

HW7_P2

November 27, 2018

```
In [60]: import numpy as np
import matplotlib.pyplot as plt

In [61]: import csv
import pandas as pd
## reference: http://www.albertauyeung.com/post/python-matrix-factorization/hj
DataFrameBase = pd.read_csv('C:/Users/weich/Google Drive/Rice University/3rd Semester',
                             names=['user id', 'item id', 'rating', 'timestamp'], sep='\t')

DataFrameTest = pd.read_csv('C:/Users/weich/Google Drive/Rice University/3rd Semester',
                             names=['user id', 'item id', 'rating', 'timestamp'], sep='\t')

In [62]: num_user = 943
num_item = 1682
X_base = np.zeros((num_user, num_item))
X_test = np.zeros((num_user, num_item))

In [63]: for i in range(len(DataFrameBase)):
X_base[DataFrameBase['user id'][i]-1][DataFrameBase['item id'][i]-1] = DataFrameBase['rating'][i]

for i in range(len(DataFrameTest)):
X_test[DataFrameTest['user id'][i]-1][DataFrameTest['item id'][i]-1] = DataFrameTest['rating'][i]

In [6]: X_base

Out[6]: array([[5., 3., 4., ..., 0., 0., 0.],
               [4., 0., 0., ..., 0., 0., 0.],
               [0., 0., 0., ..., 0., 0., 0.],
               ...,
               [5., 0., 0., ..., 0., 0., 0.],
               [0., 0., 0., ..., 0., 0., 0.],
               [0., 5., 0., ..., 0., 0., 0.]])

In [ ]:

In [130]: class MatrixFactor():

def __init__(self, X_train, k, alpha, iterations):
    self.X_train = X_train
```

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self.num_users, self.num_items = X_train.shape
self.k = k
self.alpha = alpha
self.iterations = iterations

def train(self):
    self.U = np.random.normal(scale=1./self.k, size=(self.num_users, self.k))
    self.V = np.random.normal(scale=1./self.k, size=(self.num_items, self.k))

    self.b_u = np.zeros(self.num_users)
    self.b_t = np.zeros(self.num_items)
    self.b = np.mean(self.X_train[np.where(self.X_train != 0)])

    self.samples = [
        (i, j, self.X_train[i, j])
        for i in range(self.num_users)
        for j in range(self.num_items)
        if self.X_train[i, j] > 0
    ]

    training_process = []
    for i in range(self.iterations):
        np.random.shuffle(self.samples)
        self.SGM()
        loss = self.loss()
        training_process.append((i, loss))

    return training_process

def loss(self):
    xs, ys = self.X_train.nonzero()
    predicted = self.matrix()
    error = 0
    for x, y in zip(xs, ys):
        if self.X_train[x, y] != 0:
            error += pow(self.X_train[x, y] - predicted[x, y], 2)
    return np.sqrt(error)

def SGM(self):
    for i, j, y in self.samples:
        prediction = self.get_rating(i, j)
        l = (y - prediction)

        self.b_u[i] += self.alpha * l
        self.b_t[j] += self.alpha * l

        self.U[i, :] += self.alpha * l * self.V[j, :]
        self.V[j, :] += self.alpha * l * self.U[i, :]

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def get_rating(self, i, j):
    prediction = self.b + self.b_u[i] + self.b_t[j] + self.U[i, :].dot(self.V[j, :])
    return prediction

def matrix(self):
    return mf.b + mf.b_u[:, np.newaxis] + mf.b_t[np.newaxis:, :] + mf.U.dot(mf.V.T)

```

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In [147]: loss_temp = np.zeros(min(num_user, num_item))
for i in range(min(num_user, num_item)):
    mf = MatrixFactor(X_base, k=i+1, alpha=0.01, iterations=20)
    loss = mf.train()
    if i%20==0:
        print('k: ', i+1)
    loss_temp[i] = loss[-1][1]

```

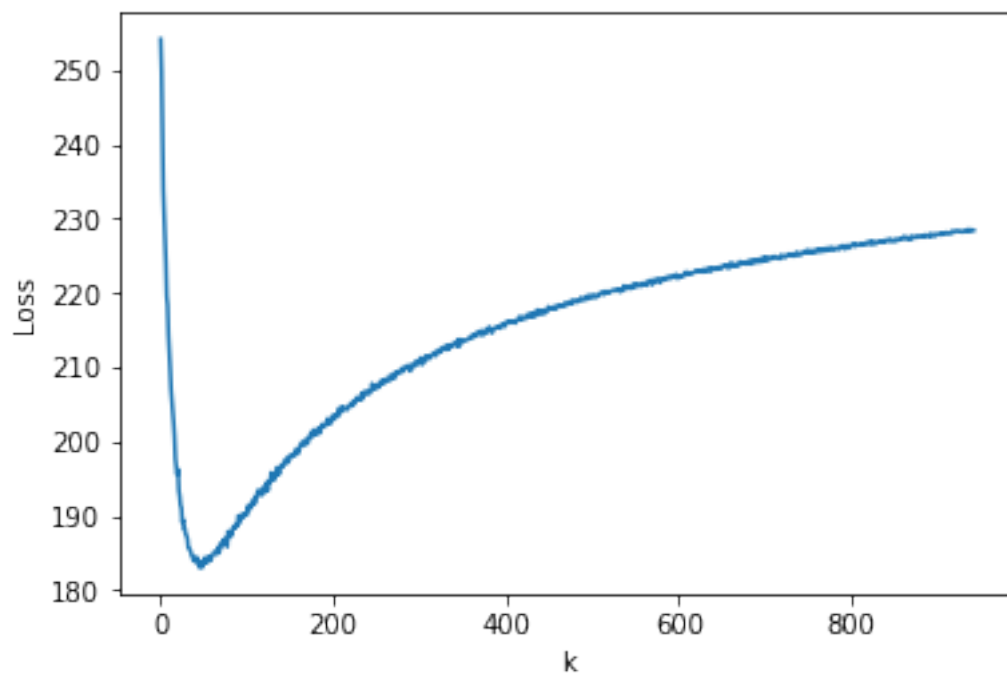
```

k: 1
k: 21
k: 41
k: 61
k: 81
k: 101
k: 121
k: 141
k: 161
k: 181
k: 201
k: 221
k: 241
k: 261
k: 281
k: 301
k: 321
k: 341
k: 361
k: 381
k: 401
k: 421
k: 441
k: 461
k: 481
k: 501
k: 521
k: 541
k: 561
k: 581
k: 601
k: 621

```

```
k: 641  
k: 661  
k: 681  
k: 701  
k: 721  
k: 741  
k: 761  
k: 781  
k: 801  
k: 821  
k: 841  
k: 861  
k: 881  
k: 901  
k: 921  
k: 941
```

```
In [148]: plt.plot(loss_temp)  
          plt.xlabel("k")  
          plt.ylabel("Loss")  
          plt.show()
```



```
In [155]: print('k: ', np.argmin(loss_temp)+1)
```

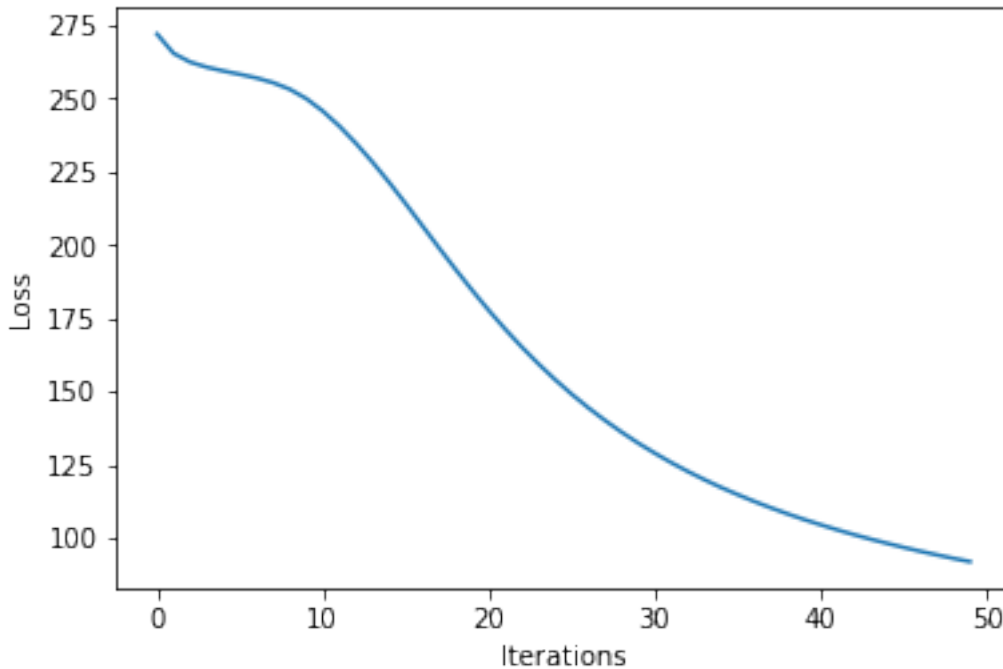
k: 46

```
In [150]: mf = MatrixFactor(X_base, k=np.argmin(loss_temp)+1, alpha=0.01, iterations=50)
          loss = mf.train()
```

```
[iteration, loss]: [25, 154.01673162936905]
```

```
[iteration, loss]: [50, 91.92494033373379]
```

```
In [151]: x = [x for x, y in loss]
          y = [y for x, y in loss]
          plt.plot(x, y)
          plt.xlabel("Iterations")
          plt.ylabel("Loss")
          plt.show()
```



```
In [152]: X_predict = mf.matrix()
          X_predict[X_test==0] = 0

          acc = np.linalg.norm(X_predict - X_test) / (num_user*num_item)
          print('prediction accuracy (MSE): ', acc)
```

```
prediction accuracy (MSE): 9.797028778546268e-05
```

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In [159]: # test set training on k=20
          mf = MatrixFactor(X_base, k=20, alpha=0.01, iterations=50)
          loss = mf.train()

[iteration, loss]: [25, 181.64863510653004]
[iteration, loss]: [50, 153.79777389429117]

In [160]: # test set training on k=50
          mf = MatrixFactor(X_base, k=50, alpha=0.01, iterations=50)
          loss = mf.train()

[iteration, loss]: [25, 151.78350894891759]
[iteration, loss]: [50, 86.70767413942713]

In [156]: # test set training on k=100
          mf = MatrixFactor(X_base, k=100, alpha=0.01, iterations=50)
          loss = mf.train()

[iteration, loss]: [25, 148.81299714853253]
[iteration, loss]: [50, 48.50950871832002]

In [157]: # test set training on k=200
          mf = MatrixFactor(X_base, k=200, alpha=0.01, iterations=50)
          loss = mf.train()

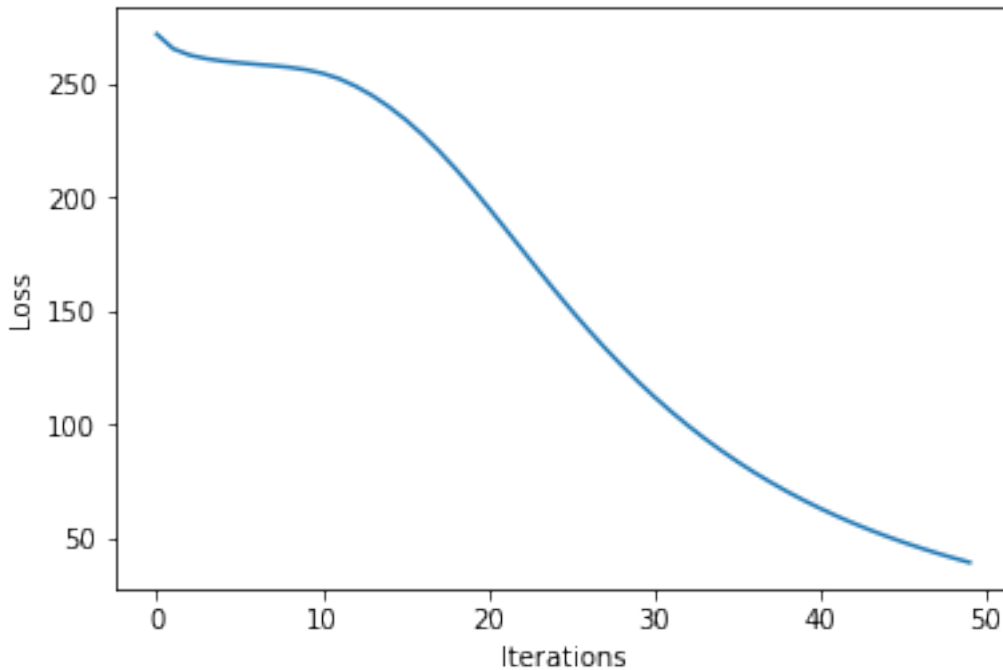
[iteration, loss]: [25, 158.0019377442411]
[iteration, loss]: [50, 39.337055889734536]

In [164]: # test set training on k=210
          mf = MatrixFactor(X_base, k=210, alpha=0.01, iterations=50)
          loss = mf.train()

[iteration, loss]: [25, 159.10459421501375]
[iteration, loss]: [50, 39.33493373929054]

In [165]: x = [x for x, y in loss]
          y = [y for x, y in loss]
          plt.plot(x, y)
          plt.xlabel("Iterations")
          plt.ylabel("Loss")
          plt.show()

```



```
In [166]: X_predict = mf.matrix()
          X_predict[X_test==0] = 0

          acc = np.linalg.norm(X_predict - X_test) / (num_user*num_item)
          print('prediction accuracy (MSE): ', acc)
```

prediction accuracy (MSE): 8.726503731261758e-05

```
In [163]: # test set training on k=220
          mf = MatrixFactor(X_base, k=220, alpha=0.01, iterations=50)
          loss = mf.train()
```

[iteration, loss]: [25, 159.9410897235963]

[iteration, loss]: [50, 39.37698362444992]

```
In [162]: # test set training on k=250
          mf = MatrixFactor(X_base, k=250, alpha=0.01, iterations=50)
          loss = mf.train()
```

[iteration, loss]: [25, 162.6205223341625]

[iteration, loss]: [50, 39.47122230960694]

```
In [161]: # test set training on k=300
mf = MatrixFactor(X_base, k=300, alpha=0.01, iterations=50)
loss = mf.train()
```

```
[iteration, loss]: [25, 166.0481260008579]
[iteration, loss]: [50, 39.908420985281055]
```

```
In [158]: # test set training on k=500
mf = MatrixFactor(X_base, k=500, alpha=0.01, iterations=50)
loss = mf.train()
```

```
[iteration, loss]: [25, 177.33400400866373]
[iteration, loss]: [50, 42.74075671531363]
```

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In [ ]:
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