

$$\begin{aligned}
-\frac{d^2u}{dx^2} - u &= \sin x \\
u(0) &= 0 \\
\frac{du(2)}{dx} - u(2) &= 0 \\
[0, 2] \ni x &\rightarrow u(x) \in \mathbb{R}
\end{aligned}$$

$$\begin{aligned}
f'(x) &= \frac{f(x+h) - f(x-h)}{2h} \\
f''(x) &= \frac{f(x+h) + f(x-h) - 2f(x)}{h^2}
\end{aligned}$$

$$\begin{aligned}
-u'' - u &= \sin x \\
-\frac{u(x+h) + u(x-h) - 2u(x)}{h^2} - u(x) &= \sin x \\
-\frac{u_{i+1} + u_{i-1} - 2u_i}{h^2} - u_i &= \sin x_i \\
u_{i-1} \left[ \frac{-1}{h^2} \right] + u_i \left[ \frac{2}{h^2} - 1 \right] + u_{i+1} \left[ \frac{-1}{h^2} \right] &= \sin x_i
\end{aligned}$$

$$u_0 = 0$$

$$\begin{aligned}
u'(2) - u(2) &= 0 \\
\frac{u(2+h) - u(2-h)}{2h} - u(2) &= 0 \\
\frac{u_{n+1} - u_{n-1}}{2h} - u_n &= 0 \\
u_{n+1} - u_{n-1} - 2hu_n &= 0 \\
u_{n+1} &= u_{n-1} + 2hu_n
\end{aligned}$$

$$\begin{aligned}
u_{n-1} \left[ \frac{-1}{h^2} \right] + u_n \left[ \frac{2}{h^2} - 1 \right] + (u_{n-1} + 2hu_n) \left[ \frac{-1}{h^2} \right] &= \sin x_n \\
u_{n-1} \left[ \frac{-1}{h^2} \right] + u_n \left[ \frac{2}{h^2} - 1 \right] + u_{n-1} \left[ \frac{-1}{h^2} \right] + u_n \left[ \frac{-2}{h} \right] &= \sin x_n \\
u_{n-1} \left[ \frac{-2}{h^2} \right] + u_n \left[ \frac{2}{h^2} - 1 - \frac{2}{h} \right] &= \sin x_n
\end{aligned}$$

$$\begin{bmatrix}
1 & 0 & & \cdots & & & & 0 \\
& & \ddots & & & & & \\
\vdots & \cdots & 0 & \left[ \frac{-1}{h^2} \right] & \left[ \frac{2}{h^2} - 1 \right] & \left[ \frac{-1}{h^2} \right] & 0 & \cdots & \vdots \\
& & & & \ddots & & & & \\
0 & & & \cdots & & & \left[ \frac{-2}{h^2} \right] & \left[ \frac{2}{h^2} - 1 - \frac{2}{h} \right] & 
\end{bmatrix} \cdot \begin{bmatrix} u_0 \\ \vdots \\ u_n \end{bmatrix} = \begin{bmatrix} 0 \\ \vdots \\ \sin x_i \\ \vdots \\ \sin x_n \end{bmatrix}$$