

Chapter 10

Analog details

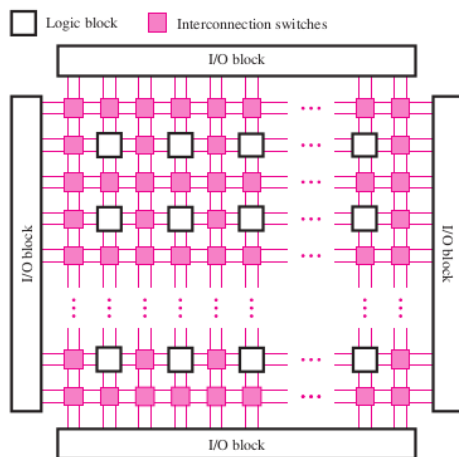
Some of the material is out of the textbook. Additional resources include Appendix B of Brown and Vranesic book, "Fundamentals of digital logic."

10.1 Objectives

1. Describe how tri-state and open-collector outputs are different from totem-pole outputs
2. Compute noise margin of one device driving the same time

10.2 FPGA [3, Section B.6.5]

Verilog → ASIC



(a) General structure of an FPGA

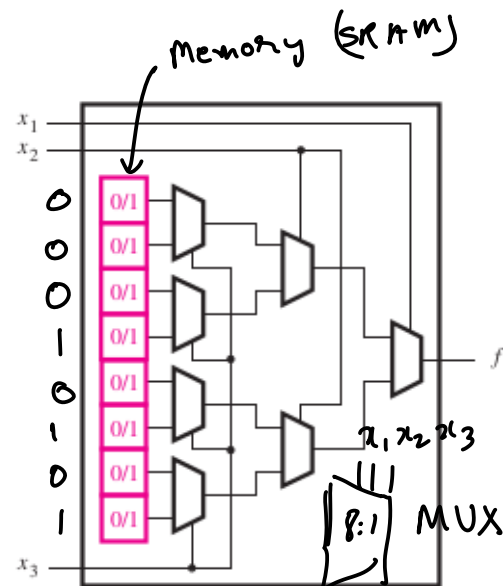


Figure B.37

A three-input LUT

Look up table

x_1	x_2	x_3	f
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

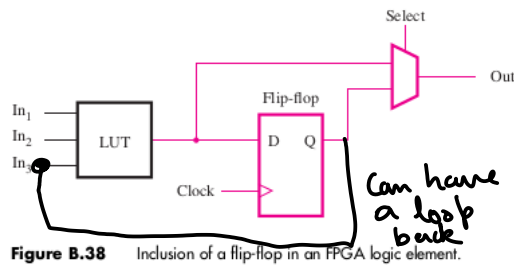


Figure B.38 Inclusion of a flip-flop in an FPGA logic element.

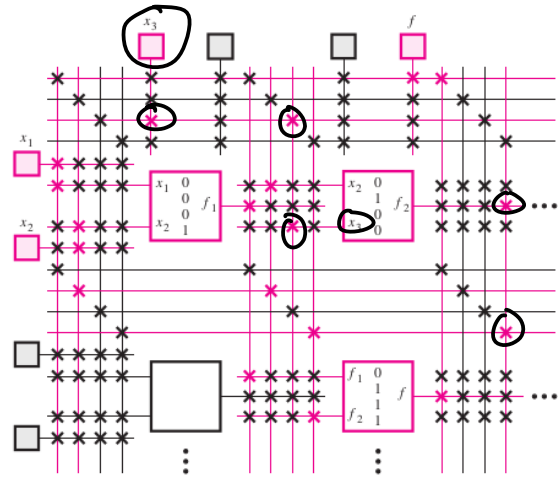


Figure B.39 A section of a programmed FPGA.

Definition 10.1 (Random Access Memory (RAM)). Structure of a RAM is as follows:

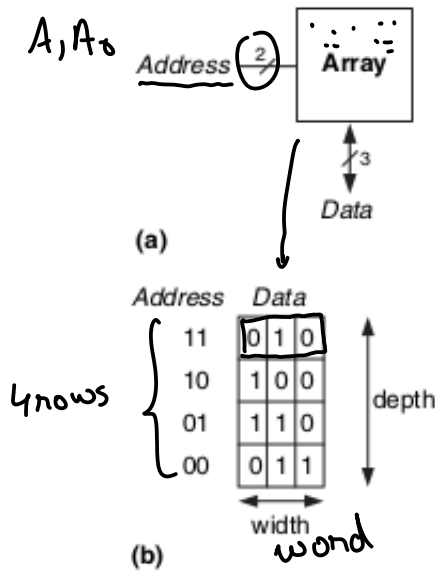


Figure 5.39 4 × 3 memory array: (a) symbol, (b) function

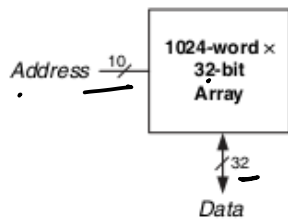


Figure 5.40 32 Kb array: depth = $2^{10} = 1024$ words, width = 32 bits

How can we arrange single bit memory cells into an addressable memory?

How many location can be encoded in a n -bit address bus?

$$2^n$$

$$2^{10} = 1024 \approx 10^3$$

$$\begin{matrix} A_1 & A_0 \\ 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{matrix}$$

n mos switches

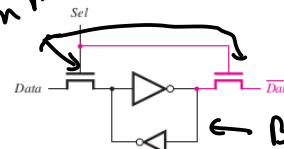


Figure B.64 An SRAM cell.

Bistable

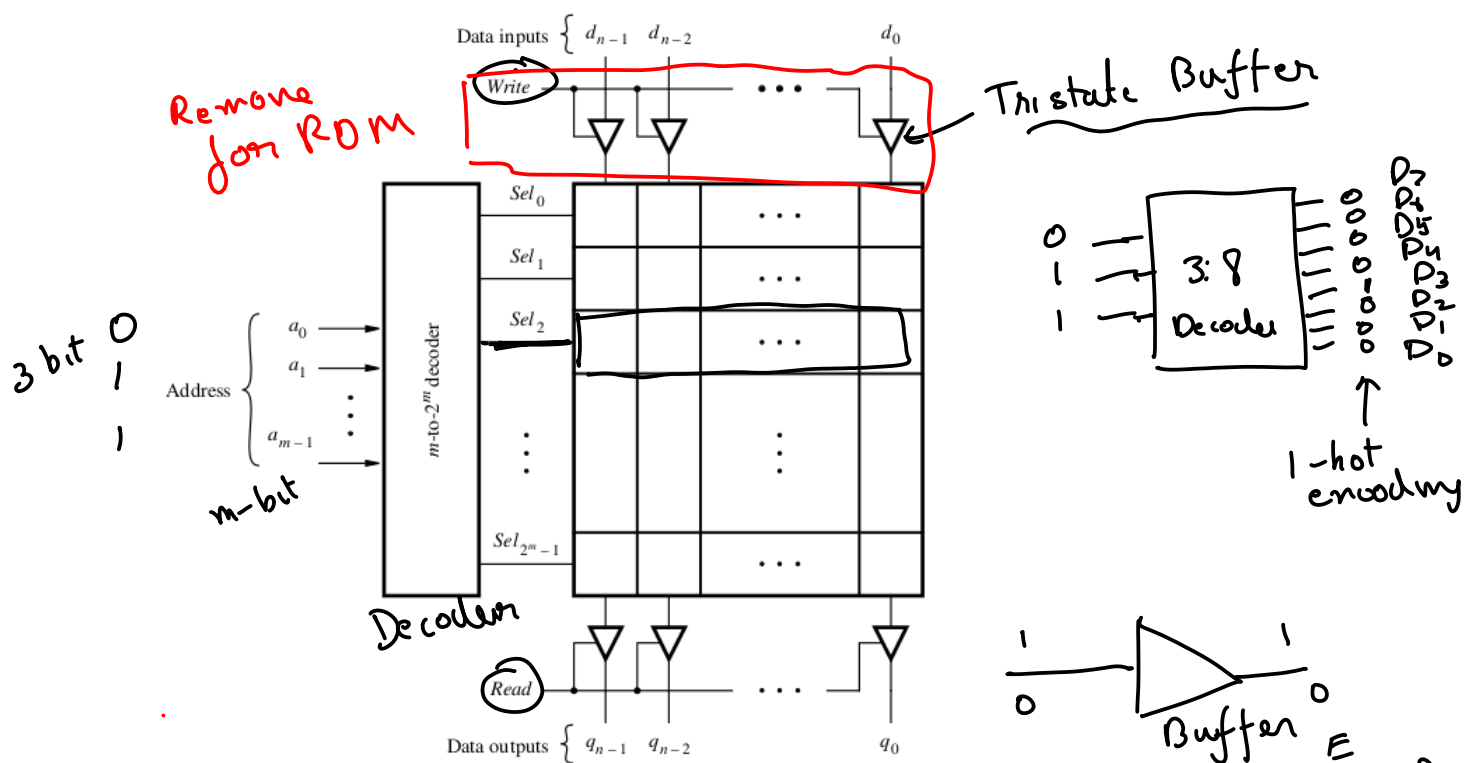
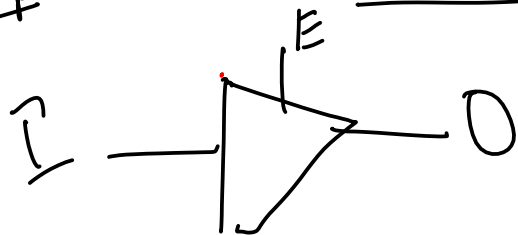


Figure B.66 A $2^m \times n$ SRAM block.

Definition 10.2 (Read Only Memory (ROM)). Structure of a ROM is as follows:

skip



E	O
0	floating = Z
1	$O = I$

E	O
1	I
0	Z

floating
floating
0/1/Z/x
↑
undefined

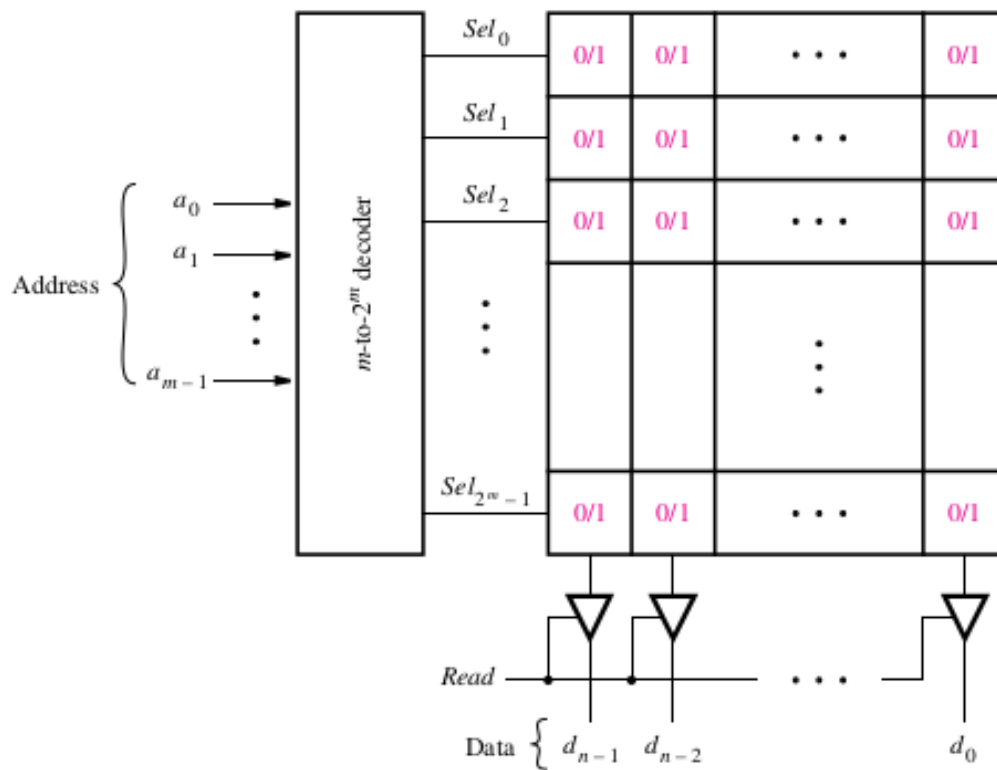


Figure B.72 A $2^m \times n$ read-only memory (ROM) block.

Example 10.1. Draw a Multiplexer using sum of products form. *Already covered*

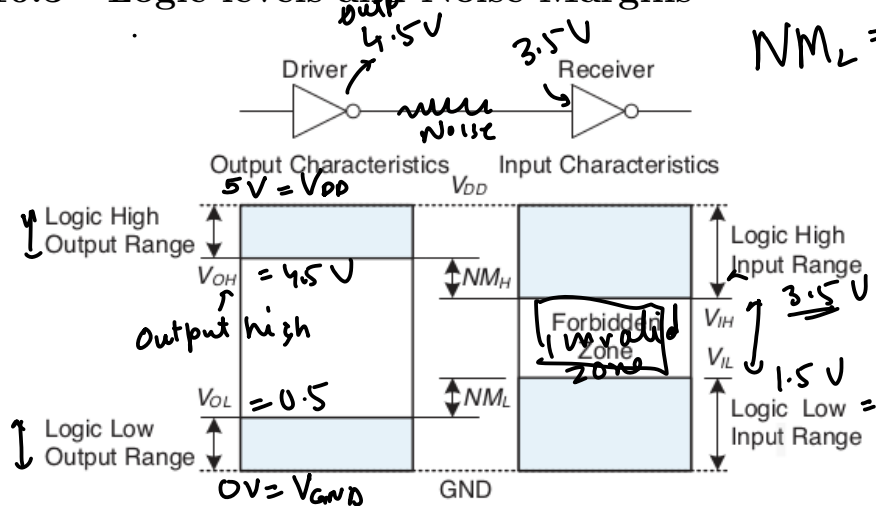
Noise Margin

$$NM_H = V_{OH} - V_{IH}$$

$$NM_L = V_{IL} - V_{OL}$$

D = Drain

output



Boolean 1

Boolean 0

Definition 10.3 (Supply Voltage ($V_{DD}/V_{CC}/V_{+}$)). The highest DC voltage that drives a digital circuit. As chips have progressed to smaller transistors, V_{DD} has dropped from 5V to 1.2V or even lower to save power.

Drain collection

Definition 10.4 (Ground Voltage (V_{GND})). The lowest DC voltage that drives a digital circuit, typically 0V.

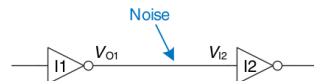
 $V_{SS} \leftarrow$ Source

Definition 10.5 (Input high (V_{IH}) and Input Low (V_{IL}) of a gate). V_{IH} is the voltage level, such that an input voltage to a gate between V_{DD} and V_{IH} is considered HIGH. Similarly, input voltage to a gate between V_{IL} and V_{GND} is considered LOW.

Definition 10.6 (Output high (V_{OH}) and Output low (V_{OL}) of gate). V_{OH} is the voltage level, such that an output voltage to a gate between V_{DD} and V_{OH} is considered HIGH. Similarly, output voltage to a gate between V_{OL} and V_{GND} is considered LOW.

Definition 10.7 (Positive logic and Negative logic). What we have considered so far is Positive logic where HIGH voltage is equated to Boolean logic TRUE or 1 and LOW is considered FALSE or 0. In negative logic these are reversed. Same physical circuit can represent different logical circuits in positive logic and negative logic.

Definition 10.8 (Noise margins (NM_L and NM_H) of a channel). The maximum amount of noise that can be added (or subtracted) to a channel without exceeding the logic level specifications of a gate. $NM_L = V_{IL} - V_{OL}$
 $NM_H = V_{OH} - V_{IH}$

**Example 10.2.**

If $V_{DD} = 5V$, $V_{IL} = 1.35V$, $V_{IH} = 3.15V$, $V_{OL} = 0.33V$ and $V_{OH} = 3.84V$ for both the "inverters", then what are the low and high noise margins? Can the circuit tolerate 1V of noise at the channel?

No

$$NM_L = 1.02 = 1.35 - 0.33 = V_{IL} - V_{OL}$$

$$NM_H = 0.69 = 3.84 - 3.15 = V_{OH} - V_{IH}$$

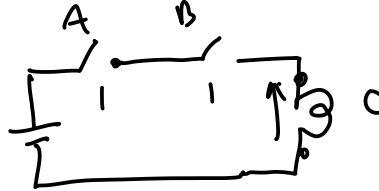
10.4 Semiconductors and Doping

Not in syllabus but good to know

Elements recognized as metalloids

	13	14	15	16	17
2	B Boron	C Carbon	N Nitrogen	O Oxygen	F Fluorine
3	Al Aluminium	Si Silicon	P Phosphorus	S Sulfur	Cl Chlorine
4	Ga Gallium	Ge Germanium	As Arsenic	Se Selenium	Br Bromine
5	In Indium	Sn Tin	Sb Antimony	Te Tellurium	I Iodine
6	Tl Thallium	Pb Lead	Bi Bismuth	Po Polonium	At Astatine

Commonly recognized (86-99%): B, Si, Ge, As, Sb, Te
 Irregularly recognized (40-49%): Po, At
 Less commonly recognized (24%): Se
 Rarely recognized (8-10%): C, Al
 (All other elements cited in less than 6% of sources)
 Arbitrary metal-nonmetal dividing line: between Be and B, Al and Si, Ge and As, Sb and Te, Po and At



Logic level definitions:

$L=0$
 $H=1$ logic +ve

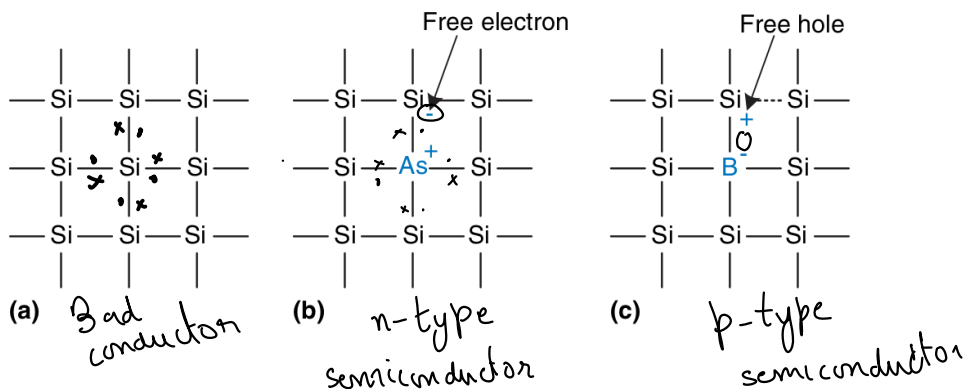
$L=1$
 $H=0$ -ve logic

AND gate

A	B	O
L	L	L
L	H	L
H	L	L
H	H	H

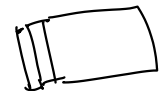
OR gate

A	B	O
L	L	L
L	H	H
H	L	H
H	H	H



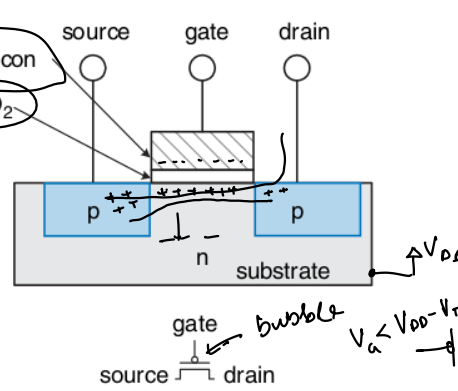
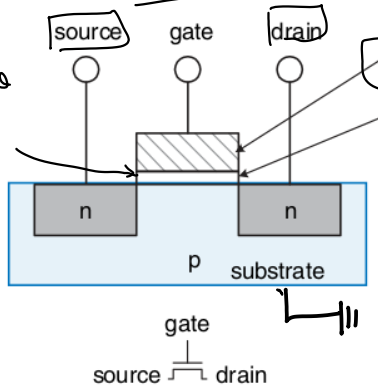
10.5 MOSFET: Metal Oxide Field Effect Transistors

Not in syllabus but good to know



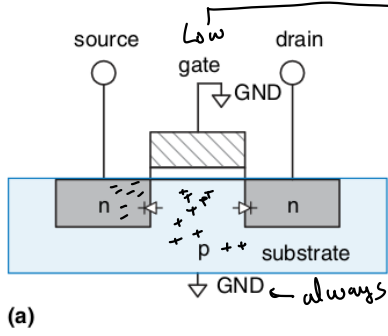
n-MOS

p-MOS

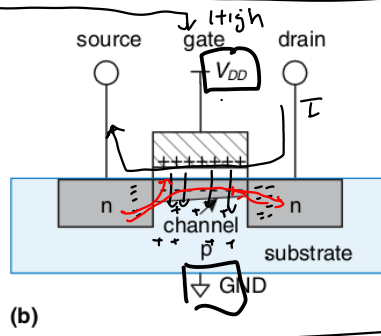


(a) nMOS

(b) pMOS



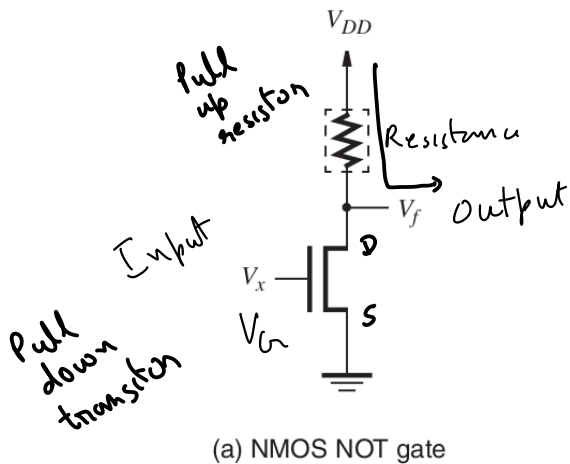
(a)



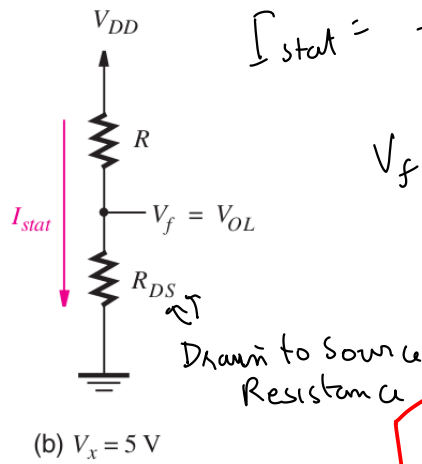
(b)

N-MOS

10.6 DC Transfer characteristic



(a) NMOS NOT gate

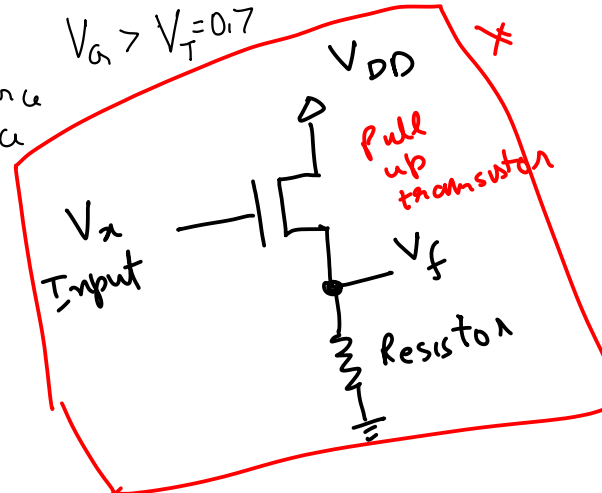


(b) $V_x = 5\text{ V}$

$$I_{\text{stat}} = \frac{V_{DD}}{R + R_{DS}}$$

$$V_f = \left(\frac{R_{DS}}{R + R_{DS}} \right) V_{DD}$$

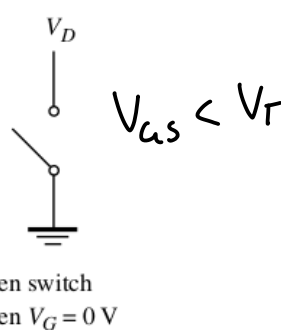
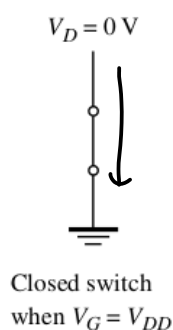
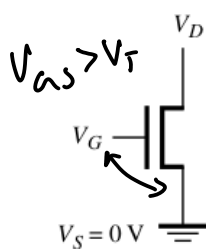
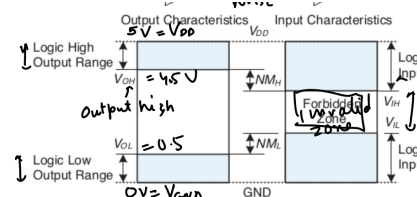
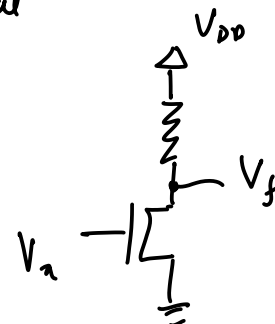
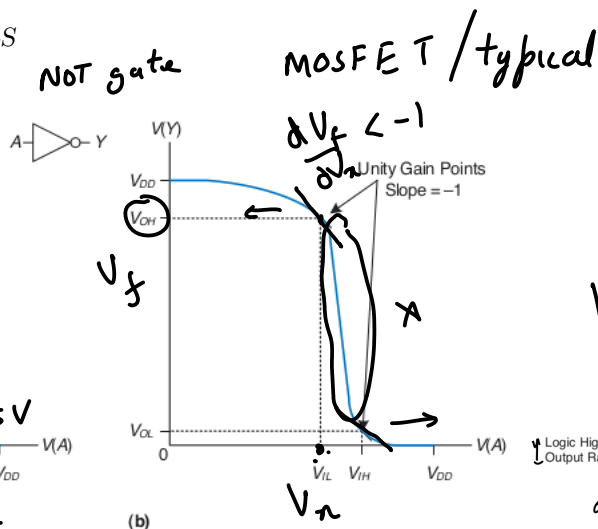
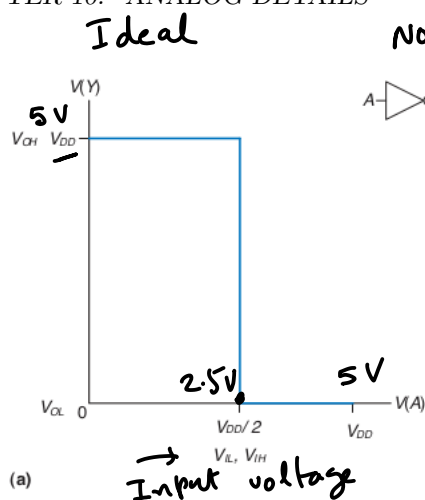
$$V_G > V_T = 0.7$$



n-MOS should not be used as a pull up transistor
only used it as a pull down transistor

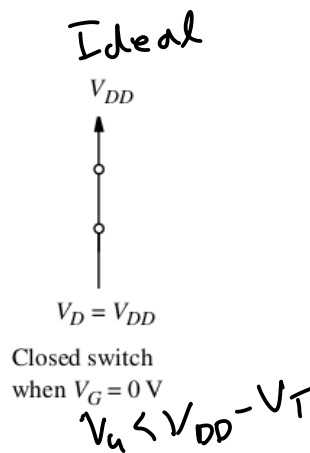
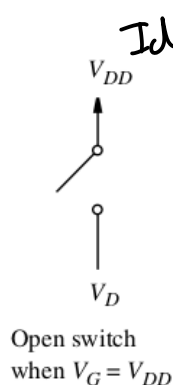
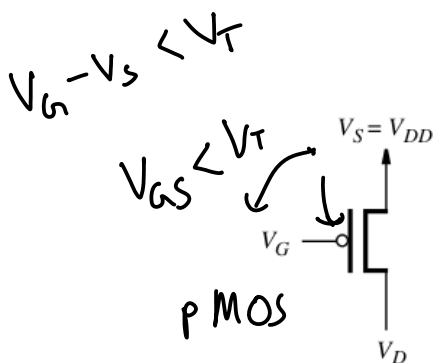
Vice-versa for p-MOS. p-MOS: pull up transistor.
Why?

Output voltage



$V_T = \text{Threshold voltage}$

(a) NMOS transistor



(b) PMOS transistor

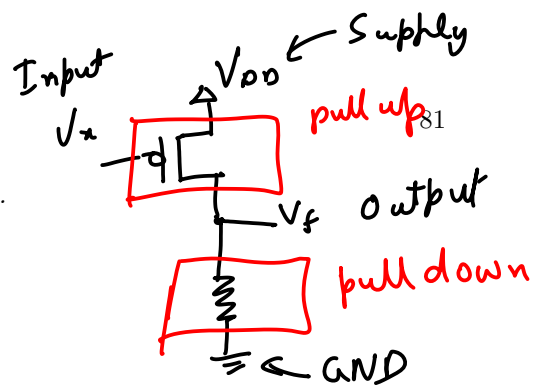
Example 10.3. Draw a NOT gate using nMOS transistors.

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Example 10.4. Draw a NOT gate using pMOS transistors.

V_x	V_f
L	H
H	L

pull down

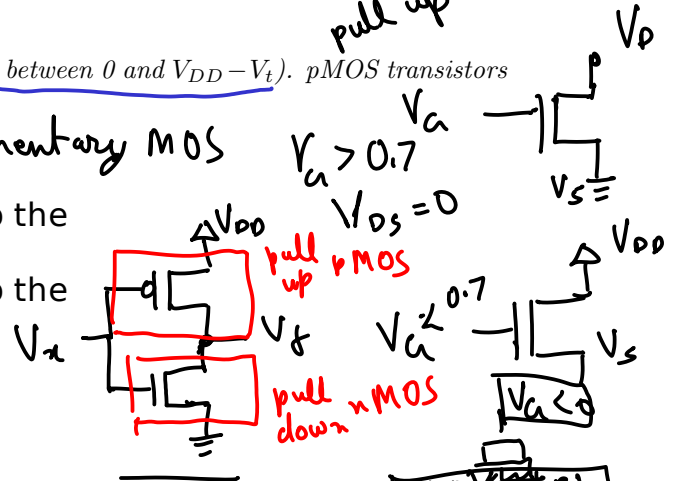


Remark 10.1. nMOS transistors pass 0's well (output between 0 and $V_{DD} - V_t$). pMOS transistors pass 1's well (output between V_t and V_{DD}).

Example 10.5. Draw CMOS NOT Gate.

complementary MOS

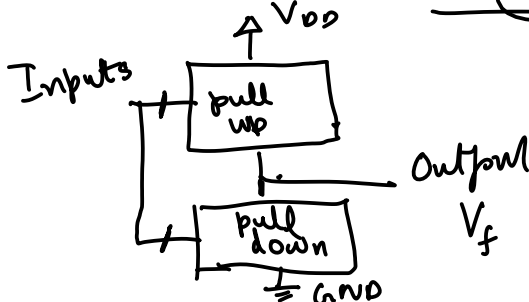
pull up



n-MOS behaves well when gate voltage is opposite to the substrate voltage (V_{GND}).
p-MOS behaves well when gate voltage is opposite to the substrate voltage (V_{DD}/supply)

Example 10.6. Draw a two input CMOS NAND Gate

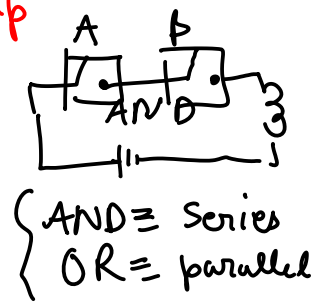
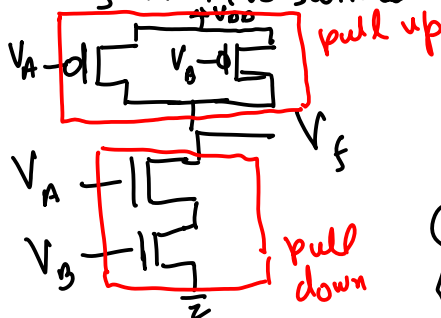
A	B	f
0	0	1
0	1	1
1	0	1
1	1	0



Definition 10.9 (Negative logic).

$$f = \overline{A \cdot B} = \overline{A} + \overline{B}$$

① Design pull down using n-MOS switches



② Design pull up side as DeMorgan inverse of pull down side

Example 10.7. Analyze the above circuit under negative logic.

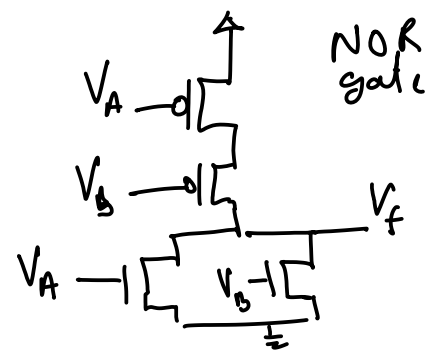
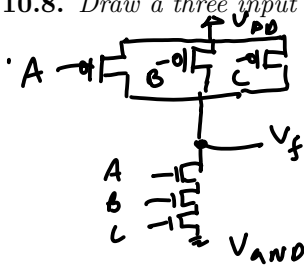
V_A	V_B	V_f
L	L	H
L	H	H
H	L	H
H	H	L

-ve logic
L=1
H=0

A	B	f
1	1	0
1	0	0
0	1	0
0	0	1

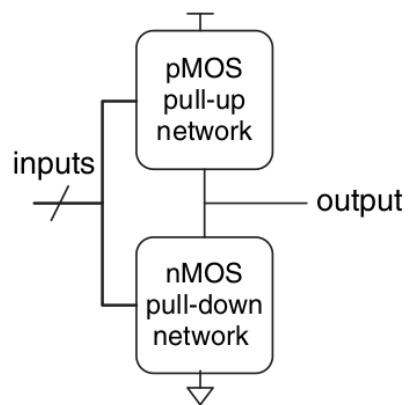
NOR gate $f = \overline{A + B}$

Example 10.8. Draw a three input NAND using CMOS.

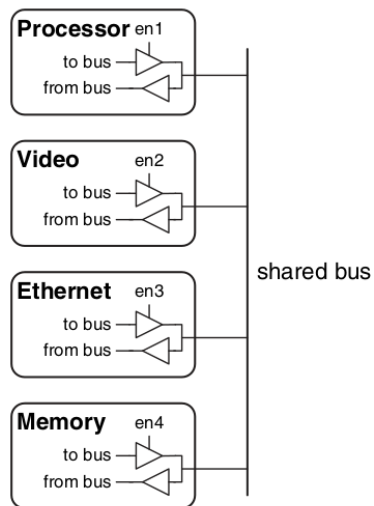


Example 10.9. Draw a three input NOR using CMOS.

Example 10.10. Draw a two input AND gate using CMOS.



10.6.1 Gates with floating output



Definition 10.10 (Transmission gate). Draw a schematic of transmission gate and truth table for transmission gate. What is its commonly used symbol?

Definition 10.11 (Tristate buffer). What is tristate buffer? Draw its symbol and truth table? Where is it used?

Example 10.11. Draw a Multiplexer using transmission gates.

Example 10.12. *Draw a Multiplexer using tristate buffers.*

Definition 10.12 (Totem-pole). *Draw a Push-pull (or Totem-pole) output NAND gate using CMOS. Can you connect this gate to a shared bus?*

Definition 10.13 (Tristate). *Draw a Tristate output NAND gate using CMOS with an output enable (OE) input. Can you connect this gate to a shared bus?*

Definition 10.14 (Open-collector). *Draw a open-collector output NAND gate. Can you connect this gate to a shared bus?*

10.7 Verilog truth tables

Table 11-11—Bitwise binary AND operator

&	0	1	x	z
0	0	0	0	0
1	0	1	x	x
x	0	x	x	x
z	0	x	x	x

Table 11-12—Bitwise binary OR operator

	0	1	x	z
0	0	1	x	x
1	1	1	1	1
x	x	1	x	x
z	x	1	x	x

Bibliography

- [1] Sarah L Harris and David Harris. *Digital design and computer architecture*. Morgan Kaufmann, 2022.
- [2] Randy Katz and Gaetano Barriello. *Contemporary Logic Design*. Prentice Hall, 2004.
- [3] Brown Stephen and Vranesic Zvonko. *Fundamentals of digital Logic with Verilog design*. McGraw Hill, 2022.