

$$f = \frac{v_s}{\sqrt{v_s^2 + v_c^2}} + j \frac{v_c}{\sqrt{v_s^2 + v_c^2}}$$

$$\frac{df}{dv_s} = \frac{1}{\sqrt{v_s^2 + v_c^2}} + v_s \cdot \frac{d(v_s^2 + v_c^2)^{-1/2}}{dv_s} + j \frac{v_c d(v_s^2 + v_c^2)^{-1/2}}{dv_s}$$

$$= \frac{1}{\sqrt{v_s^2 + v_c^2}} - \frac{v_s}{2} \cdot \frac{2v_s}{(v_s^2 + v_c^2)^{3/2}} + j \left[-\frac{1}{2} \frac{2v_s \cdot v_c}{(v_s^2 + v_c^2)^{3/2}} \right]$$

$$= \frac{1}{\sqrt{v_s^2 + v_c^2}} \left(\frac{v_c^2}{v_s^2 + v_c^2} - j \frac{v_s v_c}{v_s^2 + v_c^2} \right)$$

$$\frac{df}{dv_c} = -\frac{v_s v_c}{(v_s^2 + v_c^2)^{3/2}} + j \left[\frac{1}{\sqrt{v_s^2 + v_c^2}} + v_c \cdot \left(-\frac{1}{2} \frac{2v_c}{(v_s^2 + v_c^2)^{3/2}} \right) \right]$$

$$= \frac{1}{\sqrt{v_s^2 + v_c^2}} \left[-\frac{v_s v_c}{v_s^2 + v_c^2} + j \frac{v_s^2}{v_s^2 + v_c^2} \right]$$

$$v_s = \frac{4V_g}{\pi} \frac{R_{eq}}{R_{eq}^2 + X_{eq}^2}$$

$$v_c = -\frac{4V_g}{\pi} \frac{X_{eq}}{R_{eq}^2 + X_{eq}^2}$$

$$\|Z_{s,1}\| = \sqrt{v_s^2 + v_c^2}$$

$$\Rightarrow k_{rs} = k_{rc} = \frac{R_{eq} \cdot v_s v_c}{v_s^2 + v_c^2} = \frac{X_{eq} R_{eq}^2}{R_{eq}^2 + X_{eq}^2}$$

$$\Rightarrow R_s = \frac{R_{eq} v_c^2}{v_s^2 + v_c^2} = \frac{R_{eq} \cdot X_{eq}^2}{R_{eq}^2 + X_{eq}^2}$$

$$\Rightarrow R_c = \frac{R_{eq} - v_s^2}{v_s^2 + v_c^2} = \frac{R_{eq} - R_{eq}^2}{R_{eq}^2 + X_{eq}^2}$$