Empirical Performance Investigation of a Büchi Complementation Construction

Master's Thesis Presentation

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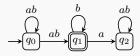
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Outline

1. GOAL

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Büchi automata



- Finite state automata running on infinite words (ω -words) $\in \Sigma^\omega$
- A word is accepted if it has an accepting run
- A run is accepting if it visits an accepting state infinitely often

Büchi complementation

The complement of a Büchi automaton A is another Büchi automaton B, such that:

B accepts a word if and only if it is not accepted by A

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Büchi Complementation Constructions



- \bullet Different constructions produce different complements B for the same automaton A
- Main performance measure: number m of states of B in relation to number n of states of A
 - State complexity
 - Also known as state growth, state blow-up, or state explosion
 - E.g. if n=10 and m=100, then $m=n^2$
 - ▶ Biggest problem of Büchi complementation

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The Fribourg Construction

- Slice-based complementation construction
- Worst-case state complexity: $(1.59n)^n$
- Optimisations:
 - ▶ R2C: if input automaton is complete, remove states whose rightmost component is 2-coloured
 - ▶ M1: merge certain adjacent components $(1.195n)^n$)
 - ▶ M2: keep not more than one 2-coloured component in every state $(0.86n^n)$

- Graphical Tool for Omega-Automata and Logics
- http://goal.im.ntu.edu.tw/wiki/doku.php
- Create and manipulate ω -automata

Graphical user interface

Command line interface

```
$ ./gc generate -t fsa -a nbw -s 15 -A classical -m density -dt 1.6 -da 0.3
<?xml version="1.0" encoding="UTF-8" standalone="no"?>
<Structure label-on="Transition" type="FiniteStateAutomaton">
    <Name/>
   <Description/>
   <Formula/>
   <Alphabet type="Classical">
       <Symbol>a</Symbol>
   <Symbol>b</Symbol>
   <StateSet>
       <State sid="0">
           <Y>160</Y>
           <X>346</X>
           <Properties/>
       </State>
       <State sid="1">
           <Y>54</Y>
           <X>291</X>
           <Properties/>
       <State sid="2">
           <Y>104</Y>
           <X>486</X>
           <Properties/>
       <State sid="3">
```

GOAL: Büchi Complementation Constructions

 Implementations of several Büchi complementation constructions (GOAL version 2014–11–17)

GOAL Name	Reference
Ramsey	[Sistla et al., 1985, Sistla et al., 1987]
Safra	[Safra, 1988a, Safra, 1988b]
MS	[Muller and Schupp, 1995]
ModifiedSafra	[Althoff et al., 2006]
Piterman	[Piterman, 2006, Piterman, 2007]
WAA	[Kupferman and Vardi, 1997, Kupferman and Vardi, 2001]
WAPA	[Thomas, 1999]
Rank	[Schewe, 2009]
Slice+P	[Vardi and Wilke, 2007]
Slice	[Kähler and Wilke, 2008]

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Fribourg Construction Plugin for GOAL

- GOAL is built with the Java Plugin Framework (JPF)¹
 - Extensibility: create plugins containing extensions for pre-defined extension points
- Our plugin adds the Fribourg construction to GOAL
 - ... in a fully integrated way

Graphical user interface



Command line interface



 Download: https://frico.s3.amazonaws.com/goal_plugins/ch. unifr.goal.complement.zip

¹http://jpf.sourceforge.net/

GOAL and Plugin Demo



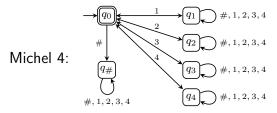
Test Data: GOAL Test Set

- Created and used for [Tsai et al., 2011]
- 11,000 automata
 - ▶ 15 states
 - Alphabet $\Sigma = \{0, 1\}$
 - ▶ 11 transition densities
 - $\mathcal{T} = (1.0, 1.2, 1.4, 1.6, 1.8, 2.0, 2.2, 2.4, 2.6, 2.8, 3.0)$
 - 10 acceptance densities
 - $\mathcal{A} = (0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0)$
 - lacksquare 110 classes at 100 automata for each combination of $\mathcal{T} \times \mathcal{A}$
- Analysis
 - ▶ 61.8% universal automata
 - ▶ 0.6% empty automata
 - ▶ 9.0% complete automata
- Download: https://frico.s3.amazonaws.com/test_sets/goal.zip

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Test Data: Michel Test Set

- Four Michel automata
 - Michel 1: 3 states, 2 symbols, 5 transitions
 - ▶ Michel 2: 4 states, 3 symbols, 8 transitions
 - Michel 3: 5 states, 4 symbols, 11 transitions
 - Michel 4: 6 states, 5 symbols, 14 transitions



- Automata used by [Michel, 1988] to prove n! lower bound
- Very high state complexity
- Download: https://frico.s3.amazonaws.com/test_sets/michel.zip

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Test Setup

- Internal tests
 - Compare different versions of the Fribourg construction
- External tests
 - Compare Fribourg construction with other constructions

	GOAL test set	Michel test set		
Internal tests	 Fribourg Fribourg+R2C Fribourg+R2C+C Fribourg+M1 Fribourg+M1+R2C Fribourg+M1+R2C+C Fribourg+M1+M2 Fribourg+R 	 Fribourg Fribourg+R2C Fribourg+M1 Fribourg+M1+M2 Fribourg+M1+M2+R2C Fribourg+R 		
External tests	Fribourg+M1+R2CPiterman+EQ+RORank+TR+ROSlice+P+RO+MADJ+EG	Fribourg+M1+M2+R2CPiterman+EQ+RORank+TR+ROSlice+P+RO+MADJ+EG		

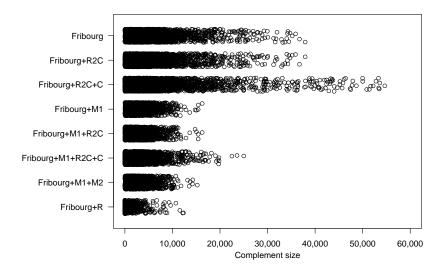
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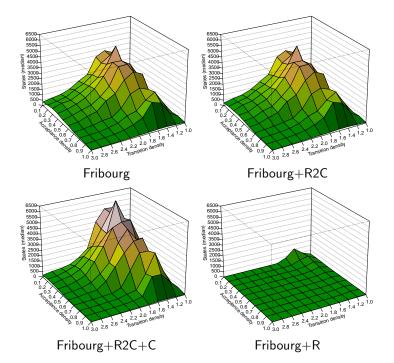
Results: Internal Tests on GOAL Test Set

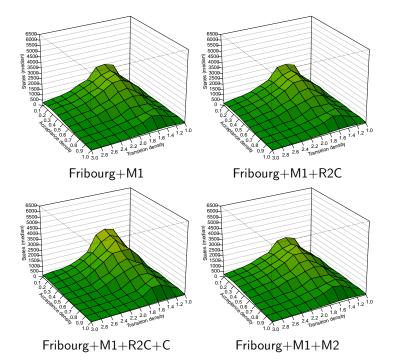
Construction	Mean	Min.	P25	Median	P75	Max.
Fribourg	2,004.6	2	222.0	761.0	2,175.0	37,904
Fribourg+R2C	1,955.9	2	180.0	689.0	2,127.5	37,904
Fribourg+R2C+C	2,424.6	2	85.0	451.0	2,329.0	54,648
Fribourg + M1	963.2	2	177.0	482.0	1,138.0	16,260
Fribourg+M1+R2C	937.7	2	152.0	447.0	1,118.0	16,260
Fribourg+M1+R2C+C	1,062.6	2	83.0	331.0	1,208.5	25,002
Fribourg+M1+M2	958.0	2	181.0	496.0	1,156.5	15,223
Fribourg+R	136.3	1	1.0	1.0	21.0	12,312

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Results: Internal Tests on GOAL Test Set







Thank you very much for listening!

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