

Analog details behind the digital abstraction

Vikas Dhiman for ECE275

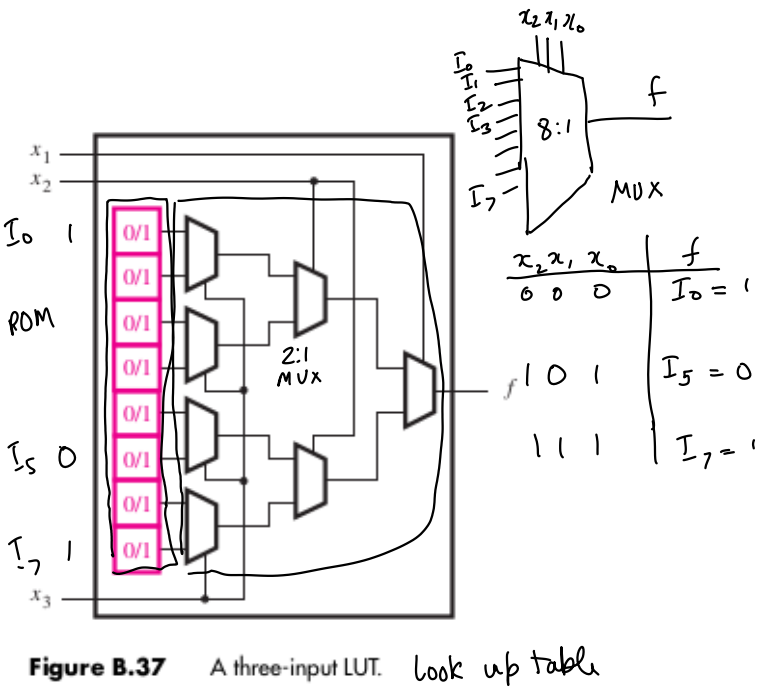
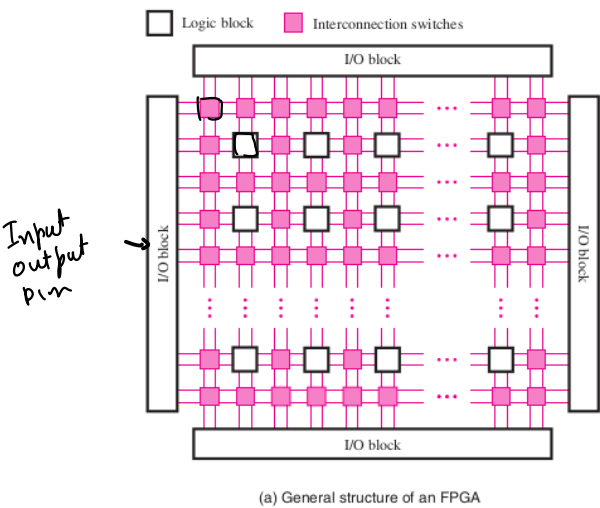
November 17, 2023

Some of the material is out of the textbook. Additional resources include Appendix B of Brown and Vranesic book, “Fundamentals of digital logic.”

1 Objectives

1. Describe how tri-state and open-collector outputs are different from totem-pole outputs
2. Compute noise margin of one device driving the same time

2 FPGA [1, Section B.6.5]



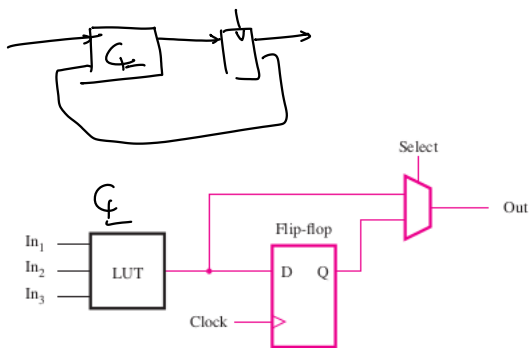


Figure B.38 Inclusion of a flip-flop in an FPGA logic element.

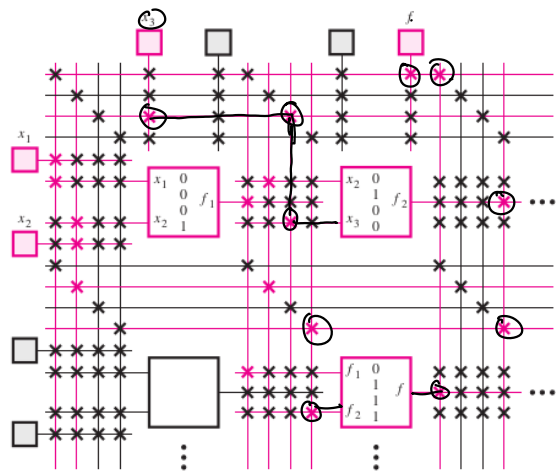


Figure B.39 A section of a programmed FPGA.

Definition 1 (Random Access Memory (RAM)). *Structure of a RAM is as follows:*

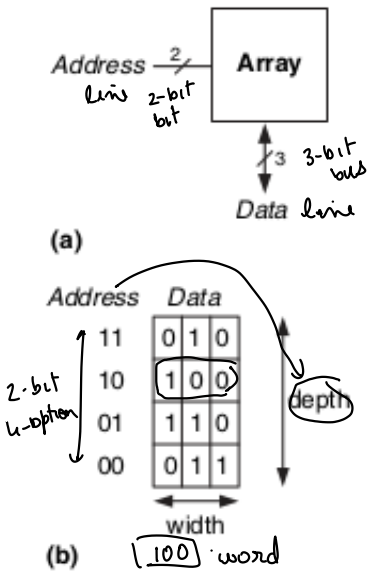


Figure 5.39 4 × 3 memory array: (a) symbol, (b) function

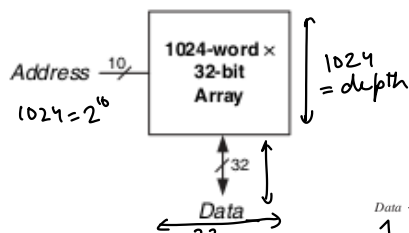


Figure 5.40 32 Kb array: depth = $2^{10} = 1024$ words, width = 32 bits

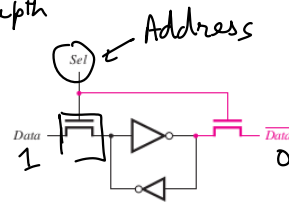
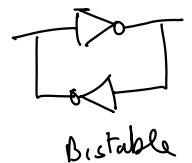


Figure B.64 An SRAM cell.



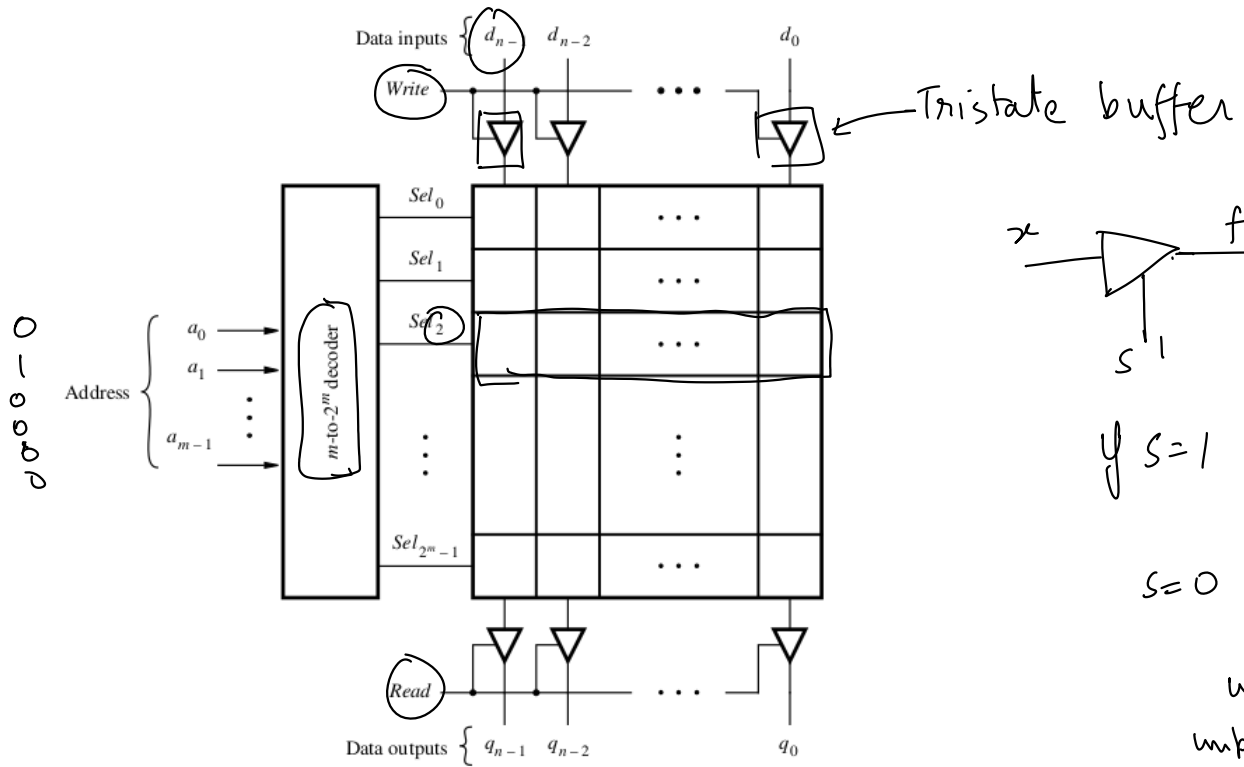
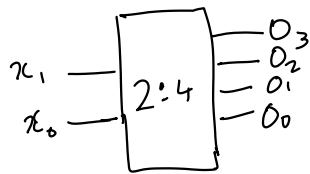


Figure B.66 A $2^m \times n$ SRAM block.

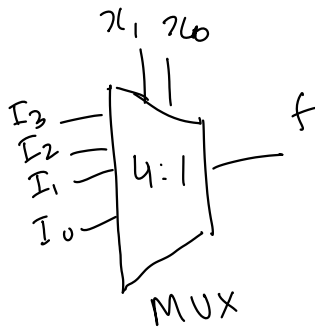
Definition 2 (Read Only Memory (ROM)). Structure of a ROM is as follows:

Decoder



Decoder

3:8, 4:16



x_1	x_0	O_3	O_2	O_1	O_0
0	0	0	0	0	1
0	1	0	0	1	0
1	0	0	1	0	0
1	1	1	0	0	0

x_1	x_0	f
0	0	I_0
0	1	I_1
1	0	I_2
1	1	I_3

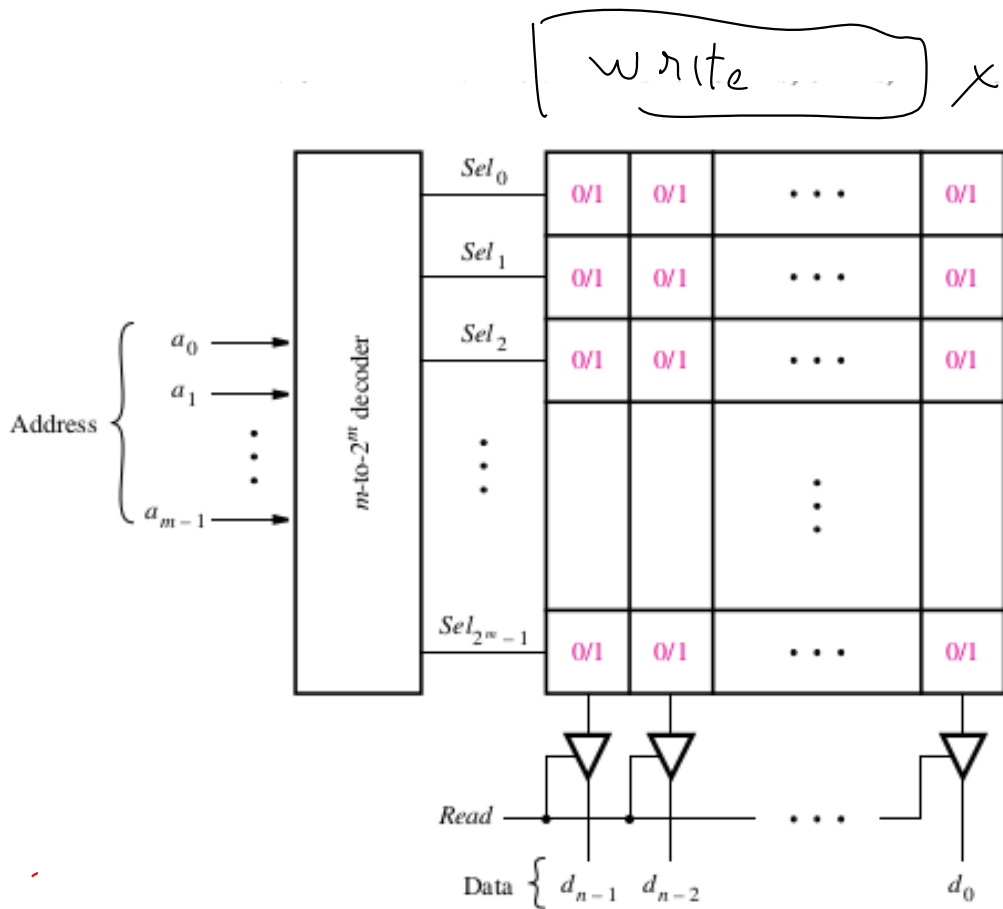
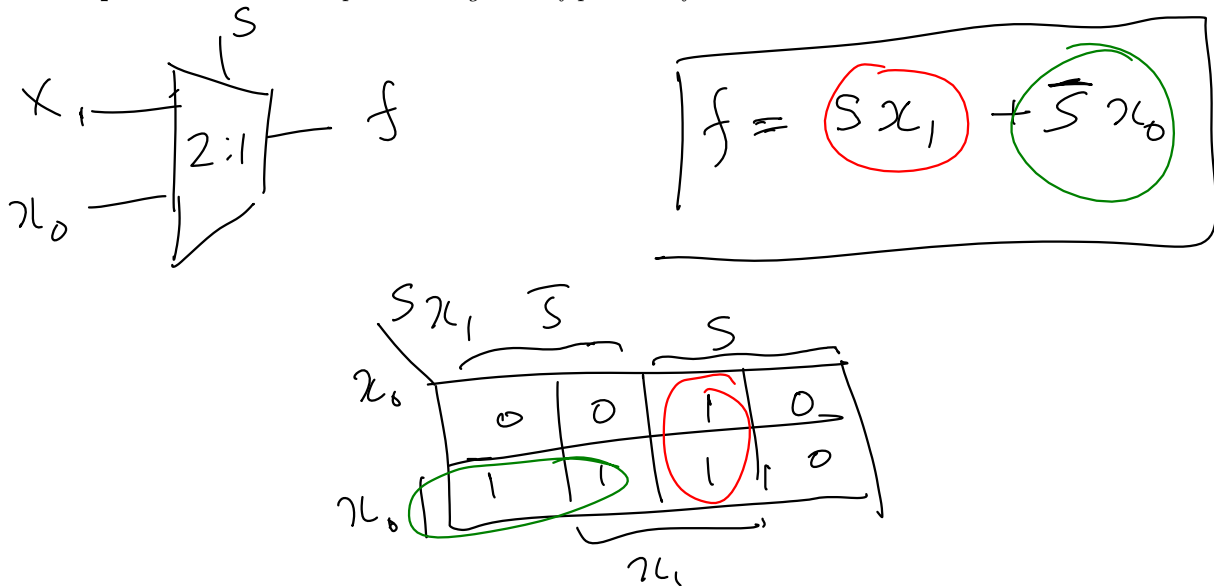
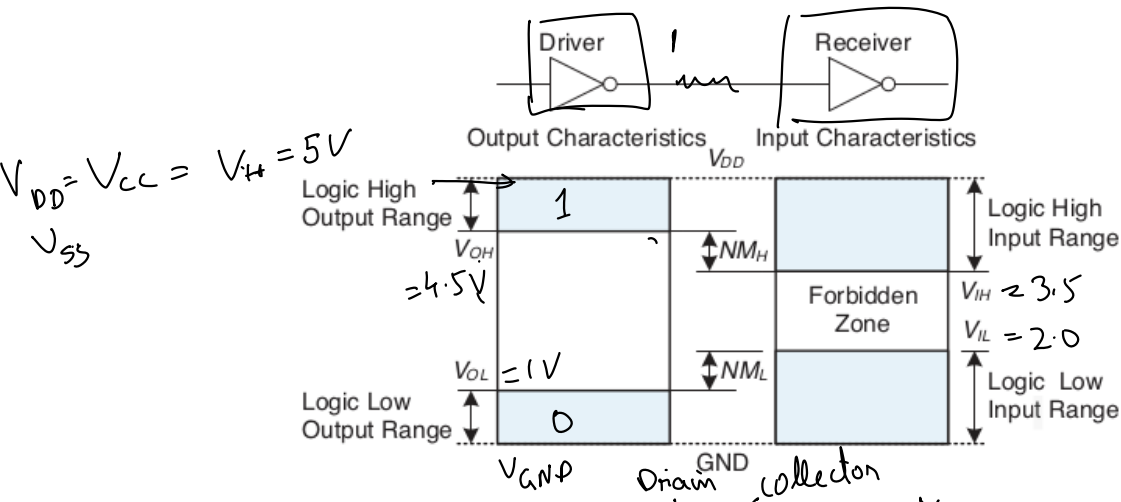


Figure B.72 A $2^m \times n$ read-only memory (ROM) block.

Example 1. Draw a Multiplexer using sum of products form.



3 Logic levels and Noise Margins



Boolean	Voltage
1	5V - 4.5V
0	0V - 1.0V

Positive logic

$$V_{IH} = 3.5V$$

$$V_{IL} = 2.0V$$

Definition 3 (Supply Voltage ($V_{DD}/V_{CC}/V_{SS}$)).

The highest voltage a circuit can output

Definition 4 (Ground Voltage (V_{GND})).

The lowest

Definition 5 (Input high (V_{IH}) and Input Low (V_{IL}) of a gate).

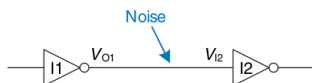
Definition 6 (Output high (V_{OH}) and Output low (V_{OL}) of gate).

Assume positive logic | for boolean output 1, $V_{OH} \leq V \leq V_{CC}$ | for '1'
Boolean 1 | V_{OH} is the lowest acceptable output voltage for boolean 1
0 | V_{OL} is the highest acceptable output voltage for boolean 0

Definition 7 (Positive logic and Negative logic).

Pos Logic V_{CC}
Neg Logic V_{GND}

Definition 8 (Noise margins (NM_L and NM_H) of a channel).



Example 2.

If $V_{DD} = 5V$, $V_{IL} = 1.35V$, $V_{IH} = 3.15V$, $V_{OL} = 0.33V$ and $V_{OH} = 3.84V$ for both the "inverters", then what are the low and high noise margins? Can the circuit tolerate 1V of noise at the channel?

$$NM_H = 0.69 = V_{OH} - V_{IH} = 3.84 - 3.15$$

$$NM_L = 1.02 = V_{IH} - V_{OL} = 3.15 - 0.33$$

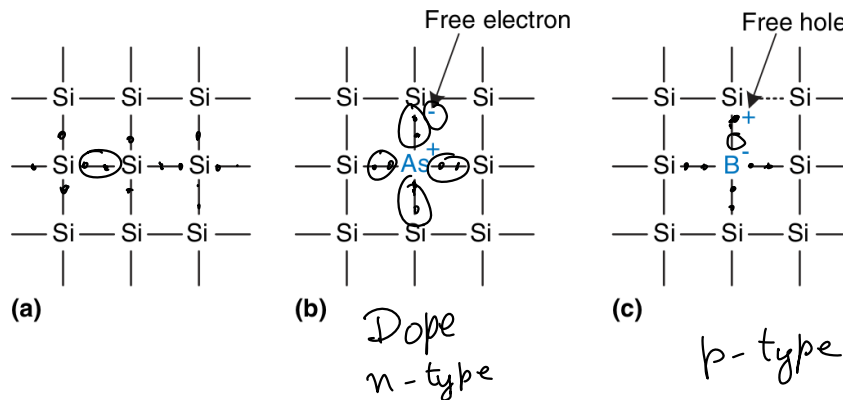
4 Semiconductors and Doping

Not in syllabus but good to know

Elements recognized as metalloids V•T•E

	13	14	15	16	17
2	B Boron	C Carbon	N Nitrogen	O Oxygen	F Fluorine
3	Al Aluminium	Si Silicon	P Phosphorus	S Sulfur	Cl Chlorine
4	Ga Gallium	Ge Germanium	As Arsenic	Se Selenium	Br Bromine
5	In Indium	Sn Tin	Sb Antimony	Te Tellurium	I Iodine
6	Tl Thallium	Pb Lead	Bi Bismuth	Po Polonium	At Astatine

Commonly recognized (86–99%): B, Si, Ge, As, Sb, Te
Irregularly recognized (40–49%): Po, At
Less commonly recognized (24%): Se
Rarely recognized (8–10%): C, Al
(All other elements cited in less than 6% of sources)
 Arbitrary metal-nonmetal dividing line: between Be and B, Al and Si, Ge and As, Sb and Te, Po and At



ECE 341
Nuri

5 MOSFET: Metal Oxide Field Effect Transistors

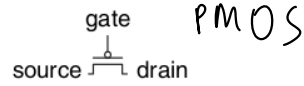
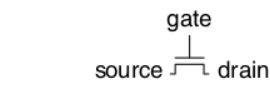
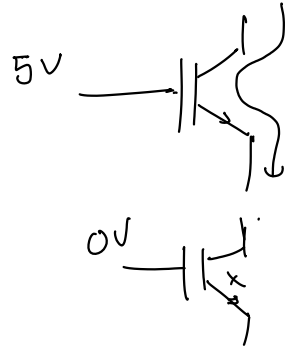
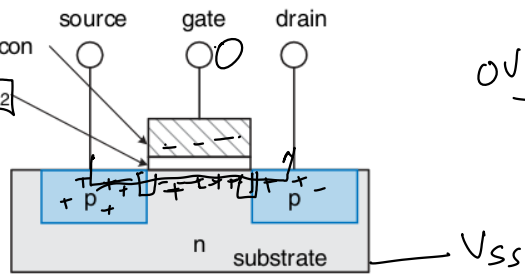
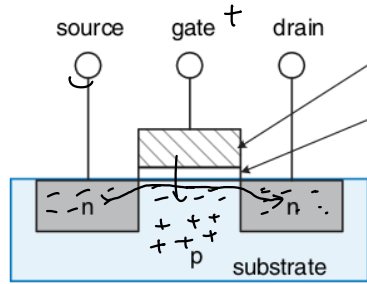
Not in syllabus but good to know

MOSFET

nMOS

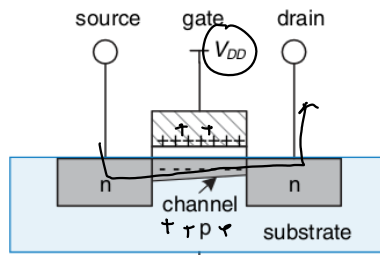
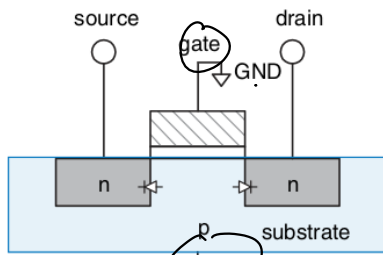
pMOS

Field



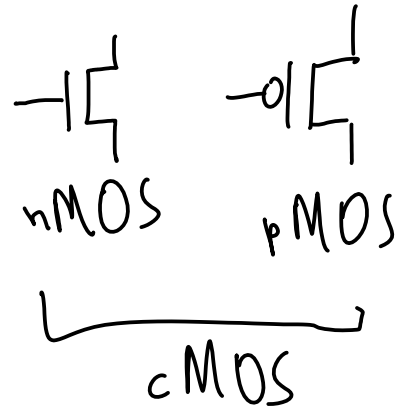
(a) nMOS

(b) pMOS

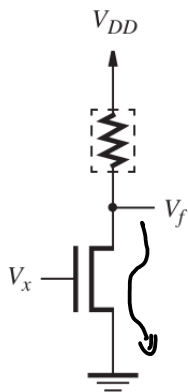


(a)

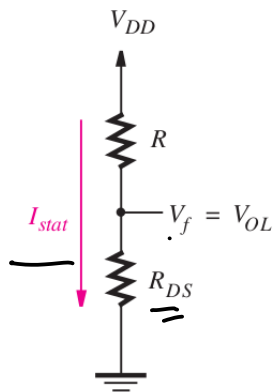
(b)



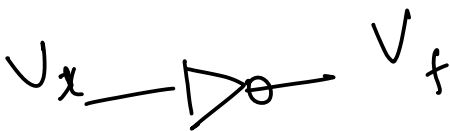
6 DC Transfer characteristic



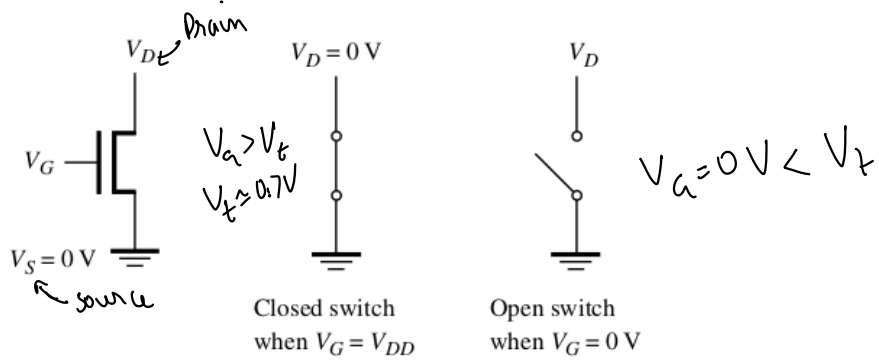
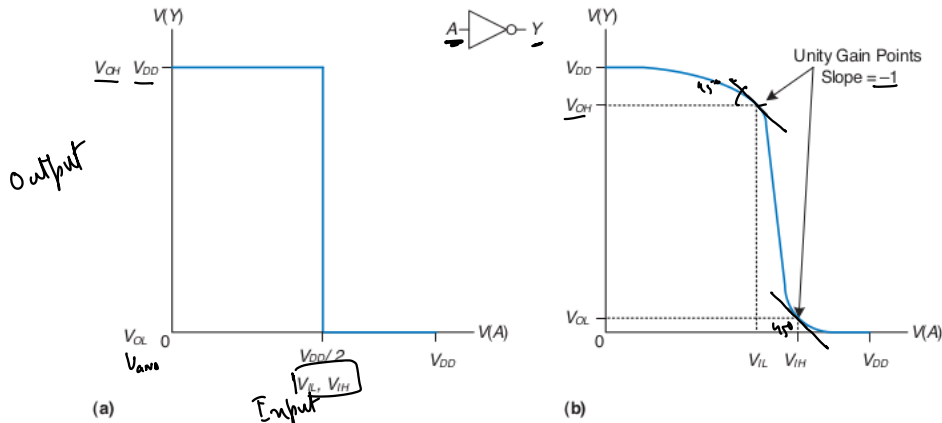
(a) NMOS NOT gate



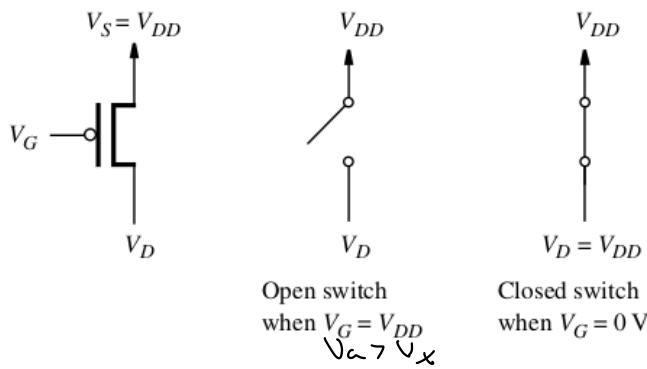
(b) $V_x = 5\text{ V}$



Ideal gate

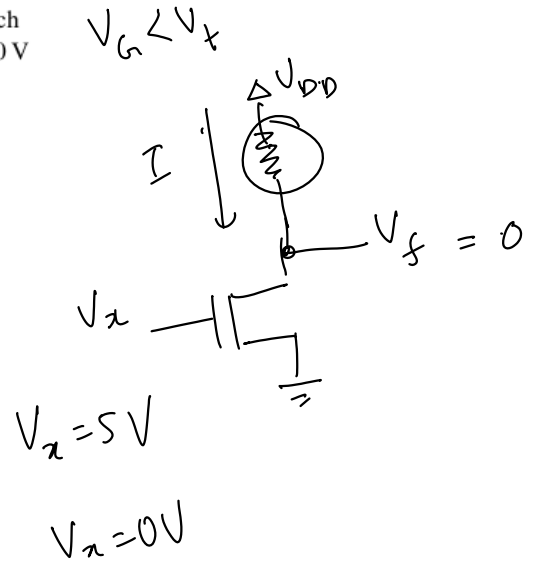


(a) NMOS transistor



(b) PMOS transistor

Example 3. Draw a NOT gate using nMOS transistors.

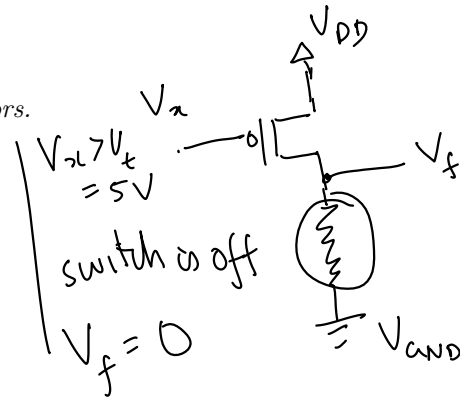


Example 4. Draw a NOT gate using pMOS transistors.

When $V_x < V_t = 0$

the transistor switch is ON

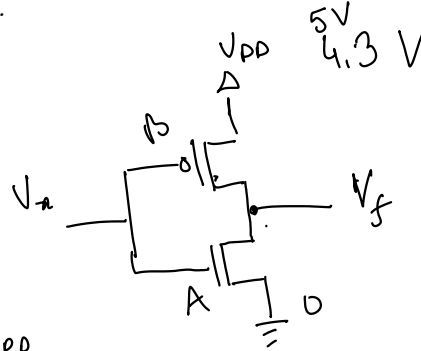
$$V_f = V_{DD} = 5V$$



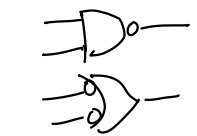
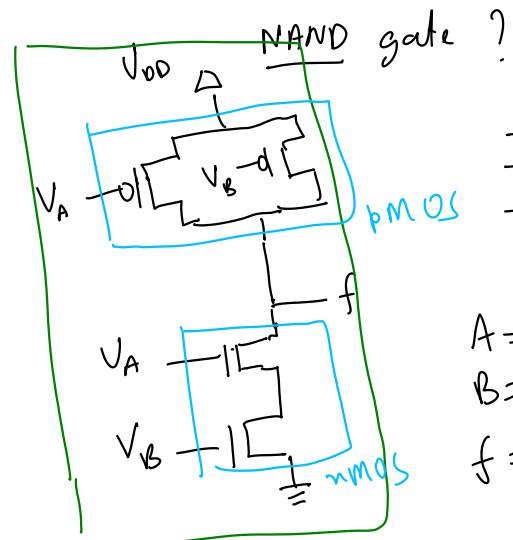
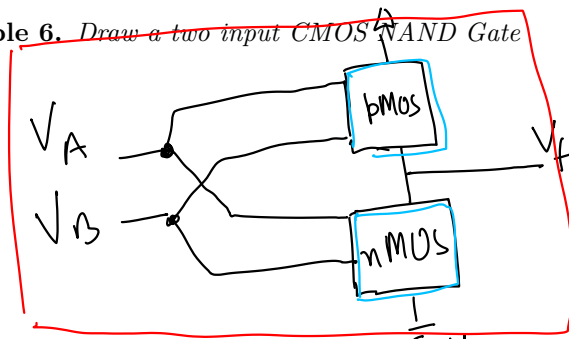
Remark 1. nMOS transistors pass 0's well (output between 0 and $V_{DD} - V_t$). pMOS transistors pass 1's well (output between V_t and V_{DD}).

Example 5. Draw CMOS NOT Gate.

Complementary MOS gates



Example 6. Draw a two input CMOS NAND Gate



$$A = 1$$

$$B = 1$$

$$f = \overline{A \cdot B} = 0$$

Definition 9 (Negative logic).

Boolean	Positive logic	Negative logic
0	Low	High
1	High	Low

Example 7. Analyze the above circuit under negative logic.

V_A	V_B	V_f
L	L	H
L	H	H
H	L	H
H	H	L

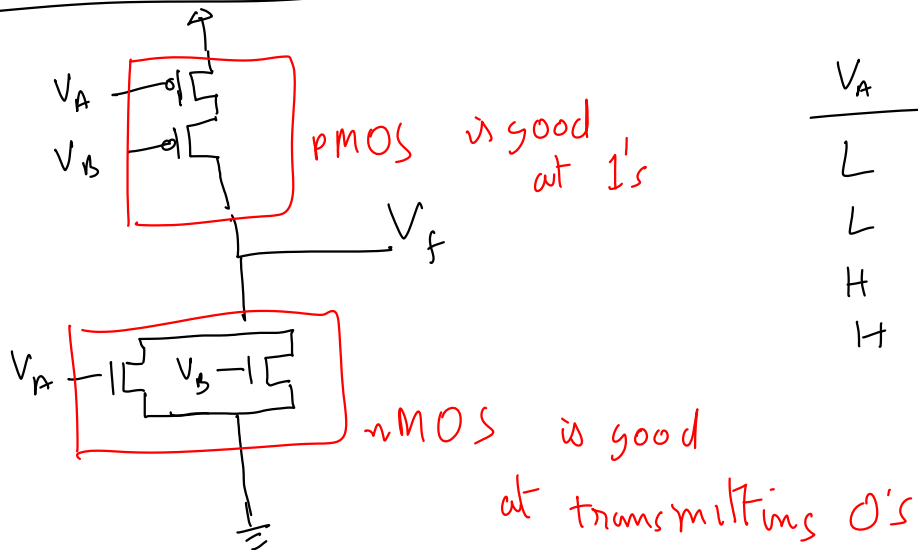
A	B	F
1	1	0
1	0	0
0	1	0
0	0	1

NOR gate

Example 8. Draw a three input NAND using CMOS.

Draw a CMOS NOR gate

H = 5V
L = 0V



V_A	V_B	V_f
L	L	H
L	H	L
H	L	L
H	H	L

Positive logic

$$f = \overline{A + B} \quad \text{NMOS}$$

$$f = \overline{A + B} \quad \text{PMOS}$$

$$= \overline{A} \cdot \overline{B} \quad \text{Series of switches}$$

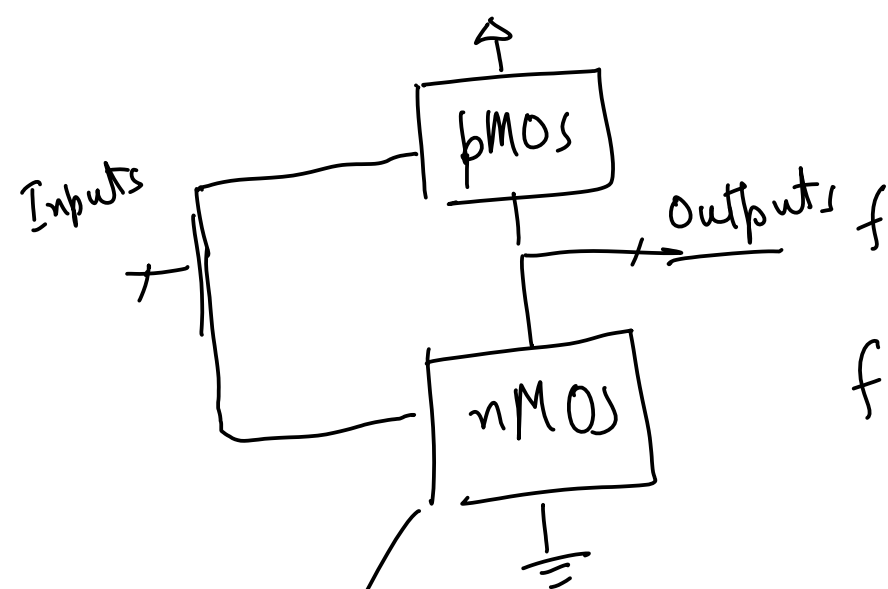
Parallel = OR = +
Series = AND = .

Example

$$f = x_1 x_2 + x_3 x_4 + x_5$$

Implement this using CMOS technology

Complex gate (CMOS)



$$f = \overline{x_1 x_2 + x_3 x_4 + x_5}$$

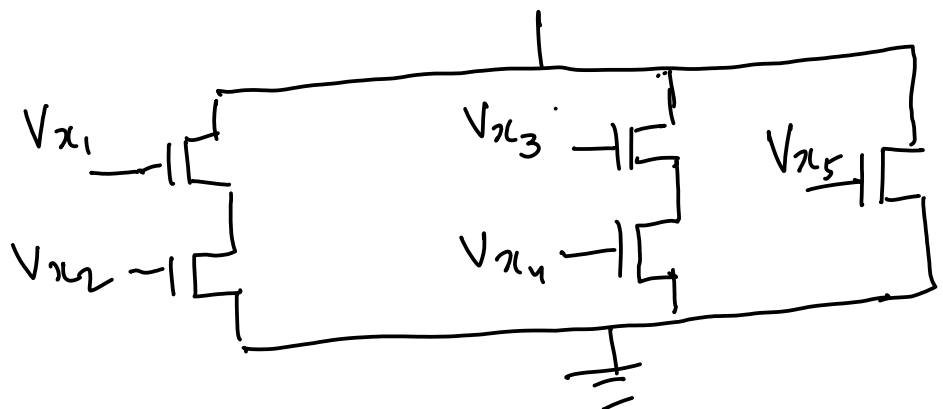
For

nMOS block $\overline{f} = x_1 x_2 + x_3 x_4 + x_5$

(1) Design for \overline{f}

(2) Replace $\cdot = \text{AND} \equiv \text{series}$
 $+ = \text{OR} \equiv \text{parallel}$

nMOS
block

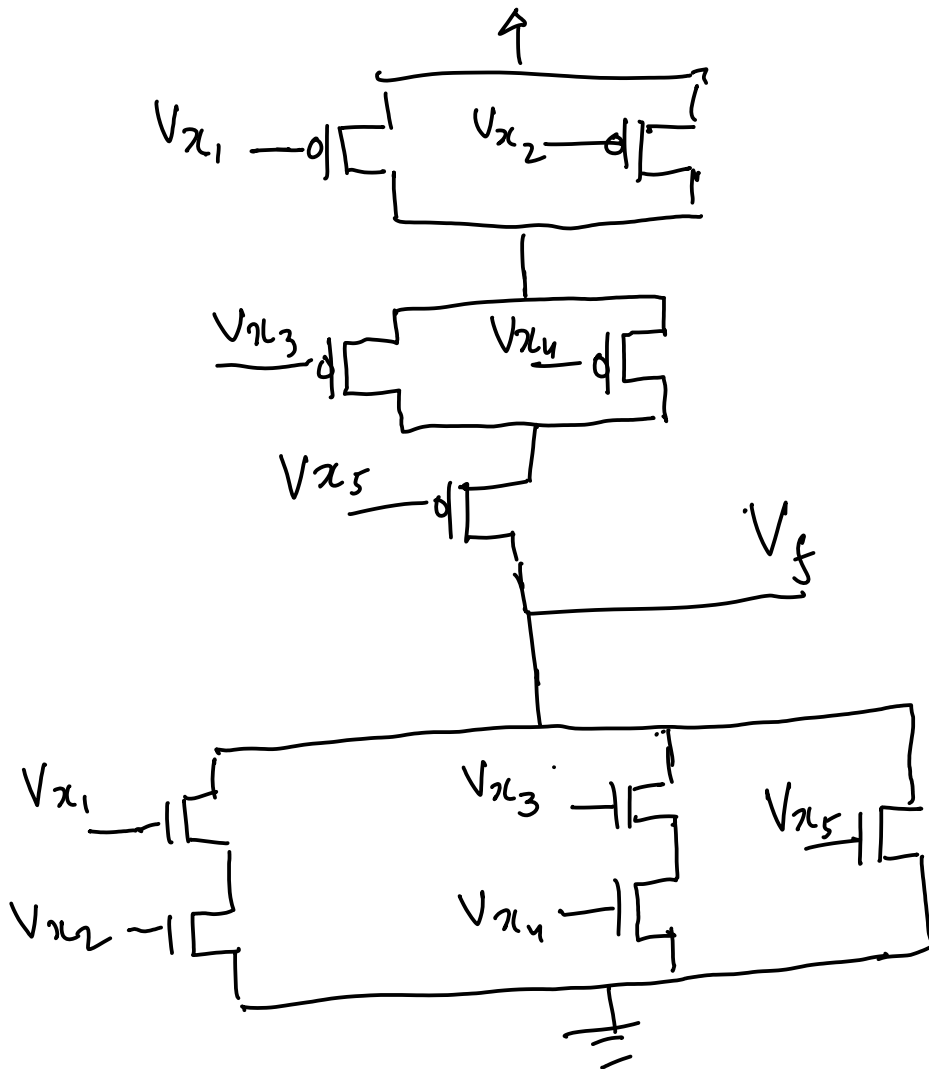


pMOS block

$$f = \overline{x_1 x_2 + x_3 x_4 + x_5}$$

$$= (\bar{x}_1 + \bar{x}_2) \cdot (\bar{x}_3 + \bar{x}_4) \cdot \bar{x}_5$$

② Replace $\cdot \equiv$ Series
 $+ \equiv$ parallel



PMOS
 block
 good at
 transmitting
 1s
 0-5
 0.7-5.0

Practice

$$f = \bar{x}_1 \bar{x}_2 x_3 + \bar{x}_1 x_2 \bar{x}_3 + x_1 \bar{x}_2 \bar{x}_3$$

Design a CMOS complex gate for this
Count the number of nMOS + pMOS Transistors

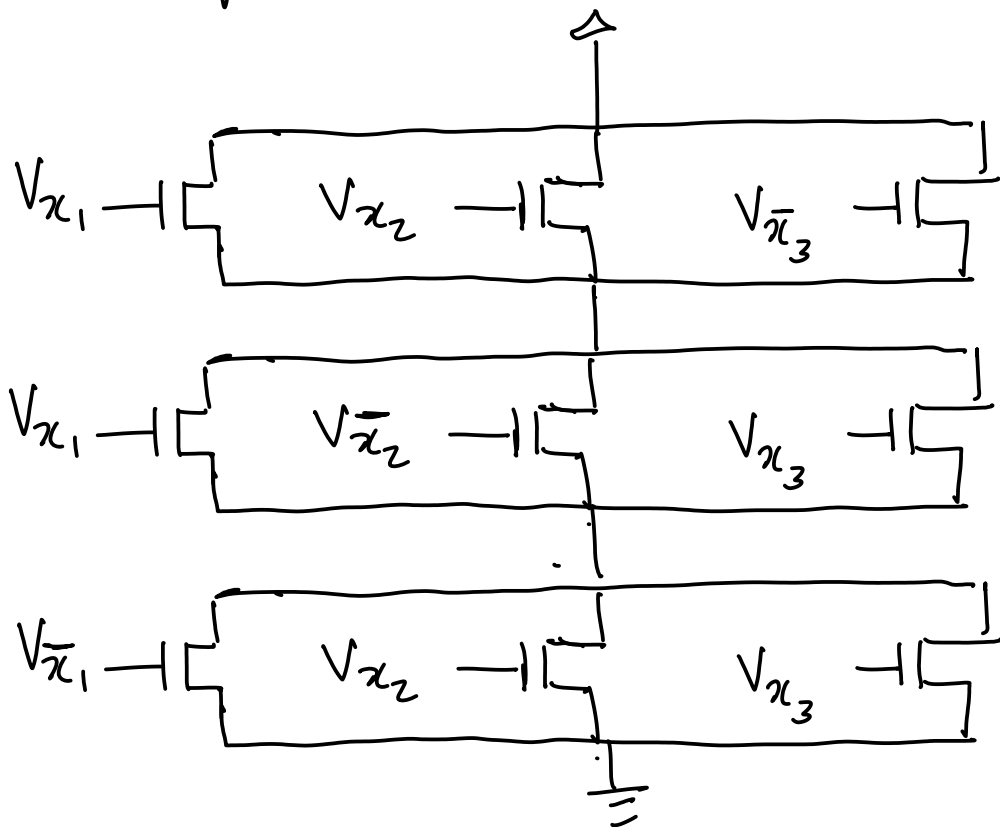
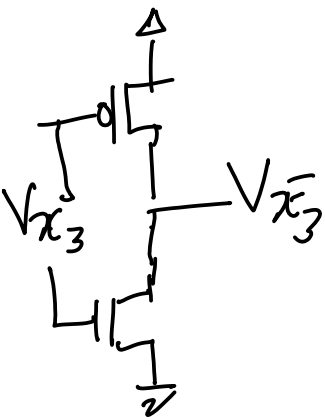
For nMOS block

f $x_1 x_2$

0^0	1^2	0^6	1^4
1^1	0^3	0^7	0^5

$$\bar{f} = (x_1 + x_2 + \bar{x}_3)(\bar{x}_1 + \bar{x}_2 + x_3)(\bar{x}_1 + x_2 + x_3)$$

Replace \cdot with series
+ with parallel



2x3
for NOT gates only

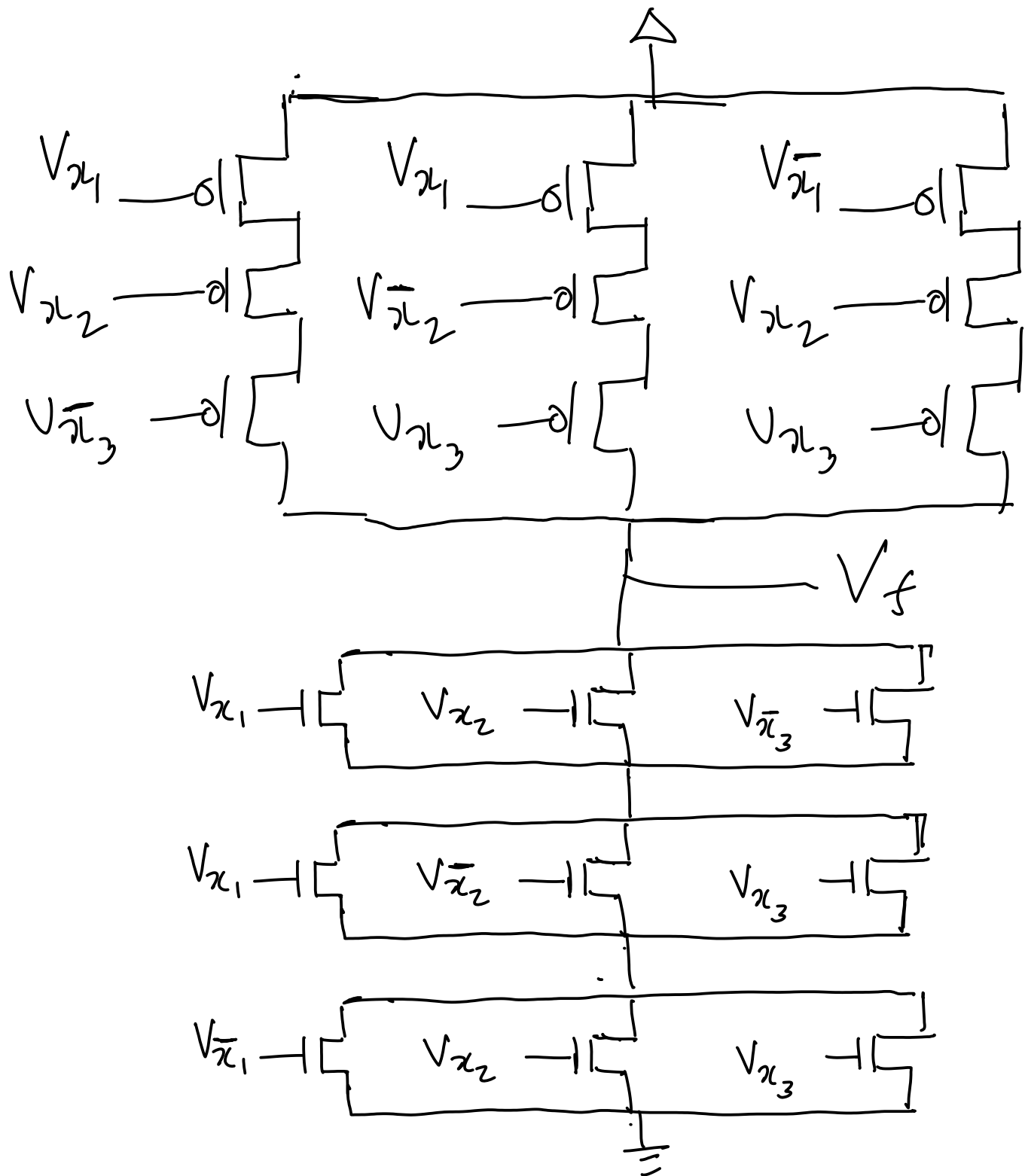
+

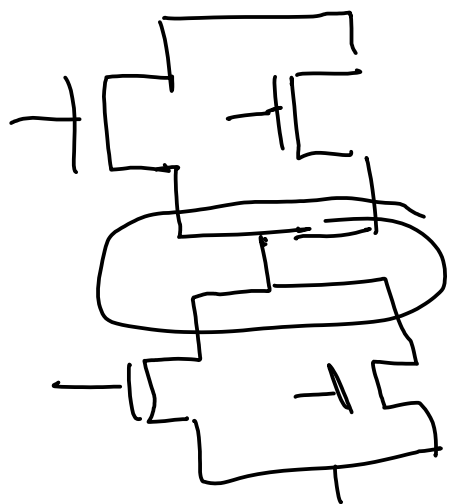
9 nMOS

+ 9 pMOS

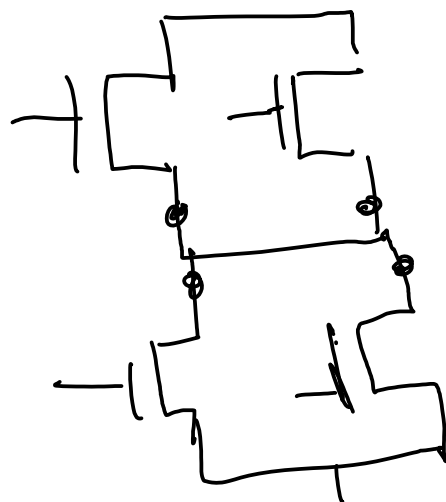
for PMOS block

$$f = \bar{x}_1 \cdot \bar{x}_2 \cdot x_3 + \bar{x}_1 \cdot x_2 \cdot \bar{x}_3 + x_1 \cdot \bar{x}_2 \cdot \bar{x}_3$$





\equiv



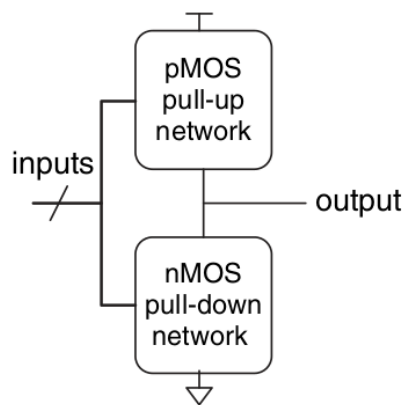
Example 9. Draw a three input NOR using CMOS.

Example 10. Draw a two input AND gate using CMOS.

$$f = A \cdot B$$

nMOS block

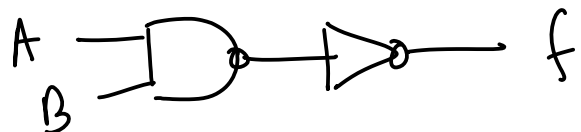
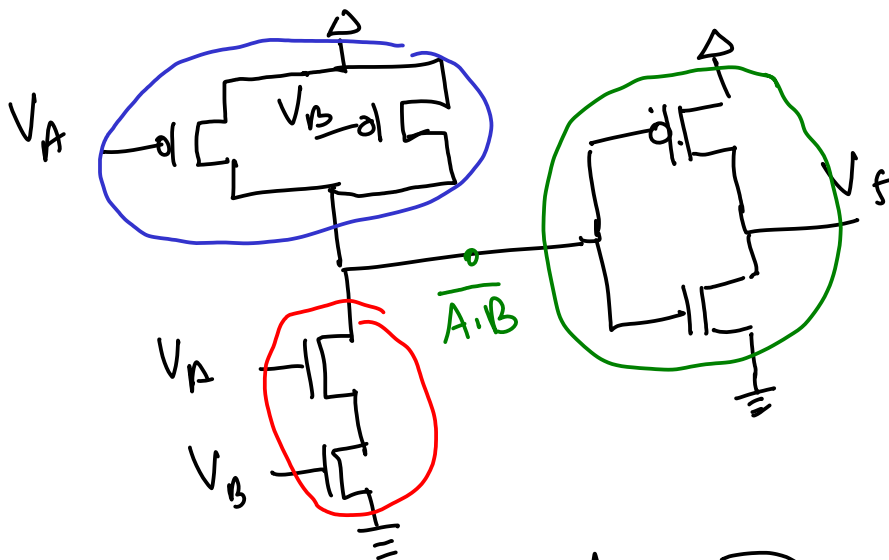
$$\overline{f} = \overline{A \cdot B} \quad \text{or} \quad \overline{A} + \overline{B}$$



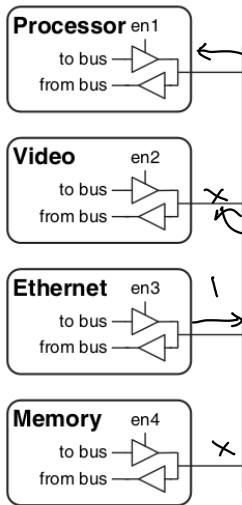
pMOS block

$$f = A \cdot B$$

$$\text{or} \quad \overline{\overline{A} + \overline{B}}$$



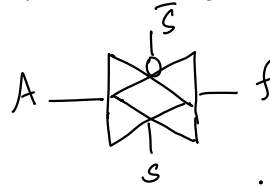
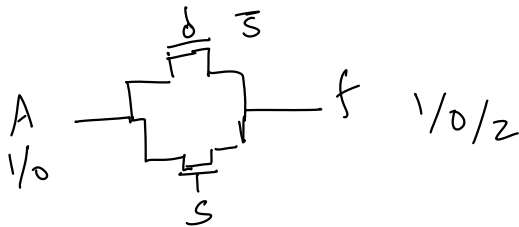
6.1 Gates with floating output



← common set of wires

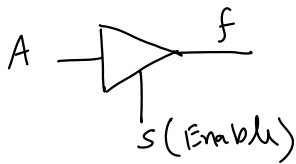
disconnected state is called high impedance output Z

Definition 10 (Transmission gate). Draw a schematic of transmission gate and truth table for transmission gate. What is its commonly used symbol?



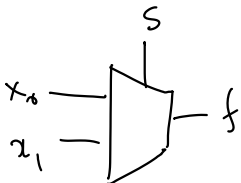
S	f
0	Z ← High impedance state
1	A

Definition 11 (Tristate buffer). What is tristate buffer? Draw its symbol and truth table? Where is it used?

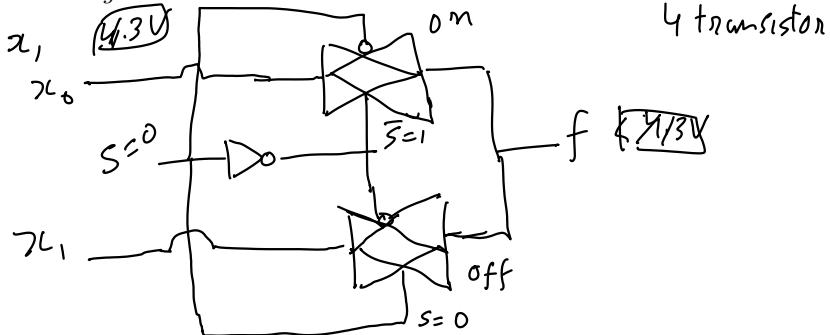


S	f
0	Z
1	A

Example 11. Draw a Multiplexer using transmission gates.

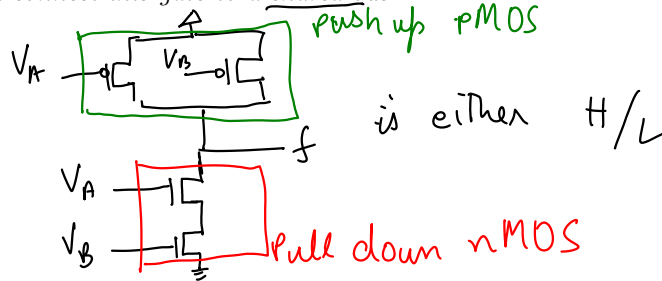


$$f = \bar{S} x_0 + S x_1$$

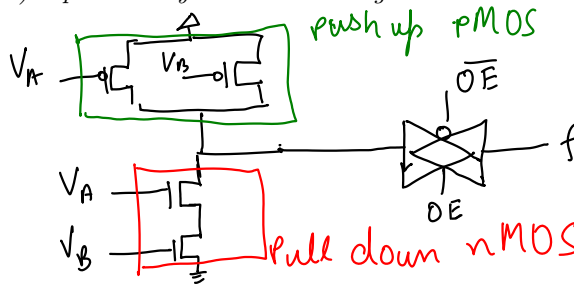


Example 12. Draw a Multiplexer using tristate buffers.

Definition 12 (Totem-pole). Draw a Push-pull (or Totem-pole) output NAND gate using CMOS. Can you connect this gate to a shared bus? NO



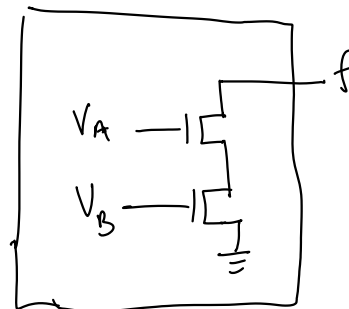
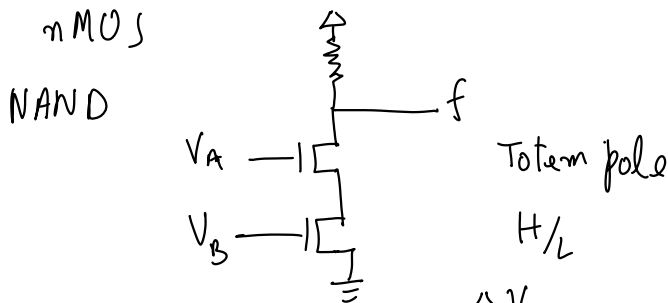
Definition 13 (Tristate). Draw a Tristate output NAND gate using CMOS with an output enable (OE) input. Can you connect this gate to a shared bus? (YES)



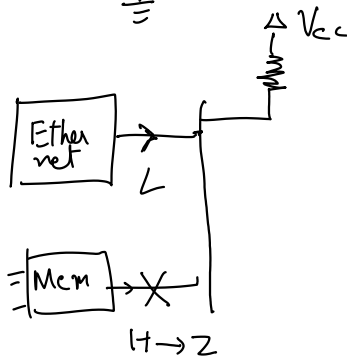
OE	f
0	1
1	$\overline{A \cdot B}$

High impedance

Definition 14 (Open-collector). Draw an open-collector output NAND gate. Can you connect this gate to a shared bus? (YES)



V _A	V _B	f
L	L	Z
L	H	Z
H	L	Z
H	H	0



7 Verilog truth tables

Table 11-11—Bitwise binary AND operator Table 11-12—Bitwise binary OR operator

$A \rightarrow$ $A \& B = 1$
 $0 \& 0 = 0$
 $0 \& 1 = 0$
 $1 \& 0 = 0$
 $1 \& 1 = 1$

$B \downarrow$

&	0	1	x	z
0	0	0	0	0
1	0	1	x	x
x	0	x	x	x
z	x	x	x	x

	0	1	x	z
0	0	1	x	x
1	1	1	1	1
x	x	1	x	x
z	x	1	x	x

$A | B$
 $1 | 0 = 1$
 $1 | 1 = 1$

References

- [1] Brown Stephen and Vranesic Zvonko. *Fundamentals of digital Logic with Verilog design*. McGraw Hill, 2022.