

Number system and conversions (section 1.4 of textbook)

Vikas Dhiman for ECE275

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6 Signed binary numbers

Signed numbers include both negative and positive numbers. There three common signed number representations

1. Sign magnitude representation
2. One's complement
3. Two's complement

6.1 Sign-magnitude representation

The Most significant (left most) *bit* (binary digit) represents sign ($0 = +$ and $1 = -$), the rest represent the magnitude. Example, a 5-bit number $(11010)_2$ in signed magnitude representation has the value of $(-1010)_2 = -10$. Note that $+10$ has to be represented by a leading 0 at the most significant bit (MSB) $+10 = (01010)_2$. Hence, the number of bits have to be specified.

Problem 5 • Write down all possible 4-digit binary numbers and corresponding decimal values if they are in signed magnitude format? What is the minimum and maximum value?

- What is the minimum and maximum value of n -digit signed binary number in sign-magnitude format?

4-digit	Binary	Decimal
	0000	= +0
	0001	= +1
	0010	= +2
	0011	= +3
	0100	= +4
	0101	= +5
	0110	= +6
	0111	= +7
	1000	= -0
	1001	= -1
	1010	= -2
	1011	= -3
	1100	= -4
	1101	= -5
	1110	= -6
	1111	= -7

$(0000)_2 = (1000)_2$

Max $2^3 - 1$

Min $-(2^3 - 1)$

n -digit

$2^{n-1} - 1$

$-(2^{n-1} - 1)$

6.2 One's complement negation

Negate $13_{10} = 01101_2$ using 5-bit one's complement.

Negate -13_{10} using 5-bit one's complement.

6.3 One's complement binary numbers

Problem 6 *Determine the decimal values of the following 1's complement 6-digit binary numbers :*

1. *01101110*

2. *10101101*

Problem 7 *Convert the decimal numbers -17 and +23 into the 6-digit one's complement binary numbers and try adding them. What adjustments will you need to make to get the right result's (23-17=6) in binary representation.*

6.4 Two's complement negation

Negate $13_{10} = 01101$ using 5-bit two's complement.

Negate -13_{10} using 5-bit two's complement.

6.5 Two's complement representation

Problem 8 *Determine the decimal values of the following 2's complement 6-digit numbers :*

1. *01011110*

2. *10010111*

Problem 9 *Convert the decimal numbers -17 and +23 into the 6-digit two's complement binary numbers and try adding them. What adjustments will you need to make to get the right result's (23-17=6) in binary representation.*

Problem 10 *Convert the decimal numbers 73, 23, -17, and -163 into signed 8-bit numbers in the following representations:*

1. *Sign and magnitude*
2. *1's complement*
3. *2's complement*

6.6 Arithmetic overflow

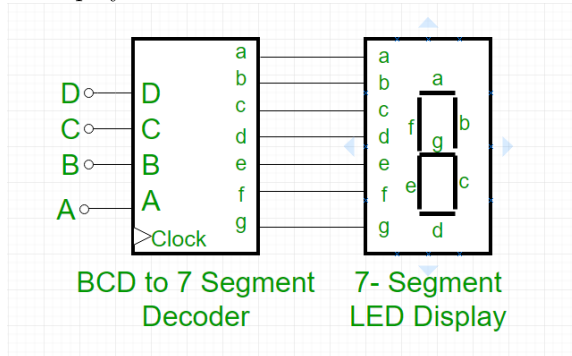
Problem 11 *Consider addition of 4-digit two's complement binary numbers*

1. $1010_2 + 1101_2$
2. $1011_2 + 1100_2$

In which case overflow happens? Can you come up with a rule to easily detect overflow?

7 Binary coded decimal

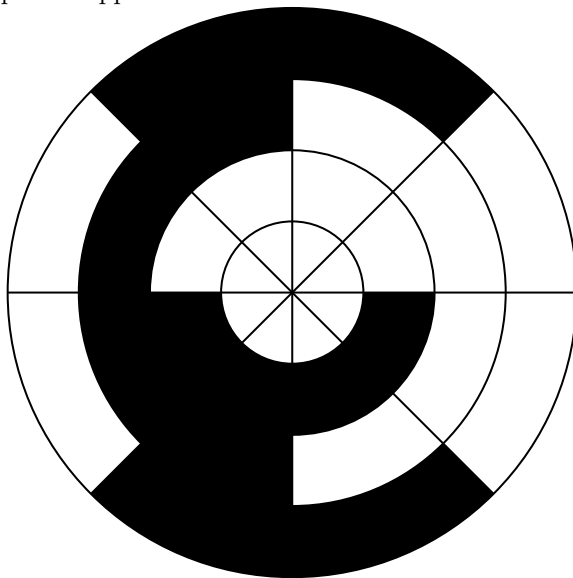
In Binary coded decimal (BCD), each decimal digit is represented by 4 bits. For example, $1047 = (0001.0000.0100.0111)_{BCD}$. It is useful in input-output applications where the number has to be either displayed as decimal or received as decimal.



Problem 12 Convert 11, 23, 35, 57 and 103897 to BCD?

8 Gray code

A sequence of binary numbers where only one bit changes when the number increases by 1. It is helpful in applications like wheel encoders



Problem 13 Write all possible 3-bit binary numbers in gray-code