Chapter S:III

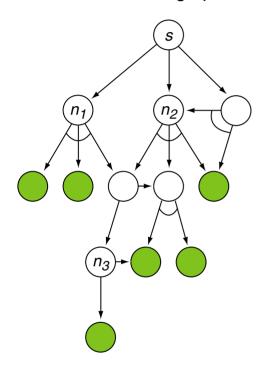
III. Informed Search

- □ Best-First Search
- □ Best-First Search for State-Space Graphs
- □ Cost Functions for State-Space Graphs
- □ Evaluation of State-Space Graphs
- □ Algorithm A*
- □ BF* Variants
- Hybrid Strategies
- □ Best-First Search for AND-OR Graphs
- Relation between GBF and BF
- Cost Functions for AND-OR Graphs
- □ Evaluation of AND-OR Graphs
- □ Relation to Dynamic Programming

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Illustration of Solution Graphs and Solution Bases

Problem-reduction graph:

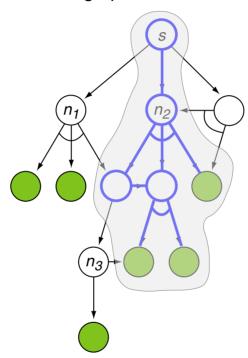


Solved rest problem

Illustration of Solution Graphs and Solution Bases

Problem-reduction graph:

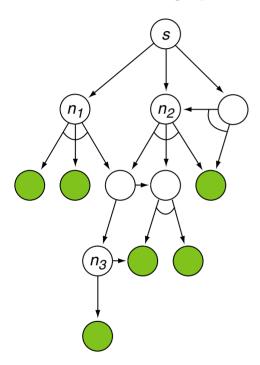
Solution graph for node *s*:



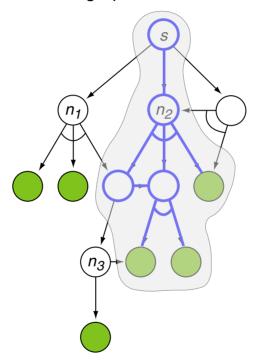
Solved rest problem

Illustration of Solution Graphs and Solution Bases

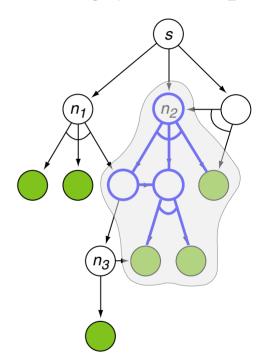
Problem-reduction graph:



Solution graph for node *s*:



Solution graph for node n_2 :

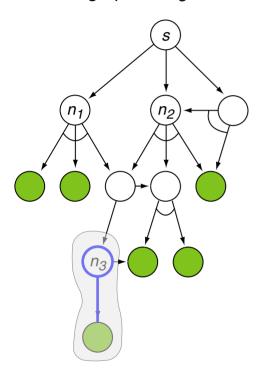


Solved rest problem

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Illustration of Solution Graphs and Solution Bases (continued)

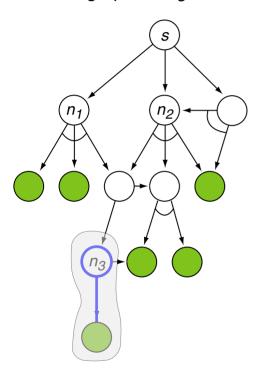
Solution graph for n_3 :



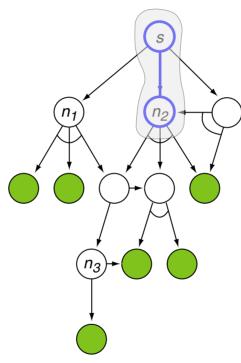
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Illustration of Solution Graphs and Solution Bases (continued)

Solution graph for n_3 :



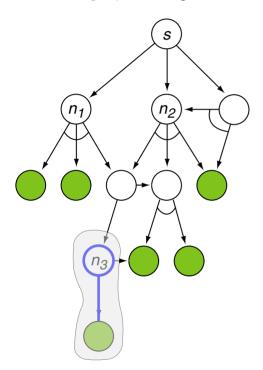
Solution base for s:



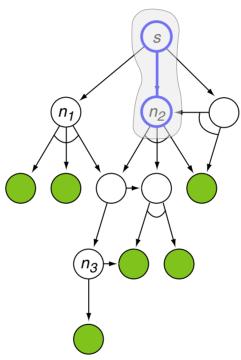
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Illustration of Solution Graphs and Solution Bases (continued)

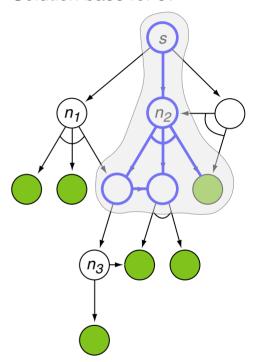
Solution graph for n_3 :



Solution base for s:



Solution base for s:



Compare: Solution paths and solution bases in a state-space graphs.

Principles of Algorithm GBF [BF principles]

Properties of Problem-Reduction Graphs

- 1. *G* is an implicitly defined directed AND-OR graph.
- 2. *G* is acyclic and locally finite.

- \Box the underlying problem-reduction graph G is assumed to be acyclic,
- \Box f_1 evaluates solution bases H,
- \square a most promising solution base minimizes f_1 ,
- a most promising solution base is searched among all solution bases maintained by GBF,
- \Box solution bases maintained by GBF are solution bases for s in the explicit part G_e of G with tip nodes in OPEN,
- \Box f_2 returns a most informative node in a solution base.

Principles of Algorithm GBF [BF principles]

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Remarks:

- \Box Again, G denotes the explored part of the search space graph.
- When searching AND-OR graphs with the algorithm GBF, only solution bases H need to be considered that have not been considered so far. I.e., only solution bases H with leaf nodes that are goal nodes or nodes in OPEN and inner nodes in CLOSED are considered.
- ☐ In an AND-OR graph, a node may be part of several solution bases.
- \Box Usually, the evaluation function $f_1(H)$ is based on a heuristic h(n).
- \Box h(n) estimates the optimum cost of solution graphs for the rest problem associated with a node n. Ideally, h(n) should consider the probability of the solvability of the problem at node n.
- \Box Compared to $f_2(H)$, the evaluation function $f_1(H)$ is usually more important.
- □ Searching AND-OR graphs with cycles is intricate. Note that the algorithms presented by Martelli and Montanari [1973, 1978], Nilsson [1980], or Pearl [1984] presume graphs without cycles. In the following, we will restrict to acyclic graphs as well.
- ☐ In the context of Markov Decision Processes, MDP, and advanced planning algorithms researchers have dealt with AND-OR graphs that contain cycles. [Bonet/Geffner 2005]

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Algorithm: GBF

Input: s. Start node representing the initial problem.

successors(n). Returns the successors of node n.

 $is_solved(n)$. Predicate that is *True* if n is labeled "solved" or n is a goal node.

 $f_1(H)$. Evaluation function for solution bases.

 $f_2(H)$. Selection function for OPEN-nodes in a solution base.

Output: A solution graph or the symbol *Fail*.

```
GBF(s, successors, is_solved, f_1, f_2)

1. insert(s, OPEN); add_node(s, G_e); // G_e is the explored part of G.

2. LOOP

3. IF (OPEN = \emptyset) THEN RETURN(Fail);

4.a

4.b
```

// Is n' goal node

?

6. ENDLOOP

```
GBF(s, successors, is_solved, f_1, f_2)

1. insert(s, OPEN); add_node(s, G_e); // G_e is the explored part of G.

2. LOOP

3. IF (OPEN = \emptyset) THEN RETURN(Fail);

4.a H = min\_solution\_base(s, G_e, f_1); // Find most prom. sol. base in G_e.

4.b n = f_2(H); // Find most informative non-goal node in H.

remove(n, OPEN); push(n, CLOSED);

5.
```

// Is n' goal node

7

6. ENDLOOP

ENDLOOP

```
GBF(s, successors, is_solved, f_1, f_2)

1. insert(s, OPEN); add_node(s, G_e); // G_e is the explored part of G.

2. LOOP

3. IF (OPEN = \emptyset) THEN RETURN(Fail);

4.a H = min\_solution\_base(s, G_e, f_1); // Find most prom. sol. base in G_e.

4.b n = f_2(H); // Find most informative non-goal node in H.

remove(n, OPEN); push(n, CLOSED);

5. FOREACH n' IN successors(n) DO
```

```
insert(n', \mathtt{OPEN}); \;\; add\_node(n', G_e); add\_backpointer(n', n); \mathtt{IF} \;\; is\_solved(n') \;\; // \;\; \mathtt{Is} \;\; n' \;\; \mathtt{goal} \;\; \mathtt{node} \mathtt{THEN} \qquad \qquad propagate\_label(n'); \mathtt{IF} \;\; is\_solved(s) \;\; \mathtt{THEN} \;\; \mathtt{RETURN}(compute\_solution\_graph(G_e)); \mathtt{ENDDO} \mathtt{ENDDO}
```

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Best-First Search for AND-OR Graphs [BF, BF*, GBF*]

```
GBF(s, successors, is_solved, f_1, f_2)
  1. insert(s, OPEN); add\_node(s, G_e); // G_e is the explored part of G.
  2.
     LOOP
     IF (OPEN = \emptyset) THEN RETURN(Fail);
 3.
 4.a H = min\_solution\_base(s, G_e, f_1); // Find most prom. sol. base in G_e.
 4.b n = f_2(H); // Find most informative non-goal node in H.
       remove(n, OPEN); push(n, CLOSED);
       FOREACH n' IN successors(n) DO
 5.
         IF ( n' \in OPEN OR n' \in CLOSED ) // Instance of n' seen before?
         THEN // Use old instance of n' instead.
           n' = retrieve(n', OPEN \cup CLOSED);
         ELSE //n' encodes an instance of a new state.
           insert(n', OPEN); add\_node(n', G_e);
         ENDIF
         add_backpointer(n', n);
         IF is\_solved(n') // Is n' goal node or labeled solvable?
         THEN
           propagate\_label(n');
           IF is\_solved(s) THEN RETURN(compute\_solution\_graph(G_e));
         ENDIF
       ENDDO
  6. ENDLOOP
```

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Remarks:

□ Finding dead ends can be handled in the same way as finding goal nodes.

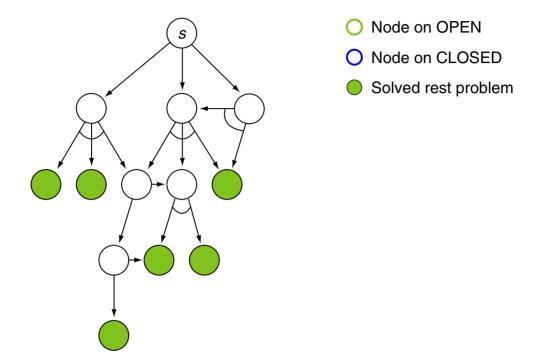
```
IF ( \perp (n') OR is\_labeled(n') ) // Is n' unsolvable? THEN propagate\_label(n'); \text{ IF } is\_unsolvable(s) \text{ THEN RETURN}(\textit{Fail}); \\ \text{ENDIF}
```

- \Box The expansion of nodes in G can be implemented with or without occurrence check:
 - (a) With occurrence check. If an already existing rest problem is encountered, only an additional link is added to G_e . As a consequence, G_e is a subgraph of the underlying search space graph G.
 - (b) Without occurrence check. Each successor becomes a new node, irrespective of duplicate rest problems. As a consequence, G_e corresponds to an AND-OR tree that can be considered as an unfolding of the underlying search space graph G.

Therefore, using an occurrence check or not can be seen as different ways of modeling a problem.

The construction of solution bases depends strongly on the structure of the evaluation function f_1 . In the general case, an individual construction of all possible solution bases plus an individual computation of the f_1 -values cannot be avoided. However, if f_1 can be stated in a recursive manner using specific functions, computation of the minimum f_1 value and computation of a most promising solution base can be done very efficiently.

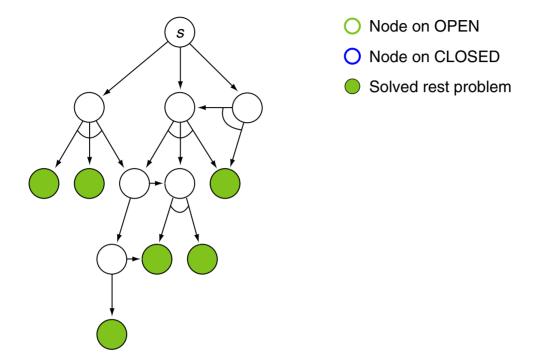
Illustration of GBF



The underlying AND-OR graph of the following GBF illustration.

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Illustration of GBF



- $f_1(H)$ Evaluates solution bases H in regard to their edge count. Answers the question: What does the solution associated with H cost?
- $f_2(H)$ Returns the node with a most expensive rest problem in H. Answers the question: What node to expand next?
 - h(n) Estimates the number of edges for the rest problem at node n.

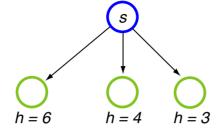
Remarks:

- \Box The evaluation function $f_1(H)$ estimates the total number of edges of a solution graph extending solution base H. Obviously, $f_1(H)$ will be based on the heuristic h(n).
- \square Rationale for f_1 . Searching the smallest solution may quickly lead to a first solution graph. Keyword: *Small-is-Quick Principle*
- Rationale for f_2 . A possible estimation error of h, which allegedly claims an unsolvable rest problem as a solvable one, should be detected earliest. Since it is reasonable to assume that the estimation error is proportional to the cost estimate, we pick a most expensive rest problem first.
- Recall that the complete AND-OR graph is neither given nor manageable for real-world problems.

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Illustration of GBF (continued)

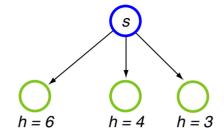
1. *s* is expanded and moved to CLOSED.



- Node on OPEN
- Node on CLOSED
- Solved rest problem

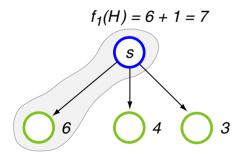
Illustration of GBF (continued)

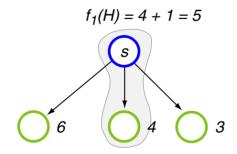
1. s is expanded and moved to CLOSED.

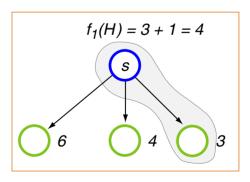


- Node on OPEN
- Node on CLOSED
- Solved rest problem

Possible solution bases:



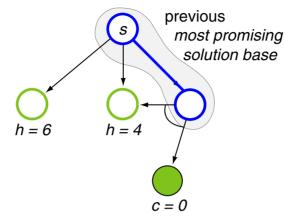




Most promising solution base H

Illustration of GBF (continued)

2. Expansion of the node $n \in (\mathsf{OPEN} \cap H)$.

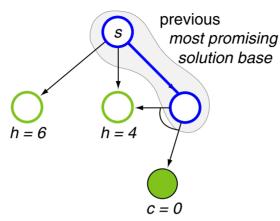


- Node on OPEN
- Node on CLOSED
- Solved rest problem

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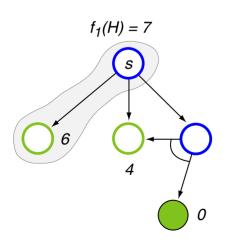
Illustration of GBF (continued)

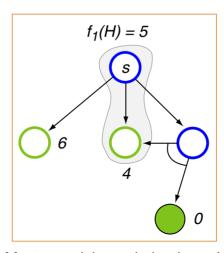
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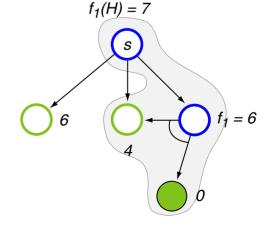


- Node on OPEN
- Node on CLOSED
- Solved rest problem

Possible solution bases:





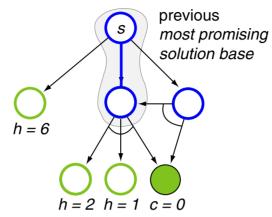


Most promising solution base H

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Illustration of GBF (continued)

3. Expansion of the node $n \in (\mathsf{OPEN} \cap H)$.

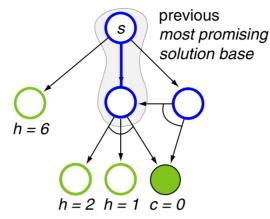


- Node on OPEN
- Node on CLOSED
- Solved rest problem

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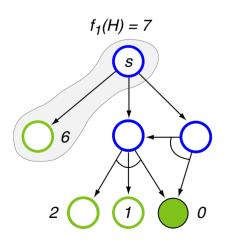
Illustration of GBF (continued)

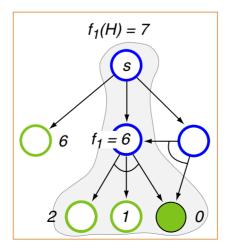
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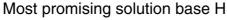


- Node on OPEN
- Node on CLOSED
- Solved rest problem

Possible solution bases:







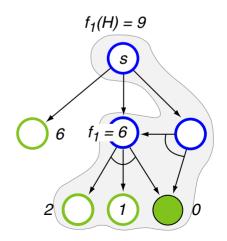
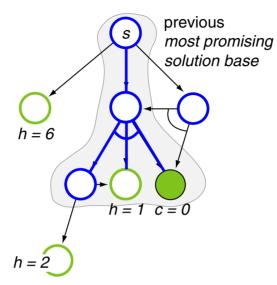


Illustration of GBF (continued)

4. Based on $f_2(n)$: expansion of some node $n \in (\mathsf{OPEN} \cap H)$.

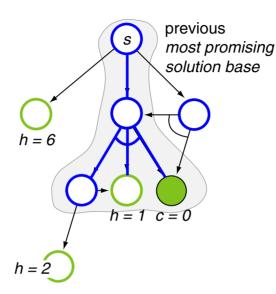


- Node on OPEN
- Node on CLOSED
- Solved rest problem

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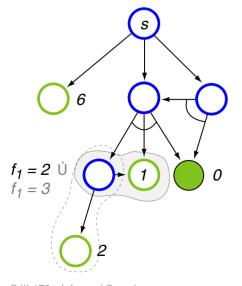
Illustration of GBF (continued)

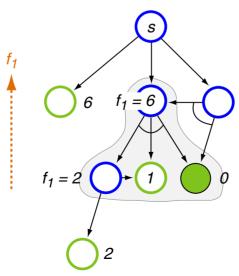
4. Based on $f_2(n)$: expansion of some node $n \in (\mathsf{OPEN} \cap H)$.



- Node on OPEN
- Node on CLOSED
- Solved rest problem

Solution bases:





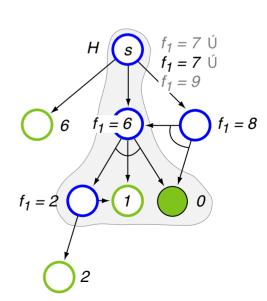
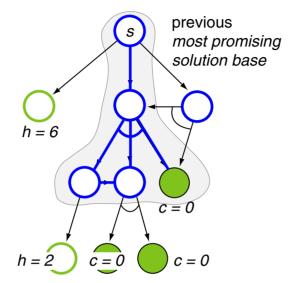


Illustration of GBF (continued) [next step]

5. Expansion of the node $n \in (\mathsf{OPEN} \cap H)$.

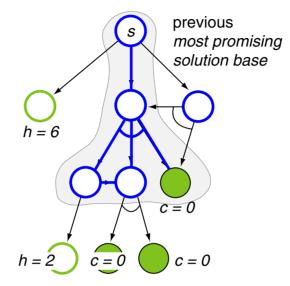


- Node on OPEN
- Node on CLOSED
- Solved rest problem

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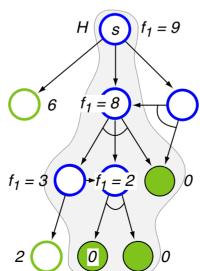
Illustration of GBF (continued) [next step]

5. Expansion of the node $n \in (\mathsf{OPEN} \cap H)$.



- Node on OPEN
- Node on CLOSED
- Solved rest problem

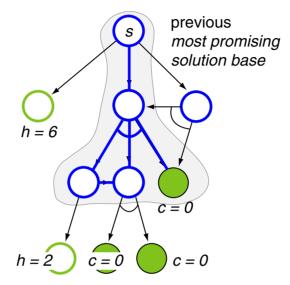
A solution graph H:



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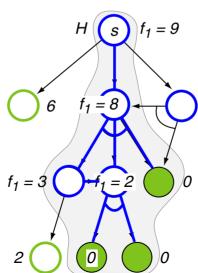
Illustration of GBF (continued) [next step]

5. Expansion of the node $n \in (\mathsf{OPEN} \cap H)$.



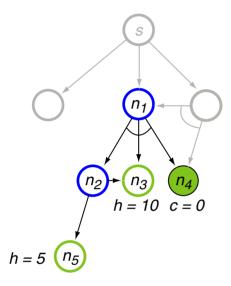
- Node on OPEN
- Node on CLOSED
- Solved rest problem

A solution graph H:



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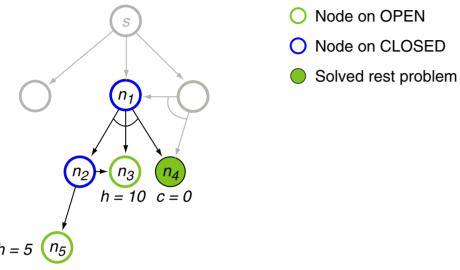
Multiple Accounting of a Node

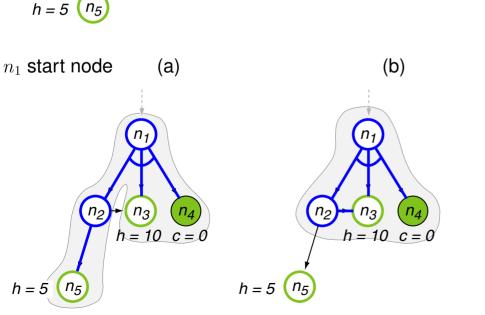


- Node on OPEN
- Node on CLOSED
- Solved rest problem

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Multiple Accounting of a Node



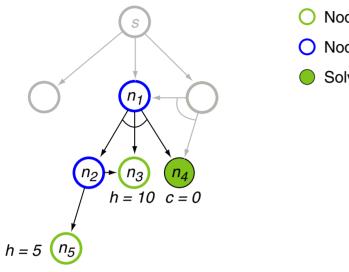


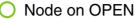
 $C_G(n_1)$ (a) (b)

duplicate count

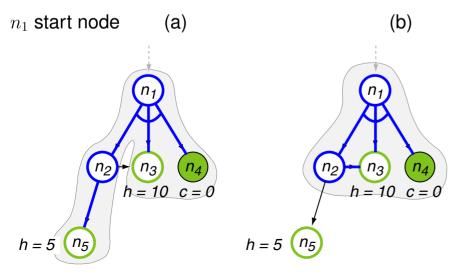
true count

Multiple Accounting of a Node



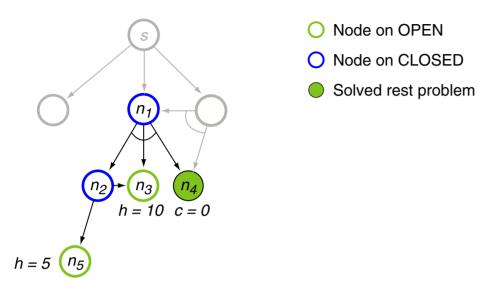


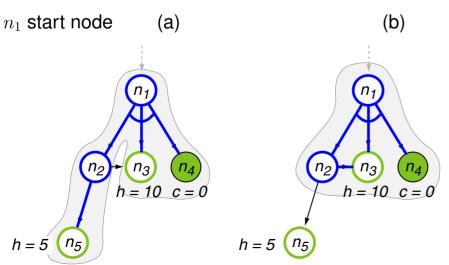
- Node on CLOSED
- Solved rest problem



$C_G(n_1)$	(a)	(b)
duplicate count	19	24
true count		

Multiple Accounting of a Node





$C_G(n_1)$	(a)	(b)
duplicate count	19	24
true count	19	14

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Remarks:

The minimum cost contribution of node n_2 to a solution is not constant, depending or	n the
multiple accounting of node n_3 .	

 \Box Q. Which approach is to be preferred—simple computation of f_1 (\sim multiple accounting) or true accounting?

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Optimality of Algorithm GBF [BF optimality]

In general, the first solution found by Algorithm GBF may not be optimum with respect to the evaluation function f_1 .

Important preconditions for (provably) finding optimum solution graphs in AND-OR-graphs by general best-first algorithms:

- 1. The cost estimate underlying f_1 must be optimistic, i.e., underestimating costs or overestimating merits.
 - In particular, the true cost of a cheapest solution graph H extending a solution base H exceeds its f_1 -value: $C_H(s) \ge f_1(H)$.
- 2. The termination in case of success ($is_solved(s) = True$) must be delayed
 - In particular, there is no call to $solved_labeling$ after node expansion, but each time when determining a most promising solution base H.
 - Algorithm GBF with delayed termination is called Algorithm GBF*.

Optimality of Algorithm GBF [BF optimality]

In general, the first solution found by Algorithm GBF may not be optimum with respect to the evaluation function f_1 .

Important preconditions for (provably) finding optimum solution graphs in AND-OR-graphs by general best-first algorithms:

- 1. The cost estimate underlying f_1 must be optimistic, i.e., underestimating costs or overestimating merits.
 - In particular, the true cost of a cheapest solution graph H extending a solution base H exceeds its f_1 -value: $C_H(s) \ge f_1(H)$.
- 2. The termination in case of success ($is_solved(s) = True$) must be delayed.
 - In particular, there is no call to $solved_labeling$ after node expansion, but each time when determining a most promising solution base H.
 - Algorithm GBF with delayed termination is called Algorithm GBF*.

Best-First Search for AND-OR Graphs [BF, BF*, GBF]

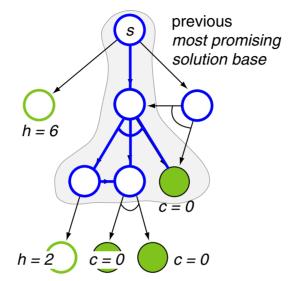
```
GBF*(s, successors, is\_solved, f_1, f_2)
 1. insert(s, OPEN); add\_node(s, G_e); // G_e is the explored part of G.
 2.
     LOOP
     IF (OPEN = \emptyset) THEN RETURN(Fail);
 3.
4.a H = min\_solution\_base(s, G_e, f_1); // Find most prom. sol. base in G_e.
       solved\_labeling(H); // Is H a solution graph?
       IF is\_solved(s) THEN RETURN(H); // Delayed termination.
  →
       n=f_2(H); // Find most informative non-goal node in H.
4.b
       remove(n, OPEN); push(n, CLOSED);
       FOREACH n' IN successors(n) DO
 5.
         IF ( n' \in \mathsf{OPEN} OR n' \in \mathsf{CLOSED} ) // Instance of n' seen before?
         THEN // Use old instance of n' instead.
          n' = retrieve(n', OPEN \cup CLOSED);
         ELSE //n' encodes an instance of a new state.
           insert(n', OPEN); add\_node(n', G_e);
         ENDIF
         add\_backpointer(n', n);
         IA[//i$//$Q|V@d(/n/')}
         THATA
          EWD/I/E
       ENDDO
```

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ENDLOOP

Illustration of GBF* (continued) [previous step]

5. Expansion of the node $n \in (\mathsf{OPEN} \cap H)$.

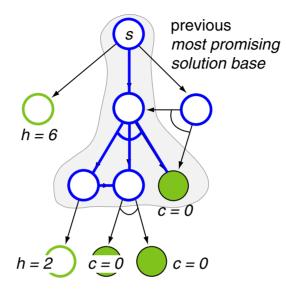


- Node on OPEN
- Node on CLOSED
- Solved rest problem

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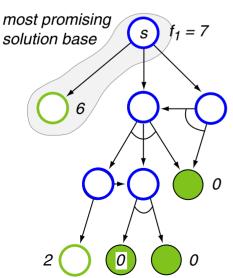
Illustration of GBF* (continued) [previous step]

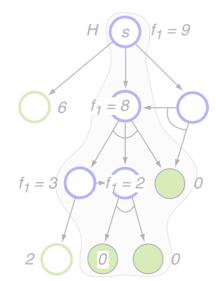
5. Expansion of the node $n \in (\mathsf{OPEN} \cap H)$.



- Node on OPEN
- Node on CLOSED
- Solved rest problem

Solution base / graph:

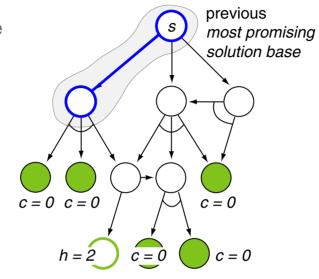




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Illustration of GBF* (continued)

6. Expansion of the node $n \in (\mathsf{OPEN} \cap H)$.

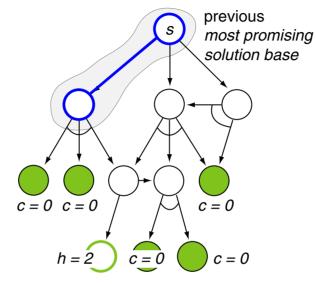


- Node on OPEN
- Node on CLOSED
- Solved rest problem

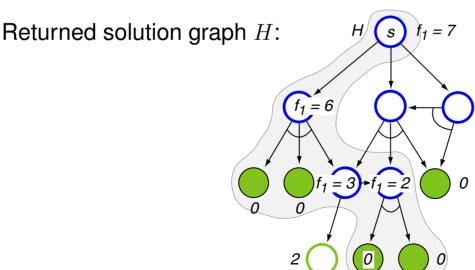
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Illustration of GBF* (continued)

6. Expansion of the node $n \in (\mathsf{OPEN} \cap H)$.



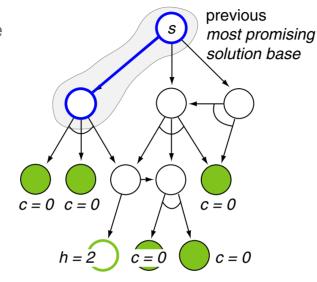
- Node on OPEN
- Node on CLOSED
- Solved rest problem



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Illustration of GBF* (continued)

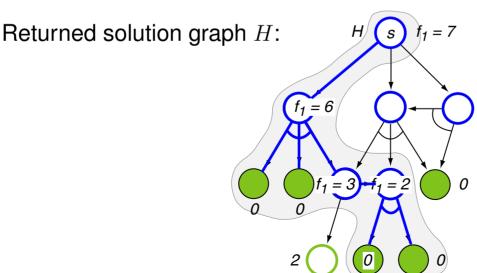
6. Expansion of the node $n \in (\mathsf{OPEN} \cap H)$.



Node on OPEN

Node on CLOSED

Solved rest problem



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Algorithm GBF applied to a state-space graph will simulate Algorithm BF. (if the evaluation function f in BF is order preserving) [S:III Evaluation of State-Space Graphs]

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Algorithm GBF applied to a state-space graph will simulate Algorithm BF. (if the evaluation function f in BF is order preserving) [S:III Evaluation of State-Space Graphs]

The key difference between GBF and BF:

GBF Solution bases are graphs. (clear due to nature of the problem)

BF Solution bases are paths. (clear due to nature of the problem)

Algorithm GBF applied to a state-space graph will simulate Algorithm BF. (if the evaluation function f in BF is order preserving) [S:III Evaluation of State-Space Graphs]

The key difference between GBF and BF:

- GBF Solution bases are graphs. (clear due to nature of the problem)
- GBF The most promising solution base is searched among all possible solution bases in G_e , the explored part of the search space graph.
 - BF Solution bases are paths. (clear due to nature of the problem)
 - BF At each point in time the union of the considered solution bases forms a tree with root s. The tree structure is maintained by always discarding the inferior path of two paths leading to the same node. The most promising solution base is searched among all paths in this tree.

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Algorithm GBF applied to a state-space graph will simulate Algorithm BF. (if the evaluation function f in BF is order preserving) [S:III Evaluation of State-Space Graphs]

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Algorithm GBF applied to a state-space graph will simulate Algorithm BF. (if the evaluation function f in BF is order preserving) [S:III Evaluation of State-Space Graphs]

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 - BF The discarding of a path (solution base) is *irrevocable*.

Remarks:

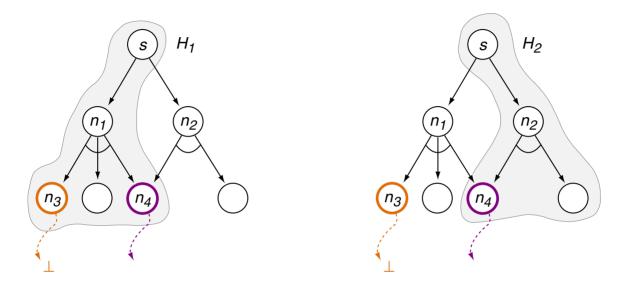
- (Under BF) the tree formed by the union of all solution bases is also called traversal tree. It
 is defined by the backpointers that are set by the Algorithm BF.
- □ (Under BF) the decision to discard an inferior path (solution base) is based on a single parameter, usually a cost value, which is maintained at the respective OPEN node.
- □ Under BF the cost value assigned to a node is unique. Under GBF, however, a node can be used in different solution bases and may get assigned different cost values for different solution bases at the same time.
- □ Under BF there is a 1:1 relationship between expansion candidates (the nodes on OPEN) and solution bases (the paths that start at *s* and end at some node on OPEN). Put another way, each node on OPEN represents a solution base, and there is no solution base without a corresponding OPEN node.
- Under BF) the term "irrevocable" means that an inferior path from s so some n will never become part of solution that also contains the node n. Irrevocability has wide-ranging consequences, which may be both crucial and reasonable, depending on the search problem at hand.

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Irrevocability is not Amenable to Problem Reduction Graphs

[Irrevocability in State-Space Graphs]

 \Leftrightarrow



The following equivalence does not generally hold for problem reduction graphs:

"Solution base H_1 can be completed to a solution"

"Solution base H_2 can be completed to a solution."

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Remarks:

The illustrated solution bases H_1 , H_2 , do not fulfill the equivalence. They share the continuation at node n_4 , and let us assume that H_2 is inferior to H_1 : $f_1(H_1) < f_1(H_2)$. However, H_2 cannot be discarded since at a later point in time the problem associated with node n_3 may turn out to be unsolvable. If we discarded H_2 , GBF would miss the only possible solution.

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