### IMDB graph exploration

Project for the exam of advanced algorithms and graph mining

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Lecturers:
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#### Chosen questions

- **1.G)** Considering only the movies up to year x with x in {1930,1940,1950,1960,1970,1980,1990,2000,2010,2020}, write a function which, given x, computes the average number of movies per actor up to year x.
- **2.3)** Considering only the movies up to year x with x in {1930,1940,1950,1960,1970,1980,1990,2000,2010,2020} and restricting to the largest connected component of the graph. Approximate the closeness centrality for each node. Who are the top-10 actors?
- 3.III) Which is the pair of movies that share the largest number of actors?
- **4.-)** Which is the pair of actors who collaborated the most among themselves?

.tsv read by pandas, structure achieved  $\Rightarrow$ 

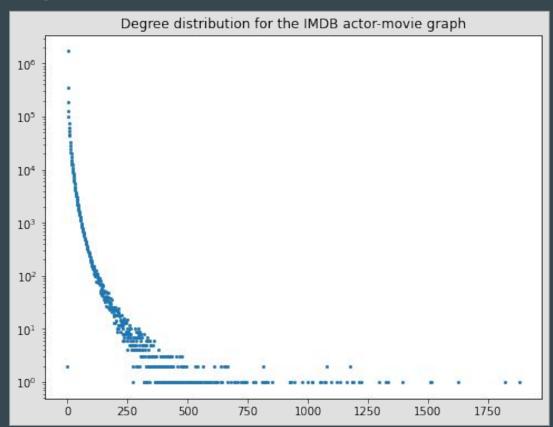
13509	Abuda, Rob	Blind Eyes (2003) (V)	2003
13510	Abude, Leonardo Cesare	La passione di Giosu? l'Ebreo (2005)	2005
13511	Abudi, Ilan	Shitat HaShakshuka (2008)	2008
13512	Abudin, Mohammed	Go-Con! Japanese Love Culture (2000)	2000
13513	Abudlkar, Tahira	Belles & Whistles (2002)	2002
13514	Abudo, Abijiang	Guangzhou laile Xinjiang wa (1995)	1995

Year separated by movie title by a simple regex applied through pandas  $df[2] = df[1].str.extract(r'(\d{4})', expand=True)$ 

Having the dataframe, I generate the actor and movies nodes.

```
# get all that will be the actor nodes
                                                                             Nodes
actors = df.actor.unique() #*
# find all unique movies records, create a list of tuples of type
# ('Movie title', {year: xxxx} which allows graph population through networkx method :)
movies_dict = df.drop(columns='actor').drop_duplicates().set_index('movie').to_dict('index')
movies_tuples_list = [(k, v) for k, v in movies_dict.items()]
oriGinal = nx.Graph()
oriGinal.add_nodes_from(actors, bipartite = 0)  # 0  is actors, 1  is movies
print(f"Number of nodes after adding actors is {oriGinal.number_of_nodes()}")
oriGinal.<u>add_nodes_from(movies_tuples_list</u>, bipartite = 1)
edges = df.to_records(index=False)
                                                                             Edges
oriGinal.add_edges_from(edges)
```

G = nx.convert\_node\_labels\_to\_integers(oriGinal, label\_attribute='original\_name')



Degree distribution

#### Q.1.G. Average number of movies per actor up to year x

Strategy

#### Given the graph:

- 1. Create subgraph composed of all actors, and the movies up to year x
- 2. Get the cardinalities of the neighborhoods of each actor node of subgraph
- 3. Calculate the average (two flavors):
  - a. Considering all actors, regardless of the year
  - b. Considering only actors that made at least one movie

Cycle for all the years of interest

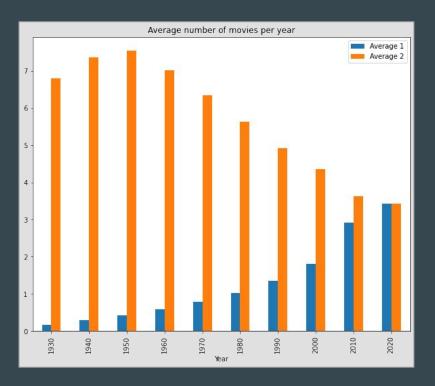
#### Q.1.G. Average number of movies per actor up to year x

#### Pythonized version

```
def avgMoviesPerActorUpToYear(graph, act_nodes, mv_nodes, year):
    # get movies nodes up to a certain year
    movies_up_to_year = {x for x,y in graph.nodes(data=True) if y['bipartite'] == 1 and y['year'] <= year}
    # define the nodes of interest for the year (i.e. both movie and actor nodes)
    nodes_subset = movies_up_to_year.union(act_nodes)
    subgraph = graph.subgraph(nodes_subset)
    assert subgraph.number_of_nodes() == len(nodes_subset)
    subgraph_actor_nodes = {n for n, d in subgraph.nodes(data=True) if d["bipartite"] == 0}
    degrees = subgraph.degree(nbunch = subgraph_actor_nodes)
    deg_data = pd.DataFrame(degrees)
    sol = (year, deg_data[1].mean(), deg_data[1].replace(0, np.NaN).mean()) #convenient for output later
    return sol</pre>
```

### Q.1.G. Average number of movies per actor up to year x

- Results



	Avg <sub>1</sub>	Avg <sub>2</sub>
1930	0.163	6.790
1940	0.300	7.355
1950	0.427	7.533
1960	0.583	7.018
1970	0.782	6.345
1980	1.030	5.627
1990	1.350	4.925
2000	1.813	4.356
2010	2.912	3.624
2020	3.427	3.427

- □ Up to a certain year x, with x in {1930, 1940, 1950, 1960, 1970, 1980, 1990, 2000, 2010, 2020}
- ⇒ Restricting to the largest connected component

In this case, literal implementation of the pseudocode in the original article [\*] was implemented

- 1. Let *k* be the number of iterations needed to obtain the desired error bound.
- 2. In iteration i, pick vertex  $v_i$  uniformly at random from G and solve the SSSP problem with  $v_i$  as the source.
- 3. Let

$$\hat{c}_u = 1/\sum_{i=1}^k \frac{n \, d(v_i, u)}{k(n-1)}$$

be the centrality estimator for vertex u.

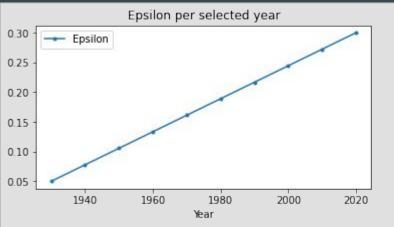
```
def closenessCentralityUpToYear(graph, act_nodes, year, k = None, epsilon = None):
    # fundamental lines for the methods are shown. Before: subselection of nodes up to a certain year and largest CC
      [\ldots]
    # calculate sample size, if an epsilon is specified
    if epsilon is not None:
        import math
        k = math.ceil(math.log(cc_subgraph.number_of_nodes())/math.pow(epsilon, 2))
    # sample k nodes
    starting_nodes = random.sample(list(largest_cc), k)
    # find shortest paths starting from sample nodes
    sssp_s = list(map(lambda x: nx.single_source_shortest_path_length(cc_subgraph, x), tqdm(starting_nodes)))
    sssp_s_dict = {}
    for starting_node in tqdm(starting_nodes):
        sssp_s_dict[starting_node] = nx.single_source_shortest_path_length(cc_subgraph, starting_node)
    n = len(largest_cc)
    distances_df = pd.DataFrame(sssp_s).T
    distances_df['centrality'] = distances_df.mean(numeric_only=True, axis=1).apply(lambda x: 1/(x*(n/(n-1))))
    return distances df
```

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                                           V<sub>2</sub>
                                                 ٧<sub>3</sub>
                                     d<sub>1.1</sub>
                                           d_{12}
    s<sub>i</sub> - i-th source
                                                 d_{13}
    v<sub>i</sub> - j-th node
                                     d_{2,1}
                                                 d_{2.3}
                               S<sub>2</sub>
                                     d_{3,1}
```

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                                               d<sub>1.2</sub>
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                                                                                   d_{2.1}
     s<sub>;</sub> - i-th source
                                                      d_{13}
                                                                     V<sub>1</sub>
                                                                                          d_{31}
    v<sub>i</sub> - j-th node
                                                      d_{2.3}
                                                                            d<sub>1.2</sub>
                                                                                   d_{2.2}
                                  S<sub>2</sub>
                                        d_{2,1}
                                               d_{2.2}
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                                                                            d_{1.3}
                                         d_{3,1}
                                                                                          d_{3.3}
```

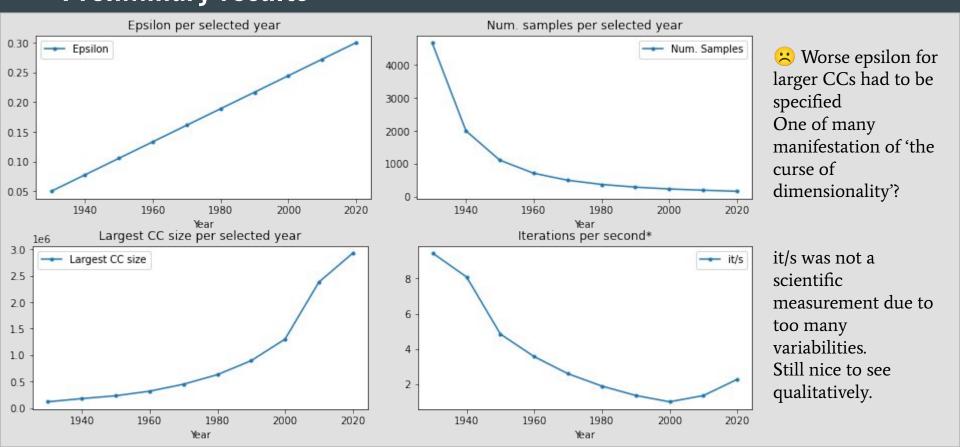
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     return distances df
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                                                                                                                                  centr
                                           ۷<sub>1</sub>
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                                           d<sub>1.1</sub>
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     s<sub>;</sub> - i-th source
                                    S₁
                                                         d<sub>1.3</sub>
                                                                         V<sub>1</sub>
                                                                                               d_{31}
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     v<sub>i</sub> - j-th node
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                                                         d_{2.3}
                                                                                d<sub>1.2</sub>
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     d'_{ii} - d(s_i, v_i)
                                                                                 d<sub>1,3</sub>
                                                                                       d_{2.3}
                                           d_{3,1}
                                                                                               d_{3.3}
                                                                                                                   \overline{d}(s_3)
                                                                                                                                  \hat{c}(s_3)
```

## Q.2.3 Approximate the closeness centrality for each node. - Preliminary results



Choice for epsilon followed a linear progression from 0.05 to 0.3 (unfortunately quite large), for each of the input years. The choice was heuristically made, the objective was to have "reasonable results" (in terms of errors) in reasonable times.

### Q.2.3 Approximate the closeness centrality for each node. - Preliminary results



1970

1980

1990

2000

2010

2020

Results

\*colorations were made by hand, therefore coloration-completeness is not guaranteed 'Bracey, Sidney', 'Fawcett, George', 'Beery, Noah (1)', 'Siegmann, George', 'Marshall, Tully', 'De Brulier, Nigel', 'Holmes, Stuart', 'Swickard, Josef', 'McDowell, Claire', 'Pitts, Zasu']

1930

['Steers, Larry', 'Bracey, Sidney', 'White, Leo (1)', 'Lucas, Wilfred', 'Semels, Harry (1)', 'Corrado, Gino', 'Mulhall, Jack', 'Brady, Ed (111)', 'Hoyt, Arthur', "O'Malley, Pat (1)"]

1940 ['Steers, Larry', 'Corrado, Gino', 'Flowers, Bess', 'Semels, Harry (I)', 'Harris, Sam (II)', 'White, Leo (I)', 'Holmes, Stuart', 'Blue, Monte', "O'Malley, Pat (I)", 'Hagney, Frank'] 1950

1960 ['Flowers, Bess', 'Harris, Sam (II)', 'Steers, Larry', 'Corrado, Gino', 'Farnum, Franklyn', 'Chefe, Jack', 'Auer, Mischa', 'Miller, Harold (I)', "O'Brien, William H.", 'Holmes, Stuart']

['Harris, Sam (II)', 'Flowers, Bess', 'Tamiroff, Akim', 'Welles, Orson', 'Farnum, Franklyn', 'Miller, Harold (I)', 'Frees, Paul', 'Sayre, Jeffrey', 'Stevens, Bert (I)', 'Quinn, Anthony (I)']

[Welles, Orson], 'Hitler, Adolf, 'Carradine, John', 'Quinn, Anthony (1)', 'Flowers, Bess', 'Douglas, Kirk (1)', 'Sinatra, Frank', 'Fonda, Henry', 'Wayne, John (1)', 'Harris, Sam (11)']

['Reagan, Ronald (1)', 'Hitler, Adolf, 'Madonna', 'De Niro, Robert, 'Schwarzenegger, Arnold', 'Kidman, Nicole', 'Pitt, Brad', 'Hanks, Tom', 'Caine, Michael (1)', Hopper, Dennis']

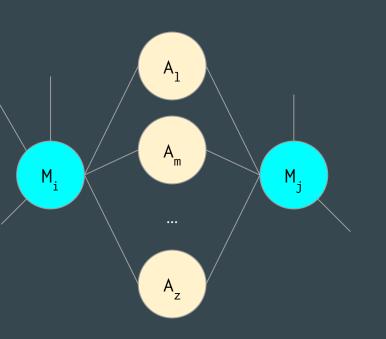
['Jackson, Samuel L.', 'Hitler, Adolf', 'Depp, Johnny', 'Sheen, Martin', 'De Niro, Robert', 'Willis, Bruce', 'Madonna', 'Lee, Christopher (1)', 'Clooney, George', 'Hanks, Tom']

['Flowers, Bess', 'Harris, Sam (II)', 'Welles, Orson', 'Miller, Harold (I)', 'Tamiroff, Akim', 'Farnum, Franklyn', 'Sayre, Jeffrey', 'Niven, David (I)', 'Quinn, Anthony (I)', 'Holmes, Stuart']

['Steiger, Rod', 'Sutherland, Donald (1)', 'Lee, Christopher (1)', Hitler, Adolf, 'Welles, Orson', 'Caine, Michael (1)', 'Loren, Sophia', 'Schell, Maximilian', 'York, Michael (1)', Hopper, Dennis]

### Q.3.III Which is the pair of movies that share the largest number of actors?

### Q.3.III Which is the pair of movies that share the largest number of actors?



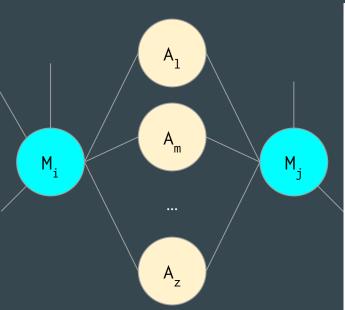
#### Reasoning:

Given two movie nodes  $M_i$  and  $M_j \in G$ , the common actors are represented by  $\mathbf{N}(M_i) \cap \mathbf{N}(M_j)$ 

 $\Rightarrow$  find maximum intersection

### Q.3.III Which is the pair of movies that share the largest number of

actors?



Basic strategy: for each two different nodes, intersect the adjacency lists to find common neighbors.

Main idea to solve this would be to do an intersection of the edges of each of the movies.

Doing the intersections of all sets can become very expensive timewise.

Given an unordered set of sets  $\hat{S} = \{S_1, \ldots, S_N\}$  for any  $N \in \mathbb{N}$  s.t.  $|S_i| \leq M$  for any  $i = 1, \ldots, N$  and  $M \in \mathbb{N}$ ; finding the max intersection would cost  $\mathcal{O}(N)$ , and  $\mathcal{O}(\min\{|U_i|, |U_j|\})$  (python documentation), reaching  $\mathcal{O}(N*M)$ .

In this case I use the following simple observations:

- For any two given sets  $S_i \neq S_j$  (for  $i \neq j = 1, ..., N$ ) it is true that  $|S_i \cap S_j| \leq \min\{|S_i|, |S_j|\}$
- Let m be the maximum intersection found until a certain iteration. Then if  $U_i$  (or  $U_j$ ) is s.t.  $|U_i| < m$  (or  $|U_j| < m$ ) then necessarily  $|U_i \cap U_j| < m$ , i.e. it is not necessary to do the intersection to infer that the cardinality of that intersection would now surpass the current max. Therefore, it's possible to only check the cardinality and skip the calculation of the intersections.

With this heuristic, although the formal complexity would be essentially the same, in practice a lot of the intersections are skipped.

### Q.3.III Which is the pair of movies that share the largest number of actors?

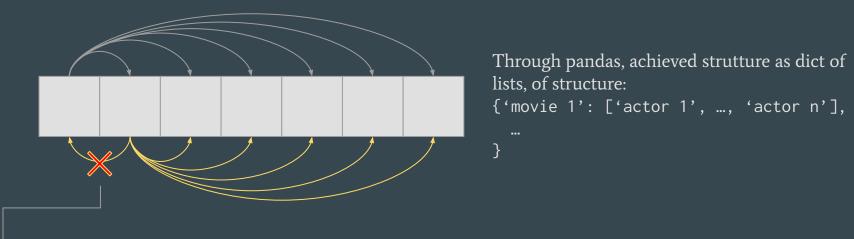
```
def moviesWithMaxCommonNumActors(graph, mv_nodes):
    mv_act = nx.to_dict_of_lists(graph)
    print(mv_act[1])
    current_solution = (None, None)
   current_max = 0
    for movie in tqdm(mv_nodes):
        if len(mv_act[movie]) >= current_max:
            for second_movie in mv_nodes:
                if len(mv_act[second_movie]) >= current_max and movie != second_movie:
                    temp = len(set(mv_act[movie]).intersection(set(mv_act[second_movie])))
                    if current_max < temp:</pre>
                        current_solution = (movie, second_movie)
                        current_max = temp
                        print(f"Current max: {current_max}")
    return current_solution
```

### Q.3.III Which is the pair of movies that share the largest number of actors? - Results

'Kingdom Hearts II (2005) (VG)' 
→ 'Kingdom Hearts II: Final Mix+ (2007) (VG)'

194 common actors (mainly, voice actors)

Graph constructed from the given dataset (not from previous graph due to memory limitations)
 For the graph generation:



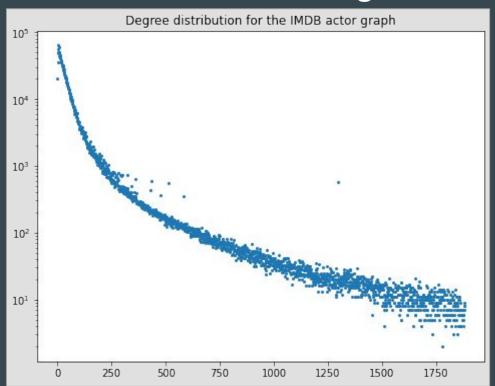
Skipped calculation of intersections, both for correctness (to avoid double counting an edge) and performance reasons.

```
def constructGraphAndFindMaxCollaborationGivenActorsGraph(imdb df f):
    actor graph dict = imdb df f.groupby('movie')['actor'].apply(list).to dict()
   mass = 0
    sol = (None, None)
    for movie in tqdm(actor graph dict):
       current actors list = actor graph dict[movie]
        for i in range(len(current actors list)):
            for j in range(i+1, len(current actors list)):
                if current actors list[i] != current actors list[j]:
                    if not actor graph.has edge(current actors list[i], current actors list[j]):
                        actor graph.add edge(current actors list[i], current actors list[j], weight=1)
                    else:
                        actor graph[current actors list[i]][current actors list[j]]['weight'] += 1
                        if actor_graph[current_actors_list[i]][current_actors_list[j]]['weight'] > mass:
                            mass = actor graph[current actors list[i]][current actors list[j]]['weight']
                            sol = (current actors list[i], current actors list[j])
    return (actor graph, mass, sol)
```

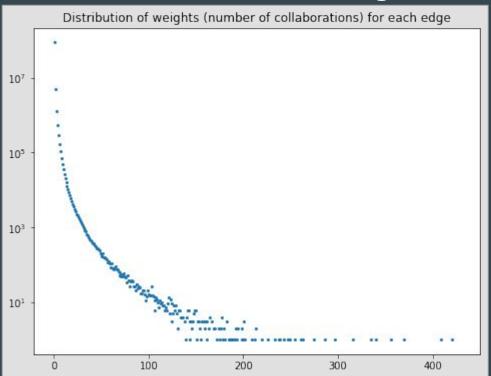
```
archi = gr.edges(data=True)
massimo = 0
sol = (None, None)
hist = [0]*500
i = 0
sol = (None, None)
for arco in archi:
    curr weight = arco[2]['weight']
    #print(curr weight)
    if massimo < curr weight:</pre>
        massimo = curr weight
        sol = (arco[0], arco[1])
    hist[curr weight] += 1
    i+=1
```

As an alternative.. classic algorithm for finding max, given the constructed graph.

```
Result: ('Byron, Tom (I)', 'North, Peter (I)') collaborated 420 times
```



Degree distribution for the actor graph x axis: degree y axis: number of occurrences of the degree



Horizontal axis: edge weight

Vertical axis: number of edges with said weight

### Thank you