## PNTE Program

Referred manuscript title: "A program for estimating the tortuosity of rocks from cast thinsection images". The program is composed of a main function file "PNTE.m" and 11 subroutines. The subroutines' corresponding inputs and outputs are introduced in front of each subroutine (see also Table 1 to 3). In this file, we provide a brief guide to using the program.

Step 1. Input tortuosity definition flags.

Parameter	Value
dtype	=1 width of the image,
	=2 straight-line distance between the inlet and the outlet.
ttype	=1 average tortuosity among all pi,
	=2 minimum tortuosity among all pi.

Step 2. Input pore space segmentation parameters (HSV color model).

Parameter	Value
Hmin	minimum of hue.
Hmax	maximum of hue.
Smin	minimum of saturation.
Vmin	minimum of value.

Step 3. Input dilation factor Df.

Parameter	Value
dilaf	dilation factor Df.
4-4-11-	= 1 show the figures referred to detailed procedures,
details	= 0 turn off the figures showing the detailed procedures.

Outputs: taun- the tortuosity of the pore network.

Table 1. Functions of the subroutines

Subroutines	Purpose
PoreSegmentation	The function segments the pore space from a cast thin section image.
mothus vision	The function is designed to generate and revise the pore network
pathrevision	from the pore space.
IOIB	The function figures out inlets, outlets, and intersectional points &
ЮІВ	blocks of the pore network.
DWG	The function segments the pore space from a cast thin section image.
neiberdis1	The function provides the paths, lengths, and ends of all the path
neiberdisi	forks referred to the vertex di.
neiberdis2	The function provides the paths, lengths, and ends of all the path
neiberdisz	forks referred to the vertex di.
EWalaanithaa	The function is Floyd-Warshall algorithm for solving all pairs
FWalgorithm	shortest path problems.
tau	The function segments the pore space from a cast thin section image.
SPtrace	The function traces the shortest paths.
tracepath	The function figures out the trace and path between two vertices.

Table 2. Inputs of the subroutines.

Subroutines	Iutput	Description
	Image	RGB image of a cast thin section
PoreSegmentation	Hmin	minimum of hue
	Hmax	maximum of hue
	Smin	minimum of saturation
	Vmin	minimum of value
	pp	the number of the rows of the cast thin section image
	qq	the number of the coloumns of the cast thin section image
nothroxidian	dilaf	dilation factor
pathrevision	pores1	the pore space
	sp1	the pore network
	details	flag parameter defined in the main function
	pp	the row number of the cast thin section image
IOIB	qq	the column number of the cast thin section image
	sp1	the pore network
	bw	the final pore network
DWG	pois	the collections (vertices ) of inlets, outlets, and
	pois	intersectional points & blocks of the pore network
	di	the vertex di
	bw	the final pore network
neiberdis1	pois	the collections (vertices) of inlets, outlets, and intersectional
		points & blocks of the pore network
	blocks	the intersectional blocks of the pore network
	di	the vertex di
	bw	the final pore network
neiberdis2	pois	the collections (vertices) of inlets, outlets, and intersectional
	Pois	points & blocks of the pore network
	blocks	the intersectional blocks of the pore network
	path	the fork paths of the vertex di
drpath	lpath	the lengths of the fork paths of the vertex di
u.p.u	bns	the vertex number of the fork ends referred to all the vertices
		in the pore network
	dis	the distance-weighted graph
	tnote	the matrix of the intermediate vertices used in the Floyd-
Fwalgorithm		Warshall algorithm
	pois	the collections (vertices ) of inlets, outlets, and
	1	intersectional points & blocks of the pore network

Continued Table 2. Inputs of the subroutines.

Subroutines	Iutput	Description
	sp	the inlets of the pore network
	ep	the outlets of the pore network
	4:	the distance-weighted graph after applying the Floyd-
	dis	Warshall algorithm
tau	dtype	=1 width of the image, =2 straight-line distance between the
		inlet and the outlet
	ttype	=1 average tortuosity among all pi, =2 minimum tortuosity
		among all pi
	qq	the column numbers of the cast thin section image
	mm	the total number of rows of the final pore network image
	sp	the inlets of the pore network
	pi	the outlets referred to each pi
	bw	the final pore network image
SPtrace	tnote	the matrix of the intermediate vertices used in the Floyd-
Sittacc		Warshall algorithm
	tpath	the fork paths of each vertex in the pore network
	tbns	the vertex number of the fork ends referred to all the vertices
		in the pore network
	nt	the indices of the minimum tortuosity among all pi
	startp	start pixel
	endp	end pixel
	tnote	the matrix of the intermediate vertices used in the Floyd-
tracepath		Warshall algorithm
пасерані	tpath	the fork paths of each vertex in the pore network
	tbns	the vertex number of the fork ends referred to all the vertices
		in the pore network
	mm	the total number of rows of the final pore network image

Table 3. Outputs of the subroutines.

PoreSegmentation pores1 the acquired pore space  pathrevision osp1 the new pore network  bw the final pore network image  the collections of inlets, outlets, and intersectional points & blocks of the pore network  sp the inlets of the pore network  ep the outlets of the pore network  mp the intersectional points of the pore network  bp the intersectional blocks of the pore network  dis the distance-weighted graph  the matrix of the intermediate vertices used in the Floyd-Warshall algorithm  tpath the fork paths of each vertex in the pore network  the vertex number of the fork ends referred to all the
bw the final pore network image the collections of inlets, outlets, and intersectional points & blocks of the pore network  sp the inlets of the pore network ep the outlets of the pore network mp the intersectional points of the pore network bp the intersectional blocks of the pore network dis the distance-weighted graph the matrix of the intermediate vertices used in the Floyd-Warshall algorithm  tpath the fork paths of each vertex in the pore network the vertex number of the fork ends referred to all the
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IOIB  points & blocks of the pore network  sp the inlets of the pore network  ep the outlets of the pore network  mp the intersectional points of the pore network  bp the intersectional blocks of the pore network  dis the distance-weighted graph  the matrix of the intermediate vertices used in the  Floyd-Warshall algorithm  tpath the fork paths of each vertex in the pore network  the vertex number of the fork ends referred to all the
IOIB  sp the inlets of the pore network  ep the outlets of the pore network  mp the intersectional points of the pore network  bp the intersectional blocks of the pore network  dis the distance-weighted graph  the matrix of the intermediate vertices used in the Floyd-Warshall algorithm  tpath the fork paths of each vertex in the pore network  the vertex number of the fork ends referred to all the
by the intersectional points of the pore network bp the intersectional blocks of the pore network dis the distance-weighted graph the matrix of the intermediate vertices used in the Floyd-Warshall algorithm tpath the fork paths of each vertex in the pore network the vertex number of the fork ends referred to all the
DWG  the intersectional points of the pore network  the intersectional blocks of the pore network  dis  the distance-weighted graph  the matrix of the intermediate vertices used in the  Floyd-Warshall algorithm  tpath  the fork paths of each vertex in the pore network  the vertex number of the fork ends referred to all the
bp the intersectional blocks of the pore network  dis the distance-weighted graph  the matrix of the intermediate vertices used in the Floyd-Warshall algorithm  tpath the fork paths of each vertex in the pore network  the vertex number of the fork ends referred to all the
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DWG  tnote Floyd-Warshall algorithm  tpath the fork paths of each vertex in the pore network the vertex number of the fork ends referred to all the
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tpath the fork paths of each vertex in the pore network the vertex number of the fork ends referred to all the
the vertex number of the fork ends referred to all the
tbns vertices in the pore network
outlpath the fork paths of the vertex di
outlpath the lengths of the fork paths of the vertex di
neiberdis 1  the vertex number of the fork ends referred to all the
branchends vertices in the pore network
outlpath the fork paths of the vertex di
outlpath the lengths of the fork paths of the vertex di
neiberdis2  the vertex number of the fork ends referred to all the
branchends vertices in the pore network
opath the output fork paths of the vertex di
olpath the output lengths of the fork paths of the vertex di
drpath  the output vertex number of the fork ends referred to obns
all the vertices in the pore networ
dis the distance-weighted graph after applying the Floyd
Warshall algorithm
Fwalgorithm the matrix of the intermediate vertices after applying tnote
the Floyd-Warshall algorithm
taupi tortuosity of the shortest path pi
taun tortuosity of the pore network
pi the outlets referred to each pi
nt the indices of the minimum tortuosity among all pi
nettrace the indices of the paths of all pi
SPtrace netpath the paths of all pi
trace the distance-weighted graph
tracepath the matrix of the intermediate vertices used in the
spath Floyd-Warshall algorithm