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## February 4, 2023

## The Vanishing Gradient Problem :

The problem: As more layers using certain activation functions are added to neural networks, the gradients of the loss function approaches zero, making the network hard to train.

Why: Certain activation functions, like the sigmoid function, squishes a large input space into a small input space between 0 and 1. Therefore, a large change in the input of the sigmoid function will cause a small change in the output. Hence, the derivative becomes small.

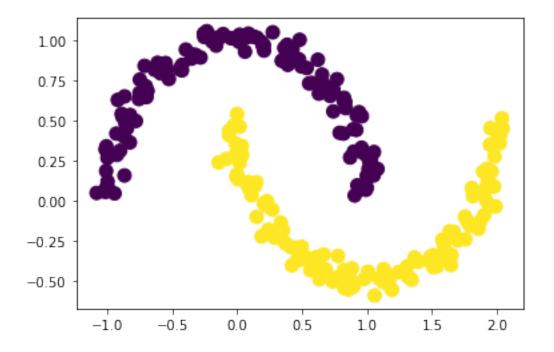
## Solutions:

The simplest solution is to use other activation functions, such as ReLU, which doesn't cause a small derivative.

```
[29]: import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
import tensorflow as tf
import keras
from sklearn.datasets import make_moons
from sklearn.model_selection import train_test_split
from keras.layers import Dense
from keras.models import Sequential
```

```
[2]: X,y = make_moons(n_samples=250, noise=0.05, random_state=42)
```

```
[3]: plt.scatter(X[:,0],X[:,1], c=y, s=100) plt.show()
```



```
[4]: model = Sequential()
    model.add(Dense(10,activation='sigmoid',input_dim=2))
    model.add(Dense(10,activation='sigmoid'))
    model.add(Dense(10,activation='sigmoid'))
    model.add(Dense(1, activation='sigmoid'))
[5]: model.compile(loss='binary_crossentropy',optimizer='adam',metrics=['accuracy'])
    model.get_weights()[0]
[6]: array([[ 0.18404245, 0.2700578 , -0.1796683 ,
                                                    0.4289047, -0.49278128,
            -0.16220212, -0.5465988, 0.25976235,
                                                    0.09992492, 0.28631818],
                                                    0.4220243, 0.01249403,
            [-0.49214402, 0.52247757, 0.10643345,
            -0.41913083,
                          0.400917 , -0.03765839,
                                                    0.11924303, 0.10320246]],
          dtype=float32)
    old_weights = model.get_weights()[0]
[8]: X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.20,__
      →random_state=42)
[9]: model.fit(X_train, y_train, epochs = 100)
    Epoch 1/100
                              ======] - 1s 4ms/step - loss: 0.7124 - accuracy:
```

```
0.5100
Epoch 2/100
0.5100
Epoch 3/100
0.5100
Epoch 4/100
0.5100
Epoch 5/100
0.5100
Epoch 6/100
0.5100
Epoch 7/100
0.5100
Epoch 8/100
0.5100
Epoch 9/100
0.5100
Epoch 10/100
0.5100
Epoch 11/100
0.5150
Epoch 12/100
0.6750
Epoch 13/100
0.7100
Epoch 14/100
0.7100
Epoch 15/100
0.7300
Epoch 16/100
0.7150
Epoch 17/100
```

```
0.7000
Epoch 18/100
0.7200
Epoch 19/100
0.7250
Epoch 20/100
0.7300
Epoch 21/100
0.7350
Epoch 22/100
7/7 [=========== ] - Os 36ms/step - loss: 0.6837 - accuracy:
0.7500
Epoch 23/100
0.7450
Epoch 24/100
0.7400
Epoch 25/100
0.6750
Epoch 26/100
0.5500
Epoch 27/100
0.6750
Epoch 28/100
0.7300
Epoch 29/100
0.7400
Epoch 30/100
0.7600
Epoch 31/100
0.7600
Epoch 32/100
0.7700
Epoch 33/100
```

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0.7750
Epoch 34/100
0.7800
Epoch 35/100
0.7900
Epoch 36/100
0.7750
Epoch 37/100
0.7700
Epoch 38/100
0.7700
Epoch 39/100
0.7650
Epoch 40/100
0.7700
Epoch 41/100
0.7700
Epoch 42/100
7/7 [=========== ] - Os 28ms/step - loss: 0.6593 - accuracy:
0.7750
Epoch 43/100
0.7700
Epoch 44/100
0.7800
Epoch 45/100
0.7700
Epoch 46/100
0.7700
Epoch 47/100
0.7750
Epoch 48/100
0.7700
Epoch 49/100
```

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0.7700
Epoch 50/100
0.7850
Epoch 51/100
0.7700
Epoch 52/100
0.7700
Epoch 53/100
0.7800
Epoch 54/100
0.7850
Epoch 55/100
0.7850
Epoch 56/100
0.7900
Epoch 57/100
0.7900
Epoch 58/100
0.7900
Epoch 59/100
0.7900
Epoch 60/100
0.7900
Epoch 61/100
0.7850
Epoch 62/100
0.7850
Epoch 63/100
0.7850
Epoch 64/100
0.7850
Epoch 65/100
```

```
0.7900
Epoch 66/100
0.7900
Epoch 67/100
0.8000
Epoch 68/100
0.8000
Epoch 69/100
0.7900
Epoch 70/100
0.7900
Epoch 71/100
0.7900
Epoch 72/100
0.7900
Epoch 73/100
0.7900
Epoch 74/100
0.7900
Epoch 75/100
0.7900
Epoch 76/100
7/7 [=========== ] - 0s 12ms/step - loss: 0.5210 - accuracy:
0.7950
Epoch 77/100
0.7900
Epoch 78/100
0.7900
Epoch 79/100
0.7950
Epoch 80/100
0.8050
Epoch 81/100
```

```
0.8050
Epoch 82/100
0.8100
Epoch 83/100
0.8100
Epoch 84/100
0.8100
Epoch 85/100
0.8100
Epoch 86/100
0.8100
Epoch 87/100
0.8100
Epoch 88/100
0.8100
Epoch 89/100
0.8100
Epoch 90/100
0.8100
Epoch 91/100
0.8100
Epoch 92/100
0.8100
Epoch 93/100
0.8100
Epoch 94/100
0.8100
Epoch 95/100
0.8100
Epoch 96/100
0.8100
Epoch 97/100
```

```
0.8100
    Epoch 98/100
    Epoch 99/100
    Epoch 100/100
    7/7 [======
                        =======] - Os 4ms/step - loss: 0.4164 - accuracy:
    0.8100
[9]: <keras.callbacks.History at 0x7f511b305550>
[10]: new_weights = model.get_weights()[0]
[11]: model.optimizer.get_config()["learning_rate"]
[11]: 0.001
[12]: gradient = (old_weights - new_weights)/ 0.001
     percent_change = abs(100*(old_weights - new_weights)/ old_weights)
[13]: gradient
[13]: array([[ -680.3453 ,
                        283.82428, -310.81702, -561.9538, 569.8005,
            -715.84015, 541.0472, 590.6196, -606.09546, -568.54803],
           [ 1103.66 , -634.56476, 462.43475, 954.51483, -1085.3569 ,
            1065.5938 , -1082.2494 , -917.213 , 968.9136 , 960.5847 ]],
          dtype=float32)
[14]: percent_change
[14]: array([[ 369.6676 , 105.09761 , 172.99492 , 131.02068 , 115.62949 ,
            441.32602 ,
                       98.984344, 227.36925, 606.5509, 198.57213],
           [ 224.25552 , 121.453026 , 434.48254 , 226.17532 , 8687.007
            254.23897 , 269.9435 , 2435.6138 , 812.5537 , 930.77704 ]],
          dtype=float32)
[15]: old_weights
[15]: array([[ 0.18404245,  0.2700578 , -0.1796683 ,  0.4289047 , -0.49278128,
           -0.16220212, -0.5465988, 0.25976235, 0.09992492, 0.28631818],
           [-0.49214402, 0.52247757, 0.10643345, 0.4220243, 0.01249403,
           -0.41913083, 0.400917 , -0.03765839, 0.11924303, 0.10320246]],
          dtype=float32)
[16]: new_weights
```

```
[16]: array([[ 0.86438775, -0.0137665 , 0.13114873, 0.99085855, -1.0625818 ,
           0.55363804, -1.087646 , -0.33085737, 0.7060204 , 0.85486627],
          [-1.5958041, 1.1570424, -0.35600132, -0.53249055, 1.0978509,
          -1.4847246 , 1.4831663 , 0.8795547 , -0.8496706 , -0.8573823 ]],
         dtype=float32)
[17]: model = Sequential()
    model.add(Dense(10,activation='relu',input_dim=2))
    model.add(Dense(10,activation='relu'))
    model.add(Dense(1, activation='sigmoid'))
[18]: model.compile(loss='binary crossentropy',optimizer='adam',metrics=['accuracy'])
[19]: old_weights = model.get_weights()[0]
[20]: X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.20, ___
     →random state=42)
[21]: model.fit(X_train, y_train, epochs = 100)
    Epoch 1/100
    0.5100
    Epoch 2/100
    7/7 [=========== ] - 0s 8ms/step - loss: 0.6900 - accuracy:
    0.5400
    Epoch 3/100
    0.7550
    Epoch 4/100
    0.7500
    Epoch 5/100
    0.8400
    Epoch 6/100
```

```
0.8550
Epoch 7/100
0.8800
Epoch 8/100
0.8800
Epoch 9/100
0.8600
Epoch 10/100
0.8550
Epoch 11/100
0.8750
Epoch 12/100
0.8550
Epoch 13/100
0.8850
Epoch 14/100
0.8850
Epoch 15/100
0.9000
Epoch 16/100
0.8950
Epoch 17/100
0.9050
Epoch 18/100
0.8950
Epoch 19/100
0.9150
Epoch 20/100
0.9100
Epoch 21/100
0.9200
Epoch 22/100
```

```
0.9100
Epoch 23/100
0.9200
Epoch 24/100
0.9050
Epoch 25/100
0.9250
Epoch 26/100
0.9150
Epoch 27/100
0.9200
Epoch 28/100
0.9250
Epoch 29/100
0.9300
Epoch 30/100
0.9300
Epoch 31/100
0.9350
Epoch 32/100
0.9250
Epoch 33/100
0.9300
Epoch 34/100
0.9250
Epoch 35/100
0.9250
Epoch 36/100
0.9300
Epoch 37/100
0.9500
Epoch 38/100
```

```
0.9250
Epoch 39/100
0.9350
Epoch 40/100
0.9500
Epoch 41/100
0.9250
Epoch 42/100
0.9500
Epoch 43/100
0.9600
Epoch 44/100
0.9500
Epoch 45/100
0.9600
Epoch 46/100
0.9550
Epoch 47/100
0.9650
Epoch 48/100
0.9650
Epoch 49/100
0.9650
Epoch 50/100
0.9650
Epoch 51/100
0.9900
Epoch 52/100
0.9650
Epoch 53/100
0.9600
Epoch 54/100
```

```
0.9750
Epoch 55/100
0.9700
Epoch 56/100
0.9800
Epoch 57/100
0.9900
Epoch 58/100
0.9900
Epoch 59/100
0.9900
Epoch 60/100
0.9950
Epoch 61/100
0.9850
Epoch 62/100
0.9850
Epoch 63/100
0.9950
Epoch 64/100
1.0000
Epoch 65/100
0.9950
Epoch 66/100
1.0000
Epoch 67/100
0.9950
Epoch 68/100
1.0000
Epoch 69/100
1.0000
Epoch 70/100
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1,0000
Epoch 71/100
1.0000
Epoch 72/100
1.0000
Epoch 73/100
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Epoch 74/100
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Epoch 75/100
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Epoch 76/100
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Epoch 77/100
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Epoch 78/100
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Epoch 79/100
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Epoch 80/100
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Epoch 81/100
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Epoch 82/100
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Epoch 83/100
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Epoch 84/100
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Epoch 85/100
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Epoch 86/100
```

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1,0000
 Epoch 87/100
 1.0000
 Epoch 88/100
 1.0000
 Epoch 89/100
 1.0000
 Epoch 90/100
 7/7 [=========== ] - 0s 6ms/step - loss: 0.0050 - accuracy:
 1.0000
 Epoch 91/100
 7/7 [=========== ] - 0s 6ms/step - loss: 0.0048 - accuracy:
 1,0000
 Epoch 92/100
 1.0000
 Epoch 93/100
 1.0000
 Epoch 94/100
 1,0000
 Epoch 95/100
 1.0000
 Epoch 96/100
 1.0000
 Epoch 97/100
 1.0000
 Epoch 98/100
 1.0000
 Epoch 99/100
 1.0000
 Epoch 100/100
 1.0000
[21]: <keras.callbacks.History at 0x7f511b25de20>
[22]: new_weights = model.get_weights()[0]
```

```
[23]: model.optimizer.get_config()["learning_rate"]
[23]: 0.001
[24]: gradient = (old weights - new weights)/ 0.001
      percent_change = abs(100*(old_weights - new_weights)/ old_weights)
[25]:
     gradient
[25]: array([[ 238.1037
                               8.366286,
                                           -25.899588,
                                                         -39.772747,
                                                                        -4.219502,
               146.7252
                              11.92063 ,
                                           -25.667309,
                                                         -32.940685,
                                                                        34.258266],
              [-29.849901,
                              24.193523,
                                            75.90496 ,
                                                          62.46665 , -164.69519 ,
              -209.34384 ,
                              33.327938,
                                           -13.049423,
                                                          90.38502 ,
                                                                      -11.896818]],
            dtype=float32)
      percent_change
[26]:
[26]: array([[ 55.869396 ,
                                                          8.081712 ,
                                                                        0.9096341,
                              1.5076709,
                                            4.005221 ,
              169.42677
                              1.9219062,
                                            3.7337885,
                                                          6.117841 ,
                                                                       30.70192 ],
              [ 22.507624 ,
                              3.7737753,
                                           12.581471 ,
                                                         17.776312 ,
                                                                       24.384586 ,
               35.327286 ,
                             46.407158 ,
                                            1.8619287,
                                                         19.620298 ,
                                                                        3.2026446]],
            dtype=float32)
      old_weights
[27]: array([[-0.42617914,
                             0.55491465,
                                           0.6466457 ,
                                                         0.49213272,
                                                                       0.46386808,
               0.08660096,
                             0.6202504 ,
                                           0.6874334 ,
                                                         0.5384365 ,
                                                                       0.11158347],
                                           0.60330755, -0.3514039,
              [ 0.13262129,
                             0.64109606,
                                                                       0.675407
                                           0.7008552 , -0.46067095 ,
              -0.592584
                             0.07181638,
                                                                      0.3714686 ]],
            dtype=float32)
[28]: new_weights
[28]: array([[-0.66428286,
                             0.54654837,
                                           0.6725453 ,
                                                        0.5319055 ,
                                                                      0.46808758,
              -0.06012425,
                             0.6083298 ,
                                           0.71310073,
                                                         0.57137716,
                                                                       0.0773252],
              [ 0.16247119,
                                           0.5274026 , -0.41387054 ,
                             0.61690253,
                                                                       0.8401022 ,
              -0.38324016,
                             0.03848844,
                                           0.7139046 , -0.55105597 ,
                                                                      0.38336542]],
            dtype=float32)
     Solution:
     1:Reduce model complexity (if your model contains large hidden layers use few hidden layer (shallow
     network) but it is not recommended for solving complex problem
     2:Use Relu activation function
[28]:
```