#### Relational Interpreters in miniKanren

## $({\rm WORKING\ ROUGH\ DRAFT-DRAFT\ }0)$

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January 18, 2025

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#### To Dan Friedman

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#### **Preface**

The intent of this book is to share the techniques, knowledge, pitfalls, open problems, promising-looking future work/techniques, and literature of writing interpreters as relations in miniKanren. Someone who reads this book actively should be ready to understand, implement, modify, and improve interpreters written as miniKanren relations, read the related literature, and perform original research on the topic.

#### 0.1 What this book is about

This book is about writing interpreters for programming languages, especially for subsets of Scheme. While there are many books on writing interpreters, this book is unusual in that it explores how to write interpreters as relations in the miniKanren relational programming language. By writing interpreters as relations, and by using the implicit constraint solving and search in the faster-miniKanren implementation, we can use the flexibility of relational programming to allow us to experiment with programs in the language being interpreted. For example, a relational interpreter can interpret a program with missing subexpressions<sup>1</sup>, or holes, attempting to fill in the missing subexpressions with values that result in valid programs in the language being interpreted. Or we can give both a program containing holes and the value we expect the program to produce when interpreted, and let faster-miniKanren try to fill in the holes in a way to produce the expected output. We can even write an interpreter that explicitly handles errors, and ask faster-miniKanren to find inputs to the program that trigger these errors.<sup>2</sup>

#### 0.2 What you need to know to read this book

This book assumes you are familiar with the basics of Scheme or Racket, and are comfortable with the ideas of functionals programming. The book also assumes you understand the notions of evaluation order of expressions, lexical scope, environments, environment-passing interpreters.

<sup>&</sup>lt;sup>1</sup>Such programs are often called *program sketches* [TODO cite].

<sup>&</sup>lt;sup>2</sup>This is known in the literature as "angelic execution".

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[TODO add topics that the reader should know, including Scheme, miniKanren, lexical scope, environment-passing interpreters, etc]
[TODO add pointers to resources]

#### 0.3 Running the code in this book

The code in this book was tested with Chez Scheme and Racket. It should be possible to run most code in other Scheme implementations, with few or no changes, with the exception of code that makes extensive use of Chez-specific or Racket-specific features, which I will point out in those chapters, as appropriate.

#### 0.3.1 Getting pmatch from GitHub

#### 0.3.2 Getting faster-miniKanren from GitHub

https://github.com/michaelballantyne/faster-miniKanren

git clone git@github.com:michaelballantyne/faster-minikanren.git

Alternatively, you can click on <> Code button and select Download ZIP to download and uncompress the .zip file containing the entire faster-miniKanren directory.

#### 0.3.3 Using this book with Chez Scheme

**Installing Chez Scheme** 

Starting a Chez Scheme REPL

Loading a file in Chez Scheme

Loading faster-miniKanren in Chez Scheme

#### 0.3.4 Using this book with Racket

**Installing Racket** 

```
https://racket-lang.org/
https://download.racket-lang.org/
```

#### Important differences between Chez Scheme and Racket

representation of quoted values evaluation order language levels macros The DrRacket IDE and the Racket REPL Starting and configuring DrRacket

changing default language changing default memory limit

Starting a Racket REPL

Requiring a module in Racket

Requiring the faster-miniKanren module in Racket

#### 0.4 Acknowledgements

Dan Friedman and Michael Ballantyne both encouraged me to continue working on this book, and independently encouraged me to break down one giant book into more than one book, each book being more manageable. Both Dan and Michael encouraged me to avoid getting bogged down with a lot of introductory material, which had caused me to abandon previous writing efforts. Michael also encouraged me to continue working on the book in the open.

Darius Bacon wrote me a very helpful email about how using two separate lists to represent a lexical environment, rather than a single association list, can result in better performance and divergence behavior. I had played around with this representation in the past, but had abandoned it before I understood its advantages. Thank you, Darius.

My mother has continually encouraged me to work on this book, and most importantly, to finish it!

[TODO add other acknowledgements]

[TODO add acks for type setting tech, such as the fonts; also can add colophon if  ${\rm I'm}$  so inclined] x PREFACE

# A simple environment-passing Scheme interpreter in Scheme

call-by-value (CBV)  $\lambda$ -calculus (variable reference, single-argument lambda, and procedure application), plus quote and list

association-list representation of the environment empty initial environment

list is implemented as if it were a special form rather than as a variable bound, in a non-empty initial environment, to a procedure. As a result, although list can be shadowed, (list list) results in an error that there is an attempt to reference an unbound variable list.

tagged list to represent closure grammar for the language we are interpreting

```
(load "pmatch.scm")
```

[TODO make sure I explain MIT vs Indiana syntax for define]

```
(define (eval expr)
  (eval-expr expr '()))

(define (eval-expr expr env)
  (pmatch expr
        ((quote ,v)
        (guard (not-in-env? 'quote env))
        v)
        ((list . ,e*)
```

```
(guard (not-in-env? 'list env))
     (eval-list e* env))
   (,x
     (guard (symbolo? x))
     (lookup x env))
   ((,rator ,rand)
     (let ((a (eval-expr rand env)))
       (pmatch (eval-expr rator env)
         ((closure ,x ,body ,env^)
          (guard (symbol? x))
          (eval-expr body `((,x . ,a) . ,env^)))))
   ((lambda (,x) ,body)
     (guard (and (symbol? x)
                 (not-in-env? 'lambda env)))
     `(closure ,x ,body ,env))))
(define (not-in-env? x env)
 (pmatch env
   (((,y . ,v) . ,env^)
     (if (equal? y x) ;; TODO eq? vs eqv? vs equal?, with equal? being semantically cl-
         (not-in-env? x env^)))
   (() #t))) ;; TODO empty env clause comes second; Dijkstra guard, and all that
(define (eval-list expr env)
 (pmatch expr
   (() '())
   ((,a . ,d)
     (let ((t-a (eval-expr a env))
           (t-d (eval-list d env)))
       `(,t-a . ,t-d)))))
(define (lookup x env)
 (pmatch env
   (() (error 'lookup "unbound variable")) ;; TODO make sure error is introduced, and
   (((,y . ,v) . ,env^)
     (if (equal? y x)
         (lookup x env^)))))
```

# Rewriting the simple environment-passing Scheme interpreter in miniKanren

In this chapter we will translate the evaluator for the simple environment-passing interpreter from the previous chapter from a Scheme function to a miniKanren relation.

[TODO cite the code from the Quines interp in faster-miniKanren, and point to the  $2012~\mathrm{SW}$  paper on Quines]

[TODO this interp uses defrel—do I want to stick with defrel, or use define + lambda? Or maybe the book shows both (probably needs to show both at some point)]

```
(not-in-envo 'list env)
       (absento 'closure e*) ;; TODO is this absento really needed, if we have absento
       (eval-listo e* env val)))
   ((symbolo expr) (lookupo expr env val))
   ((fresh (rator rand x body env^ a)
       (== `(,rator ,rand) expr)
       (eval-expro rator env `(closure ,x ,body ,env^))
       (eval-expro rand env a)
       (eval-expro body `((,x . ,a) . ,env^) val)))
   ((fresh (x body)
       (== `(lambda (,x) ,body) expr)
      (symbolo x)
       (not-in-envo 'lambda env)
       (== `(closure ,x ,body ,env) val)))))
(defrel (not-in-envo x env)
 (conde
   ((fresh (y v env^)
      (== `((,y . ,v) . ,env^) env)
       (=/= y x)
       (not-in-envo x env^)))
   ((== '() env))))
(defrel (eval-listo expr env val)
 (conde
   ((== '() expr)
    (== '() val))
   ((fresh (a d t-a t-d)
      (== `(,a . ,d) expr)
      (== `(,t-a . ,t-d) val)
       (eval-expro a env t-a)
       (eval-listo d env t-d)))))
(defrel (lookupo x env t)
 (fresh (y v env^)
   (== `((,y . ,v) . ,env^) env)
   (conde
      ((== y x) (== v t))
      ((=/= y x) (lookupo x env^ t)))))
```

## Quine time

```
McCarthy challenge given in 'A Micromanual for LISP'
(run 1 (e) (evalo e e))
=>
(((((lambda (_.0) (list _.0 (list 'quote _.0)))
   '(lambda (_.0) (list _.0 (list 'quote _.0))))
  (=/= ((_.0 closure)) ((_.0 list)) ((_.0 quote)))
  (sym _.0)))
> ((lambda (_.0) (list _.0 (list 'quote _.0)))
    '(lambda (_.0) (list _.0 (list 'quote _.0))))
((lambda (_.0) (list _.0 (list 'quote _.0)))
  '(lambda (_.0) (list _.0 (list 'quote _.0))))
   We replace \_.0 with the arbitrary free variable name x to produce the canon-
ical LISP/Scheme Quine:
((lambda (x) (list x (list 'quote x)))
 '(lambda (x) (list x (list 'quote x))))
> ((lambda (x) (list x (list 'quote x)))
   '(lambda (x) (list x (list 'quote x))))
((lambda (x) (list x (list 'quote x)))
  '(lambda (x) (list x (list 'quote x))))
  Twines
   every Quine is trivially a Twine; we can add a disequality constraint to
ensure p and q are distinct terms
> (run 1 (p q)
    (=/= p q)
```

```
(evalo p q)
    (evalo q p))
[TODO add the answer]
   Thrines
> (run 1 (p q r)
    (=/= p q)
    (=/= p r)
    (=/= q r)
    (evalo p q)
    (evalo q r)
    (evalo r p))
[TODO add the answer]
   Structurally boring Quines, Twines, and Thrines
   just moving quotes around
   absento trick to generate more interesting Quines, Twines, and Thrines
> (run 1 (p q)
    (absento p q)
    (absento q p)
    (evalo p q)
    (evalo q p))
[TODO add the answer]
   [similarly for Thrines]
   Revisiting our original Quine query with the absento trick
(run 1 (p)
  (fresh (expr1 expr2)
    (absento expr1 expr2)
    (== `(,expr1 . ,expr2) p)
    (evalo p p)))
=>
((((lambda (_.0)
     (list (list 'lambda '(_.0) _.0) (list 'quote _.0)))
   '(list (list 'lambda '(_.0) _.0) (list 'quote _.0)))
  (=/= ((_.0 closure)) ((_.0 list)) ((_.0 quote)))
  (sym _.0)))
```

 $<sup>^{1}</sup>$ I thank Larry Moss and the Indiana University Logic Symposium [TODO check the name of the symposium] for inviting me to give a talk where I demonstrated Quine generation, and where Larry suggested I tried generating Twines.

# Using a two-list representation of the environment

association-list representation of an environment where x is mapped to the list (cat dog) and y is mapped to 5:

```
((x . (cat dog))
 (y.5)
   "split" two-list representation of the same environment:
(x y); variables
((cat dog) 6); values
   ;; a-list env ;; ((x . (cat dog)) ;; (y . 5))
   ;; split env ;; (x y) ;; ((cat dog) 6)
   absento trick for lazy not-in-envo
   ;; (absento 'closure expr)
  ;; (absento t1 t2)
   ;; (not-in-envo 'lambda env) ;; (absento 'lambda '(x y))
(defrel (evalo expr val)
  (eval-expro expr '(() . ()) val))
(defrel (eval-expro expr env val)
  (conde
    ;; quote, list, and variable reference/lookup clauses elided
    ((fresh (rator rand body env^ a x x* v*)
       (== `(,rator ,rand) expr)
       (== `(,x* . ,v*) env^)
```

```
(eval-expro rator env `(closure ,x ,body ,env^))
       (eval-expro rand env a)
       (eval-expro body
                   `((,x . x*) . (,a . v*))
                  val)))
    ;; lambda clause elided
    ))
(defrel (not-in-envo x env)
  (fresh (x* v*)
    (== `(,x* . ,v*) env)
    (absento x x*)))
   [TODO discuss tradeoffs between asserting (symbolo x) in these helper
relations—how stand-alone do we want them?]
(defrel (lookupo x env t)
  (fresh (y x* v v*)
    (== `((,y . ,x*) . (,v . ,v*)) env)
    (conde
      ((== y x) (== v t))
      ((=/= y x) (lookupo x `(,x* . ,v*) t)))))
```

# Extending the interpreter to handle append

add cons, car, cdr, null?, and if extend lambda and application to handle multiple arguments and variadic

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# Using a non-empty initial environment

new case to handle prim app rather than user-defined closure app
 cons, car, cdr, and null? bound in the initial env to prims
 list bound in the initial env to the closure that results from evaluating the
 variadic (lambda x x)

Adding explicit errors

# Angelic execution

[TODO look at my code from PolyConf 2015, which includes an interpreter for an imperative language, along with angelic execution]

# Adding mutation

[TODO look at my code from PolyConf 2015, which includes an interpreter for an imperative language, along with angelic execution]

support set! (can we get away with supporting set! without adding a store?)

support mutiple pairs and have an explicit store

# Adding delimited control operators

delimited continuations and/or effect handlers—can we do so in such a way that avoids "breaking the wires"?

talk about the problem with call/cc and breaking the wires

Writing a parser as a relation

Writing a type inferencer as a relation

Build your own Barliman

# Speeding up the interpreter

[restrict to interpreter changes that don't require hacking faster-miniKanren or in-depth knowledge of the implementation]

dynamic reordering of conjuncts, especially for application fast environment lookup for environments that are sufficiently ground

Open problems