

Primary property: When counting, only one bit changes at a time.  
In binary code, as many as 3 bits can change at a time (e.g., 011  $\rightarrow$  100)

A couple of ways to generate Gray code:

Recursively:

1-bit  
code

0  
1

2-bit  
code

0 0  
0 1  
1 1  
1 0

↑  
prepend

3-bit  
code

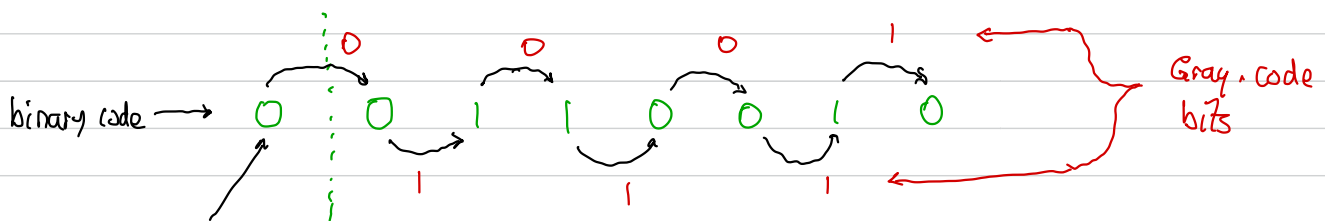
0 00  
0 01  
0 11  
0 10  
1 10  
1 11  
1 01  
1 00

↑  
prepend

Another way: Start with a binary code

— scan left-to-right; catalog bit changes  
(record 1 for change, 0 for no change).

Example: Convert 0110010<sub>2</sub> to Gray code



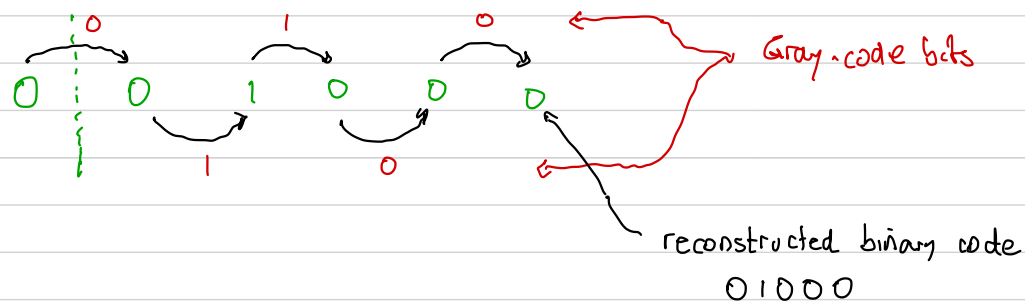
assume a zero  
as starting point

Gray code: 0101011

Going from Gray to binary

— Gray code tells us how to reconstruct a binary code.

Example: convert 01100 to binary



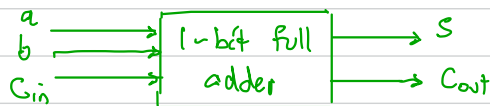
## Logic gates

We know how to use binary variables to represent information. We now explore logic circuits. Two important classes:

Combinational circuits: outputs depend only on current values of inputs.

Sequential circuits: same, but also depends on the history of inputs (a later course topic)

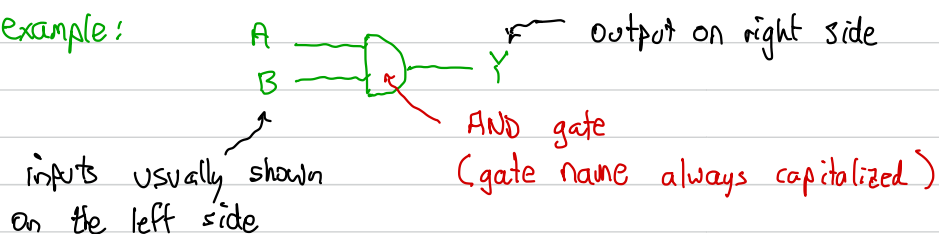
Simple combinational circuits:



A key building block in digital circuits is a logic gate.

Logic gate: a combinational circuit with 1 or more inputs, and one output.

for example:



$$Y = AB$$

Relationship between inputs and outputs are described by a truth table, or Boolean expression

## 1- input gates

The NOT gate, also called an inverter.



the "bubble" denotes inversion.

$$Y = \bar{A} \quad \text{"Y equals NOT A"}$$

Notation: The inversion is denoted algebraically with an overbar  $Y = \bar{A}$

~ previous ENEC 353 textbooks use  $Y = A'$  <sup>apostrophe</sup>

Truth table:

A	Y
0	1
1	0

## The buffer gate



Truth table

A	Y
0	0
1	1

Y is simply a copy of A

The buffer behaves as a wire does

- however, it's a useful gate to have to improve reliability of some large circuits.