# Assignment 1 (main part): Arithmetic Expressions

#### Version 1.0

Due: Wednesday, September 15, 2021 at 20:00

The objective of this assignment is to gain some initial hands-on programming experience with Haskell. Please read through the *entire* assignment text before you start working on it.

**Note** This assignment also includes a collection of simple warm-up exercises, as described on Absalon. For those, you are *only* asked to submit your working code, but not a separate design/implementation document, assessment, or evidence of testing. If you want to communicate anything extra about your solutions to the warm-up exercises, place your remarks as comments in the source code.

## 1 Simple arithmetic expressions

Consider the following algebraic data type, representing simple arithmetic expressions:

```
data Exp =
    Cst Integer
    | Add Exp Exp
    | Sub Exp Exp
    | Mul Exp Exp
    | Div Exp Exp
    | Pow Exp Exp
    | Pow dational constructors; see next section)
```

That is, an arithmetic expression is either an (unbounded) integer constant, or one of the following five operations on two subexpressions: addition, subtraction, multiplication, division, or power (aka. exponentiation). Note that there is no provision for including explicit parentheses in the representation, as the tree structure of an Exp-typed value already encodes the intended grouping: the arithmetic expression conventionally written as  $2 \times (3+4)$  is represented as Mul (Cst 2) (Add (Cst 3) (Cst 4)), whereas  $(2 \times 3) + 4$  corresponds to Add (Mul (Cst 2) (Cst 3)) (Cst 4).

### 1.1 Printing expressions

Define a function

```
showExp :: Exp -> String
```

that renders an arithmetic expression as a string, using normal mathematical/Haskell infix notation, as in the examples above. Use "+", "-", "\*", "'div'", and "-" to represent the five arithmetic operators. (In Haskell, the operator "/" represents division with a potentially fractional result, which is not the intent here.) Include enough parentheses in the output to

ensure that the output string can be correctly read and evaluated as a Haskell expression, and that any two different Exp-trees have distinct renderings (even if they would evaluate to the same result, such as "(2+3)+4" and "2+(3+4)"). You are explicitly *allowed* to insert nominally redundant (according to the usual mathematical conventions) parentheses in the output, e.g., "((2\*3)+4)".

If the expression to be printed is not one of the above-mentioned six forms (i.e., if it belongs to the commented-out part of the data Exp declaration), your code should explicitly report the problem with an appropriate message (using the standard function error), rather than crash out with a non-exhaustive pattern-match error.

## 1.2 Evaluating expressions

Arithmetic expressions can be evaluated to numeric results. In this assignment, we only consider integer arithmetic, with n 'div' m (for  $m \neq 0$ ) defined as  $\lfloor \frac{n}{m} \rfloor$ , where  $\lfloor r \rfloor$  (the floor of r) is the greatest integer less than or equal to r. (So  $\lfloor \frac{7}{2} \rfloor = 3$ , while  $\lfloor \frac{-7}{2} \rfloor = -4$ .) Also, we require that the exponent (second subexpression) in a Pow-operation is non-negative, and we specify that  $n^0 = 1$  for all integers n, including 0.

Define a Haskell function

```
evalSimple :: Exp -> Integer
```

such that evalSimple e computes the value of e, under the interpretation of the arithmetic operators specified above. If an error occurs inside a builtin operation (e.g., a division by zero), it is fine to just abort with the relevant Haskell runtime error. And, like for printing, expressions not in the "simple" fragment of Exp should be explicitly reported as errors. If there are multiple errors in an expression, it doesn't matter which one gets reported.

## 2 Extended arithmetic expressions

We now consider a richer class of expressions, given by the full datatype:

```
data Exp =
-- ... (6 constructors from above)
  | If {test, yes, no :: Exp}
  | Var VName
  | Let {var :: VName, def, body :: Exp}
  | Sum {var :: VName, from, to, body :: Exp}

type VName = String
```

Here, the expression form If  $e_1$   $e_2$   $e_3$  (or, more verbosely, If {test =  $e_1$ , yes =  $e_2$ , no =  $e_3$ }) represents a conditional expression (analogous to  $e_1 ? e_2 : e_3$  in C). That is, its value is either the value of  $e_2$ , if  $e_1$  evaluates to a non-zero number; or the value of  $e_3$ , if  $e_1$  evaluates to zero. Only the selected branch,  $e_2$  or  $e_3$ , is evaluated; for example, evaluating the expression

```
If {test = Sub (Cst 2) (Cst 2),
    yes = Div (Cst 3) (Cst 0),
    no = Cst 5}
```

should return 5, and *not* abort with a division by zero.

The expression  $Var\ v$ , where v is a variable name (represented as a Haskell string), returns the current value (as specified below) of the variable v. If the variable has no current value, an error is signaled.

Conversely, the expression Let v  $e_1$   $e_2$  is used to bind the variable v to the value of  $e_1$  for (only) the duration of evaluating  $e_2$ ; afterwards, the previous binding (if any) of v is reinstantiated. Thus, for example, the expression

corresponding to the more human-readable Haskell notation

```
let x = 5 in (let x = 3 + 4 in x * x) + x
```

should evaluate to  $(3+4)^2 + 5 = 54$ .

It is deliberately left *unspecified* (i.e., you as the implementer may decide) whether an error occurring in the defining expression  $e_1$  should be signaled if the bound variable v is not actually used in the body  $e_2$ . For instance,

```
Let "x" (Div (Cst 4) (Cst 0)) (Cst 5)
```

is allowed to evaluate to 5, or to abort with a division-by-zero error (but nothing else).

Finally, the expression form Sum v  $e_1$   $e_2$   $e_3$  corresponds to the mathematical summation notation  $\sum_{v=e_1}^{e_2} e_3$ . That is, it first evaluates  $e_1$  and  $e_2$  to numbers  $n_1$  and  $n_2$ , and then computes the sum of the results of evaluating  $e_3$ , where v is bound to each of the values  $n_1, n_1 + 1, ..., n_2$  in turn. For example, the expression

```
Sum "x" (Cst 1) (Add (Cst 2) (Cst 2))
      (Mul (Var "x") (Var "x"))
```

evaluates to  $1^2 + 2^2 + 3^2 + 4^2 = 30$ . If  $n_1 > n_2$ , the sum is defined to be 0 (and  $e_3$  should not be evaluated at all).

We keep track of variable bindings in an *environment*, which maps variable names to their values (if any). We represent environments as *functional values*:

```
type Env = VName -> Maybe Integer
```

That is, for an environment r:: Env and variable v:: VName, the application r v returns Nothing if v has no binding in r, and Just n if v is bound to the integer n. The environment in which all variables are unbound can be written as simply initEnv = v - N Nothing, while the one in which variable "ans" is bound to 42 (and all others are unbound) would be represented as the following function:

```
\v \rightarrow if v == "ans" then Just 42 else Nothing
```

Define a function

```
extendEnv :: VName -> Integer -> Env -> Env
```

such that extendEnv v n r returns a new environment r', in which v is bound to n, and all other variables have the same bindings as they did in r.

Then define a function

```
evalFull :: Exp -> Env -> Integer
```

that evaluates an expression in a given environment. As before, errors should be signaled with error, and may now – in addition to erroneous arithmetic operations – include attempts to access unbound variables. On the other hand, all expression forms in Exp should now be covered.

Be sure to explain in the report how you chose to deal with errors in unneeded parts of Let-expressions, and why. (Simplicity of implementation is a perfectly acceptable justification.)

\*\*\*

## 3 Returning explicit errors

Promptly aborting evaluation with a Haskell error is a fairly drastic step, and in particular makes it impossible to recover gracefully from a conceptually non-fatal problem. A more flexible approach makes the evaluator function return an explicit indication of what went wrong, and lets the user of the evaluator decide what to do next. Accordingly, we first enumerate some possible failures:

Define a Haskell function,

```
evalErr :: Exp -> Env -> Either ArithError Integer
```

such that evalErr e r attempts to evaluate e in environment r, as in evalFull, but now returns either an error value (e.g. Left ENegPower) or a proper result (e.g. Right 42). evalErr should never cause a Haskell runtime error (except possibly by running out of memory).

For evalErr, we also specify explicitly that all subexpressions are to be evaluated left-toright, so that, e.g., if we are evaluating Add  $e_1$   $e_2$ , and  $e_1$  returns an error,  $e_2$  should not be evaluated. However, it is still left unspecified (meaning: you should choose) whether errors in unused Let-bindings should be reported or ignored. Again, justify your choice in the report.

\*\*\*

*Hint:* The code of evalErr may become somewhat verbose and repetitive; try to abstract common code snippets into (higher-order) auxiliary functions, so that you only have to write them once. Do not attempt to use Haskell's builtin imprecise-exception facility: it is quite finicky, and will most likely not do what you need.

## 4 Optional extensions

The problems in this section are a bit more challenging, and hence not mandatory, but still recommended for extra practice, if you finish the main task quickly. They are independent, so you may do any subset of them.

Note that your performance on the optional problems will *not* affect whether you pass the assignment: an incomplete or buggy solution here will not drag down an otherwise acceptable solution of the mandatory part; and conversely, you cannot save an otherwise failing solution of the main problems by successfully solving one or more of the optional ones.

## 4.1 Strict error-propagation in exponentiation

The semantics of exponentiation is specified above as  $n^0 = 1$  for all integers n, just like  $n \times 0 = 0$  for all n. However, in a general expression Pow  $e_1$   $e_2$ , if evaluation of the subexpression  $e_1$  results in an error (division by zero, unbound variable, etc.), we still want evaluation of the whole expression to report that same error, even if  $e_2$  evaluates to 0 (so that  $e_1$ 's actual value is not really needed). Make your implementations of especially evalSimple and evalFull ensure this, so that, e.g., (Pow (Div (Cst 0) (Cst 0)) (Cst 0)) results in an error, and not a successful result of 1. (If your evaluator already happens to behaves like this, you don't need to do anything here!). Explain briefly how/why your solution works.

\*\*\*

Hint: Think about how you can ensure that Haskell evaluates some subexpression to a value, even though that value will not matter for the final result of the whole expression. You may use the built-in function seq :: a -> b -> b, but you don't actually need it here.

### 4.2 Printing with minimal parentheses

Define a variant of the showExp function,

```
showCompact :: Exp -> String
```

that prints a simple arithmetic expression using the minimal number of parentheses (and no extra spaces), so that it can still be correctly read and evaluated by Haskell. The function must also still be one-to-one, i.e., no two different values of type Exp should be rendered into the same string. You should assume that the arithmetic operators have the conventional precedences and associativities (e.g. Add (Cst 2) (Mul (Cst 3) (Cst 4)) should print as "2+3\*4", and Add (Cst 2) (Add (Cst 3) (Cst 4)) as "2+(3+4)"). Note in particular that "2^3^4" corresponds to  $2^{3^4}$ , which conventionally means  $2^{(3^4)}$ , not  $(2^3)^4$ .

Hint: You will probably want to define showCompact in terms of an auxiliary recursive function that takes as parameters both the expression to be printed, and some additional data to determine whether explicit parentheses are needed around it, given the context it appears in. Briefly explain how your solution works.

\*\*\*

## 4.3 Explicitly eager/lazy semantics

In evalErr, the exact semantics of Let-expressions was left partially unspecified. There are in fact two natural interpretations of an expression Let  $v e_1 e_2$ : the eager one, where  $e_1$  is always evaluated proactively, regardless of whether v is used in  $e_2$ ; and the lazy one, where  $e_1$  is only evaluated as and when its value is needed for computing  $e_2$ .

Accordingly, define two functions,

```
evalEager :: Exp -> Env -> Either ArithError Integer
evalLazy :: Exp -> Env -> Either ArithError Integer
```

implementing the two variants (for all Lets occurring in the first argument). For example, the call evalLazy (Let "x" (Var "y") (Cst 0)) initEnv should now return Right 0, whereas evalEager (Let "x" (Var "y") (Cst 0)) initEnv should return Left (BadVar "y")

Hint: If your evalErr from the mandatory part already implements precisely one of the two behaviors, you can simply use it directly as the relevant definition. And again, you may want to express one or both of the evaluation functions above in terms of another, more general, function with additional and/or differently typed parameters; in particular, your internal function might use a slightly different type for the environments. Briefly explain your approach.

\*\*\*

## 5 What to hand in

#### 5.1 Code

Form To facilitate both human and automated feedback, it is very important that you closely follow the code-packaging instructions in this section. We provide skeleton/stub files for all the requested functionality in both the warm-up and the main part. These stub files are packaged in the handed-out code.zip. It contains a single directory code/, with a couple of subdirectories organized as Stack projects. You should edit the provided stub files as directed, and leave everything else unchanged.

It is crucial that you not change the provided types of any exported functions, as this will make your code incompatible with our testing framework. Also, *do not* remove the bindings for any functions you do not implement; just leave them as undefined.

When submitting the assignment, package your code up again as a single code.zip (not.rar,.tar.gz, or similar), with exactly the same structure as the original one. When rebuilding code.zip, please take care to include only the files that constitute your actual submission: your source code and supporting files (build configuration, tests, etc.), but not obsolete/experimental versions, backups, editor autosave files, revision-control metadata, .stack-work directories, and the like. If your final code.zip is substantially larger than the handed-out version, you probably included something that you shouldn't have.

For the warm-up part, just put your function definitions in code/part1/src/Warmup.hs, where indicated.

For the main part, your code must be placed in the file code/part2/src/Arithmetic.hs. It should only export the requested functionality. Any tests or examples should be put in a separate module under code/part2/tests/. For inspiration, we have provided a very minimalistic (and far from complete) test suite in code/part2/tests/Test.hs. If you are using Stack (and why wouldn't you be?), you can build and run the suite by stack test from the directory code/part2/.

The definitions for this assignment (e.g. type Exp) are available in file .../src/Definitions.hs. You should only import from this module, and not directly copy its contents into Arithmetic. And again, do not modify anything in Definitions.

Content As always, your code should be appropriately commented. In particular, try to give brief informal specifications for any auxiliary "helper" functions you define, whether locally or globally. On the other hand, avoid trivial comments that just rephrase in English what the code is already clearly saying in Haskell. Try to use a consistent indentation style, and avoid lines of over 80 characters, since those will typically be wrapped in printed listings (or if someone uses a narrower editor window than you), making them hard to read.

You may (but shouldn't need to, for this assignment) import additional functionality from the core GHC libraries only: your solution code should compile with a stack build issued from the directory code/partn/, using the provided package.yaml. For testing, you may optionally use additional packages from the course-mandated version of the Stack LTS distribution, e.g., test frameworks. Later in the course, we will use Tasty and QuickCheck.)

Your code should ideally give no warnings when compiled with ghc(i) -W; otherwise, add a comment explaining why any such warning is harmless or irrelevant in each particular instance. If some problem in your code prevents the whole file from compiling at all, be sure to comment out the offending part before submitting, or all the automated tests will fail.

### 5.2 Report

In addition to the code, you must submit a short (normally 1–2 pages) report, covering the following two points, for the main (not warm-up) part only:

- Document any (non-trivial) design and implementation choices you made. This includes, but is not necessarily limited to, answering any questions explicitly asked in the assignment text (marked with \*\*\* in the margin, for extra emphasis). Focus on high-level aspects and ideas, and explain why you did something non-obvious, not only what you did. It is rarely appropriate to do a detailed function-by-function code walk-through in the report; technical remarks about how the functions work belong in the code as comments.
- Give an honest, justified assessment of the quality of your submitted code, and the degree to which it fulfills the requirements of the assignment (to the best of your understanding and knowledge). Be sure to clearly explain any known or suspected deficiencies.
  - It is very important that you document on what your assessment is based (e.g., wishful thinking, scattered examples, systematic tests, correctness proofs?). Include any automated tests you did with your source submission, make it clear how to run them, and summarize the results in the report. If there were some aspects or properties of your code that you couldn't easily test in an automated way, explain why.

We suggest (and may later mandate) that you structure your assessment into the following subsections/paragraphs:

- Completeness Is all the asked-for (as well as optional) functionality implemented, at least in principle, even if not necessarily fully working? If not, do you have any concrete ideas for how to implement the missing parts?
- Correctness Does all implemented functionality work correctly, or are there known bugs or other limitations? In the latter case, do you have any ideas on how to potentially address those problems?
- **Efficiency** Does the runtime time and space usage of your code (as you would expect it to be executed by Haskell; you don't need to actually benchmark it) reasonably match, at least asymptotically, what one would naturally assume from a proper implementation? If not, do you have ideas on how to non-trivially improve the performance of your code?
- Maintainability Are common code snippets reasonably shared through parameterized auxiliary definitions, or is there a lot of code duplication in the form of copy-pasted segments with minor changes? (Note that this concern potentially also applies to your test suite!) Is the code otherwise in what you would consider in good shape (properly laid out, commented, etc.)?

Other Anything else you consider worth mentioning, both positive and negative.

The first two points should be substantiated by reference to the results of your formal testing. For the others, you should also justify your assessment by relevant examples or other evidence.

Your report document should be a PDF file named report.pdf and submitted separately from the code in Absalon.

#### 5.3 Timesheet

In this year's run of AP, we have particular focus on student workload in the course. To help us get a more detailed, complete, and timely picture than what's provided by the formal course evaluation at the end of the block, we ask you to fill in a short timesheet for each week, detailing how much time you spent on the various parts and aspects of the assignment, as well as on other course-related activities.

The timesheet template is located in a separate file, timesheet.txt, in the main code directory, and is meant to be machine-processed, so it's important that you fill it out properly. In particular, for each time category, you should report the time you spent in hours and/or minutes, in a natural format, e.g., "2 h", "15m", "120 m", "1h30m", etc. It is particularly important that you remember to include the units, as there is no default.

If you don't know or remember how much time you spent in a paricular category, give your best estimate. If you have no meaningful number for one or more categories, or prefer not to say, just write the time as a single "x".

You may include comments (starting with "#" and running till the end of the line) explaining or elaborating on your numbers, especially if you think they may be atypical. However, the timesheets are mainly intended for automated processing, so any textual comments may not get systematically registered. If you have any important points or observations that you want to bring to our attention, you should address them directly to a member of the teaching staff.

To help ensure a consistent interpretation of the categories, please use the following guidelines for accounting for the various course-related activities:

**Assignment** (Not an actual category. Leave as the number 1 for identification).

**Installation** Time spent on getting GHC/Stack installed and running on your platform. Do not include non-essential setup tweaks (such as getting syntax highlighting to work in your favorite editor, or similar.)

**Reading** Time spent on the recommended readings for this week, even if not directly relevant for the assignment, as well as any supplementary reading (possibly from other than the suggested sources) that you did specifically to make progress on the assignment.

**Lectures** Time spent on attending/watching the lectures. This could be less than the nominal 4 hours/week, if you skipped (parts of) a lecture for whatever reason.

**Exploration** Time spent on Haskell programming in *non-mandatory* activities, whether based on the suggested exercises or your own experiments. This also includes work on the *optional* parts of the assignment, regardless of whether you ultimately hand it in for feedback.

Warmup Time spent on the warm-up part of the assignment.

**Development** Time spent on writing and debugging the code in the main part of the assignment, *including* any integrated or ad-hoc testing you did during development.

**Tests** Time, above and beyond the above development time, dedicated specifically to documenting your testing in the form of an automated test suite. Note that this could be (close to) zero, if you already wrote the relevant test cases before, or together with, the code.

**Report** Time for writing up your design/implementation decisions and assessment.

If anything in the above directions is unclear (and would significantly affect the numbers you report), ask for clarification on the forum. Note that the categories and/or their descriptions may be adjusted for the later assignments, as needed.

Your timesheet numbers (or explicit lack thereof) will not affect your assignment grade, or be commented on by the TAs. But we hope that you will answer as accurately and completely as you can, to help us get a proper sense of what activities contribute significantly to the AP workload, and where specific corrective actions may be indicated for later assignments and/or future runs of the course.

You do not have to time yourself with a stopwatch or similar, but do try to account for any significant pauses or interruptions (e.g., lunch breaks) in blocks of time nominally dedicated to particular activities. You may find a dedicated time-tracking tool (such as clockify.me, or any number of free apps) useful and informative in general, not only for AP.

#### 5.4 General

Detailed upload instructions, in particular regarding the logistics of group submissions, can be found on the Absalon submission page.

We also *expect* to provide an automated system to give you preliminary feedback on your planned code submission, including matters of form, correctness, style, etc. The details will be announced on Absalon. You are **strongly advised** to take advantage of this opportunity to validate your submission, and – if necessary – fix or otherwise address (e.g., by documenting as known flaws) any legitimate problems it uncovers.

Note, however, that passing our automated tests is *not* a substitute for doing *and docu*menting your own testing. Your assessment must be able to stand alone, without leaning on the output from our tool.