

# Assignment 2

## Filters

### Parts 1-3

CMPUT206

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TA: Bernal Manzanilla

# Intro: Create your own 2D convolution filtering script in Python

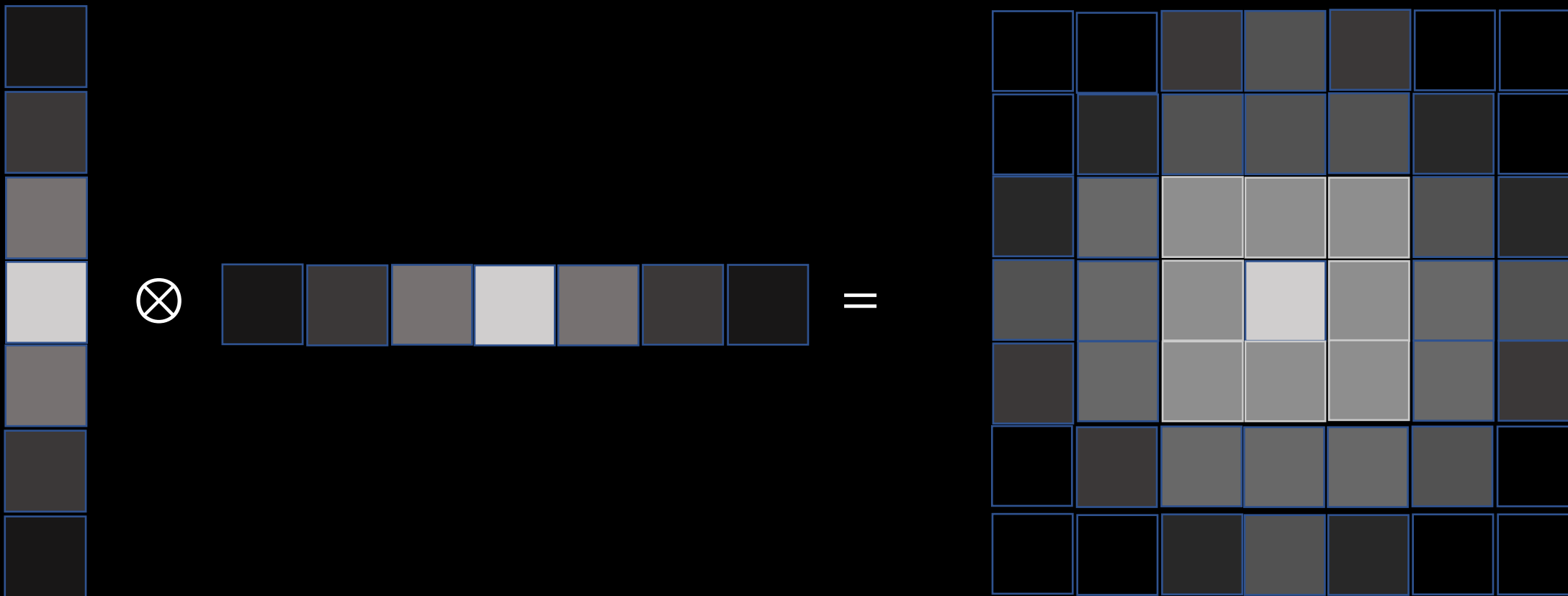
- Read a grayscale image moon.png
- Filter the grayscale image with the following filters
- Display results
- Create a 3-by-3 matrix and write your own code to implement these filters: (You cannot use any built in functions from any library for this.)

# Intro: Create your own 2D convolution filtering script in Python

- Pad image with strips of width equal to the filter size.
- Flip kernel horizontally and vertically.
- “Overlap” kernel on the top left corner of the image.
- Multiply Kernel with image pixel to pixel
- Sum
- Slide to the right.
- Once you hit the rightmost side of the image, do a line break (i.e. slide Kernel down and place it again on the left).

# Intro: Filter kernel.

$$k^T * k = K$$



# Intro: Pad. DIY or calling a command....

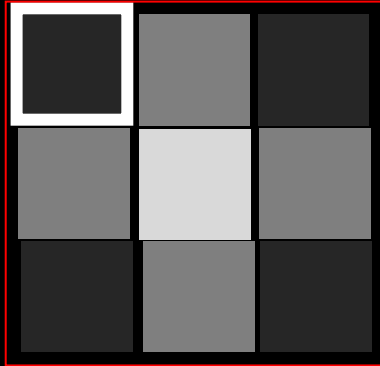
```
img_padded = np.pad(img, pad_width=1, mode=?) ←———— Calling a padding function...
```

```
img_padded = np.zeros(ImIn.shape[0]+Filtersize[0], ImIn.shape[1]+Filtersize[1])
```

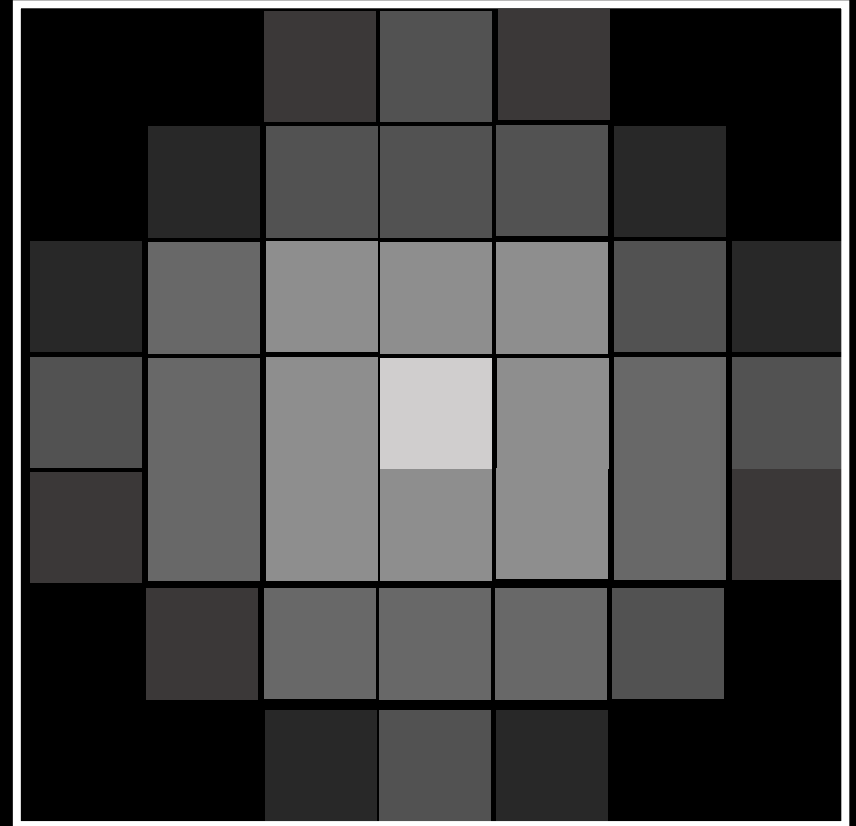
Then copy the pixels you need into the padding area....

# Intro: 2D convolution visually

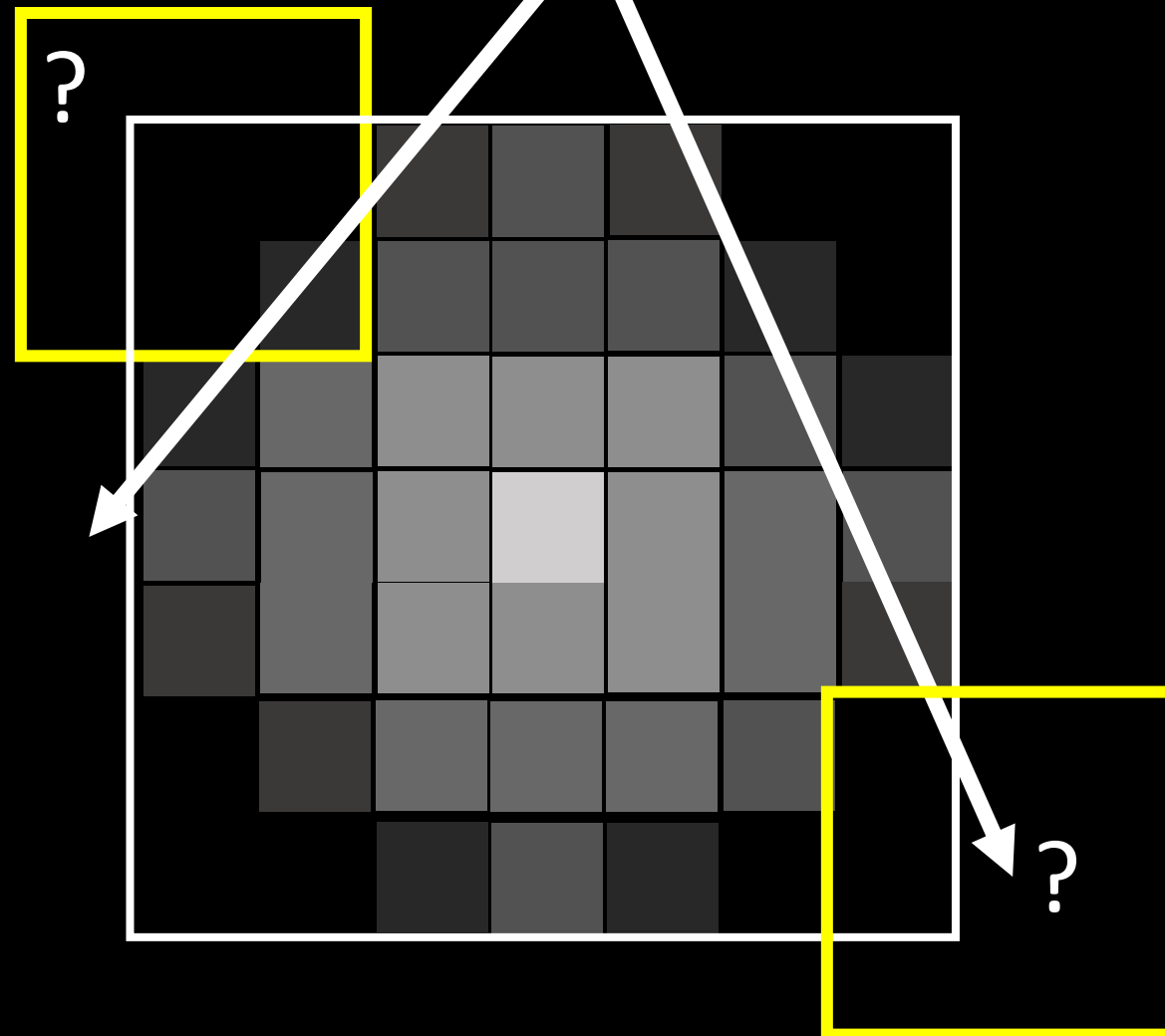
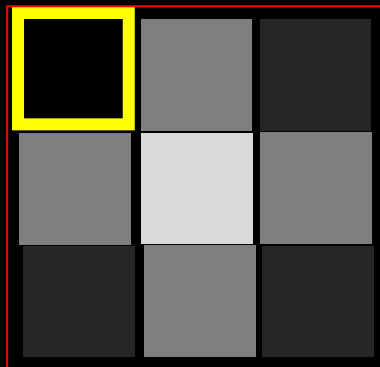
3 by 3 filter (kernel)



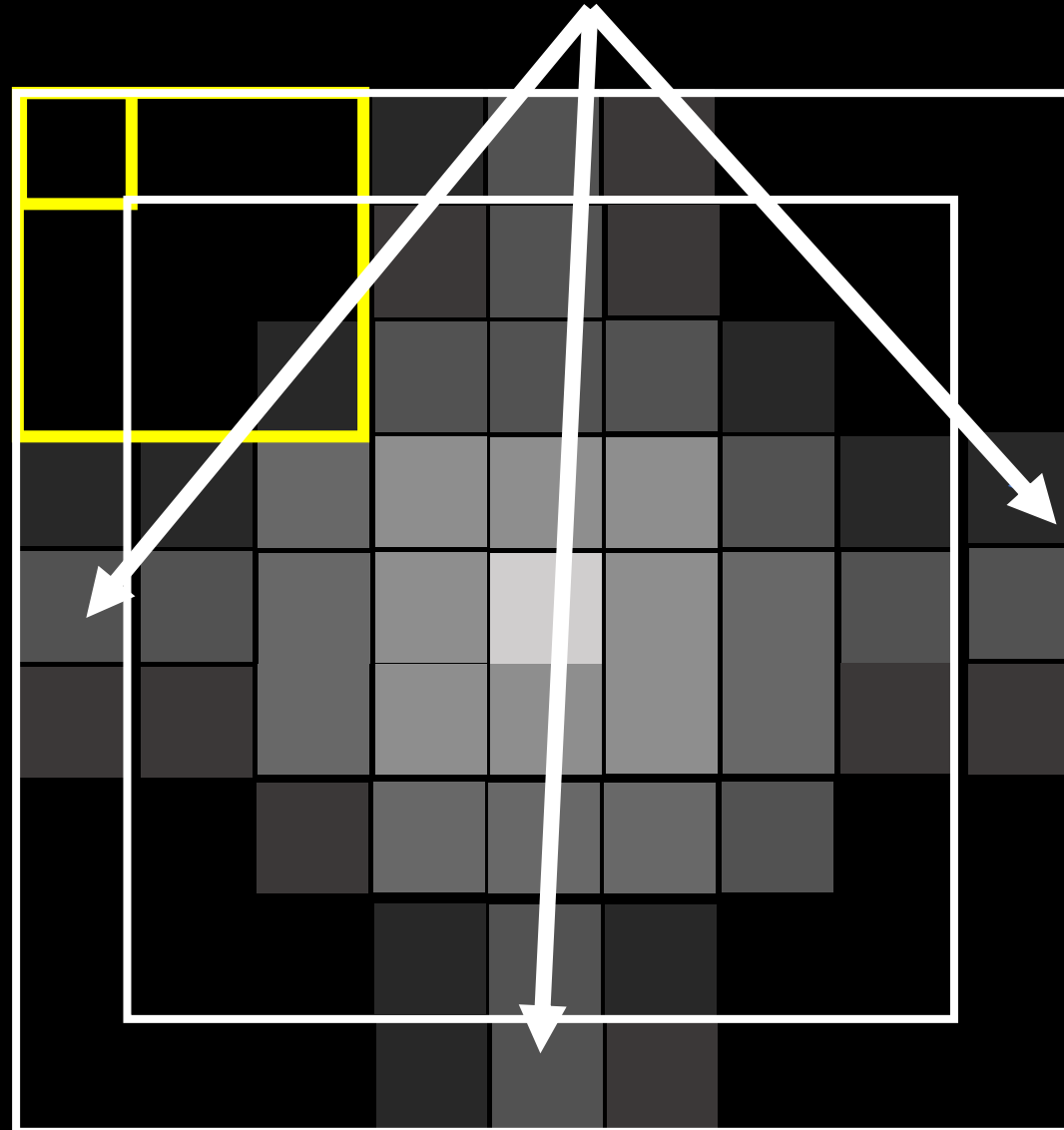
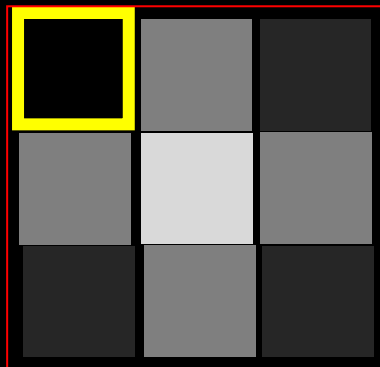
Image



Entension (copy edges...) Padding



Entension (copy edges...) Padding





# Intro: Pad



50 100 150 200 250



50 100 150 200 250



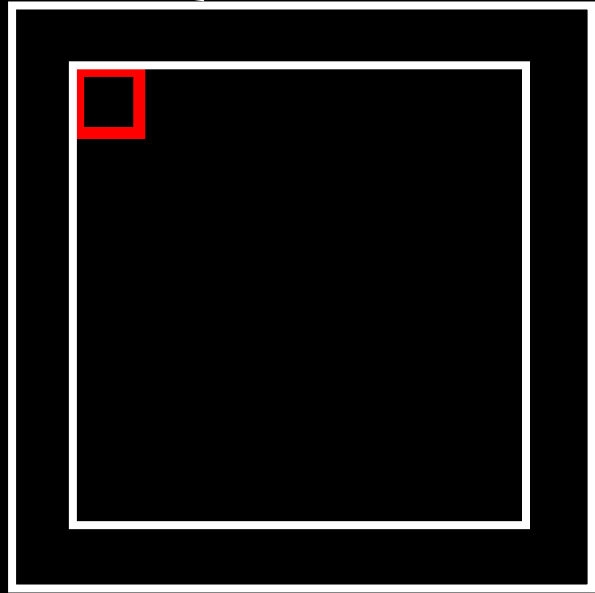
100 150 200 250 300



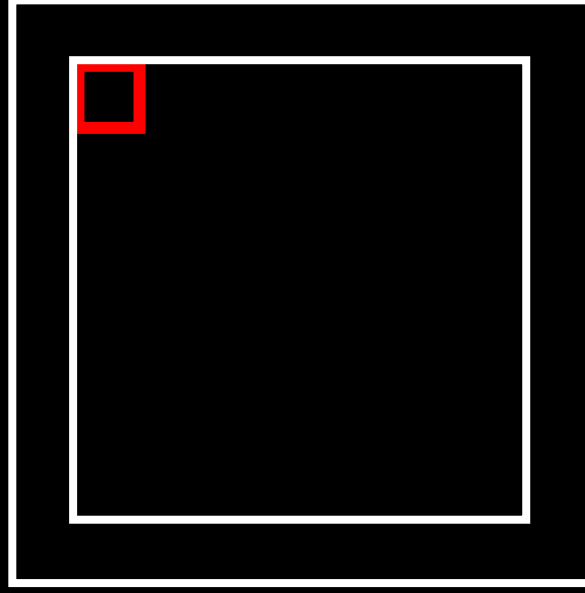
50 100 150 200

$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) =$$

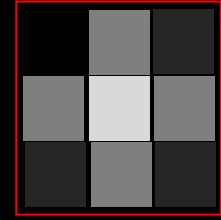
$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) + k(\mathbf{kcol}, \mathbf{krow}) \times \text{ImIn}(\text{row} + \mathbf{kcol}, \text{col} + \mathbf{krow})$$



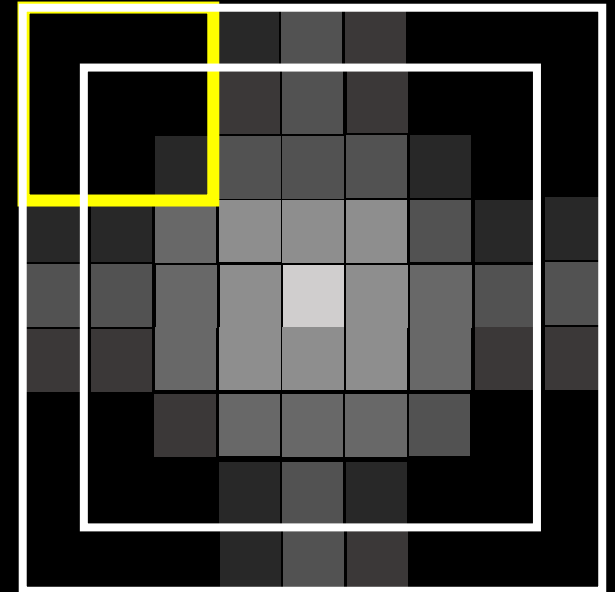
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+

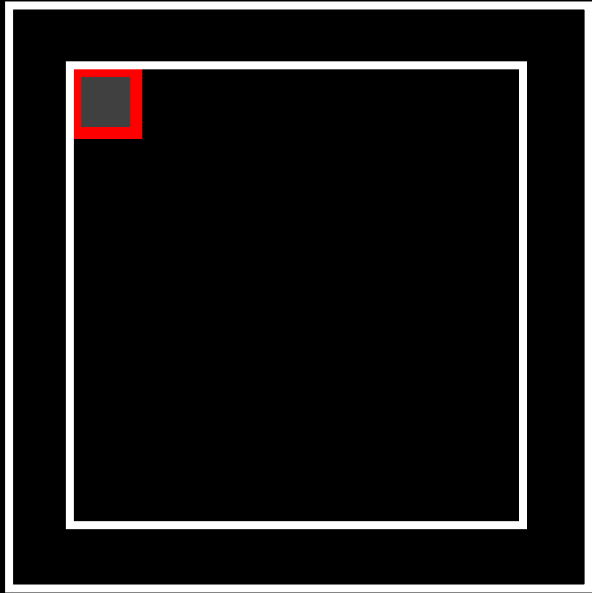


×

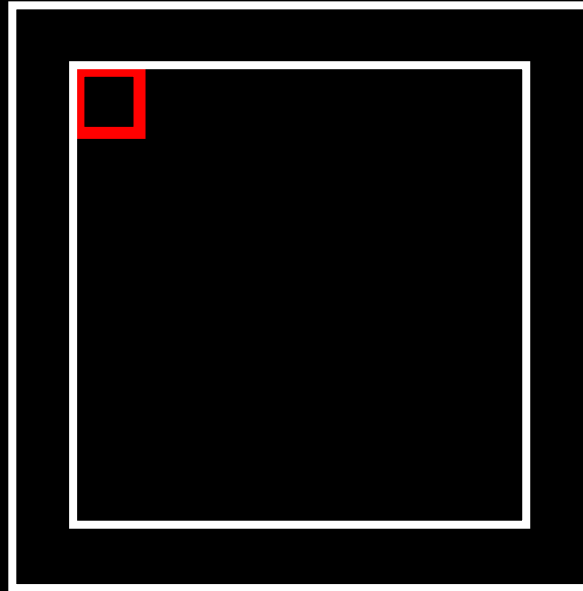


$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) =$$

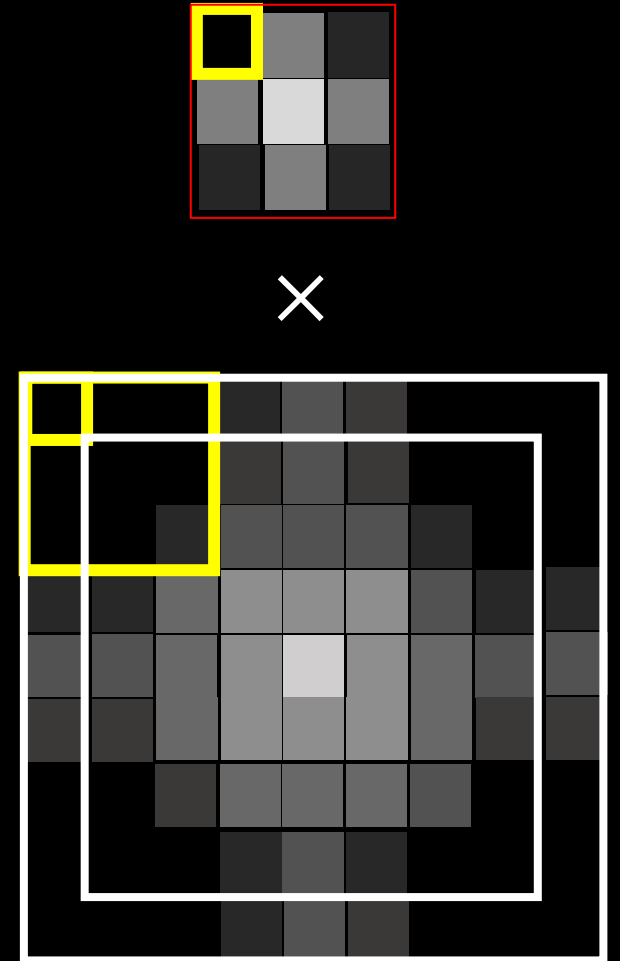
$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) + k(\mathbf{1}, \mathbf{1}) \times \text{ImIn}(\text{row} + \mathbf{1}, \text{col} + \mathbf{1})$$



=

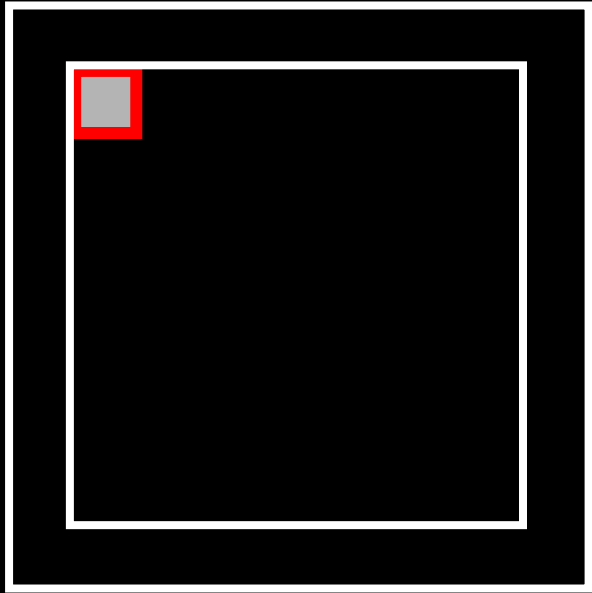


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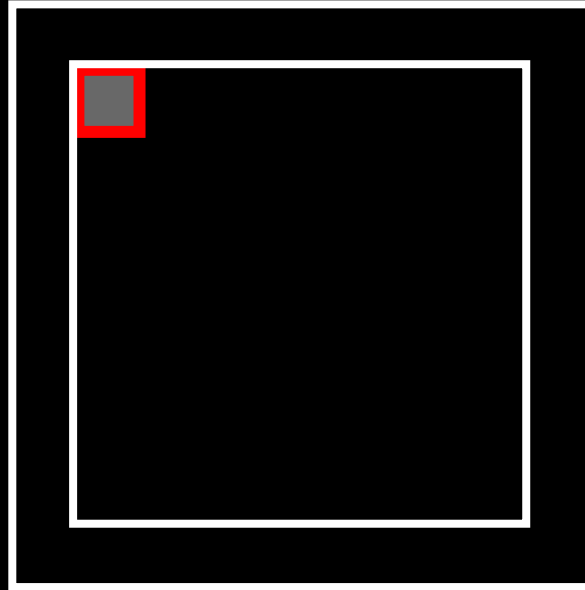


$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) =$$

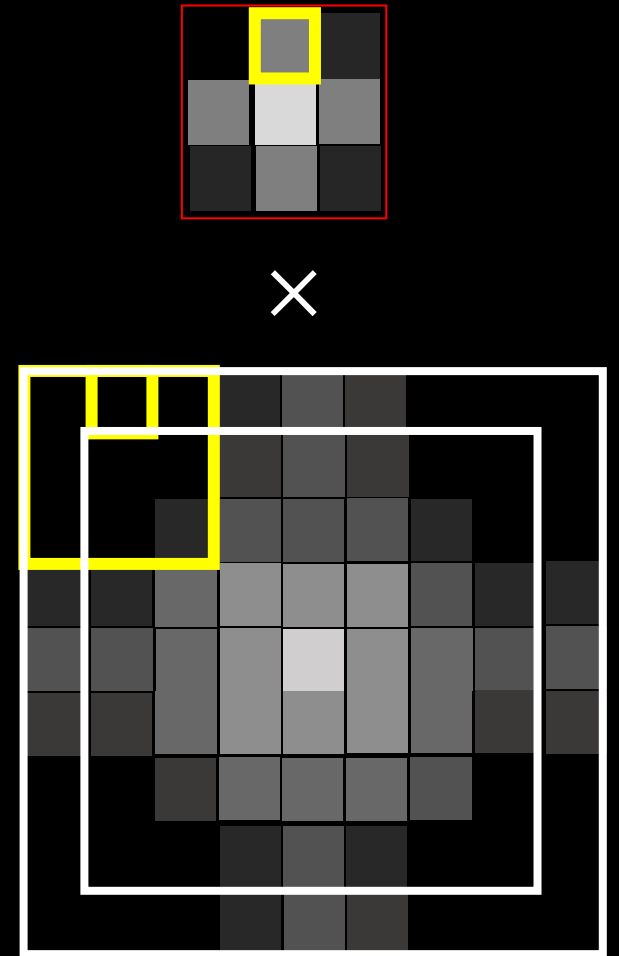
$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) + k(\mathbf{1}, \mathbf{2}) \times \text{ImIn}(\text{row} + 1, \text{col} + 2)$$



=

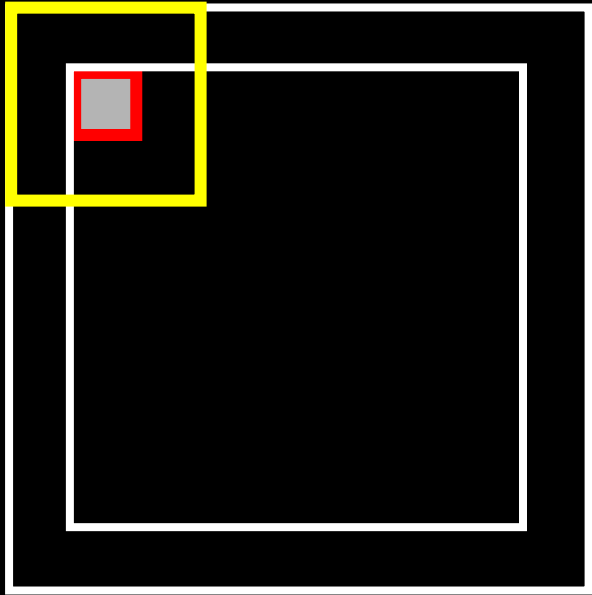


+

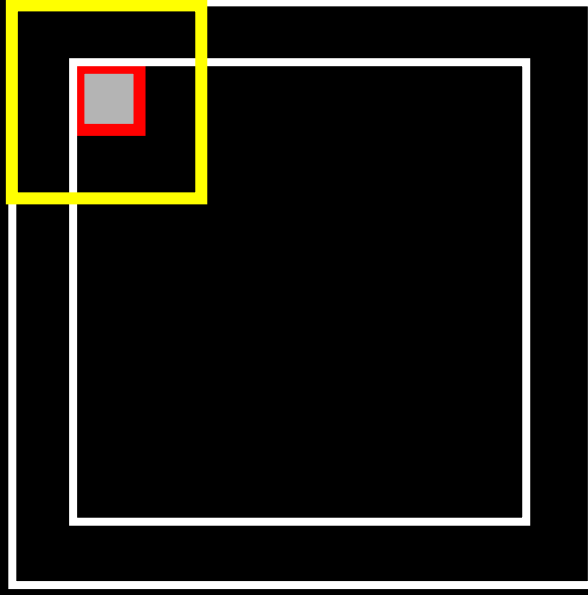


$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) =$$

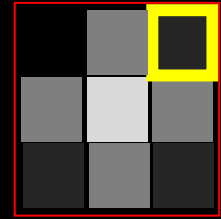
$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) + k(\mathbf{1}, \mathbf{3}) \times \text{ImIn}(\text{row} + \mathbf{1}, \text{col} + \mathbf{3})$$



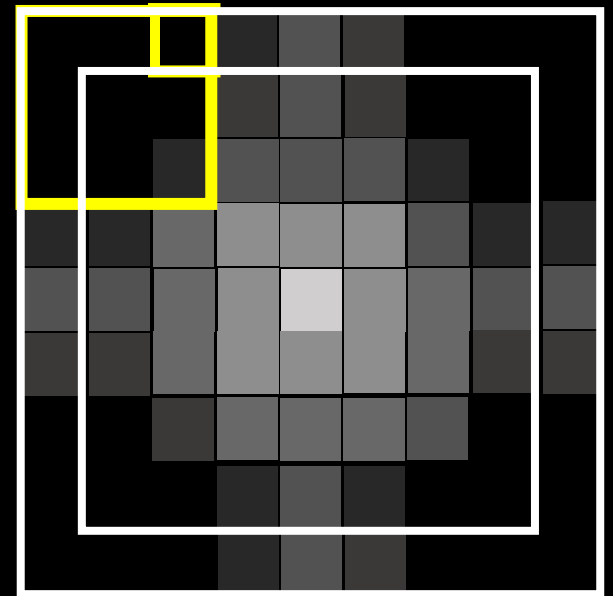
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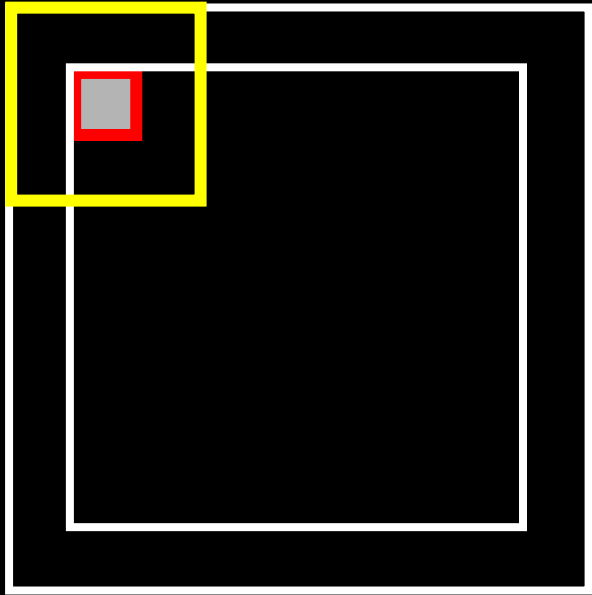


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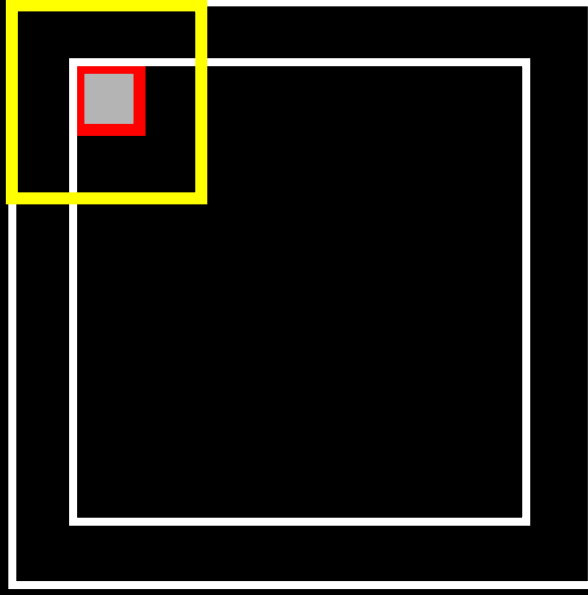


$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) =$$

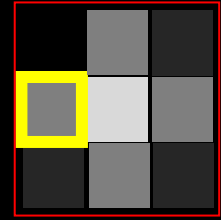
$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) + k(\mathbf{2}, \mathbf{1}) \times \text{ImIn}(\text{row} + \mathbf{2}, \text{col} + \mathbf{1})$$



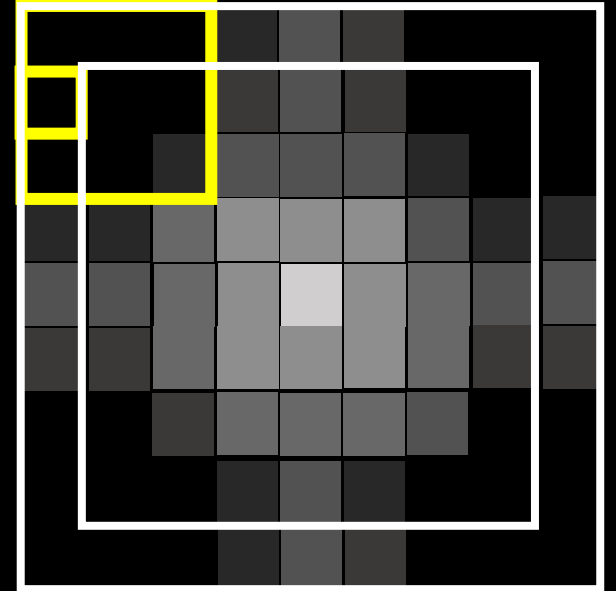
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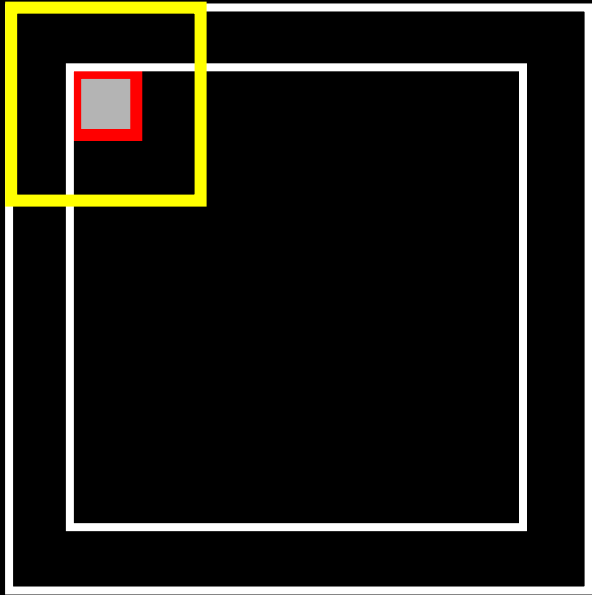


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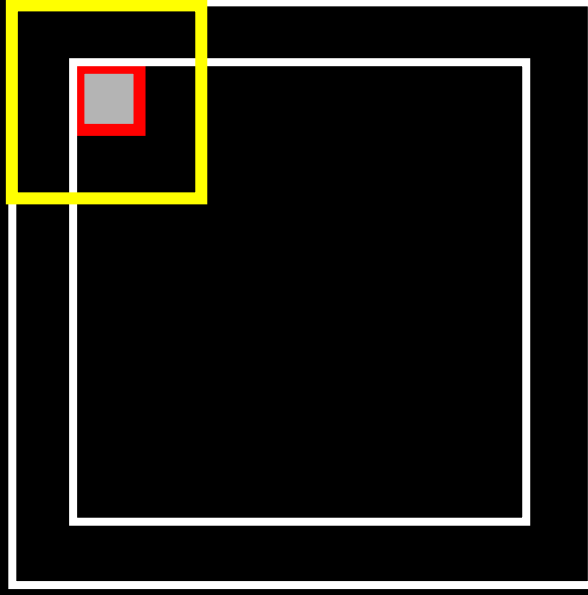


$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) =$$

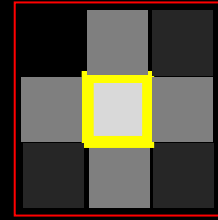
$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) + k(\mathbf{2}, \mathbf{2}) \times \text{ImIn}(\text{row} + \mathbf{2}, \text{col} + \mathbf{2})$$



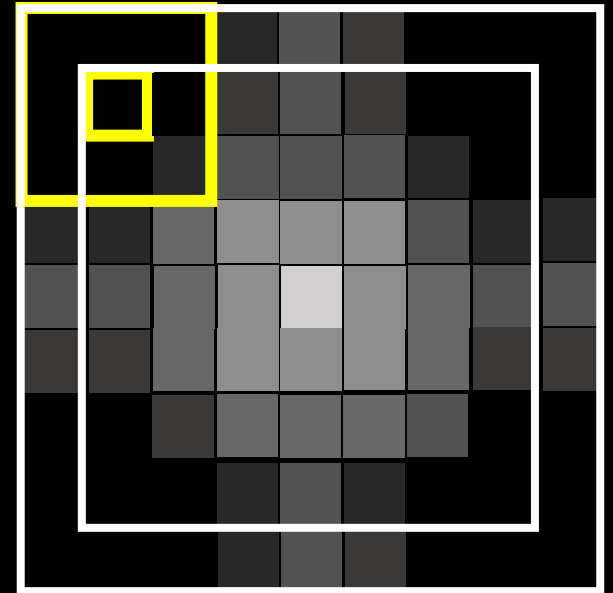
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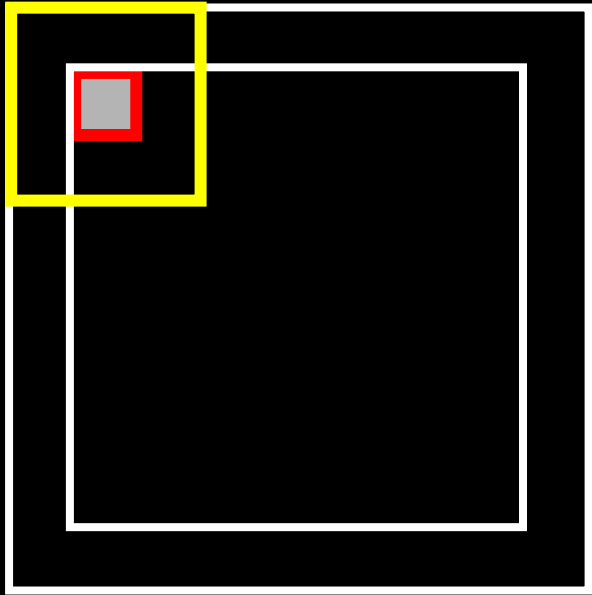


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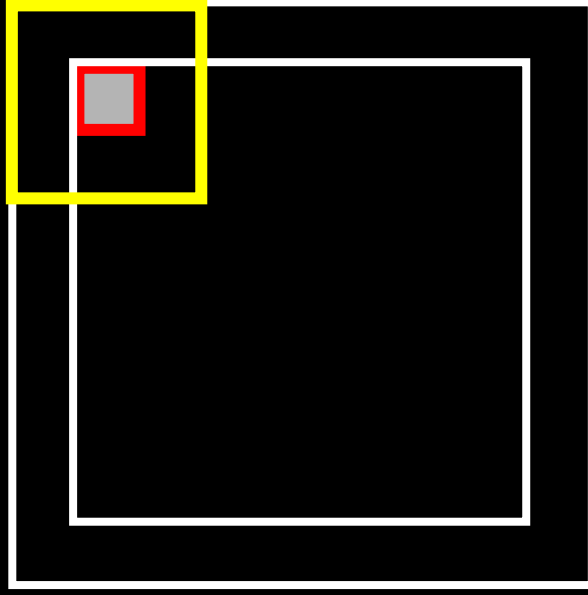


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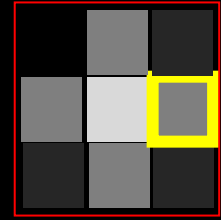
$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) + k(\mathbf{2}, \mathbf{3}) \times \text{ImIn}(\text{row} + \mathbf{2}, \text{col} + \mathbf{3})$$



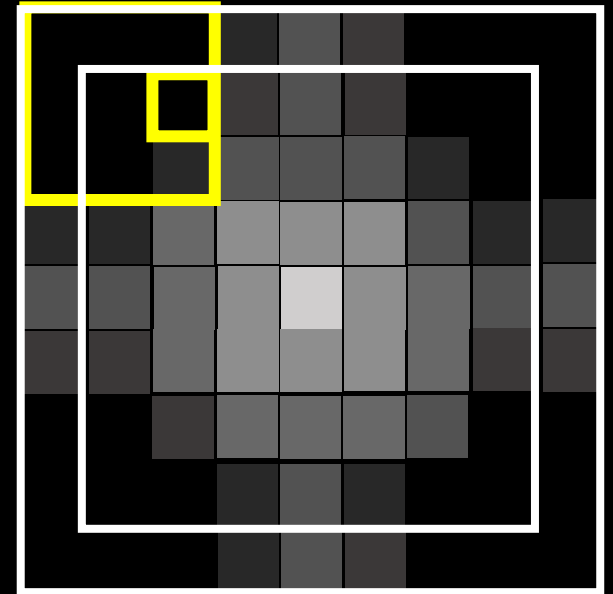
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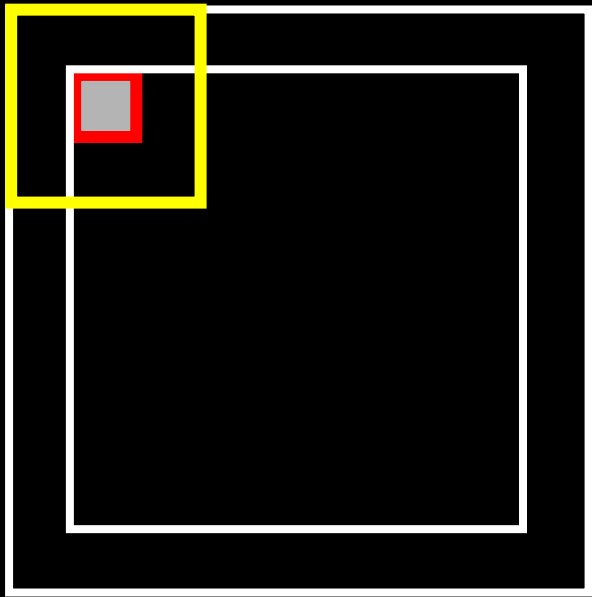
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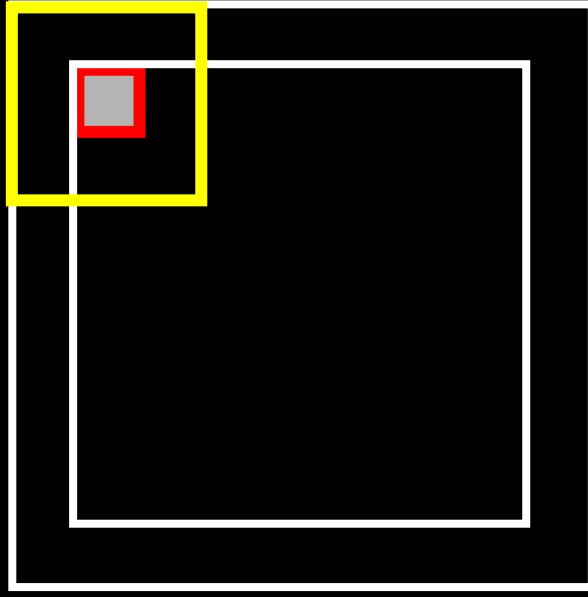


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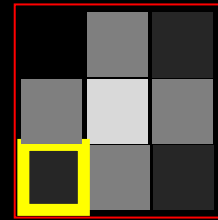
$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) + k(\mathbf{3}, \mathbf{1}) \times \text{ImIn}(\text{row} + \mathbf{3}, \text{col} + \mathbf{1})$$



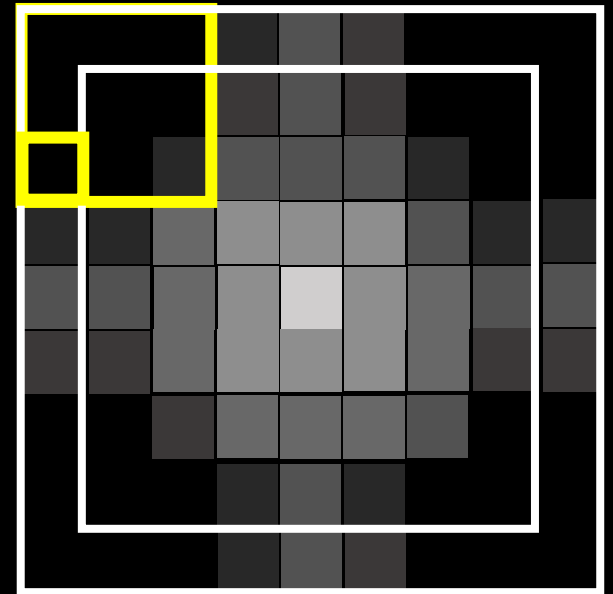
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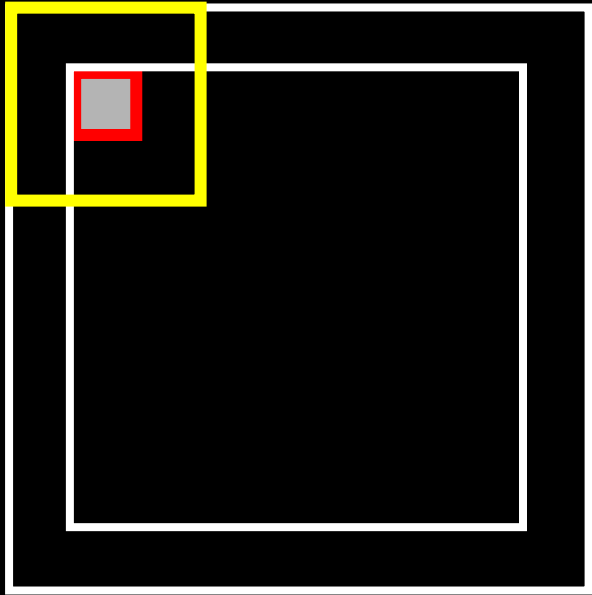


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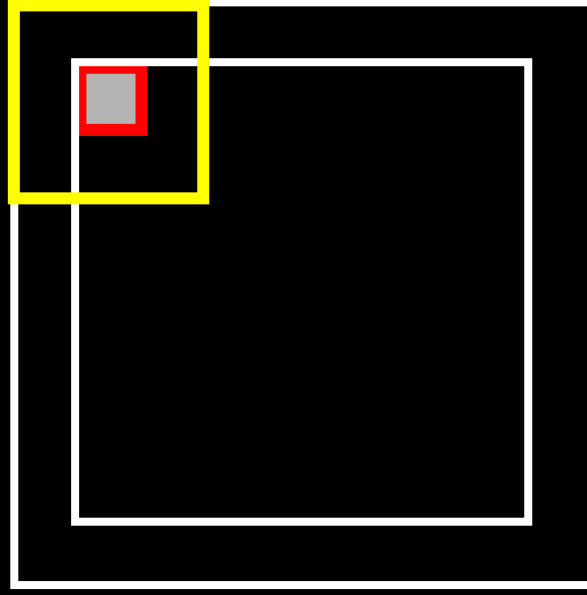


$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) =$$

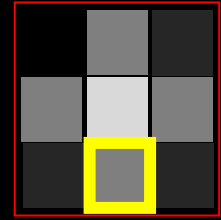
$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) + k(\mathbf{3}, \mathbf{2}) \times \text{ImIn}(\text{row} + \mathbf{3}, \text{col} + \mathbf{2})$$



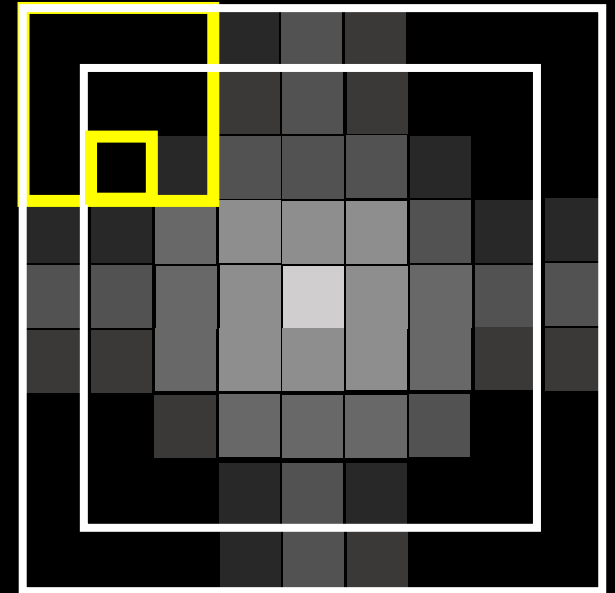
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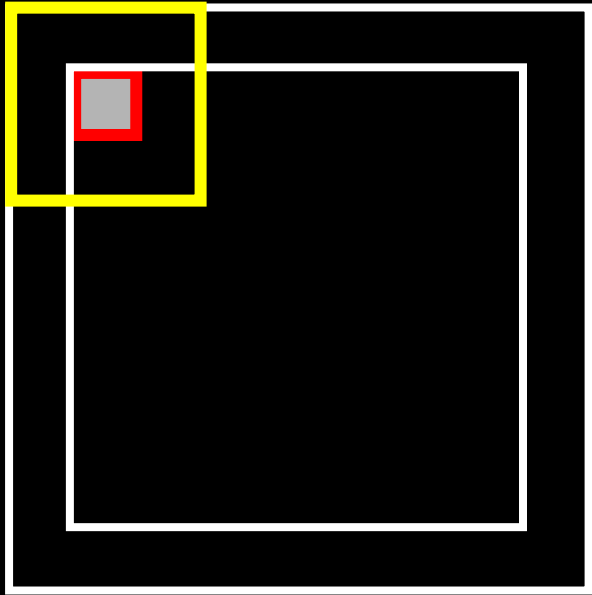


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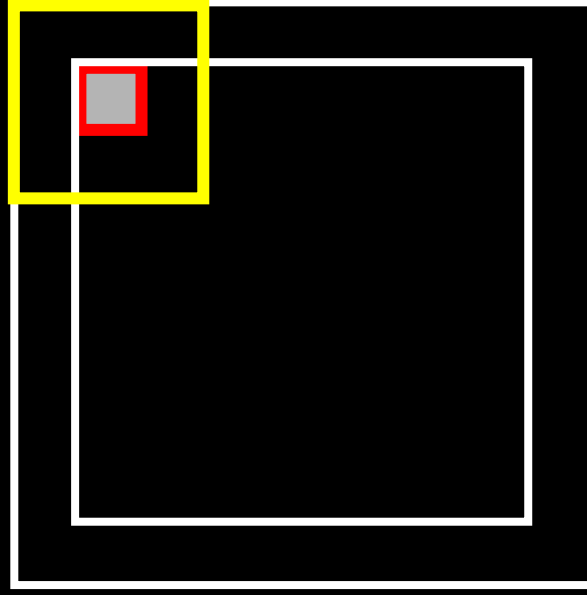


$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) =$$

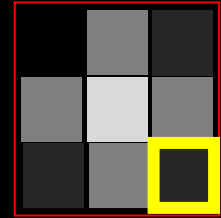
$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) + k(\mathbf{3}, \mathbf{3}) \times \text{ImIn}(\text{row} + \mathbf{3}, \text{col} + \mathbf{3})$$



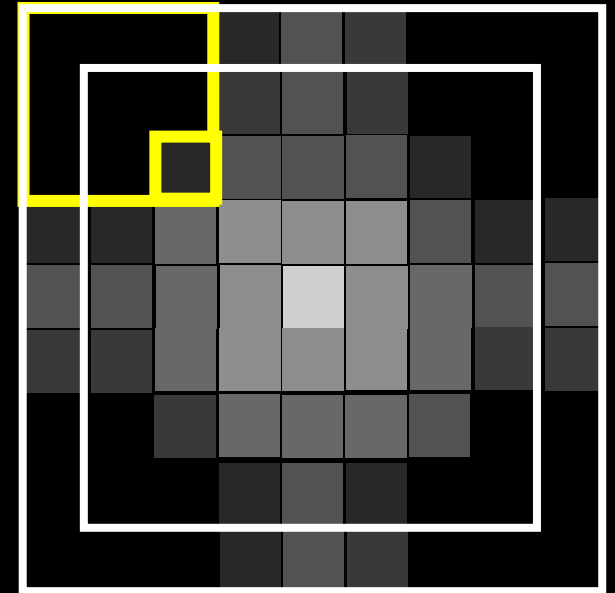
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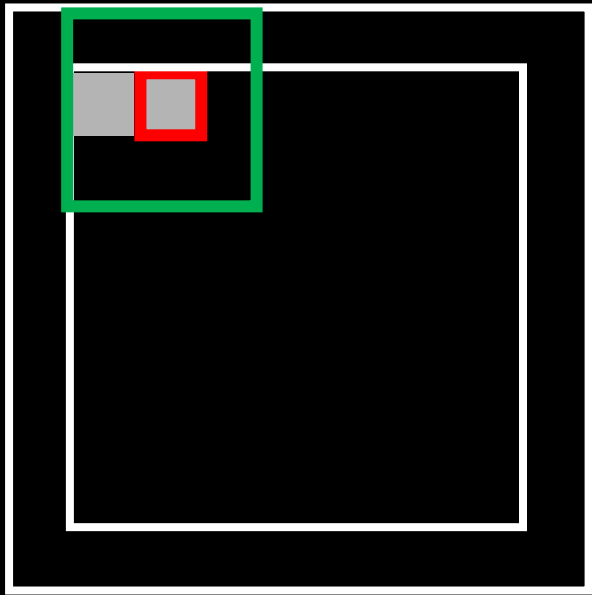


×

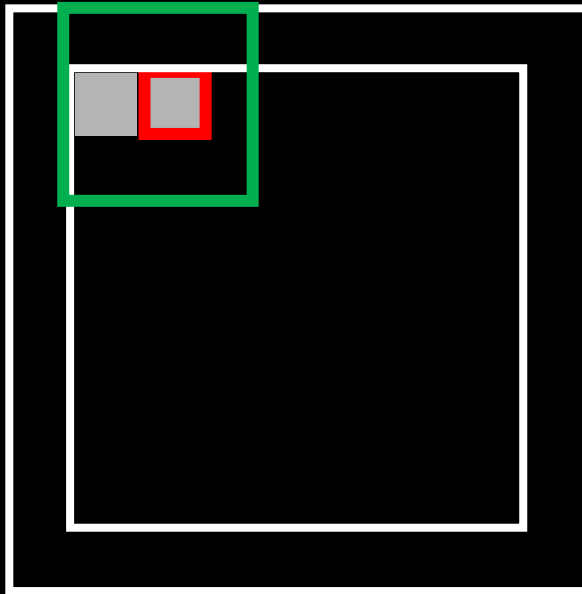


$$\text{ImOut}\left(\textcolor{teal}{row} + \frac{Kcols - 1}{2} + 1, \textcolor{teal}{col} + \frac{Krows - 1}{2} + 1\right) =$$

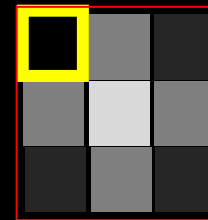
$$\text{ImOut}\left(\textcolor{teal}{row} + \frac{Kcols - 1}{2} + 1, \textcolor{teal}{col} + \frac{Krows - 1}{2} + 1\right) + k(\textcolor{yellow}{2}, \textcolor{yellow}{1}) \times \text{ImIn}(\textcolor{teal}{row} + \textcolor{yellow}{2}, \textcolor{teal}{col} + \textcolor{yellow}{1})$$



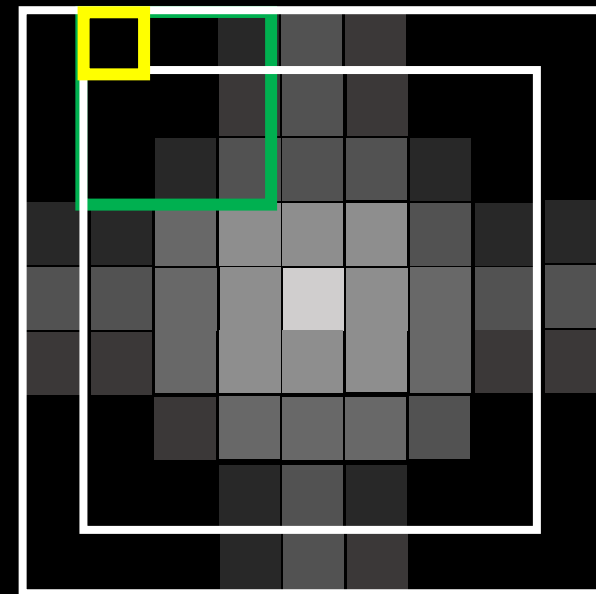
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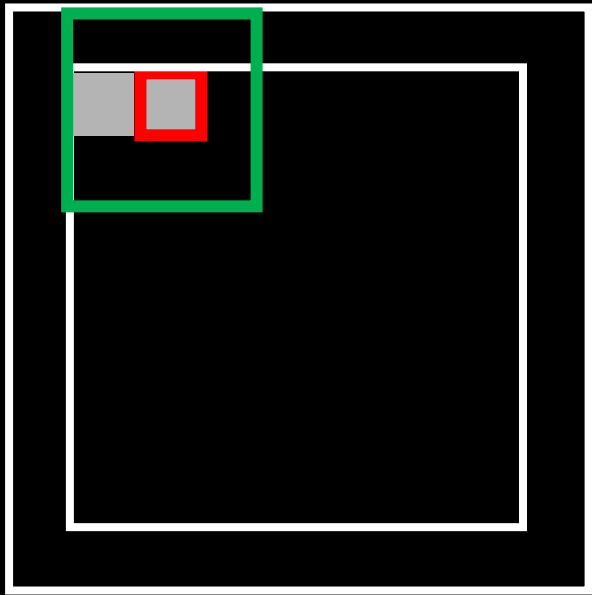


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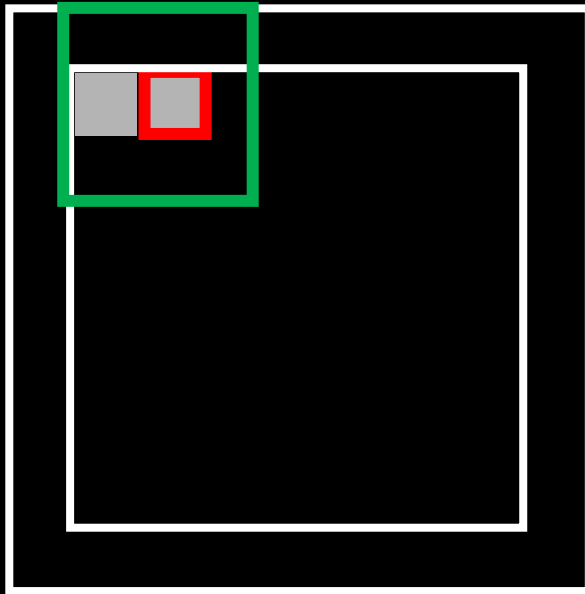


$$\text{ImOut}\left(\textcolor{teal}{row} + \frac{Kcols - 1}{2} + 1, \textcolor{teal}{col} + \frac{Krows - 1}{2} + 1\right) =$$

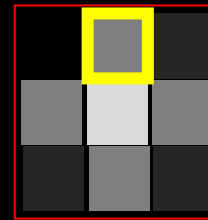
$$\text{ImOut}\left(\textcolor{teal}{row} + \frac{Kcols - 1}{2} + 1, \textcolor{teal}{col} + \frac{Krows - 1}{2} + 1\right) + k(\textcolor{teal}{2}, \textcolor{teal}{1}) \times \text{ImIn}(\textcolor{teal}{row} + 2, \textcolor{teal}{col} + 1)$$



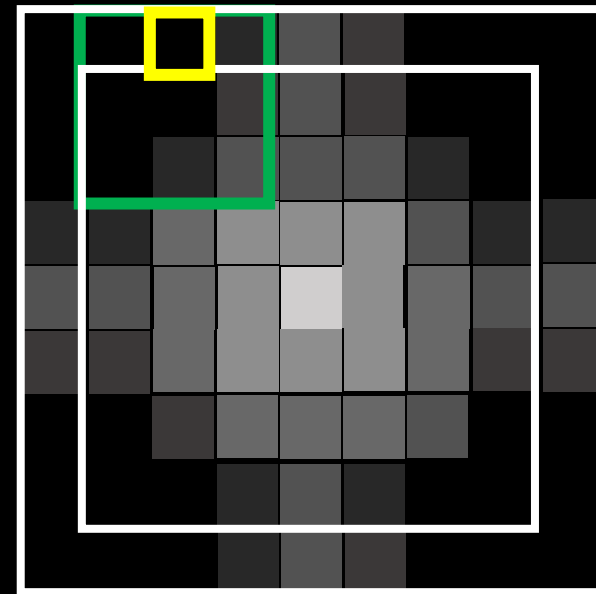
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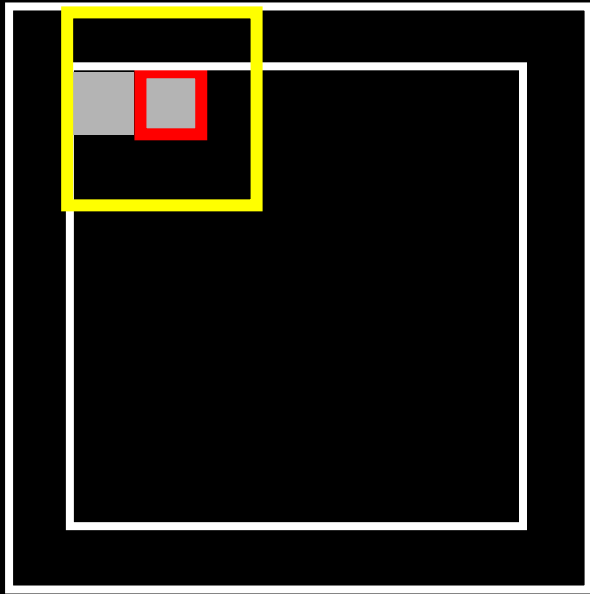


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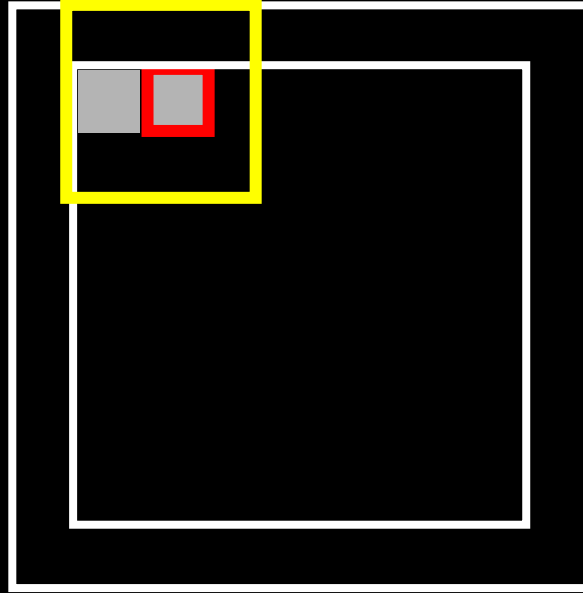


$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) =$$

$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) + k(\mathbf{2}, \mathbf{1}) \times \text{ImIn}(\text{row} + \mathbf{2}, \text{col} + \mathbf{1})$$



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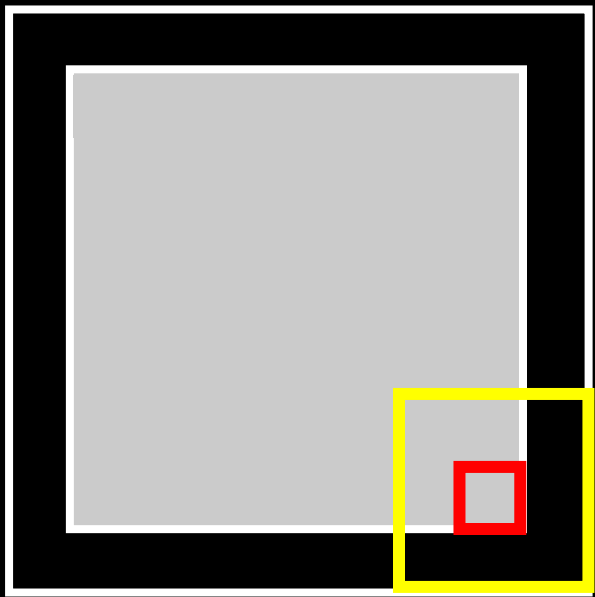


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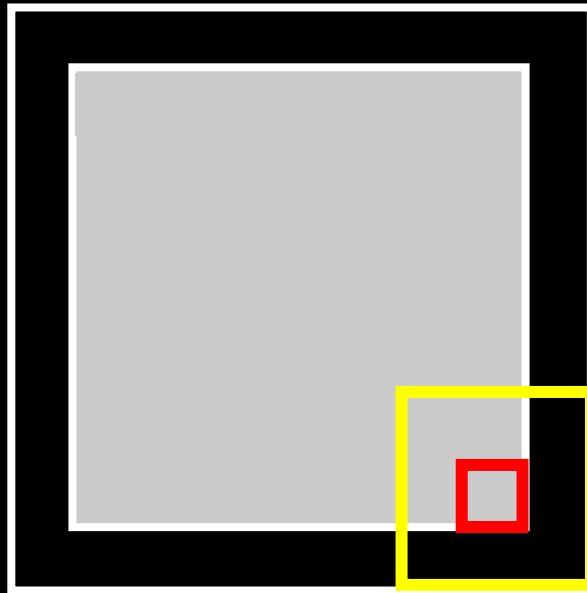
**and so  
on...  
until...**

$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) =$$

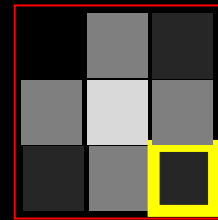
$$\text{ImOut}\left(\text{row} + \frac{K\text{cols} - 1}{2} + 1, \text{col} + \frac{K\text{rows} - 1}{2} + 1\right) + k(\mathbf{2}, \mathbf{1}) \times \text{ImIn}(\text{row} + \mathbf{2}, \text{col} + \mathbf{1})$$



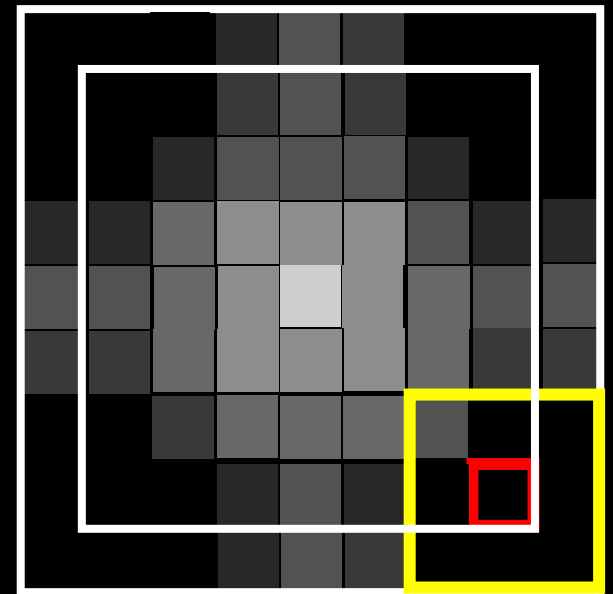
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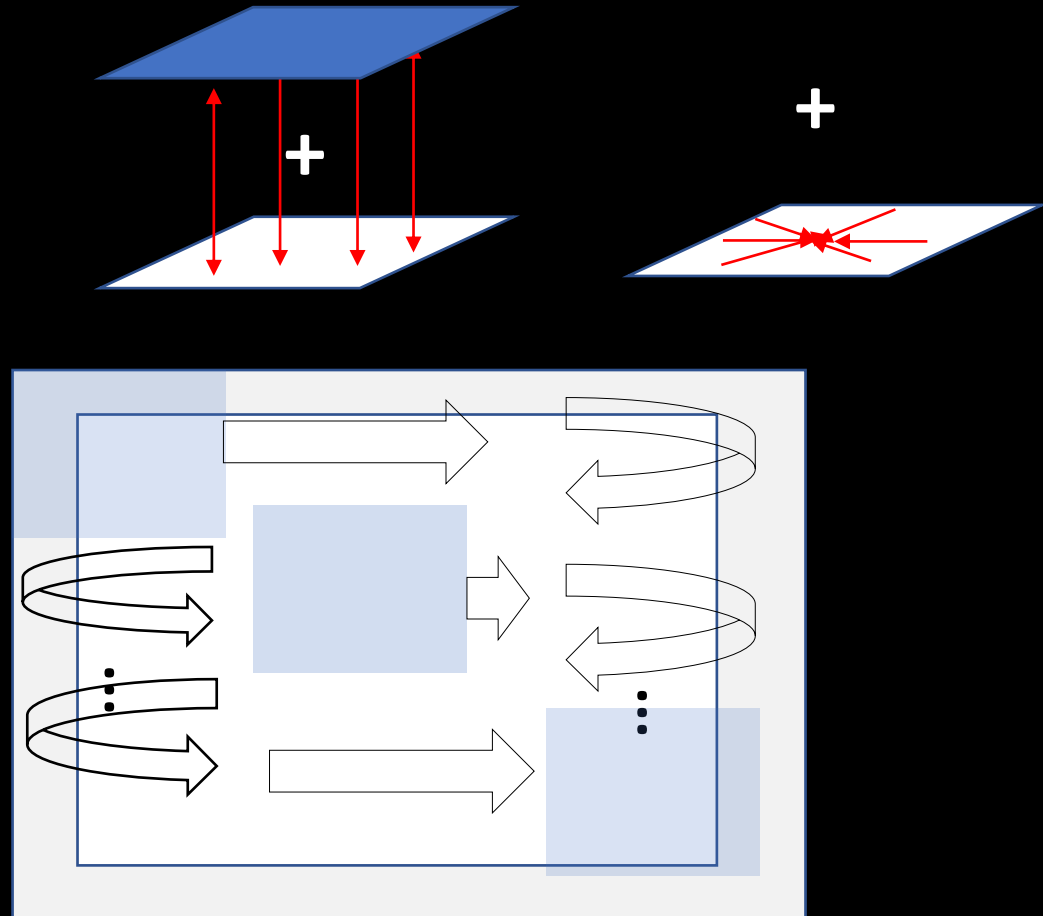
# Part 1: Create your own 2D convolution filtering script in Python

## Block 1: Filter:

1. Pad image
2. Perform pointwise multiplication of each element of filter and image patch
3. Sum and assign output center pixel position in image patch.

## Block 2: Apply filter to every pixel in the image:

- A. Slide filter to the right until you hit right edge of image.
- B. Slide one pixel down and return to the left most margin and repeat block 1.





# Intro: 2D Convolution recap

2	2	3	0	1	4	4
2	2	3	0	1	4	4
9	9	8	1	2	5	5
1	1	3	4	0	2	2
3	3	1	5	6	2	2
3	3	1	5	6	2	2

I



1	0	2
-4	3	1
0	1	2

K

=

34			

J

$$\begin{aligned}
 & (2)(1) + (2)(0) + (3)(2) + (2)(-4) \\
 & + (2)(3) + (5)(1) + (9)(0) + (9)(1) + \\
 & (8)(2) = 34
 \end{aligned}$$

$$\begin{aligned}
 & (1)(1) + (2)(0) + (5)(2) + \\
 & (4)(-4) + (0)(3) + (2)(1) + \\
 & (5)(0) + (6)(1) + (2)(2) = 7
 \end{aligned}$$

# Intro: 2D Convolution recap

Inputs: Image  $I$ , filter matrix  $K$ ; shape of  $K$  is  $(2h+1, 2w+1)$

Output: Image  $J$

Step 1: Pad  $h$  rows on the top and the bottom and  $w$  columns at the left and the right of image  $I$ ; Let  $(H, W)$  be the shape of the padded image  $I$

Step 2: Initialize output image  $J$  to all zeros;  $J$  has shape  $(H, W)$

Step 3: for  $i$  from  $h$  to  $H-h-1$   
    for  $j$  from  $w$  to  $W-w-1$   
        for  $m$  from  $-h$  to  $h$   
            for  $n$  from  $-w$  to  $w$   
                 $J[i, j] += I[i+m, j+n] * K[m+h, n+w]$

Step 4: Strip padding from  $J$ , so that  $J$  has shape  $(H-2h, W-2w)$ . Return  $J$ .

# Intro: Overlap, Slide and Multiply

```
for row in ROWS
  for col in COLS
    for Krow from  $-(KROWS-1)/2$  to  $-(KROWS-1)/2 + 1$ 
      for Kcol in  $-(KCOLS-1)/2$  to  $-(KCOLS-1)/2 + 1$ 
        Imout(row,col)=Kernel(krow+KROWS,kcol+KCOLS)*ImIn(row+krow,col+kcol)
```

# Part 1: Create your own 2D convolution filtering script in Python

$$\begin{pmatrix} 0 & -1 & 0 \\ -1 & 4 & -1 \\ 0 & -1 & 0 \end{pmatrix}$$

$$\begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{pmatrix}$$

- Remember: two fundamental operations for filtering:
- Adding (integrate) is smoothing.
- Subtracting (differentiate) is sharpening.

# Part 1: Create your own 2D convolution filtering script in Python

**Iterate** along rows

**Iterate** along columns

**Write:** `ImOut(row+(Frows-1)/2+1,col+(Fcols-1)/2+1)=sum(Filter(1:Frows,1:Fcols)*ImageInPatch(row:row+Frows,col:col+Fcols))`

## Part 2: Median and Gaussian filters

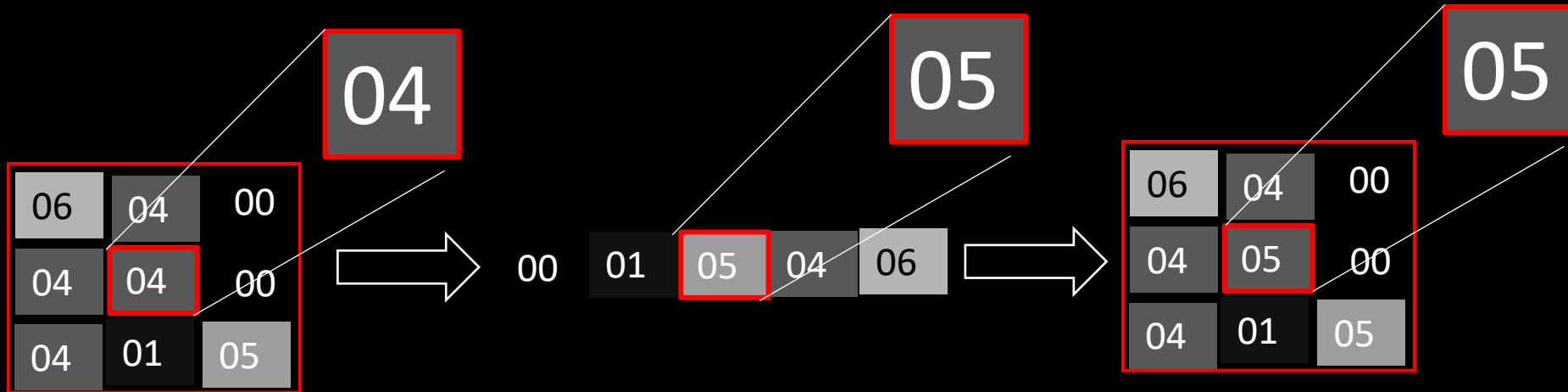
Read **"noisy.jpg"** corrupted with salt and pepper noise.

- Apply a **median filter** to remove the noise.
- Apply a **Gaussian filter** to the same noisy image.
- You **can use any scikit-image function** you like.
- Which filter was more successful?

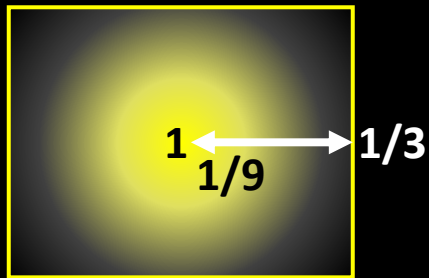
# Part 2: Median...

## Vote for your pixel!

00	01	02	03	04	05	06	07	08	09	10
06	04	00	04	09	05	08	02	03	02	01
04	04	00	04	09	02	03	02	01	00	01
04	01	05	08	02	03	08	02	03	02	01
01	09	02	03	02	01	03	02	01	00	01



# Part 2: Gaussian... merge your pixels!

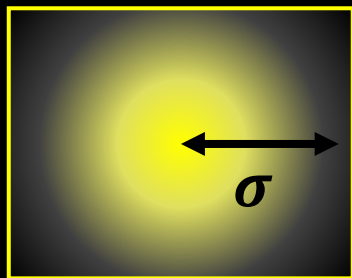


	00	01	02	03	04	05	06	07	08	09	10
06	06	04	00	04	09	05	08	02	03	02	01
04	04	04	00	04	09	02	03	02	01	00	01
04	04	01	05	08	02	03	08	02	03	02	01
01	01	09	02	03	02	01	03	02	01	00	01

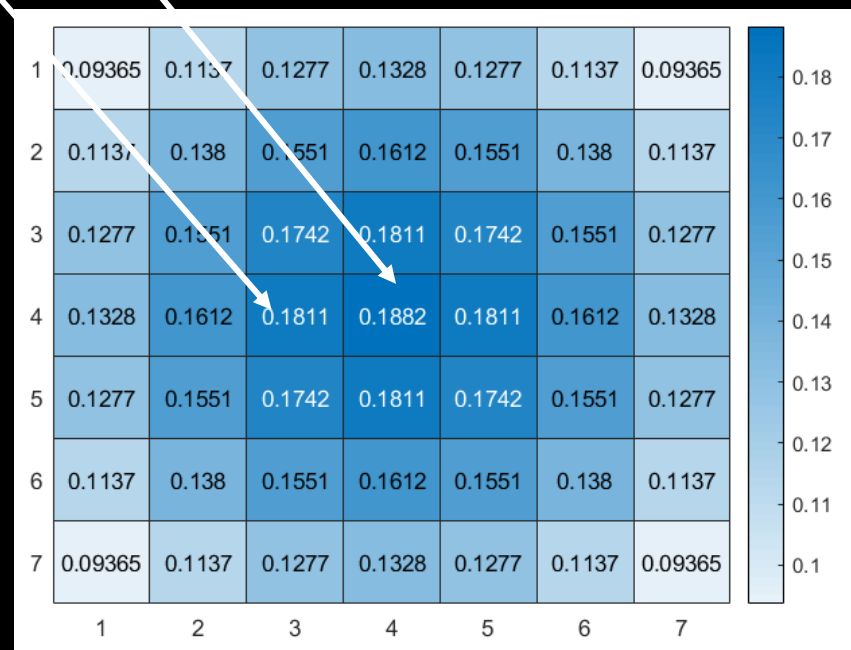
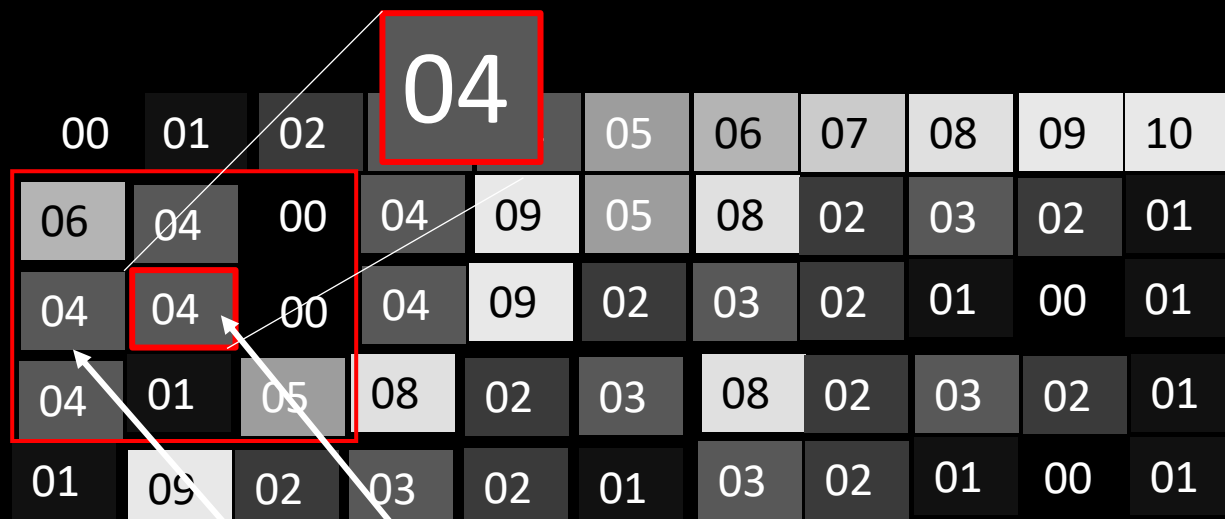




# Part 2: Gaussian... merge your pixels!

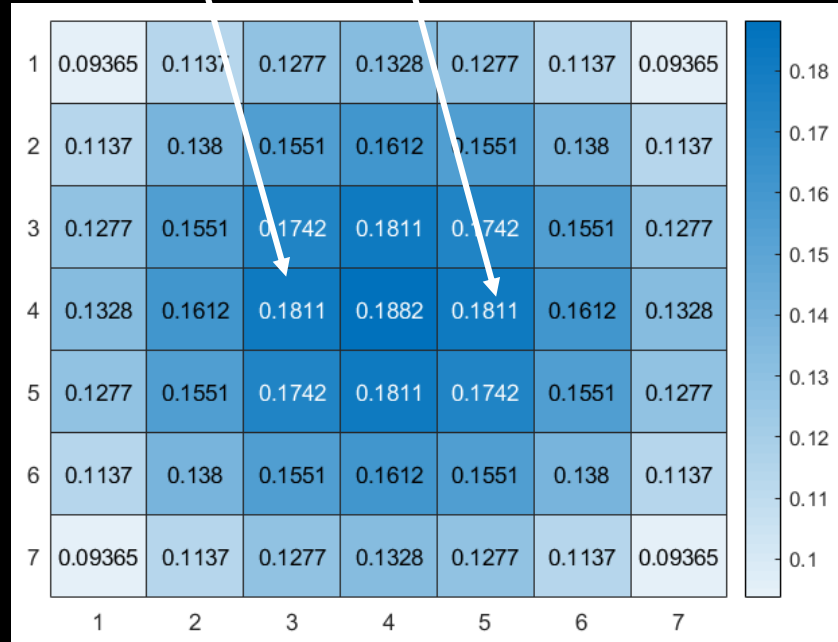


$$G = \frac{1}{2\pi\sigma^2} \exp\left(-\frac{((i - i_0)^2 + (j - j_0)^2)}{2\sigma^2}\right)$$



# Part 3: Inpainting

1. Blurr image to fill-in voids.
2. Copy “good” pixels
3. Repeat process



# Part 3: Inpainting



# Part 3: Inpainting



# Part 3: Inpainting



# Part 3: Inpainting

## Algorithm

- Input: Damaged image,  $I$  and Mask  $U$
- Output: Repaired image,  $J$
- Step 1:  $J = I$
- Repeat
  - $J = \text{GaussianSmooth}(J)$  # Smooth damaged image
  - $J(U) = I(U)$  # Copy good pixels

Let's look at the demo

# Assignment 2

## Edges

### Parts 4-6

CMPUT206

Prof. Nilanjan Ray

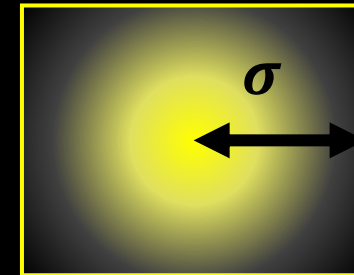
TA: Bernal Manzanilla

Parts 4-6: Subtracting is sharpening.  
Summing is smoothing.

- Taking differences of neighbouring pixels, is a discrete equivalent of a derivative, which brings up amplitudes of edges.
- Differences increase noise.
- Summing neighboring pixels is smoothing.
- Combination of summing filters and difference filters control noise and allow to sharpen or identify edges, lines and corners in natural images.

$$\frac{d(Image)}{dx} = D_x = (1/2, -1/2)$$

$$\frac{d(Image)}{dy} = D_x^T = D_y = \begin{pmatrix} 1/2 \\ -1/2 \end{pmatrix}$$



$$G = \frac{1}{2\pi\sigma^2} \exp\left(-\frac{((i - i_0)^2 + (j - j_0)^2)}{2\sigma^2}\right)$$

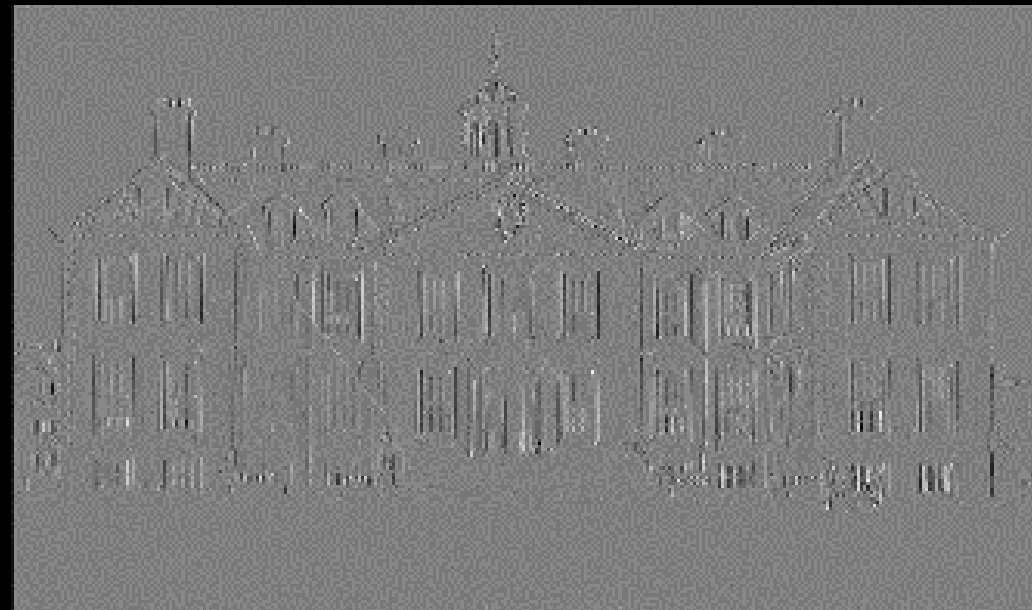


$$S_x = \begin{pmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{pmatrix}$$

Part 4: Sobel  
operator

$$S_y = \begin{pmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{pmatrix}$$

$$S_x = \begin{pmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{pmatrix}$$

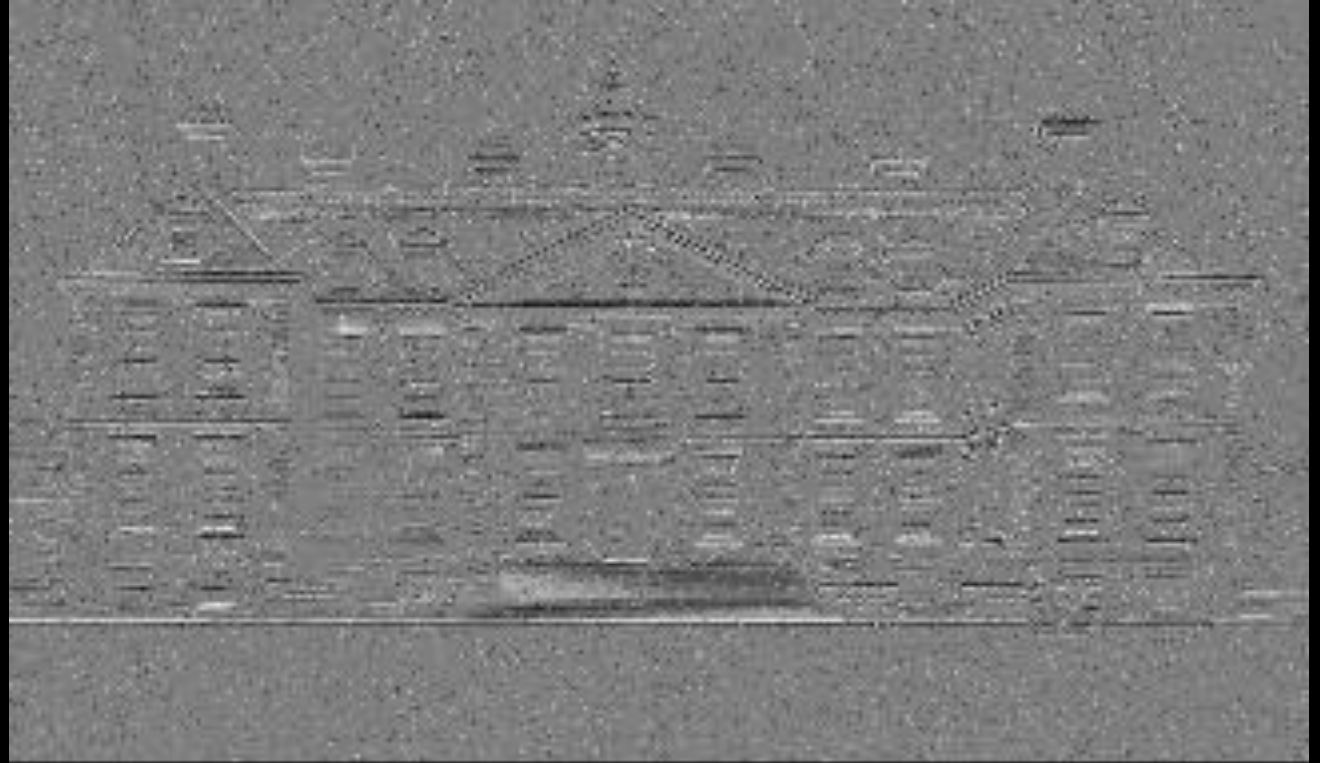


## Part 4: Sobel operator

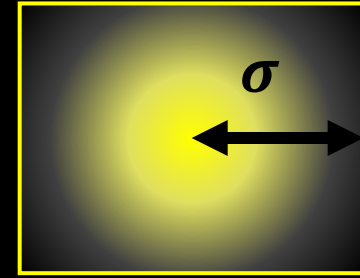
$$S_y = \begin{pmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{pmatrix}$$



# Part 5: Canny



Part 5: Canny  
filter. Smooth,  
calculate gradient  
and apply lower  
bound threshold.



$$G = \frac{1}{2\pi\sigma^2} \exp\left(-\frac{((i - i_0)^2 + (j - j_0)^2)}{2\sigma^2}\right)$$

$$I_{smooth} = G * I \Rightarrow I_{x/y} = D_{x/y} * I_{smooth}$$

$$D_x = \begin{pmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{pmatrix}$$

$$D_y = \begin{pmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{pmatrix}$$

# Part 5: Canny



Canny

Smooth

gradient

Threshold

$I$

# Part 5: Canny



Canny

Smooth

gradient

Threshold

$$I \Rightarrow I_{smooth} = G * I$$

# Part 5: Canny



Canny

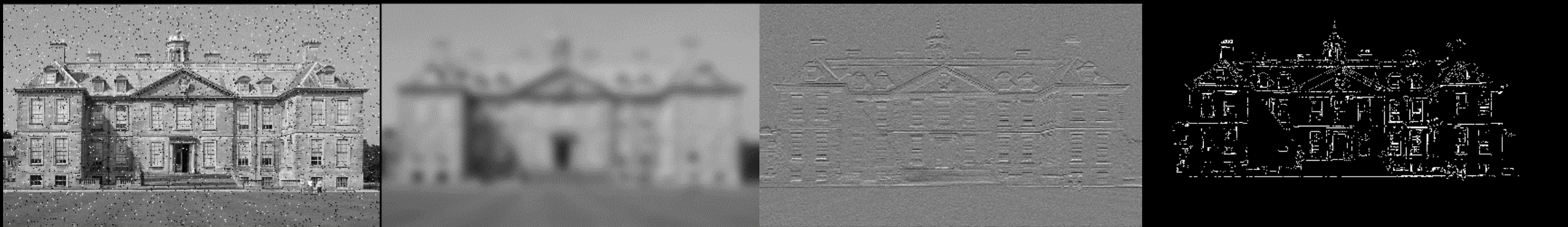
Smooth

gradient

Threshold

$$I \Rightarrow I_{smooth} = G * I \Rightarrow I_{x/y} = D_{x/y} * I_{smooth}$$

# Part 5: Canny



Canny

Smooth

gradient

Threshold

$$I \Rightarrow I_{smooth} = G * I \Rightarrow I_{x/y} = D_{x/y} * I_{smooth} \Rightarrow I_{x/y} \begin{cases} 0 & I_{x/y} < t \\ I_{x/y} & I_{x/y} \geq t \end{cases}$$