#### GAME PLAYING

Chapter 6

## Game Playing

- Game playing was thought to be a good problem for AI research:
  - game playing is non-trivial
    - players need "human-like" intelligence
    - games can be very complex (e.g., Chess, Go)
    - requires decision making within limited time
  - games usually are:
    - well-defined and repeatable
    - fully observable and limited environments
  - can directly compare humans and computers

## **Computers Playing Chess**



#### Outline

- Games
- ◆ Perfect play (最优策略)
  - minimax decisions
  - α-β pruning (剪枝)
- Resource limits and approximate evaluation
- ◆ Games of chance (包含几率因素的游戏)
- Games of imperfect information

#### Games vs. search problems

"Unpredictable" opponent  $(不可预测的对手) \Longrightarrow$  solution is a strategy specifying a move for every possible opponent reply

Time limits ⇒ unlikely to find goal, must approximate 游戏对于低效率有严厉的惩罚

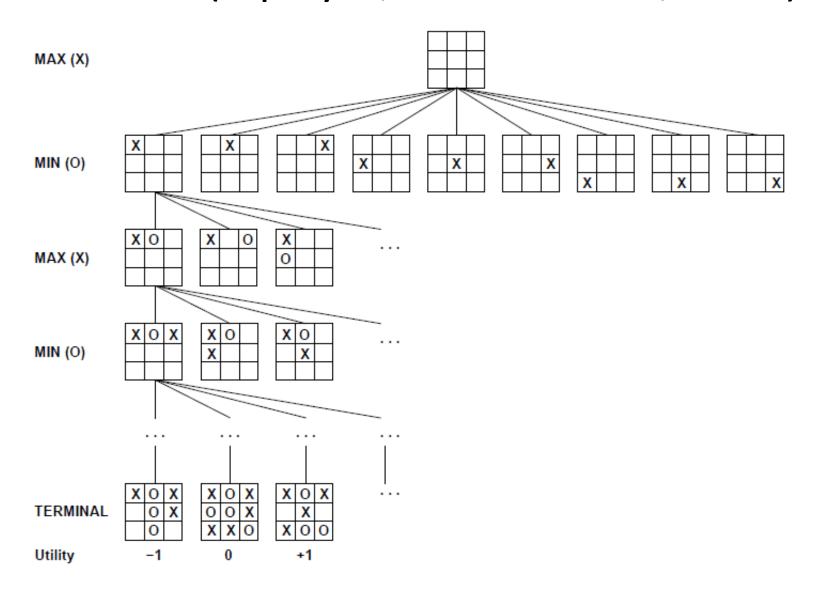
#### Plan of attack:

- Computer considers possible lines of play (Babbage, 1846)
- Algorithm for perfect play (Zermelo, 1912; Von Neumann, 1944)
- Finite horizon, approximate evaluation (Zuse, 1945; Wiener, 1948; Shannon, 1950)
- First chess program (Turing, 1951)
- Machine learning to improve evaluation accuracy (Samuel, 1952-57)
- Pruning (剪枝) to allow deeper search (McCarthy, 1956)

## Types of games

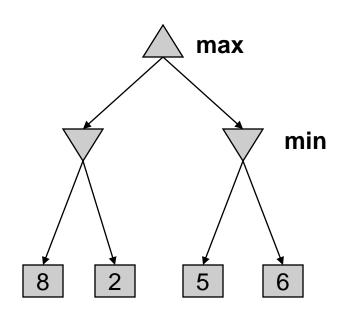
	Deterministic	Stochastic (chance)
perfect information	chess, checkers, Go(围棋), othello	Backgammon(西洋双 陆棋) monopoly
imperfect information	battleships, blind tictactoe	bridge, poker, scrabble (拼字游戏) nuclear war

#### Game tree (2-player, deterministic, turns)



#### Deterministic Two-Player

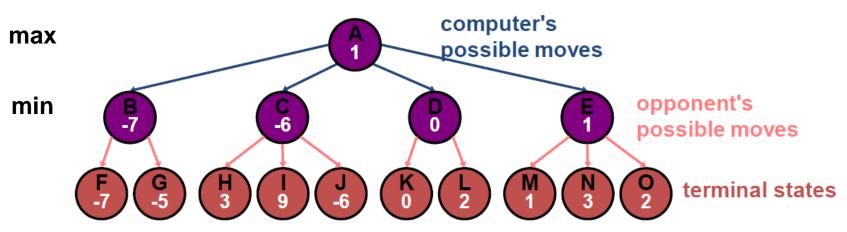
- E.g. tic-tac-toe, chess, checkers
- Game search
  - A state-space search tree
  - Players alternate
  - Each layer, or ply, consists of a round of moves
  - Choose move to position with highest achievable utility
- Zero-sum games
  - One player maximizes result
  - The other minimizes result



## Minimax Principle

#### Assume both players play optimally

- The computer assumes after it moves the opponent will choose the minimizing move
- The computer chooses the best move considering both its move and the opponent's optimal move



#### **Minimax**

Perfect play (最优策略) for deterministic, perfect-information games ldea: choose move to position with highest minimax value

= best achievable payoff against best play

在对手**也使用最优策略**的条件下,能导致至少不比其它策略差的结果

假设两个游戏者都按照最优策略进行,那么节点的极小极大值就是对应 状态的效用值(对于MAX)

- MAX优先选择有极大值的状态
- MIN优先选择有极小值的状态

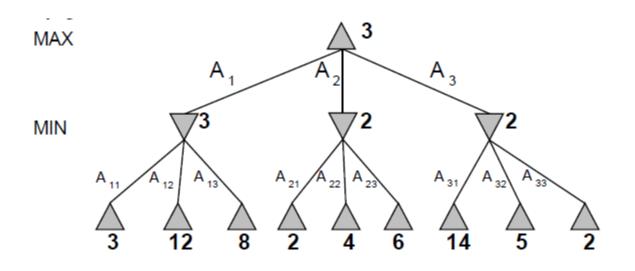
#### MINMAX - VALUE(n) =

#### Minimax

Perfect play (最优策略) for deterministic, perfect-information games Idea: choose move to position with highest minimax value

= best achievable payoff against best play

在对手**也使用最优策略**的条件下,能导致至少不比其它策略差的结果 E.g., 2-ply game:



#### Minimax algorithm

```
function MINIMAX-DECISION(state) returns an action
   inputs: state, current state in game
   return the a in ACTIONS(state) maximizing MIN-VALUE(RESULT(a, state))
function Max-Value(state) returns a utility value
   if Terminal-Test(state) then return Utility(state)
   v \leftarrow -\infty
   for a, s in Successors(state) do v \leftarrow \text{Max}(v, \text{Min-Value}(s))
   return v
function MIN-VALUE(state) returns a utility value
   if Terminal-Test(state) then return Utility(state)
   v \leftarrow \infty
   for a, s in Successors(state) do v \leftarrow \text{Min}(v, \text{Max-Value}(s))
   return v
```

**Complete**??

<u>Complete</u>?? Only if tree is finite (chess has specific rules for this).
a finite strategy can exist even in an infinite tree!
<u>Optimal</u>??

<u>Complete</u>?? Yes, if tree is finite (chess has specific rules for this)

Optimal?? Yes, against an optimal opponent. Otherwise??

Time complexity??

<u>Complete</u>?? Yes, if tree is finite (chess has specific rules for this)

Optimal?? Yes, against an optimal opponent. Otherwise??

Time complexity??  $O(b^m)$ 

Space complexity??

Complete?? Yes, if tree is finite (chess has specific rules for this)

Optimal?? Yes, against an optimal opponent. Otherwise??

Time complexity??  $O(b^m)$ Space complexity?? O(bm) (depth-first exploration)

For chess,  $b \approx 35$ ,  $m \approx 100$  for "reasonable" games

But do we need to explore every path?

⇒ exact solution completely infeasible

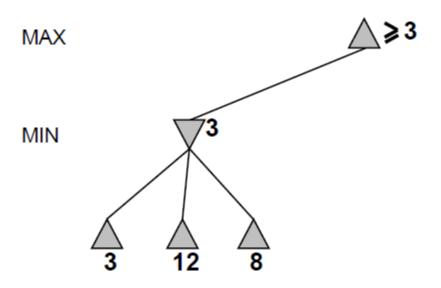
# $\alpha - \beta$ Pruning

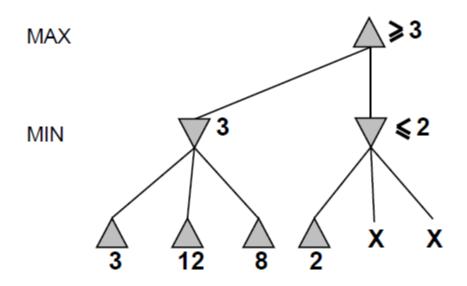
 Some of the branches of the game tree won't be taken if playing against an intelligent opponent

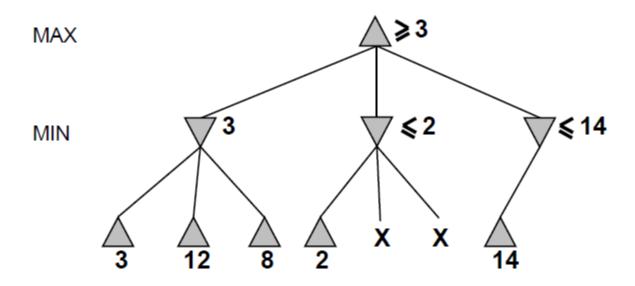
• "If you have an idea that is surely bad, don't take the time to see how truly awful it is."

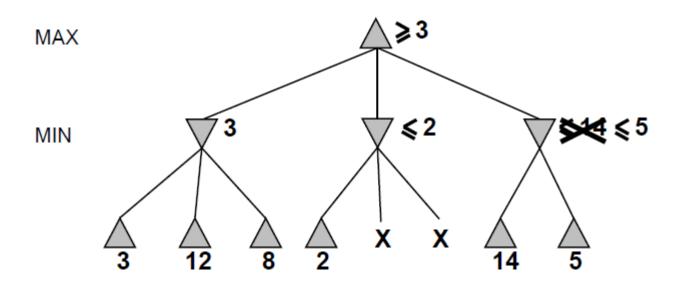
-- Pat Winston

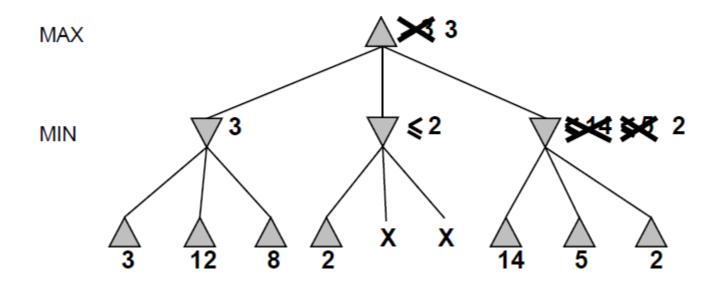
Pruning can be used to ignore some branches



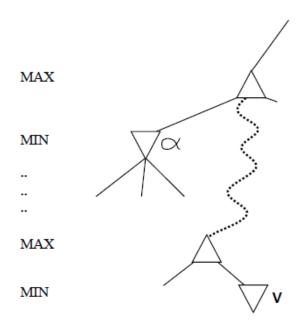








## Why is it called $\alpha - \beta$



- α is the best value (to MAX) found so far on the current path
   到目前为止在路径上的任意选择点发现的MAX的最佳(即最大值)选择
- If v is worse than  $\alpha$ , MAX will avoid it, so can stop considering v's other children  $\rightarrow$  prune that branch
- Define  $\beta$  similarly for MIN

# The $\alpha - \beta$ algorithm

```
function ALPHA-BETA-DECISION(state) returns an action
   return the a in Actions(state) maximizing Min-Value(Result(a, state))
function Max-Value(state, \alpha, \beta) returns a utility value
   inputs: state, current state in game
             \alpha, the value of the best alternative for MAX along the path to state
             \beta, the value of the best alternative for MIN along the path to state
   if TERMINAL-TEST(state) then return UTILITY(state)
   v \leftarrow -\infty
   for a, s in Successors(state) do
      v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(s, \alpha, \beta))
      if v \geq \beta then return v
      \alpha \leftarrow \text{Max}(\alpha, v)
   return v
```

function MIN-VALUE( $state, \alpha, \beta$ ) returns a utility value same as MAX-VALUE but with roles of  $\alpha, \beta$  reversed

## Effectiveness of $\alpha - \beta$ Search

• Effectiveness depends on the order in which successors are examined; more effective if best successors are examined first

#### Worst Case:

- ordered so that no pruning takes place
- no improvement over exhaustive search

#### Best Case:

- each player's best move is evaluated first
- In practice, performance is closer to best, rather than worst,
   case

## Properties of $\alpha - \beta$

Pruning does not affect final result

Good move ordering improves effectiveness of pruning

With "perfect ordering," time complexity =  $O(b^{m/2})$  $\Rightarrow$  doubles solvable depth

A simple example of the value of reasoning about which computations are relevant (a form of metareasoning)

Unfortunately, 35<sup>50</sup> is still impossible!

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#### Resource limits

Standard approach: Depth-limited search

- Use CUTOFF-TEST (截断测试) instead of TERMINAL-TEST (终止测试) e.g., depth limit (perhaps add quiescence search 静态搜索)
- Use EVAL instead of UTILITY

用可以估计棋局效用值的启发式评价函数EVAL取代效用函数 i.e., evaluation function that estimates desirability of position

Suppose we have 100 seconds, explore 104 nodes/second

 $\Rightarrow$  10<sup>6</sup> nodes per move  $\approx$  35<sup>8/2</sup>

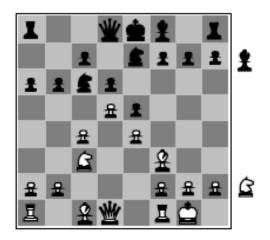
 $\Rightarrow \alpha - \beta$  reaches depth 8  $\Rightarrow$  pretty good chess program

4-ply lookahead is a hopeless chess player!

- 4-ply pprox human novice
- 8-ply  $\approx$  typical PC, human master
- 12-ply pprox Deep Blue, Kasparov

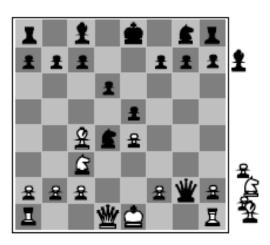
#### **Evaluation functions**

Function which scores non-terminals



Black to move

White slightly better



White to move

Black winning

- Ideal function: returns the utility of the position
- In practice: typically weighted linear sum of features (特征):

$$Eval(s) = w_1 f_1(s) + w_2 f_2(s) + ... + w_n f_n(s)$$

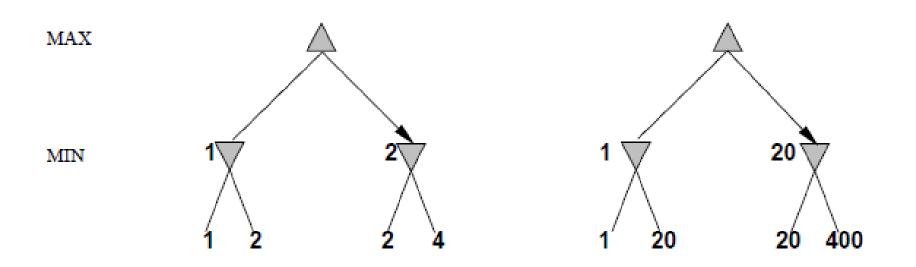
e.g., for chess,  $w_1 = 9$  with

 $f_1(s) = \text{(number of white queens)} - \text{(number of black queens)}, etc.$ 

#### More on Evaluation Functions

- The board evaluation function estimates how good the current board configuration is
- A linear evaluation function of the features is a weighted sum of f1, f2, f3,
   ...
  - More important features get more weight
- The quality of play depends directly on the quality of the evaluation function
- To build an evaluation function we have to:
  - construct good features using expert domain knowledge
  - pick or learn good weights

#### Digression: Exact values don't matter



Behavior is preserved under any monotonic (单调的) transformation of EVAL Only the order matters:

payoff (结果) in deterministic games acts as an ordinal utility (序数效用) function

#### Dealing with Limited Time

- In real games, there is usually a time limit T on making a move
- How do we take this into account?
  - cannot stop alpha-beta midway and expect to use results with any confidence
  - so, we could set a conservative depth-limit that guarantees we will find a move in time < T
  - but then, the search may finish early and the opportunity is wasted to do more search

#### Dealing with Limited Time

- In practice, iterative deepening search (IDS) is used
  - run alpha-beta search with an increasing depth limit
  - when the clock runs out, use the solution found for the last completed alpha-beta search (i.e., the deepest search that was completed)

#### Deterministic games in practice

Chess(国际象棋): Deep Blue defeated human world champion Gary Kasparov in a six-game match in 1997. Deep Blue searches 200 million positions per second, uses very sophisticated evaluation, and undisclosed methods for extending some lines of search up to 40 ply (层、厚度).

- 计算机能够预见它的决策中的长期棋局序列。机器拒绝走一步有决定性短期优势的棋—显示了非常类似于人类的对危险的感觉。——Kasparov
- Kasparov lost the match 2 wins to 3 wins and 1 tie
- Deep Blue played by "brute force" (i.e., raw power from computer speed and memory); it
  used relatively little that is similar to human intuition and cleverness
- Used minimax, alpha-beta, sophisticated heuristics

#### Deterministic games in practice

Checkers (西洋跳棋): Chinook, the World Man-Machine Checkers Champion.

- Chinook ended 40-year-reign of human world champion Marion Tinsley in 1994.
- In 2007, checkers was solved: perfect play leads to a draw.

Chinook cannot ever lose

使用了一个提前计算好的存有443,748,401,247个不多于8个棋子的棋局数

据库, 使它的残局(endgame)走棋没有缺陷

50 machines working in parallel on the problem

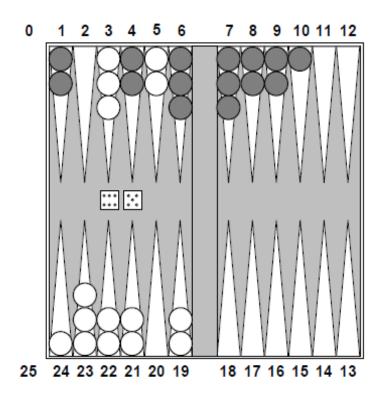
#### Deterministic games in practice

Othello (奥赛罗): human champions refuse to compete against computers, who are too good.

Go (国棋): human champions refuse to compete against computers, who are too bad. In go, b > 300(棋盘为19x19), so most programs use pattern knowledge bases to suggest plausible moves.

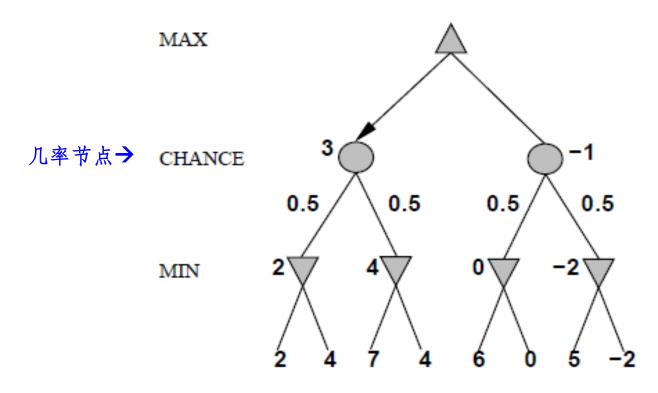
A new benchmark for Artificial Intelligence (人工智能新的试金石)

# Nondeterministic games: backgammon(西洋双陆棋)



#### Nondeterministic games in general

In nondeterministic games, chance introduced by dice, card-shuffling Simplified example with coin-flipping:



#### Nondeterministic games in general

 Weight score by the probability that move occurs

MAX

 Use expected value for move: instead of using max or min, compute the average, weighted by the probabilities of each child

CHANCE

MIN

3 0.5 0.5 0.5 0.5 0.5 2 4 0 -2 2 4 7 4 6 0 5 -2

 Choose move with highest expected value

#### Maximum Expected Utility

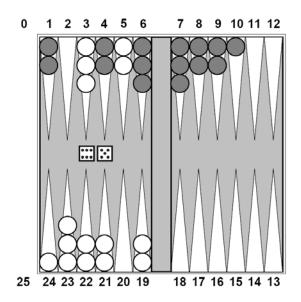
- Why should we average utilities? Why not minimax?
- Principle of maximum expected utility: an agent should chose the action which maximizes its expected utility, given its knowledge
- General principle for decision making
- Often taken as the definition of rationality
- We'll see this idea over and over in this course!

#### Algorithm for nondeterministic games

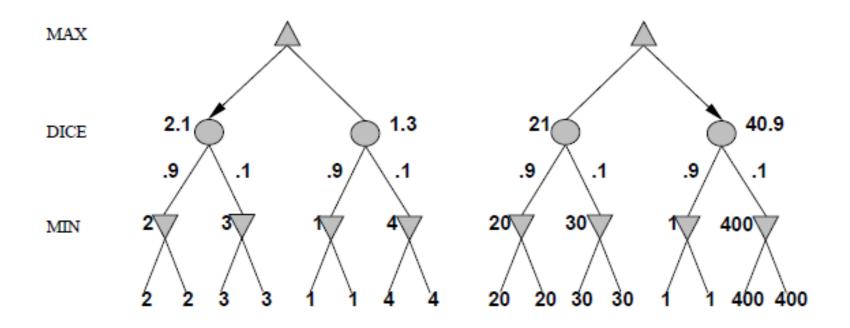
```
EXPECTIMINIMAX gives perfect play
Just like MINIMAX, except we must also handle chance nodes:
if state is a Max node then
   return the highest EXPECTIMINIMAX-VALUE of SUCCESSORS(state)
if state is a Min node then
   return the lowest EXPECTIMINIMAX-VALUE of SUCCESSORS(state)
if state is a chance node then
   return average of EXPECTIMINIMAX-VALUE of SUCCESSORS(state)
```

#### Stochastic Two-Player

- Dice rolls increase *b*: 21 possible rolls with 2 dice
  - Backgammon ≈ 20 legal moves
  - Depth  $4 = 20 \times (21 \times 20)^3 \cdot 1.2 \times 10^9$
- As depth increases, probability of reaching a given node shrinks
  - So value of lookahead is diminished
  - So limiting depth is less damaging
  - But pruning is less possible...
- TDGammon uses depth-2 search + very good eval function + reinforcement learning: world-champion level play



#### Digression: Exact values DO matter



Behaviour is preserved only by positive linear transformation of EVAL Hence EVAL should be proportional to the expected payoff 评价函数应该是棋局的期望效用值的正线性变换

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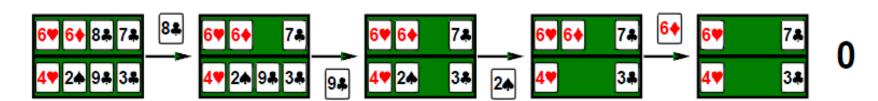
#### Games of imperfect information

E.g., card games, where opponent's initial cards are unknown Typically we can calculate a probability for each possible deal Seems just like having one big dice roll at the beginning of the game

Idea: compute the minimax value of each action in each deal, then choose the action with highest expected value over all deals 在评价一个有未知牌的给定行动过程时,首先计算出每副可能牌的出牌行动的极小极大值,然后再用每副牌的概率来计算得到对所有发牌情况的期望值。

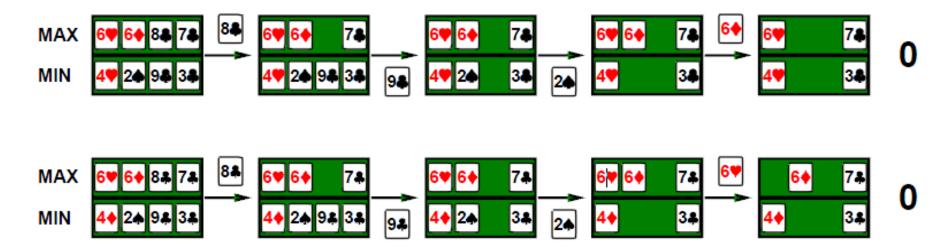
#### Example

Four-card bridge/whist/hearts hand, MAX to play first



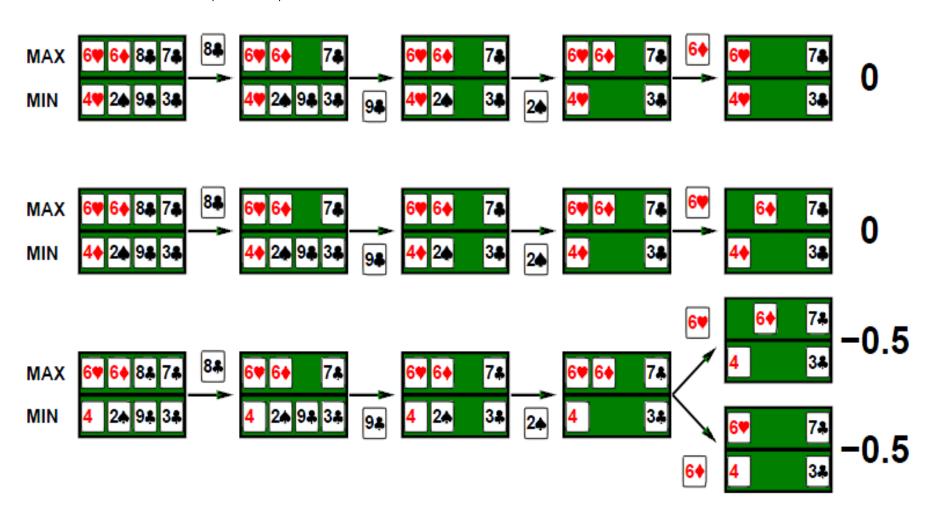
#### Example

Four-card bridge/whist/hearts hand, MAX to play first



#### Example

Four-card bridge/whist/hearts hand, MAX to play first



#### Proper analysis

\* Intuition that the value of an action is the average of its values in all actual states is WRONG

With partial observability, value of an action depends on the information state or belief state (信度状态) the agent is in

Can generate and search a tree of information states

Leads to rational behaviors such as

- Acting to obtain information
- Signaling to one's partner
- Acting randomly to minimize information disclosure

#### Summary

- Games are fun to work on!
  - perfection is unattainable → must approximate
  - Games are to Al as grand prix racing is to automobile design
- Game playing is best modeled as a search problem
  - Search trees for games represent alternate computer/opponent moves
- Evaluation functions estimate the quality of a given board configuration for each player
- Minimax is an algorithm that chooses "optimal" moves by assuming that the opponent always chooses their best move
- Alpha-beta is an algorithm that can avoid large parts of the search tree, thus enabling the search to go deeper 消除无关的子树以提高效率

### Summary of Search

Uninformed search strategies

Breadth-first search (BFS), Uniform cost search, Depth-first search (DFS), Depth-limited search, Iterative deepening search

- Informed search strategies
  - Best-first search: greedy, A\*
  - Local search: hill climbing, simulated annealing etc.
- Constraint satisfaction problems
  - Backtracking = depth-first search with one variable assigned per node
  - Enhanced with: Variable ordering and value selection heuristics, forward checking, constraint propagation

## 作业

• 6.1, 6.3, 6.5