

Relational Programming in miniKanren

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*For my H211 students: Indiana University, Fall 2010 & 2011,
and Team pw0ni3.*

Learning with always trumps learning from.

—Woodie Flowers

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Preface

This is a book about *relational programming*. Just as functional programs model mathematical functions, relational programs model mathematical relations. Relational programming is intimately related to both logic programming and relational algebra, the theory behind relational databases.

Relational programs generalize functional programs, in that they do not distinguish between the “input” arguments passed to a function and the “output” result returned by that function. For example, consider a two-argument variant of Scheme’s addition function, restricted to natural numbers: $(+ \ 3 \ 4) \Rightarrow 7$. A relational version of addition, which we’ll call $+^o$, takes three arguments: $(+^o \ 3 \ 4 \ z)$, where z is a *logic variable* that represents the result of adding the first two arguments of $+^o$. In this case z is associated with 7. More interestingly, we can write $(+^o \ 3 \ y \ 7)$, which associates y with 4; our addition relation also performs subtraction. We can also write $(+^o \ x \ y \ 7)$, which associates x and y with all pairs of natural numbers that sum to 7; $+^o$ then produces multiple answers, including $x = 3$ and $y = 4$, and $x = 0$ and $y = 7$. Finally, we can write $(+^o \ x \ y \ z)$, which enumerates all triples of natural numbers (x, y, z) such that $x + y = z$; here our $+^o$ relation produces infinitely many answers. Informally, we say that the call $(+^o \ 3 \ 4 \ z)$ runs the $+^o$ relation “forwards” (that is, in the same direction as the corresponding Scheme function), while the calls $(+^o \ 3 \ y \ 7)$, $(+^o \ x \ y \ 7)$, and $(+^o \ x \ y \ z)$ run $+^o$ “backwards.”

The remarkable flexibility of the $+^o$ relation is also exhibited by more complex relations, such as interpreters, type inferencers, and finite-state machines, as will be demonstrated in this book. For example, consider $eval^o$, a relational interpreter for a subset of Scheme. Running $eval^o$ forwards, the call $(eval^o \ '((\lambda (x) (+ \ x \ 2)) \ 4) \ val)$ associates val with 6. Of course, we can also run $eval^o$ backwards: $(eval^o \ exp \ '6)$ generates legal Scheme expressions that *evaluate* to 6, while $(eval^o \ exp \ exp)$ generates *quines*, which are Scheme expressions that evaluate to themselves.

This book will teach you how to write interesting relations, including the quine-generating $eval^o$ relation above. We will see that

If you know nothing about logic programming, relational algebra, or databases, *don't panic!* This book only assumes that you can write simple recursive programs in a functional language, and have a reading knowledge of Scheme. See the *Audience* section below for details.

The *natural numbers* are the non-negative integers: 0, 1, ...

Here we are taking a notational liberty, as $+^o$ expects 3 and 4 to be represented as *binary, little-endian* lists: (1 1) and (0 0 1), respectively. Zero is uniquely represented as the empty list, (). To ensure a unique representation of each number, lists may not end with the digit 0. This numeric representation is extremely flexible, since the lists can contain logic variables—for example, the list '(1 . x) represents any odd natural number, while '(0 . x) represents any positive even natural.

We can also perform relational arithmetic on built-in Scheme numbers, using *Constraint Logic Programming over Finite Domains*, or CLP(FD); as we will see in the book, CLP(FD) is faster, but less general, than $+^o$ and friends ($*^o$, $/^o$, etc.).

As might be expected, $eval^o$ will interpret the quoted list $(+ \ x \ 2)$ as the call $(+^o \ x \ 2 \ val)$, where the logic variable x is associated with 4.

Douglas Hofstadter coined the term *quine*, in honor of logician Willard Van Orman Quine (1908–2000). Writing quines has long been a favorite hacker activity, and quines are often featured in the The International Obfuscated C Code Contest (<http://www.ioccc.org/>). A delightful introduction to quines can be found in Doug’s classic, *GEB*:

D. R. Hofstadter. *Gödel, Escher, Bach: an Eternal Golden Braid*. Basic, 1979

running a relation in the forward direction is often simple; running a relation backwards is where the real fun begins.

Audience

This book is written for intermediate-to-advanced programmers, computer science students, and researchers. For this book, *intermediate* means that you are comfortable writing simple recursive procedures in a functional programming language, such as Scheme, Racket, Clojure, Lisp, ML, or Haskell. I also assume you have a reading knowledge of Scheme. No knowledge of relational programming, logic programming, or programming language theory is required.

If you want to learn about relational programming, but are new to programming, Dan Friedman, Oleg Kiselyov, and I have written a book just for you, called *The Reasoned Schemer*¹. In that book we assume you are familiar with the material in *The Little Schemer*², which is a very gentle introduction to recursion and functional programming.

If you are an experienced programmer, but weak on recursion, you, too, might benefit from *The Little Schemer*. If you are comfortable with recursion, but not functional programming, good introductions include *Scheme and the Art of Programming*³ and the classic *Structure and Interpretation of Computer Programs*⁴.

If you are an experienced functional programmer, but do not know Scheme, the beginning of *Structure and Interpretation of Computer Programs* should get you up to speed, while *The Scheme Programming Language, 4th Edition*⁵ describes the language in detail.

The Language

Goals

The two high-level goals for this book are to **make relational programming accessible** to a broader audience, and to **describe the state-of-the-art** in the design, implementation, and use of the miniKanren language. An important side-effect of these goals is to **provide the background** needed to understand academic work on miniKanren.

One sub-goal of this book is to **present a variety of non-trivial miniKanren relations**, written in what I consider to be **idiomatic style**, and to show **how these relations were derived**. Many of these examples draw from academic papers on miniKanren, and focus on programming language theory (interpreters, type inferencers, etc.). Other examples, such as finite state machines, should be immediately understandable by a wider audience of programmers. To make the book as accessible as possible, all of these concepts are explained

All too often, the fun never ends, as the relation diverges (loops forever).

I have attempted to deliver [these lectures] in a spirit that should be recommended to all students embarking on the writing of their PhD theses: imagine that you are explaining your ideas to your former smart, but ignorant, self, at the beginning of your studies!

—Richard P. Feynman
The Feynman Lectures on Computation

¹ D. P. Friedman, W. E. Byrd, and O. Kiselyov. *The Reasoned Schemer*. MIT Press, Cambridge, MA, 2005

² D. P. Friedman and M. Felleisen. *The Little Schemer (4th ed.)*. MIT Press, Cambridge, MA, 1996

³ G. Springer and D. P. Friedman. *Scheme and the Art of Programming*. MIT Press, Cambridge, MA, 1989

⁴ H. Abelson and G. J. Sussman. *Structure and Interpretation of Computer Programs*. MIT Press, Cambridge, MA, 2nd edition, 1996

(full text at <http://mitpress.mit.edu/sicp/full-text/book/book.html>)

⁵ R. K. Dybvig. *The Scheme Programming Language, 4th Edition*. The MIT Press, 4th edition, 2009

(full text at <http://www.scheme.com/tspl4/>)

To some extent, this book can be thought of as an updated, greatly expanded, and much more accessible version of my dissertation (full text at <http://gradworks.umi.com/3380156.pdf>):

W. E. Byrd. *Relational Programming in miniKanren: Techniques, Applications, and Implementations*. PhD thesis, Indiana University, 2009

either in the main text or in appendices. This book can therefore be used as an informal **introduction to programming language concepts**.

Margin Notes

This book is typeset in the style of Edward Tufte’s magnificent and beautiful *The Visual Display of Quantitative Information*⁶. I share Tufte’s love of margin notes, and use them in this book to help solve the problem of addressing readers with widely varying knowledge of computer science and programming. To make the book as accessible as possible, in the main text I assume the reader is the hypothetical *intermediate-level* programmer or student described in the *Audience* section above. In the margin notes, however, anything goes, and I reserve the right to geek out whenever necessary (or unnecessary).

Typographic Conventions

Acknowledgements

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July 2013

I hope to emulate the success of Benjamin Pierce’s outstanding *TAPL*, which is about types in programming languages, but also contains excellent introductions to other PL-related topics:

B. C. Pierce. *Types and Programming Languages*. MIT Press, Cambridge, MA, 2002

This book is set using the “Tufte-Style Book” L^AT_EX style, freely available from <http://www.LaTeXTemplates.com>

⁶ E. R. Tufte. *The Visual Display of Quantitative Information*. Graphics Press, Cheshire, CT, 1986

Another great lover of marginalia was David Foster Wallace (1962–2008). The *Harry Ransom Center’s* DFW collection includes heavily annotated books from Wallace’s personal library: <http://www.hrc.utexas.edu/press/releases/2010/dfw/books/>. Wallace’s love of margin notes is best demonstrated by his essay, “Host,” in:

D. F. Wallace. *Consider the Lobster and Other Essays*. Little, Brown and Co., 2005

Introduction

gl hf!

—Greg “IdrA” Fields

Conclusion

G.G.

—Sean “Day[9]” Plott

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