## **Graph Cut based Inference**

An energy / potential is called **submodular** iff for every pair of variables :

$$E(0, 0, \bar{\mathbf{x}}_{ij}) + E(1, 1, \bar{\mathbf{x}}_{ij}) \le E(0, 1, \bar{\mathbf{x}}_{ij}) + E(1, 0, \bar{\mathbf{x}}_{ij})$$

$$\arg\min_{\mathbf{x}} \sum_{i \in \mathcal{V}} \underbrace{c_{it}(1-x_i)} + \sum_{i \in \mathcal{V}} \underbrace{c_{si}x_i} + \sum_{i,j \in \mathcal{E}} \underbrace{c_{ij}(1-x_i)x_j}$$
all terms submodular