Empirical Performance Investigation of a Büchi Complementation Construction

Master's Thesis Presentation

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19 August 2015



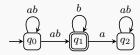
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Outline

1. Introduction

- 2. Implementation
- 3. Study Setup
- 4. Results

Büchi automata



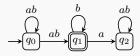
- Finite state automata running on infinite words (ω -words) $\in \Sigma^\omega$
- A word is accepted if it has an accepting run
- A run is accepting if it visits an accepting state infinitely often

Büchi complementation

The complement of a Büchi automaton A is another Büchi automaton B, such that:

B accepts a word if and only if it is not accepted by A

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- ullet State complexity: m in relation to n
 - Size of complement in relation to size of input automaton
- Also known as state growth, state blow-up, or state explosion
- Can be very high
- Inhibits the application of Büchi complementation in practice
 - ► E.g. in automata-theoretic model checking
- The lower the state complexity, the higher the performance of the construction
- Importance to investigate the state complexity of Büchi complementation constructions (see next slides)



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Worst-Case State Complexity

- Every construction has a specific worst-case state complexity
- Maximum number of states that a construction can produce
- Examples:

Complementation construction	Worst-case state complexity	Example value with $n=15$
[Büchi, 1962]	$2^{2^{O(n)}}$	$1.4 \times 10^{9,864}$
[Piterman, 2007]	$O(n^{2n})$	1.9×10^{35}
[Vardi and Wilke, 2007]	$O((3n)^n)$	6.3×10^{24}
[Schewe, 2009]	$O((0.76n)^n)$	7.1×10^{15}

 Often used to assess the performance or efficiency of a construction, but...

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 Often used to assess the performance or efficiency of a construction, but...

- Worst-case state complexity reflects only a small aspect of the state complexity of a construction
- From a practical point of view, we are interested in the performance of a construction on **concrete** automata
 - ► E.g. how does the construction perform on "typical" automata with 15 states?
- Such insights can be gained by empirical investigations
- Empirical performance investigation:
 - 1. Implement construction
 - 2. Run the implementation on test automata
 - 3. Analyse generated complements
- Aim of this thesis:
 - Empirically investigate the performance of the Fribourg construction (see next slide)

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The Fribourg Construction

- Described by [Allred and Ultes-Nitsche, 2014]
- Slice-based complementation construction
 - ► See main complementation approaches: Ramsey-based, determinisation-based, rank-based, and slice-based
- Worst-case state complexity: $O((1.59n)^n)$
- Optimisations:
 - **R2C** If input automaton is complete, remove states whose rightmost component is 2-coloured
 - M1 Merge certain pairs of adjacent components
 - Worst-case state complexity: $O((1.195n)^n)$
 - M2 Keep only one 2-coloured component in a state
 - ▶ Worst-case state complexity: $O((0.86n)^n)$

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Roadmap

1. Introduction

2. Implementation

3. Study Setup

4. Results

- Graphical Tool for Omega-Automata and Logics
- http://goal.im.ntu.edu.tw/wiki/doku.php
- Allows to create and manipulate ω -automata

Graphical user interface

GOAL - #1 🗃 🔒 📈 💢 🚷 🕟 🕠 👤 te 00 🥢 *#0: untitled Property Editor Type Name Description Lahel Color Text Color Opacity 100 Self-loon Initial indicator Position (338, 10 Apply

Command line interface

```
generate -t fsa -a nbw -s 15 -A classical -m density -dt 1.6 -da 0.3
<?xml version="1.0" encoding="UTF-8" standalone="no"?>
<Structure label-on="Transition" type="FiniteStateAutomaton">
    <Description/>
    <Formula/>
   <Alphabet type="Classical">
       <Symbol>a</Symbol>
       <Svmbol>b</Svmbol>
   </Alphabet>
   <StateSet>
       <State sid="0">
           <Y>160</Y>
           <X>346</X>
           <Properties/>
       <State sid="1">
           <Y>54</Y>
           <X>291</X>
           <Properties/>
        <State sid="2">
           <Y>184</Y>
           <X>486</X>
           <Properties/>
```

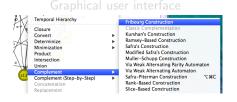
GOAL: Büchi Complementation Constructions

 GOAL contains implementations of several complementation constructions (version 2014–11–17)

GOAL Name	Reference
Ramsey	[Sistla et al., 1985, Sistla et al., 1987]
Safra	[Safra, 1988a, Safra, 1988b]
MS	[Muller and Schupp, 1995]
${\sf ModifiedSafra}$	[Althoff et al., 2006]
Piterman	[Piterman, 2006, Piterman, 2007]
WAA	[Kupferman and Vardi, 1997, Kupferman and Vardi, 2001]
WAPA	[Thomas, 1999]
Rank	[Schewe, 2009]
Slice+P	[Vardi and Wilke, 2007]
Slice	[Kähler and Wilke, 2008]

Fribourg Construction Plugin for GOAL

- GOAL is built with the Java Plugin Framework (JPF)¹
 - Allows to create plugins containing extensions for pre-defined extension points
- Our plugin adds the Fribourg construction to GOAL
 - ▶ ... in a fully integrated way



Command line interface



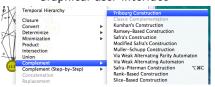
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GOAL and Plugin Demo



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Roadmap

Study setup

- Test data
- Test scenarios
- Execution

- Created and used by [Tsai et al., 2011]
- 11,000 automata
 - ▶ 15 states
 - Alphabet $\Sigma = \{0, 1\}$
 - ▶ 11 transition densities

•
$$\mathcal{T} = (1.0, 1.2, 1.4, 1.6, 1.8, 2.0, 2.2, 2.4, 2.6, 2.8, 3.0)$$

- ▶ 10 acceptance densities
 - A = (0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0)
- ▶ 110 classes at 100 automata for each combination $\mathcal{T} \times \mathcal{A}$
- Analysis
 - ▶ 61.8% universal automata
 - ▶ 0.6% empty automata
 - ▶ 9.0% complete automata
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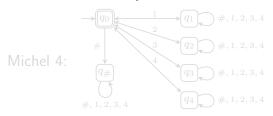
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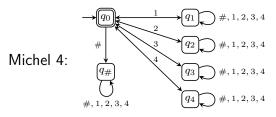
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- Four Michel automata
 - Michel 1: 3 states, 2 symbols, 5 transitions
 - ▶ Michel 2: 4 states, 3 symbols, 8 transitions
 - Michel 3: 5 states, 4 symbols, 11 transitions
 - ▶ Michel 4: 6 states, 5 symbols, 14 transitions



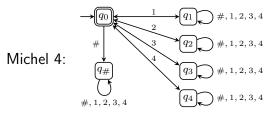
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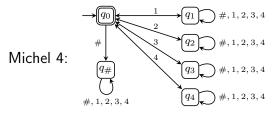
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Test Scenarios

- Internal tests
 - Compare different versions of the Fribourg construction
 - Combinations of optimisations R2C, M1, and M2
 - ► Further options:
 - C: make input automaton complete
 - R: remove unreachable and dead states from output automaton
- External tests
 - Compare Fribourg construction with other constructions
 - Choose best version of Fribourg construction for each test se
 - Other constructions:
 - Piterman [Piterman, 2006, Piterman, 2007]
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	GOAL test set	Michel test set
Internal tests		
External tests		

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Test Scenarios: Shorthand Names

	GOAL test set	Michel test set
Internal	IG	IM
External	EG	EM

- For IG and EG, we limit the resources for each complementation task (= complementation of 1 automaton)
 - ► Time: 600 seconds (CPU time)
 - Memory: 1 GB (Java heap)
- If a complementation task exceeds these limits, it is aborted
- Reason: prevent excessive resource requirements
- Effective samples
 - Automata which have been successfully complemented by all constructions of a test scenario
- Analysis of results of IG and EG is based on effective samples
- For IM and EM, we do not set limits

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Execution: Environment

- Exeuction on UBELIX: high-performance computing (HPC) cluster at the University of Bern²
- Through command line interface of GOAL
 - ▶ E.g. gc complement -m fribourg 00001.gff
 - ▶ 1 automaton = 1 process
- Usage of UBELIX hnodes 1–42 and jnodes:
 - Processor: Intel Xeon E5-2665 2.40GHz
 - Architecture: 64 bit
 - ► CPUs: 16
 - Memory (RAM): 64 GB (hnodes) or 256 GB (jnodes)
 - ▶ Operating System: Red Hat Enterprise Linux 6.6



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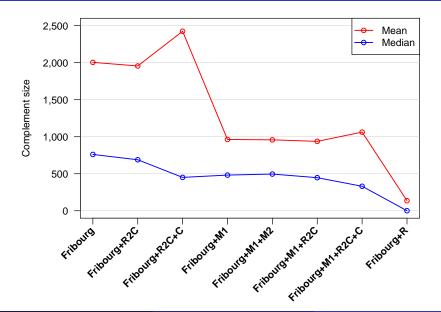
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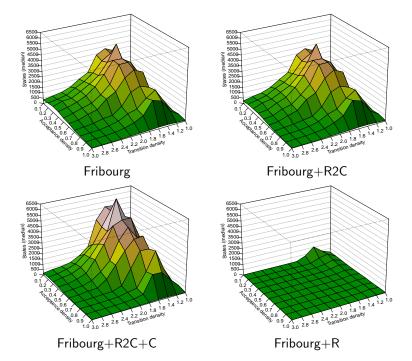
Results: Internal Tests on GOAL Test Set

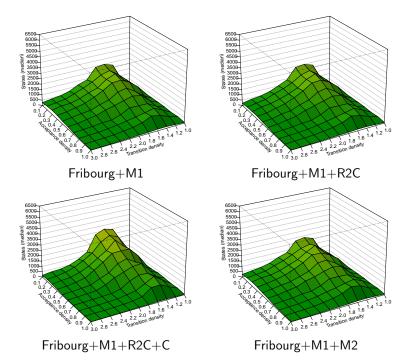
	GOAL test set	Michel test set
Internal	IG	IM
External	EG	EM

- Fribourg
- Fribourg+R2C
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- Fribourg+M1
- Fribourg+M1+R2C
- Fribourg+M1+R2C+C
- Fribourg+M1+M2
- Fribourg+R

IG: Complement Sizes (10,939 Eff. Samples)





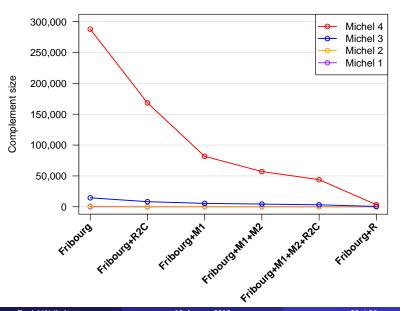


Results: Internal Tests on Michel Test Set

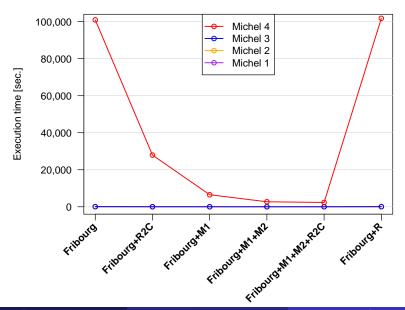
	GOAL test set	Michel test set
Internal	IG	IM
External	EG	EM

- Fribourg
- Fribourg+R2C
- Fribourg+M1
- Fribourg+M1+M2
- Fribourg+M1+M2+R2C
- Fribourg+R

IM: Complement Sizes



IM: Execution times



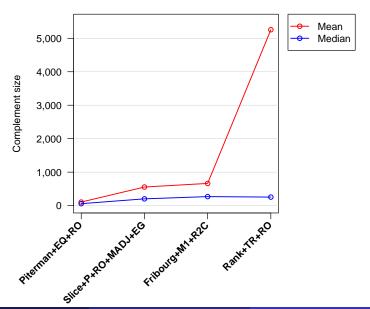
Results: External Tests on GOAL Test Set

	GOAL test set	Michel test set
Internal	IG	IM
External	EG	EM

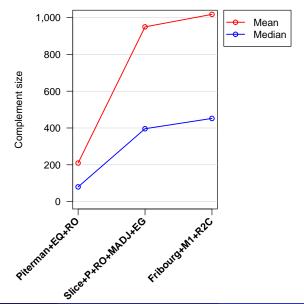
- Piterman+EQ+RO
- Rank+TR+RO
- Slice+P+RO+MADJ+EG
- Fribourg+M1+R2C

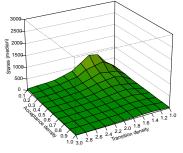
19 August 2015 30 / 38

EG: Complement Sizes (7,204 Eff. Samples)

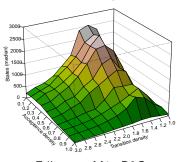


EG: Complement Sizes (10,998 Eff. Samples)

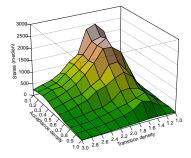




Piterman + EQ + RO



Fribourg+M1+R2C



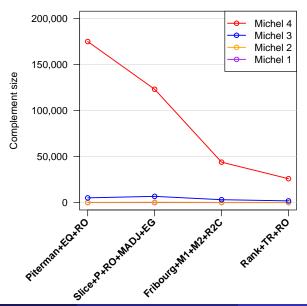
Slice+P+RO+MADJ+EG

Results: External Tests on Michel Test Set

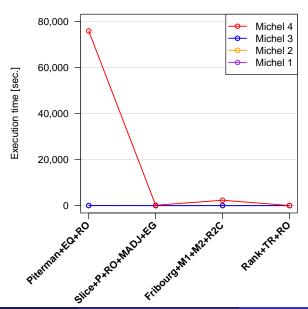
	GOAL test set	Michel test set
Internal	IG	IM
External	EG	EM

- Piterman+EQ+RO
- Rank+TR+RO
- Slice+P+RO+MADJ+EG
- Fribourg+M1+M2+R2C

EM: Complement Sizes



EM: Execution times



Conclusions

- Performance of Fribourg construction
 - Optimisations R2C and M1 have a very positive impact
 - M2 brings no overall improvement for GOAL test set
 - However, improves the performance on the Michel automata
 - R2C+C makes easy automata easier and hard automata harder
 - Mean of complement size increases, median decreases
- Büchi complementation in general
 - ▶ Worst-case complexities do not reflect actual performance
 - Actual performance is multifaceted and hard to predict
 - ▶ There is no "best" construction
 - All constructions have individual strengths and weaknesses
- Future work
 - ► Further statistical analyses of results

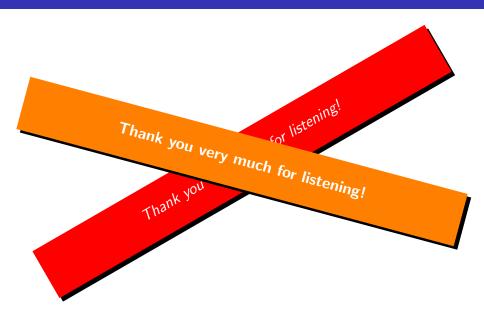
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The End



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