

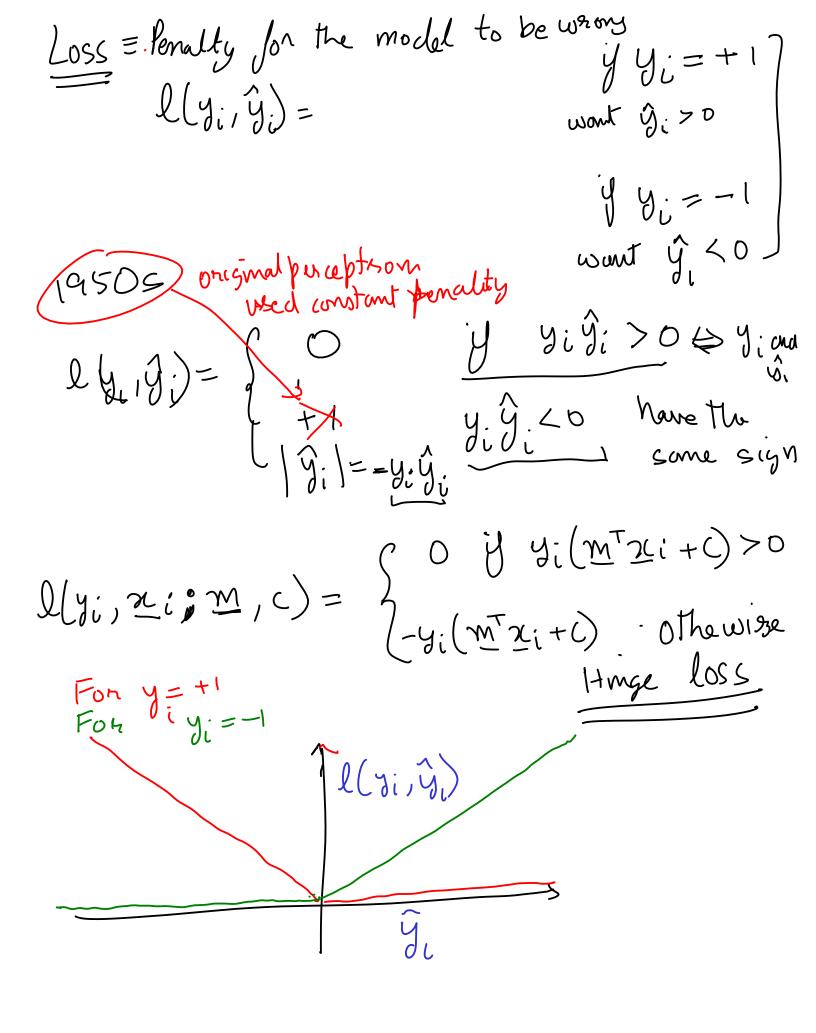
Optimization for classification

$$y = mx + c$$

$$e(y_i, x_i; m, c) = \left\{egin{array}{ll} 0 & ext{if } \operatorname{sign}(y_i - mx_i + c) = l_i \ |y_i - mx_i + c| & ext{if } \operatorname{sign}(y_i - mx_i + c)
eq l_i \end{array}
ight.$$

$$e(y_i,x_i;m,c) = \left\{egin{array}{ll} 0 & ext{if } \operatorname{sign}(y_i-mx_i+c) = l_i \ |mx_i+c| & ext{if } \operatorname{sign}(y_i-mx_i+c)
eq l_i \ & \mathbf{m} = \left[egin{array}{c} m \ c \end{array}
ight] \end{array}$$

Turning dassficution problem into optimization y, ∈ {-1,+1 } $Dataset = \begin{cases} (21, y_1) \\ (22, y_2) \end{cases}$ cats doss (zin, yn) } pixel colors/intensity from mages Model? $y_i = f(x_i) = m \pi_{i+1}$ fogr regression 10 mpm $= a \pi_{i+1} + b \pi_{i+2} + c$ Plane $\hat{y}_i = m^T 2L_i + C$ $\underline{M} = \begin{cases} M_1 \\ M_2 \\ \vdots \\ M_d \end{cases}$



$$\begin{aligned} &l(\underline{x}_{i},y_{i};\underline{M},c) = \begin{cases} 0 & \text{if } y_{i}(\underline{M}^{T}\underline{x}_{i}+c) > 0 \\ -y_{i}(\underline{M}^{T}\underline{x}_{i}+c) & \text{othewise} \end{cases} \\ &\text{we want to minimize the loss } l \\ &\nabla_{\underline{M}_{i}}cl_{X} & \underline{W} = \begin{bmatrix} m_{i} \\ m_{i} \\ m_{i} \end{bmatrix} = \begin{bmatrix} m_{i} \\ cl_{d+1} \end{bmatrix} \\ &\underline{w}^{T}\underline{x}_{i} + cl_{1} = \underbrace{\begin{bmatrix} m_{i} \\ m_{i} \\ m_{i} \end{bmatrix}}_{2} = \underbrace{\begin{bmatrix} x_{i} \\ x_{i} \\ x_{i} \end{bmatrix}}_{2} \\ &= \underbrace{\begin{bmatrix} x_{i} \\ x_{i} \\ x_{i} \end{bmatrix}}_{2} = \underbrace{\begin{bmatrix} x_{i} \\ x_{i} \\ x_{i} \end{bmatrix}}_{2} > 0 \\ &\underline{v}_{i}(\underbrace{\begin{bmatrix} x_{i} \\ m_{i} \end{bmatrix}}_$$

$$\frac{\partial}{\partial x} \left(\underbrace{b}_{x} \right) = \underbrace{b}_{x} = \nabla_{x}^{T} \left(\underbrace{b}_{x} \right)$$

$$\frac{\partial}{\partial x} \left(\underbrace{x}_{b} \right) = \underbrace{b}_{x} = \nabla_{x}^{T} \left(\underbrace{x}_{b} \right)$$

$$\nabla_{x} f(x) = \underbrace{\partial}_{x} f(x) = \underbrace{\partial}_{x} f(x)$$

$$\frac{\partial}{\partial x} f(x) = \underbrace{\partial}_{x} f(x) = \underbrace{\partial}_{x} f(x)$$

$$e(y_i, x_i; \mathbf{m}) = \left\{egin{array}{ll} 0 & ext{if } \left[\, x_i & 1 \,
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$$abla_{\mathbf{m}} e(y_i, x_i; \mathbf{m}) = \left\{egin{array}{ll} 0 & ext{if } \left[\, x_i & 1 \,
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eq l_i \end{array}$$

If $l_i \in \{-1,1\}$, then we can write

$$egin{aligned} e(y_i, x_i; \mathbf{m}) &= \max\{0, -l_i(y_i - [\,x_i \quad 1\,]\,\mathbf{m})\} \ &
abla_{\mathbf{m}} e(y_i, x_i; \mathbf{m}) &= \max\{0, l_i([\,x_i \quad 1\,])\} \end{aligned}$$

For the entire dataset, we have $\mathbf{y}=[y_1;\ldots;y_n]$ and $\mathbf{x}=[x_1;\ldots;x_n]$, $\mathbf{l}=[l_1;\ldots;l_n]$ the average error is:

$$e(\mathbf{x},\mathbf{y};\mathbf{m}) = rac{1}{n} 1_n^ op \max\{0, -\mathbf{l} \odot (\mathbf{y} - [\mathbf{x} \quad 1_n] \, \mathbf{m})\}$$

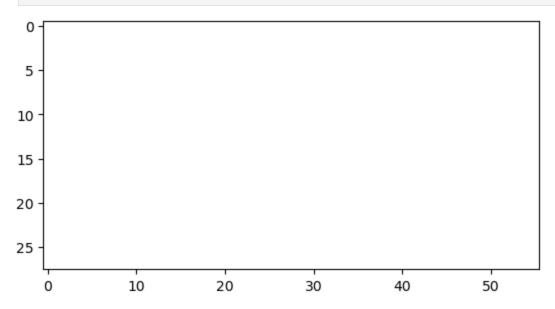
and the average gradient is:

$$abla_{\mathbf{m}} e(\mathbf{x}, \mathbf{y}; \mathbf{m}) = rac{1}{n} \mathbb{1}_n^ op \max\{0, \mathbf{l} \odot ([\mathbf{x} \quad \mathbb{1}_n])\}$$

```
In [1]: # Load MNIST dataset from uint8 byte files
        import struct
        import numpy as np
        # Ref:https://github.com/sorki/python-mnist/blob/master/mnist/loader.py
        def mnist read labels(fname='data/train-labels-idx1-ubyte'):
            with open(fname, 'rb') as file:
                # The file starts with 4 byte 2 unsigned ints
                magic, size = struct.unpack('>II', file.read(8))
                assert magic == 2049
                labels = np.frombuffer(file.read(), dtype='ul')
                return labels
        # Ref:https://github.com/sorki/python-mnist/blob/master/mnist/loader.py
        def mnist read images(fname='data/train-images-idx3-ubyte'):
            with open(fname, 'rb') as file:
                # The file starts with 4 byte 4 unsigned ints
                magic, size, rows, cols = struct.unpack('>IIII', file.read(16))
                assert magic == 2051
```

```
image_data = np.frombuffer(file.read(), dtype='ul')
images = image_data.reshape(size, rows, cols)
return images
```

```
In [2]: # Visualize the dataset
        import matplotlib.pyplot as plt
        import matplotlib.animation as animation
        import matplotlib as mpl
        mpl.rc('animation', html='jshtml')
        train images = mnist read images('data/train-images-idx3-ubyte')
        labels = mnist read labels('data/train-labels-idx1-ubyte')
        zero images = train images[labels==0, ...] # Filter by label == 0
        one images = train images[labels==1, ...] # Filter by label == 1
        # fig, axes = plt.subplots(2, 10)
        # for axrow, imgs in zip(axes, (zero images, one images)):
              for ax, img in zip(axrow, imgs):
                  ax.imshow(img, cmap='gray', vmin=0, vmax=255)
                  ax.axis('off')
        fig, ax = plt.subplots()
        # ims is a list of lists, each row is a list of artists to draw in the
        # current frame; here we are just animating one artist, the image, in
        # each frame
        ims = [[ax.imshow(np.hstack((zero images[i], one images[i])), animated=True,
            for i in range(60)]
        zero images anim = animation.ArtistAnimation(fig, ims, interval=50, blit=Tru
                                        repeat delay=1000, repeat=False)
```



Images as arrays

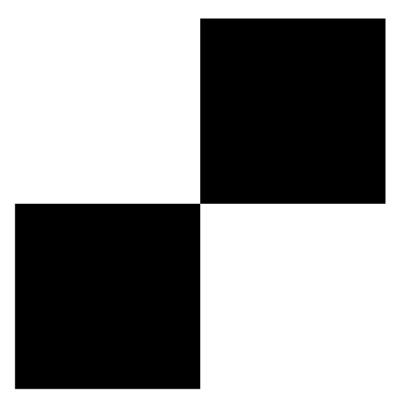
```
In [3]: train_images.shape
Out[3]: (60000, 28, 28)
```

```
In [4]: img1 = train_images[0]
img1
```

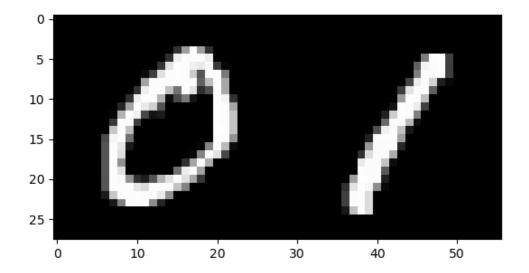
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                        0]], dtype=uint8)
In [5]: ## Visualizing matrices
        fig, ax = plt.subplots()
        ax.axis('off')
        ax.imshow([[1, 0],
                   [0, 1]], cmap='gray')
        # ax.imshow(np.random.rand(28, 28), cmap='gray')
```

Out[5]: <matplotlib.image.AxesImage at 0x7f675bbd5b10>



In [6]: zero_images_anim





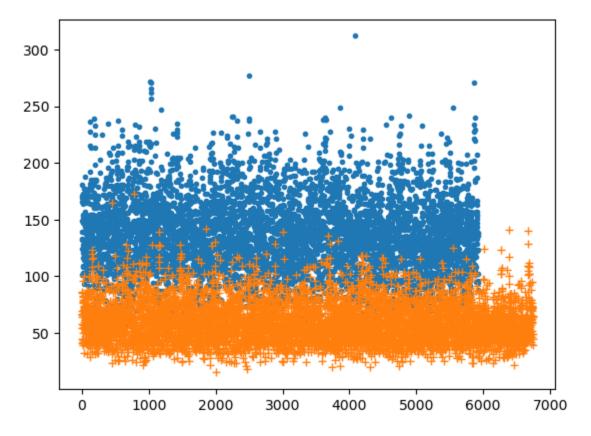
What is a feature

Any property of data sample that helps with the task.

```
In [7]: def feature_n_pxls(imgs):
    n, *shape = imgs.shape
    return np.sum(imgs[:, :, :].reshape(n, -1) > 128, axis=1)

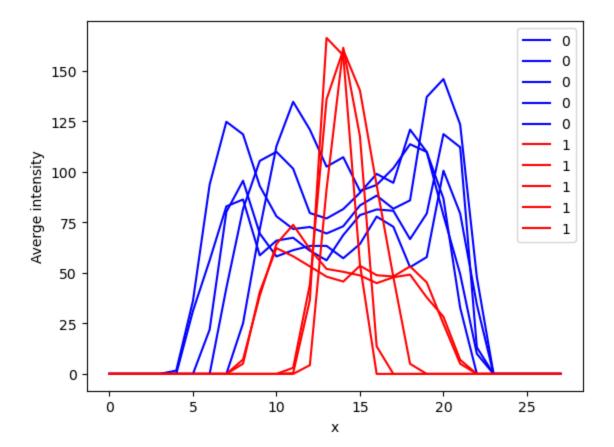
n_pxls_zero_images = feature_n_pxls(zero_images)
    n_pxls_one_images = feature_n_pxls(one_images)
    fig, ax = plt.subplots()
    ax.plot(n_pxls_zero_images, '.')
    ax.plot(n_pxls_one_images, '+')
```

Out[7]: [<matplotlib.lines.Line2D at 0x7f675baaedd0>]



```
In [8]: fig, ax = plt.subplots()
for i in range(5):
        ax.plot(zero_images[i].mean(axis=0), 'b-', label='0')
for i in range(5):
        ax.plot(one_images[i].mean(axis=0), 'r-', label='1')
ax.legend()
ax.set_xlabel('x')
ax.set_ylabel('Averge intensity')
```

Out[8]: Text(0, 0.5, 'Averge intensity')



$$\mu_x(I) = \sum_{x=1}^W rac{x I(x,y)}{\sum_{x=1}^W I(x,y)}$$

$$\sigma_x^2(I) = \sum_{x=1}^W rac{(x-\mu_x)^2 I(x,y)}{\sum_{x=1}^W I(x,y)}$$

```
In [9]: wts = zero_images[0].mean(axis=0)
    mean = (np.arange(wts.shape[0]) * wts).sum() / np.sum(wts)
    var = ((np.arange(wts.shape[0]) - mean)**2 * wts).sum() / np.sum(wts)
    var
```

Out[9]: 22.811061800377757

```
In [10]: def feature_y_var(img):
    wts = img.mean(axis=0)
    mean = (np.arange(wts.shape[0]) * wts).sum() / np.sum(wts)
    var = ((np.arange(wts.shape[0]) - mean)**2 * wts).sum() / np.sum(wts)
    return var
feature_y_var(zero_images[0]), feature_y_var(one_images[0])
```

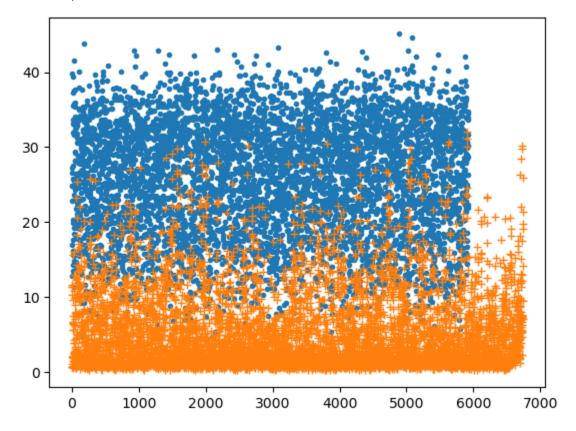
Out[10]: (22.811061800377757, 11.384958735403274)

```
In [11]: def feature_y_var(imgs):
    wts = imgs.mean(axis=-2)
    arange = np.arange(wts.shape[-1])
```

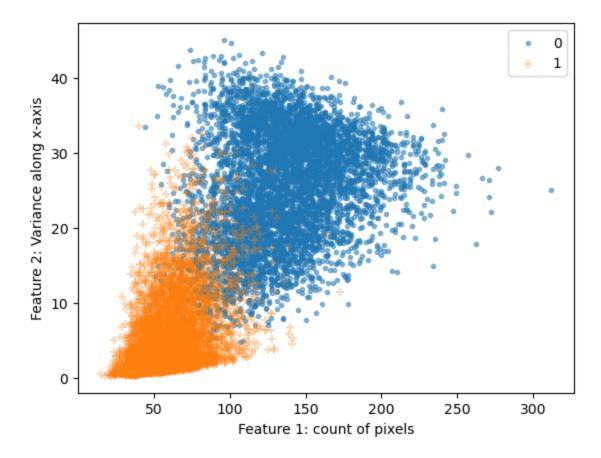
```
mean = (arange * wts).sum(axis=-1) / wts.sum(axis=-1)
mean = mean[:, np.newaxis]
var = ((arange - mean)**2 * wts).sum(axis=-1) / wts.sum(axis=-1)
return var

fig, ax = plt.subplots()
ax.plot(feature_y_var(zero_images), '.')
ax.plot(feature_y_var(one_images), '+')
```

Out[11]: [<matplotlib.lines.Line2D at 0x7f675a1fa4a0>]

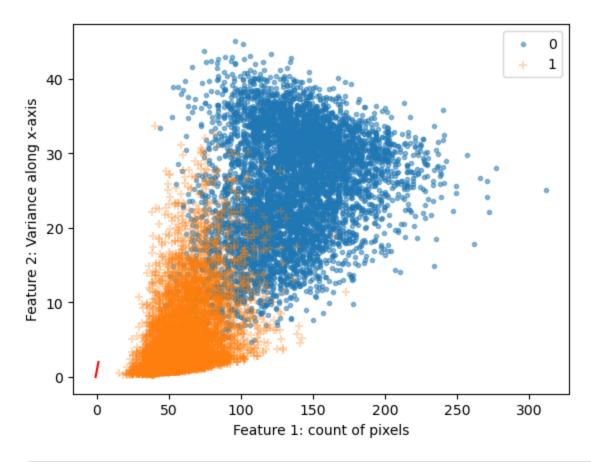


```
In [14]: fig, ax = plt.subplots()
    draw_features(ax, zero_features, one_features)
    plt.show()
```



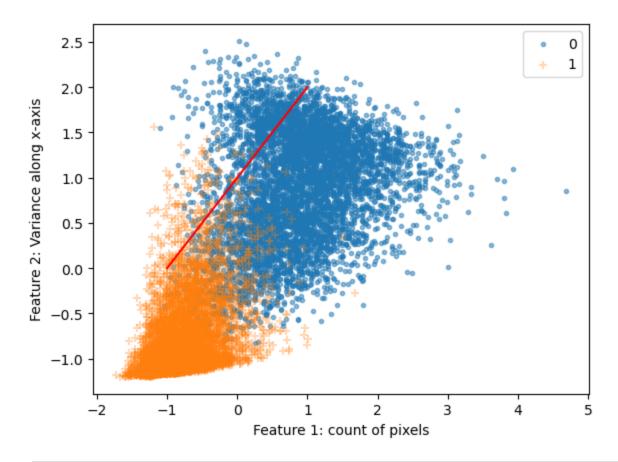
```
In [15]: bfm = np.ones(2)
fig, ax = plt.subplots()
draw_features(ax, zero_features, one_features)
x = np.linspace(-1, 1, 21)
ax.plot(x, x*bfm[0] + bfm[1], 'r-')
```

Out[15]: [<matplotlib.lines.Line2D at 0x7f6759fc66e0>]



```
In [16]: bfm = np.ones(2)
         Y = np.hstack((np.ones(zero_features.shape[0]), np.full(one_features.shape[6])
         features = np.vstack((zero features, one features))
         FEATURES_MEAN = features.mean(axis=0, keepdims=1)
         FEATURES_STD = features.std(axis=0, keepdims=1)
         def norm features(features):
             return (features - FEATURES_MEAN) / FEATURES_STD
         X = norm features(features)
         np.savez('zero_one_train_features.npz',
                  mean=FEATURES MEAN, std=FEATURES STD,
                  normed features=X,
                  labels=Y)
         fig, ax = plt.subplots()
         draw_features(ax, X[Y > 0, :], X[Y < 0, :])
         x = np.linspace(-1, 1, 21)
         ax.plot(x, x*bfm[0] + bfm[1], 'r-')
```

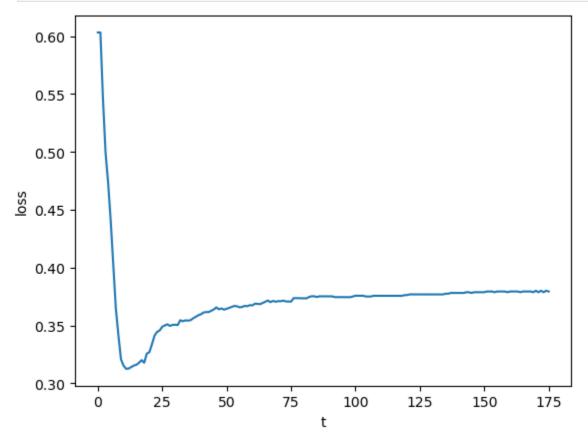
Out[16]: [<matplotlib.lines.Line2D at 0x7f675662ece0>]



```
In [17]: def error(X, Y, bfm):
             ### BEGIN SOLUTION
             return - (X[:,1] - X[:, 0] * bfm[0] - bfm[1]) * Y
             ### END SOLUTION
         def grad error(Xw, Yw, bfm):
             ### BEGIN SOLUTION
             return np.array([(Xw[:, 0]*Yw).mean(), Yw.mean()])
             ### END SOLUTION
         def train(X, Y, lr = 0.1):
             ### BEGIN SOLUTION
             bfm = np.random.rand(2)*4-2
             bfm_prev = bfm + 1
             list_of_bfms = [bfm]
             list of errors = []
             err = error(X, Y, bfm)
             grad_err = grad_error(X[err > 0, :], Y[err > 0], bfm)
             list_of_errors.append(err[err > 0].mean())
             for _{\rm in} range(400):
                 if np.linalg.norm(grad err) < 0.001:</pre>
                      break
                 err = error(X, Y, bfm)
                  grad err = grad error(X[err > 0, :], Y[err > 0], bfm)
                 bfm prev = bfm
                  bfm = bfm - lr * grad_err
                  list of bfms.append(bfm)
```

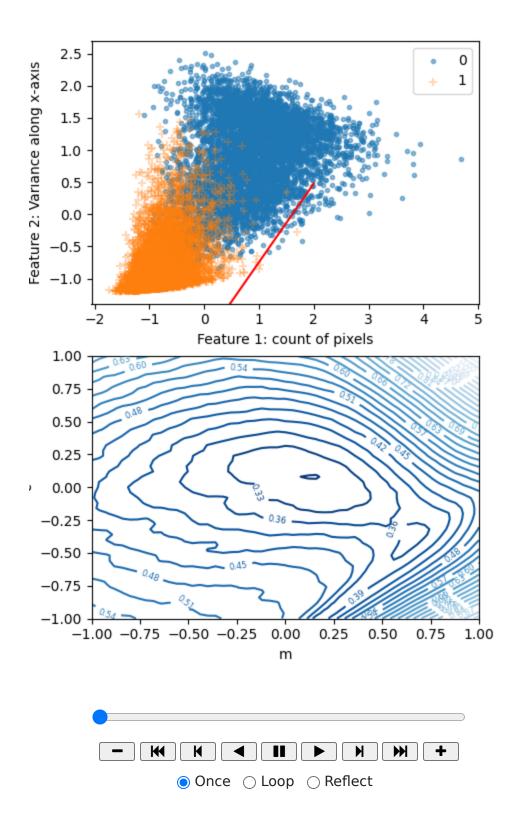
```
list_of_errors.append(err[err > 0].mean())
    return bfm, list_of_bfms, list_of_errors
    ### END SOLUTION

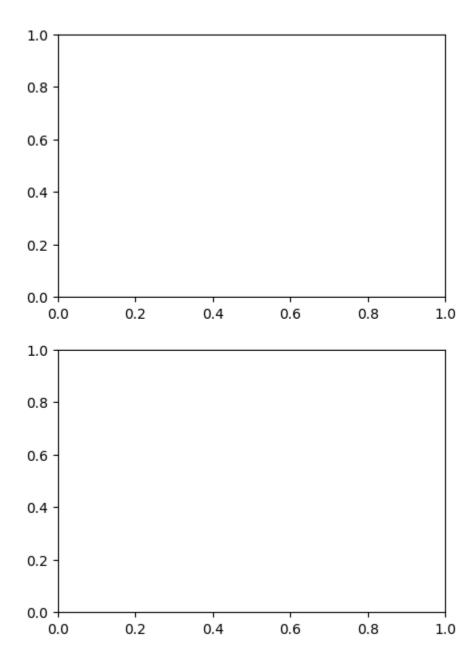
OPTIMAL_BFM, list_of_bfms, list_of_errors = train(X, Y)
fig, ax = plt.subplots()
ax.plot(list_of_errors)
ax.set_xlabel('t')
ax.set_ylabel('loss')
plt.show()
```

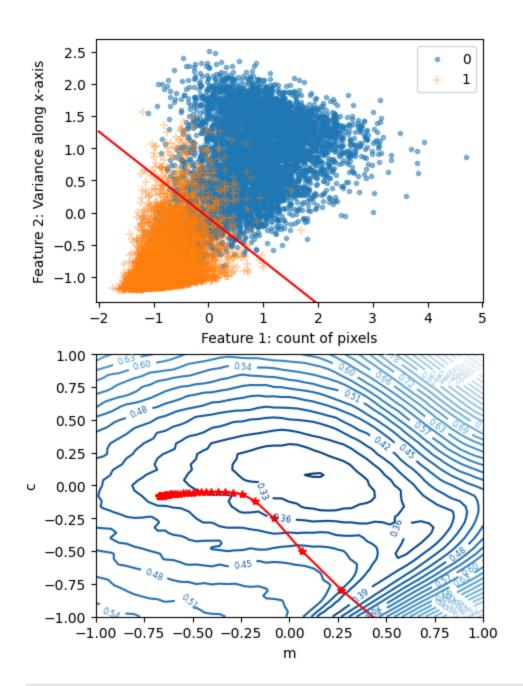


```
In [18]: fig, axes = plt.subplots(2, 1, figsize=(5, 7.5))
         class Anim:
             def __init__(self, fig, axes, X, Y):
                  self.fig = fig
                  self.ax = axes[0]
                  self.ax1 = axes[1]
                  self.fts = draw_features(self.ax, X[Y > 0, :], X[Y < 0, :])</pre>
                  self.line, = self.ax.plot([], [], 'r-')
                 m, c = np.meshgrid(np.linspace(-1, 1, 51), np.linspace(-1, 1, 51))
                  totalerr = np.empty like(m)
                  for i in range(m.shape[0]):
                      for j in range(m.shape[1]):
                          err = error(X, Y, [m[i, j], c[i,j]])
                          totalerr[i, j] = err[err > 0].mean()
                  self.ctr = self.ax1.contour(m, c, totalerr, 30, cmap='Blues r')
                  self.ax1.set xlabel('m')
                  self.ax1.set ylabel('c')
```

```
self.ax1.clabel(self.ctr, self.ctr.levels, inline=True, fontsize=6)
        self.m hist = []
        self.c hist = []
        self.line2, = self.ax1.plot([], [], 'r*-')
   def anim init(self):
        return (self.line, self.line2)
   def update(self, bfm):
        x = np.linspace(-2, 2, 21)
        self.line.set data(x, x * bfm[0] + bfm[1])
        self.m_hist.append(bfm[0])
        self.c hist.append(bfm[1])
        self.line2.set data(self.m hist, self.c hist)
        return self.line, self.line2
fig, axes = plt.subplots(2, 1, figsize=(5, 7.5))
a = Anim(fig, axes, X, Y)
animation.FuncAnimation(fig, a.update, frames=list_of_bfms[::3],
                        init func=a.anim init, blit=True, repeat=False)
```



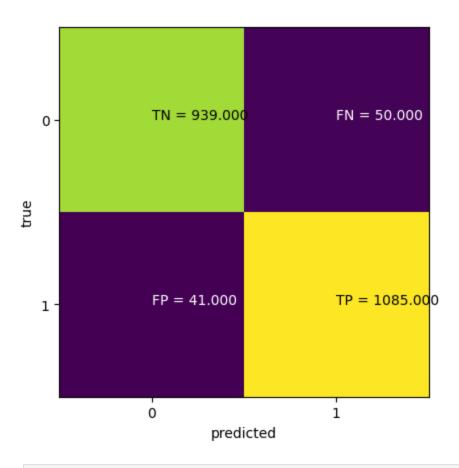


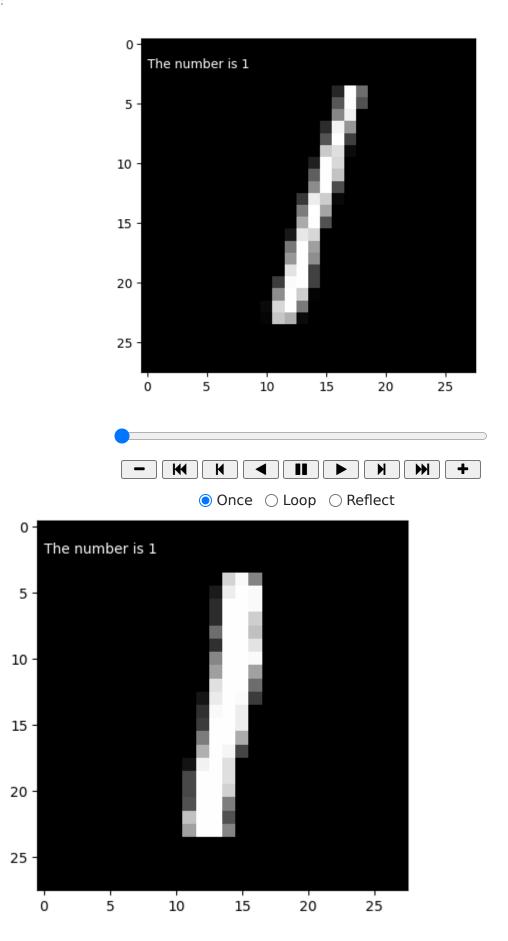


In [20]: accuracy = np.sum(zero_one_test_labels == zero_one_predicted_labels) / len(z
accuracy

```
Out[20]: 0.9569739952718677
In [21]: positive label = 1
          negative label = 0
          TP = np.sum((zero one test labels == positive label) & (zero one predicted l
Out[21]: 1085
In [22]: TN =
                np.sum((zero one test labels == negative label) & (zero one predicted
Out[22]: 939
In [23]: FP = np.sum((zero one test labels != positive label) & (zero one predicted l
          FP
Out[23]: 41
In [24]: FN = np.sum((zero one test labels != negative label) & (zero one predicted l
          FΝ
Out[24]: 50
In [25]: # Confusion matrix
          fig, ax = plt.subplots()
          ax.imshow([[TN, FN],
                    [FP, TP]])
          ax.set_xlabel('predicted')
          ax.set ylabel('true')
          ax.set xticks([0, 1])
          ax.set yticks([0, 1])
          ax.text(0, 0, 'TN = %.3f' % TN)
ax.text(1, 0, 'FN = %.3f' % FN, color='w')
          ax.text(0, 1, 'FP = %.3f' % FP, color='w')
          ax.text(1, 1, 'TP = %.3f' % TP)
```

Out[25]: Text(1, 1, 'TP = 1085.000')





Single Layer Neural Networks

Read Chapter 2 and 3 of UDL Book

Notes Single Layer Neural Networks are simplest kind of neural networks. But before we dive into single layer neural networks, may be we should focus on the name *neural* networks. The name neural networks comes from biological neurons.

Similarities between Artificial neuron and Biological neuron

- No description has been provided for this image
- No description has been provided for this image
 - 1. The excitation or firing of a biological neuron can be equated to a high positive value of units (x_1, x_2, x_3) in artificial neurons.
 - 2. The synapse in biological neuron determines which input excitations will have excitatory or inhibitary impact on output excitations. Synapses can strengthen, weaken, disconnect or form new connections during biological learning. Similarly to excitatory synapes, positive weights can cause positive input values to contribute to positive output values.
 - 3. Usually multiple excitatory inputs are required excite the output neuron.

References:

1. https://openstax.org/books/biology/pages/35-2-how-neurons-communicate

Differences

- 1. Biological neuron is all or None
- 2. Biological neuron has a time component No description has been provided for this image

notes

1. The activity of the biological neuron is an "all-or-none" process. Articial activations are typically continuous range. Even when sigmoid or softmax nonlinearities.

2. Biological neuron has time dynamics. The input activations are integrated over time.

Next

- 2. Show visualization of 1D optimization and loss functions.
- 3. Build to visualizations in the UDL book. Connect to KD tree and nearest neighbor classification.
- 4. Show the tensflow js visualization.

References

- 1. http://playground.tensorflow.org
- 2. https://knowyourdata-tfds.withgoogle.com/#tab=STATS&dataset=tf_flowers
- 3. "Flowers", The TensorFlow Team. Jan 2019. Online http://download.tensorflow.org/example_images/flower_photos.tgz