### 2. ORB特征

#### 2.1 ORB提取



# 2.2+2.3 ORB描述和暴力匹配



#### 问题回答

- ① ORB的描述符是一个二进制的向量, 因此是一个二进制特征.
- ② 取50表示有三分之二的特征描述是相似的, 当取更大值时会有很多误匹配, 取更小值则匹配数量会太少.
- ③暴力匹配约花了122ms,可以根据视差只对局部区域进行搜索,或者使用kdtree来加速搜索速度.

# 3. E恢复R, t

程序运行结果截图

```
R1 = 0.998596 -0.0516992 0.0115267

0.0513961 0.99836 0.0252005

-0.0128107 -0.0245727 0.999616

R2 = 0.365887 0.0584576 -0.928822

0.00287462 -0.998092 -0.0616848

-0.930655 0.0198996 -0.365356

t1 = -0.581301

-0.0231206

0.401938

t2 = 0.581301

0.0231206

-0.401938

t^R = -0.0203619 -0.400711 -0.0332407

0.393927 -0.035064 0.585711

-0.00678849 -0.581543 -0.0143826
```

#### 4. G-N BA

程序运行结果截图

points: 76

iteration 0 cost=622769.1141257 iteration 1 cost=12206.604278533 iteration 2 cost=12150.675965788 iteration 3 cost=12150.6753269 iteration 4 cost=12150.6753269

cost: 150.6753269, last cost: 150.6753269

estimated pose:

问题回答:

① 重投影误差定义为:

$$e_i = u_i - rac{1}{z_i} K \exp\left( \xi^\wedge 
ight) P_i$$

这里,  $u_i$ 是像素坐标,  $P_i$ 是点的3D坐标, K是相机投影矩阵,  $z_i$ 是 $P_i$ 在相机坐标系下的深度.

② 线性化 $e(\xi + \Delta \xi) = e + J\Delta \xi$ , Jacobian矩阵为:

$$\begin{split} J &= \frac{\partial e}{\partial \Delta \xi} = \frac{\partial e}{\partial P'} \frac{\partial P'}{\partial \Delta \xi} \\ &\frac{\partial e}{\partial P'} = - \left[ \begin{array}{cc} \frac{\partial u}{\partial X'} & \frac{\partial u}{\partial Y'} & \frac{\partial u}{\partial Z'} \\ \frac{\partial v}{\partial Y'} & \frac{\partial v}{\partial Y'} & \frac{\partial v}{\partial Z'} \end{array} \right] = - \left[ \begin{array}{cc} \frac{f_x}{Z'} & 0 & -\frac{f_x X'}{Z'^2} \\ 0 & \frac{f_y}{Z'} & -\frac{f_y Y'}{Z'^2} \end{array} \right] \\ &\frac{\partial P'}{\partial \Delta \xi} = \begin{bmatrix} I & -P'^{\wedge} \end{bmatrix} \\ \Rightarrow J = - \left[ \begin{array}{cc} \frac{f_x}{Z'} & 0 & -\frac{f_x X'}{Z'^2} \\ 0 & \frac{f_y}{Z'} & -\frac{f_y Y'}{Z'^2} \end{array} \right] \begin{bmatrix} I & -P'^{\wedge} \end{bmatrix} \end{split}$$

这里对K做了处理,去除掉了最后一行,其不构成误差,偏导数恒等于0.

③ 解出之后做如下更新

$$\exp(\xi) = \exp(\Delta \xi) \exp(\xi)$$

# 5. ICP轨迹对齐

程序运行结果:



