

Assignment1_part1

Haoyi Wei

2022-12-19

Investigate the exponential distribution in R and compare it with the Central Limit Theorem.

Overview

This project investigates the exponential distribution in R and compare it with the Central Limit Theorem.

Part1: Simulation Exercise

```
#set seed for reproducibility  
set.seed(123)
```

In this project you will investigate the exponential distribution in R and compare it with the Central Limit Theorem. The exponential distribution can be simulated in R with `rexp(n, lambda)` where `lambda` is the rate parameter. The mean of exponential distribution is $1/\lambda$ and the standard deviation is also $1/\lambda$. Set $\lambda = 0.2$ for all of the simulations. You will investigate the distribution of averages of 40 exponentials. Note that you will need to do a thousand simulations.

1. Show the sample mean and compare it to the theoretical mean of the distribution

```
# set the parameters per the quest of the assignment  
lambda <- 0.2 # lambda  
n <- 40 # number of exponentials  
sim <- 1000 # number of simulations  
  
# run the simulation  
sim.exp <- replicate(sim, rexp(n, lambda))  
  
# calculate mean of exponential simulations  
mean.exp <- apply(sim.exp, 2, mean)
```

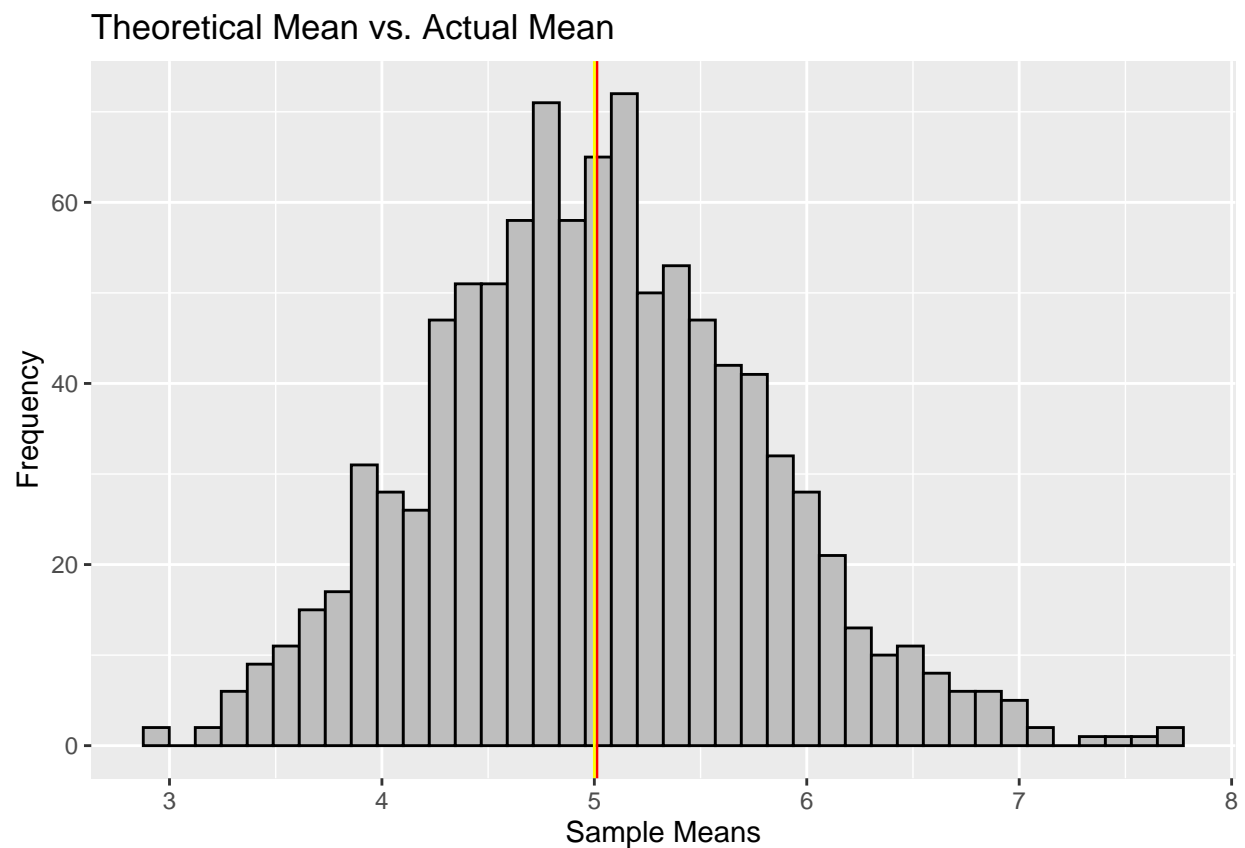
```
# mean of sample mean  
mm.exp <- mean(mean.exp)  
mm.exp
```

```
## [1] 5.011911
```

```
# Theoretical Mean
1/lambda
```

```
## [1] 5
```

```
# distribution of the sample mean
library(ggplot2)
meanexp <- data.frame(mean.exp)
ggplot(meanexp, aes(x=mean.exp)) +
  geom_histogram(bins=40, color="black", fill="grey") +
  geom_vline(aes(xintercept=mm.exp), color="red") +
  geom_vline(aes(xintercept=1/lambda), color="yellow") +
  labs(x="Sample Means", y="Frequency") +
  ggtitle("Theoretical Mean vs. Actual Mean")
```



Sample mean and theoretical mean is very similar

2. Show how variable the sample is (via variance) and compare it to the theoretical variance of the distribution.

```
# Theoretical Variance
(1/lambda)^2 / n
```

```
## [1] 0.625
```

```
# Sample Variance
sd(mean.exp)^2
```

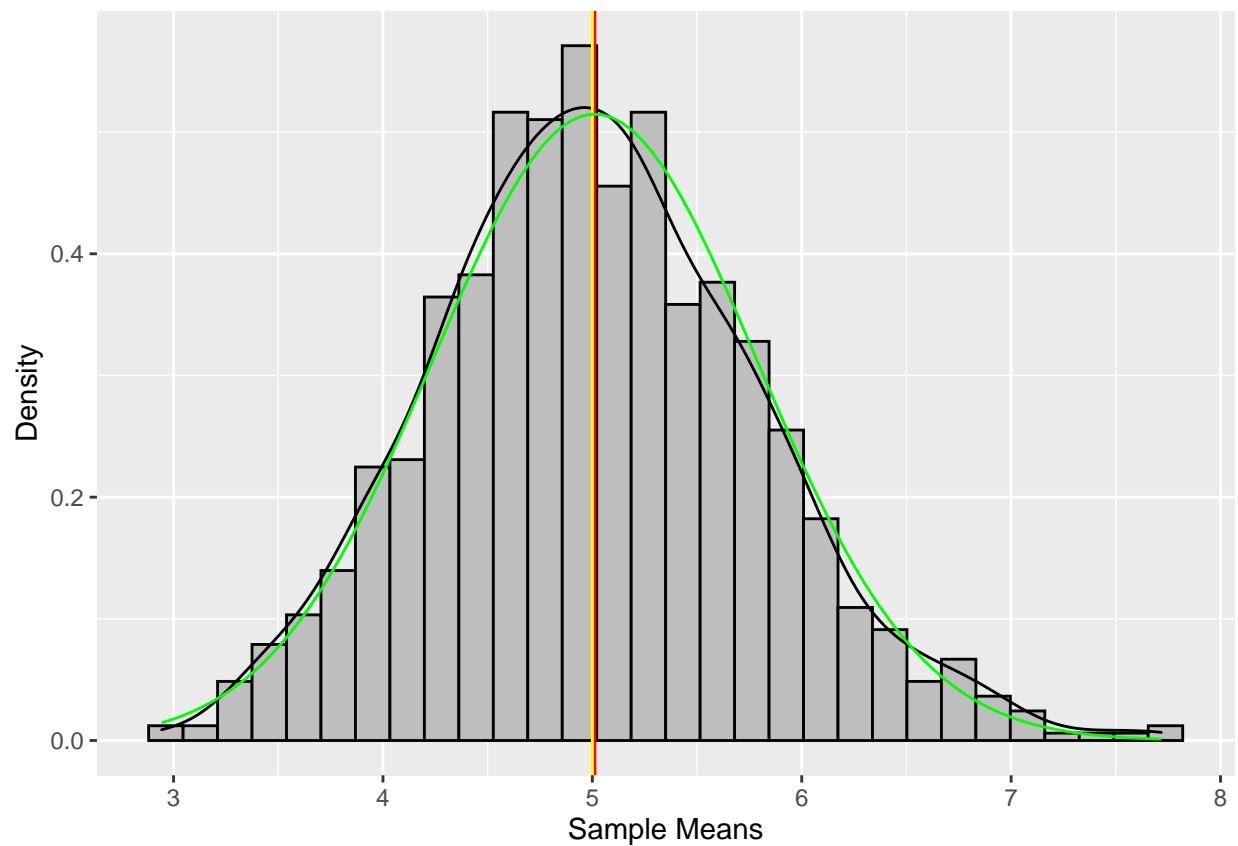
```
## [1] 0.6004928
```

Theoretical variance is close to sample variance

3. Show that the distribution is approximately normal

```
ggplot(meanexp, aes(x=mean.exp)) +
  geom_histogram(aes(y=..density..), color="black", fill="grey") +
  geom_density() +
  geom_vline(aes(xintercept=mm.exp), color="red") +
  geom_vline(aes(xintercept=1/lambda), color="yellow") +
  labs(x="Sample Means", y="Density") +
  stat_function(fun=dnorm, color="green", args=list(mean=mm.exp, sd=sd(mean.exp)))
```

```
## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.
```



The distribution is approximately normal