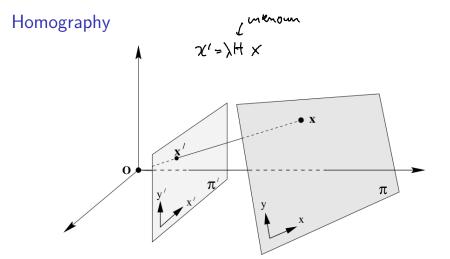
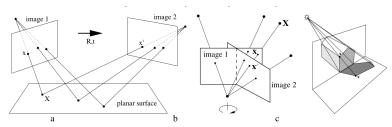
ECE 417/598: Direct Linear Transform

Vikas Dhiman

March 23, 2022

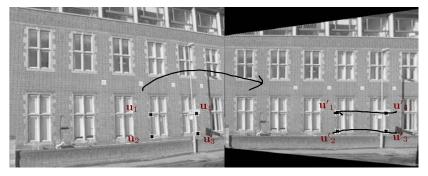


Examples of Homography





Computing Homography



Find H such that $\underline{\mathbf{u}}' = \lambda H \underline{\mathbf{u}}$ for any point on one image to another image, where $\mathbf{u}', \mathbf{u} \in \mathbb{P}^2$

2D homography

Given a set of points $\underline{\mathbf{u}}_i \in \mathbb{P}^2$ and a corresponding set of points $\underline{\mathbf{u}}_i' \in \mathbb{P}^2$, compute the projective transformation that takes each $\underline{\mathbf{u}}_i$ to $\underline{\mathbf{u}}_i'$. In a practical situation, the points $\underline{\mathbf{u}}_i$ and $\underline{\mathbf{u}}_i'$ are points in two images (or the same image), each image being considered as a projective plane \mathbb{P}^2 .

$$\frac{ui = \lambda H ui}{P_{caspedtue}} = \frac{\lambda e IR}{\lambda e IR}$$

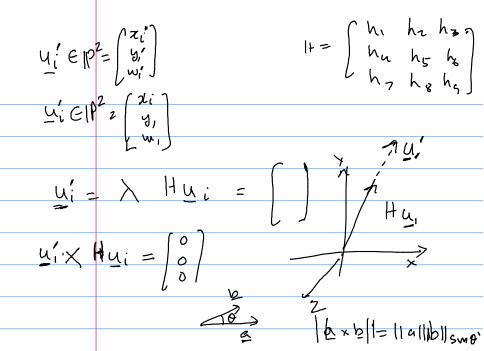
$$u = K \times \text{ in penspective shall}$$

$$u = \lambda K \times \frac{2}{3} = \frac{4}{12}$$

$$a b c \int \{y\}_{20}^{20} cx + by + c = 0$$

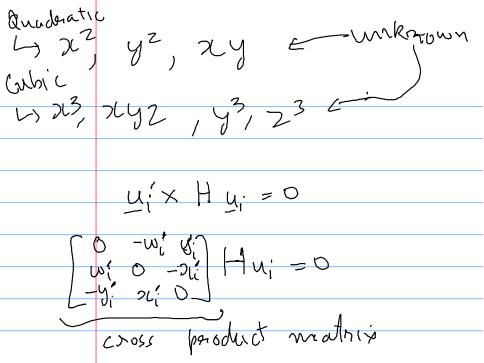
$$\frac{A \times b}{A \times b} = \frac{\lambda e IR}{\lambda e IR}$$

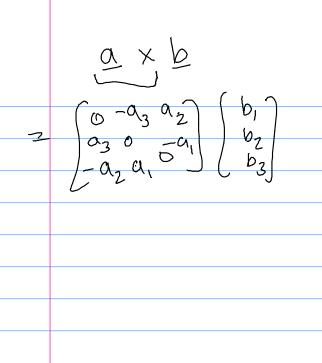
$$\frac{2}{3} = \frac{4}{12}$$



$$y = y + y = 0$$
 $y = y + y = 0$
 $y = =$

x hizi + > hz y + >hzt



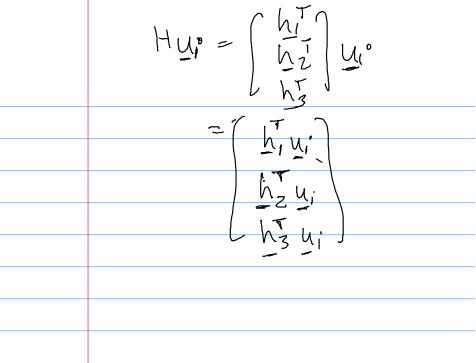


$$\begin{bmatrix}
0 & -w_i & g_i \\
w_i & 0 & -\partial_{i} & Hu_i & = 0
\end{bmatrix}$$

$$\begin{bmatrix}
-y_i & \partial_{i} & 0
\end{bmatrix}$$

$$\begin{bmatrix}
-y_i & \partial_{i} & 0
\end{bmatrix}$$

$$\begin{bmatrix}
h_1 & h_2 & h_3
\end{bmatrix}$$



$$\begin{bmatrix}
0 & -w_{i} & y_{i} \\
-y_{i} & y_{i} & y_{i}
\end{bmatrix}$$

$$\begin{bmatrix}
0 & -w_{i} & y_{i} \\
-y_{i} & y_{i} & y_{i}
\end{bmatrix}$$

$$\begin{bmatrix}
u_{i} & h_{2} \\
u_{i} & h_{3}
\end{bmatrix}$$

$$\begin{bmatrix}
0 & -w_{i} & y_{i} & y_{i} \\
-y_{i} & y_{i} & y_{i}
\end{bmatrix}$$

$$\begin{bmatrix}
0 & -w_{i} & y_{i} & y_{i} \\
-y_{i} & y_{i} & y_{i}
\end{bmatrix}$$

$$\begin{bmatrix}
0 & -w_{i} & y_{i} & y_{i} \\
-y_{i} & y_{i} & y_{i}
\end{bmatrix}$$

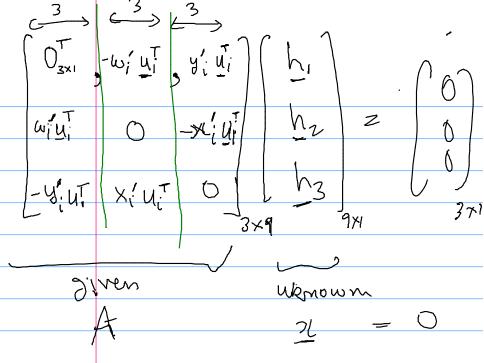
$$\begin{bmatrix}
0 & -w_{i} & y_{i} & y_{i} \\
-y_{i} & y_{i} & y_{i}
\end{bmatrix}$$

$$\begin{bmatrix}
0 & -w_{i} & y_{i} & y_{i} \\
-y_{i} & y_{i} & y_{i}
\end{bmatrix}$$

$$\begin{bmatrix}
0 & -w_{i} & y_{i} & y_{i} \\
-y_{i} & y_{i} & y_{i}
\end{bmatrix}$$

$$\begin{bmatrix}
0 & -w_{i} & y_{i} & y_{i} \\
-y_{i} & y_{i} & y_{i}
\end{bmatrix}$$

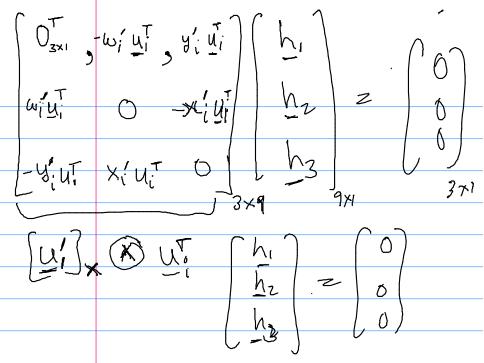
$$\begin{bmatrix}
0 & -w_{i} & y_{i} & y_{i} \\
-y_{i} & y_{i} & y_{i}
\end{bmatrix}$$



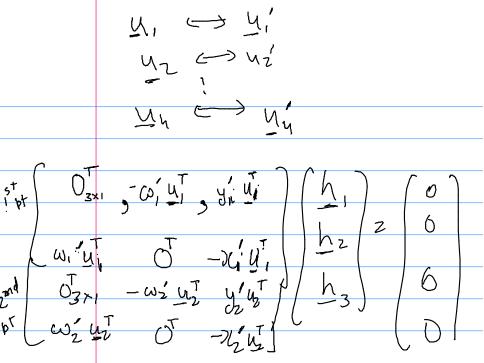
$$M = \begin{pmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{pmatrix} \qquad Nz \begin{pmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{pmatrix}$$

$$M \otimes N = \begin{pmatrix} M_{11} & N & M_{12} & N \\ M_{12} & N & M_{12} & N \end{pmatrix}$$

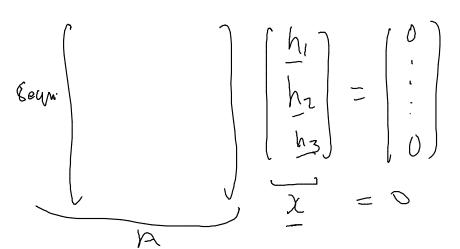
$$M \otimes N = \begin{pmatrix} M_{11} & N & M_{12} & N \\ M_{21} & N & M_{22} & M_{22} \end{pmatrix} \qquad M_{22} \qquad M_{23} \qquad M_{24} \qquad M_{24}$$



H = 3x3=9 unknows J Brause S DOF from each fount 3 eyrs 2 linearly independent equations 8/2=4 points (pair of points)



Solving for Homography



Solving for Homography