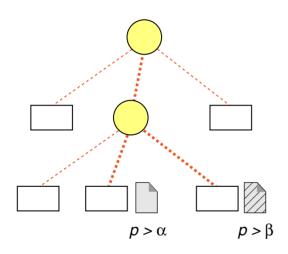
- \supset Consider similarity $\varphi(C_i, C_j)$ between correct and wrong category.
- \Box Consider graph distance $d(C_i, C_i)$ between correct and wrong category.

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In-Depth: Multi-Class Hierarchical Classification

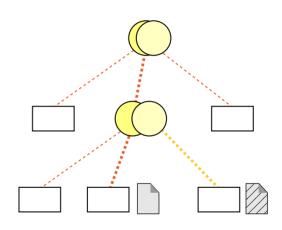
Improvements continued:

Multi-label (multi path) classification



- traverse more than one path and return all labels
- employ probabilistic classifiers with a threshold: split a path or not

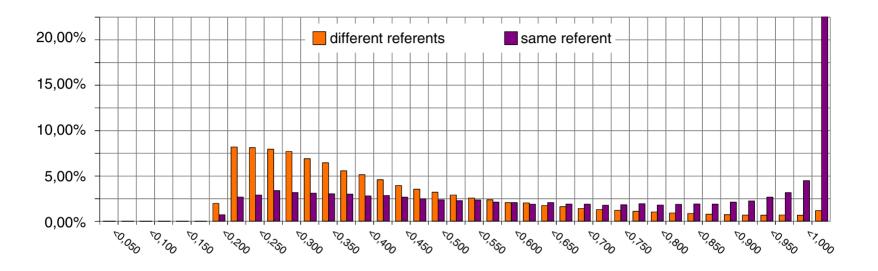
Multi-classifier (ensemble) classification



- classification result is a majority decision
- employ different classifier (different types or differently parameterized)

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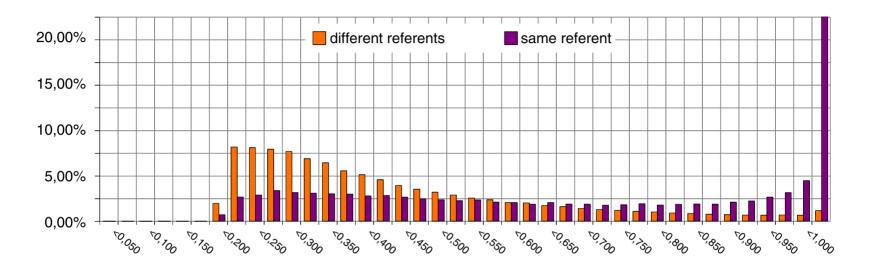
Membership Distribution under Optimized Retrieval Model Combination



Retrieval Model	$\overline{F_{1/3}}$ -Measure
tf-idf vector space	0.39
context-based vector space	0.32
ESA Wikipedia persons	0.30
phrase structure grammar	0.17
ontology alignment	0.15
optimized combination	0.42

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Membership Distribution under Optimized Retrieval Model Combination

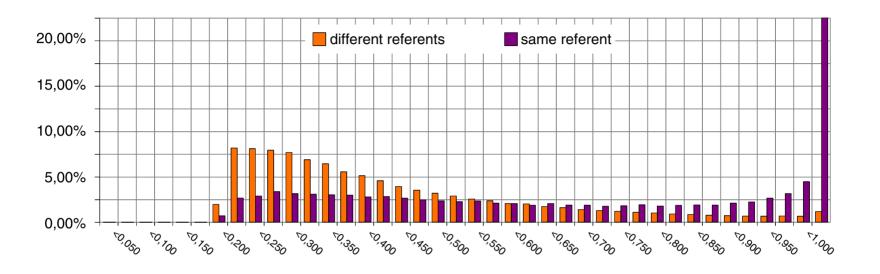


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tfidf vector space	0.39
context-based vector space	0.32
ESA Wikipedia persons	0.30
phrase structure grammar	0.17
ontology alignment	0.15
optimized combination	0.42

Referent 1		Refer	Referent 2		Referent m	
0	0	0	0		0	0
0	0	0	0	•••	0	0
0	•	0	0		0	0

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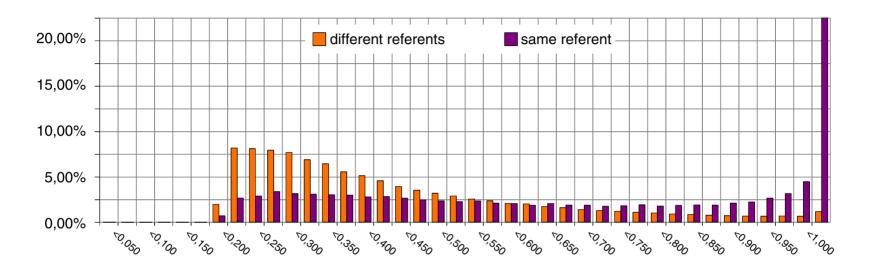
Membership Distribution under Optimized Retrieval Model Combination



		Referent 1		Referent 2		Referent m		
Retrieval Model	$F_{1/3}$ -Measure	0	0	0	0		0	0
tfidf vector space	0.39	0	0	0	0		0	0
context-based vector space	0.32	•	0	0	0		0	0
ESA Wikipedia persons	0.30							
phrase structure grammar	0.17	_	_	_			_	
ontology alignment	0.15	0	0	0	0		0	0
		0	0	0	0	•••	0	0
optimized combination	0.42	0	0	0	0		0	0

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Membership Distribution under Optimized Retrieval Model Combination

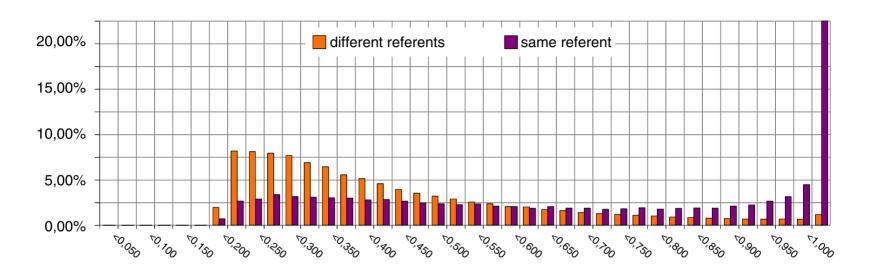


Retrieval Model	$F_{1/3}$ -Measure
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optimized combination	0.42

Referent 1		Refer	Referent 2		Referent m	
0	•	0	0		0	0
0	0	0	0		0	0
0	•	0	0		0	0
	<i></i> ³		?			?

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Membership Distribution under Optimized Retrieval Model Combination



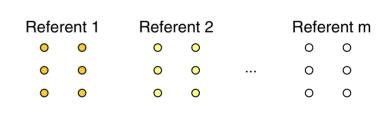
In the example:

 \Box precision = 0.4

□ recall = 0.43

 \Box $F_{1/3} = 0.41$

(if false negatives are uniformly distributed)



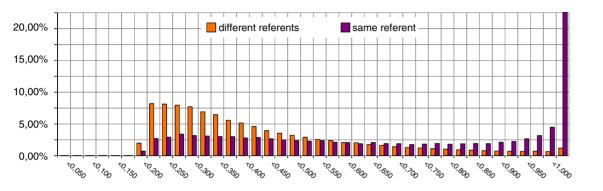




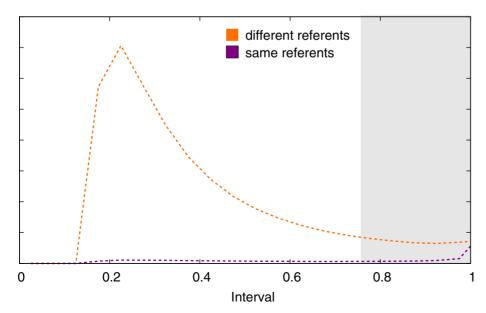
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In-Depth: Analysis of Classifier Effectiveness



Consideration of imbalance:



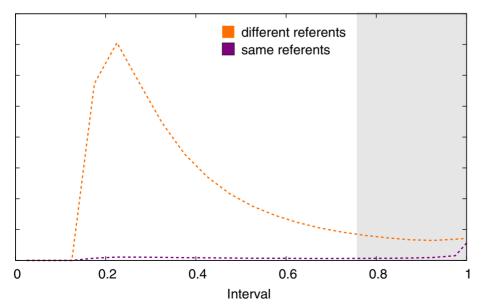
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In-Depth: Analysis of Classifier Effectiveness

- □ class imbalance factor (*CIF*) of 25
- \Rightarrow precision in interval [0.725; 1] for edges between same referents: ≈ 0.17

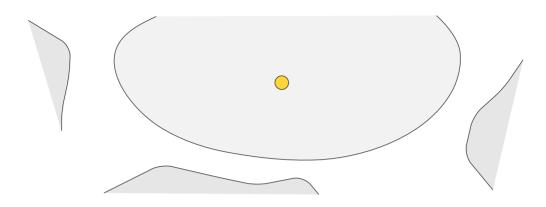
How can $F_{1/3}$ = 0.42 be achieved via cluster analysis?

Consideration of imbalance:



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In-Depth: Analysis of Classifier Effectiveness



Assumption: uniform distribution of referents over documents (here: 25 clusters with |C|=23)

- \Rightarrow | TP| true 1-similarities per cluster (here: 130 @ threshold 0.725)
- $\Rightarrow \frac{|TP|}{|C|}$ degree of true positives per node (here: 11)
- $\Rightarrow |TP|(\frac{1}{precision} 1)$ false 1-similarities per cluster (here: 760)

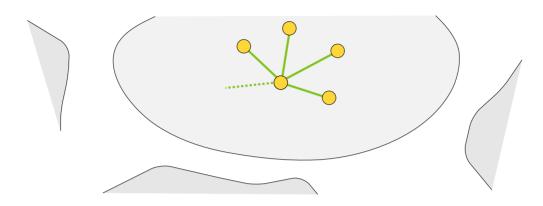
Density-based cluster analysis: effective false positives, FP*, connect to same cluster

- \Rightarrow analyze $P(|FP^*| > k \mid D, R_{iid})$ (here: $E(|FP^*|) = 2.7$)
- \Rightarrow edge tie factor (*ETF*) specifies the excess of true positives until tie (here: 3...5)

$$ETF = \frac{|TP|}{|C| \cdot E(|FP^*|)},$$
 effective precision = $precision \cdot \frac{CIF}{ETF}$

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In-Depth: Analysis of Classifier Effectiveness



Assumption: uniform distribution of referents over documents (here: 25 clusters with |C|=23)

- \Rightarrow |TP| true 1-similarities per cluster (here: 130 @ threshold 0.725)
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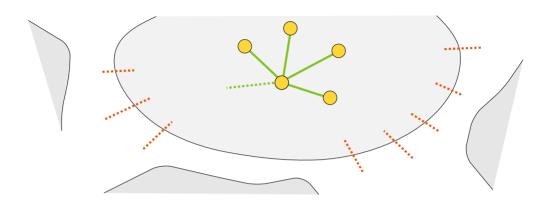
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$$ETF = \frac{|TP|}{|C| \cdot E(|FP^*|)},$$
 effective precision = $precision \cdot \frac{CIF}{ETF}$

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In-Depth: Analysis of Classifier Effectiveness



Assumption: uniform distribution of referents over documents (here: 25 clusters with |C|=23)

- \Rightarrow |TP| true 1-similarities per cluster (here: 130 @ threshold 0.725)
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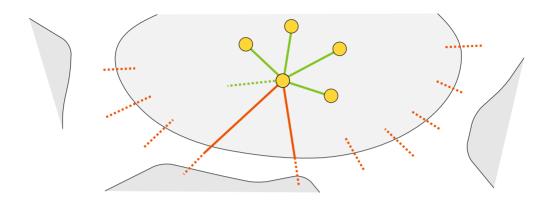
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$$ETF = \frac{|TP|}{|C| \cdot E(|FP^*|)},$$
 effective precision = $precision \cdot \frac{CIF}{ETF}$

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In-Depth: Analysis of Classifier Effectiveness



Assumption: uniform distribution of referents over documents (here: 25 clusters with $\left|C\right|=23$)

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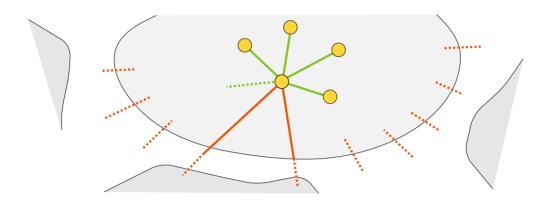
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- \Rightarrow edge tie factor (*ETF*) specifies the excess of true positives until tie (here: 3...5)

$$ETF = \frac{|TP|}{|C| \cdot E(|FP^*|)},$$
 effective precision = $precision \cdot \frac{CIF}{ETF}$

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In-Depth: Analysis of Classifier Effectiveness



Assumption: uniform distribution of referents over documents (here: 25 clusters with $\left|C\right|=23$)

- \Rightarrow |TP| true 1-similarities per cluster (here: 130 @ threshold 0.725)
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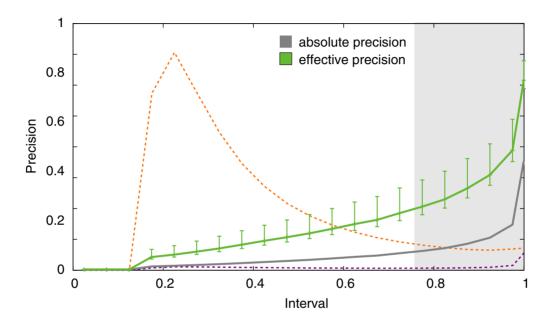
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$$ETF = \frac{|TP|}{|C| \cdot E(|FP^*|)},$$
 effective precision = precision $\cdot \frac{CIF}{ETF}$

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In-Depth: Analysis of Classifier Effectiveness



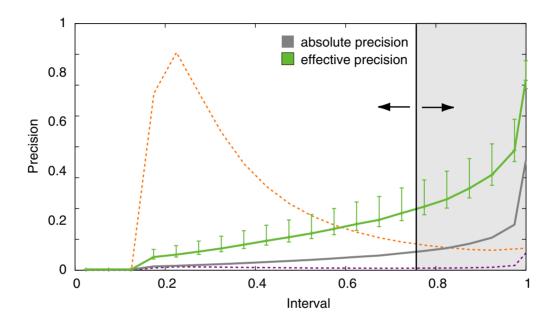
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$$ETF = \frac{|TP|}{|C| \cdot E(|FP^*|)},$$
 effective precision = $precision \cdot \frac{CIF}{ETF}$

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In-Depth: Analysis of Classifier Effectiveness



Determine optimum similarity threshold for class-membership function:

$$\theta^* = \operatorname*{argmax}\{\frac{1+\alpha}{\underbrace{\mathit{ETF}}_{\mathit{precision}_{\theta}\cdot\mathit{CIF}} + \frac{\alpha}{\mathit{recall}_{\theta}}}\}$$

 θ^* considers co-variate shift, introduces model formation bias and sample selection bias.

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Model Selection: Our Risk Minimization Strategy

Retrieval Model	$\overline{F_{1/3}}$ -Measure
tf-idf vector space	0.39
context-based vector space	0.32
ESA Wikipedia persons	0.30
phrase structure grammar	0.17
ontology alignment	0.15
optimized combination	0.42
Ensemble cluster analysis	0.40

Ensemble cluster analysis: higher bias, better generalization.

- (1) Do we speculate on a better fit for D_{test} ?
- (2) Do we expect a significant covariate shift, more noise, etc. in D_{test} ?

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Recap

- 1. Multi-document resolution can be tackled with constrained cluster analysis.
- 2. Constraints are derived from labeled examples.
- 3. Class membership function ties constraints to multiple retrieval models.
- 4. Advanced density-based clustering technology is key.

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References

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Unsupervised Discrimination of Person Names in Web	Contexts. [T. Pedersen, A. Kulkarni. CICLing 2007]
3 3	sen. Dissertation, Paderborn University, 2007

☐ GRAPE: A System for Disambiguating and Tagging People Names in Web Search.

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[L. Jiang, W. Shen, J. Wang, N. An. WWW 2010]

[B. Stein, S. Meyer zu Eissen. I-KNOW 2008]

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