# Welford’s online algorithm for computing variance

Sample mean:

|  |  |  |
| --- | --- | --- |
|  |  | () |

Treat variance as the population variance instead of sample variance,

|  |  |  |
| --- | --- | --- |
|  |  | () |

When a new item is added to the list, the sample mean could be written in recursive form,

|  |  |  |
| --- | --- | --- |
|  |  | () |
|  |  | () |

The alternative form of variance is,

|  |  |  |
| --- | --- | --- |
|  |  | () |

|  |  |  |
| --- | --- | --- |
|  |  | () |

|  |  |  |
| --- | --- | --- |
|  |  | () |

|  |  |  |
| --- | --- | --- |
|  |  | () |
|  |  | () |

|  |  |  |
| --- | --- | --- |
|  |  | () |

In recursive format,

|  |  |  |
| --- | --- | --- |
|  |  | () |

From formula 4,

|  |  |  |
| --- | --- | --- |
|  |  | () |

From formula 3,

|  |  |  |
| --- | --- | --- |
|  |  | () |

We have,

|  |  |  |
| --- | --- | --- |
|  |  | () |

The formula (11) and (13) are equivalent and can use either.

# Power Sum Average Based method

Power sum average,

|  |  |  |
| --- | --- | --- |
|  |  | () |

Mean,

|  |  |  |
| --- | --- | --- |
|  |  | () |

|  |  |  |
| --- | --- | --- |
|  |  | () |

Consider this as the sample system, the unbiased variance should be corrected using factor , refer to [[[1]](#endnote-1)], obtained,

|  |  |  |
| --- | --- | --- |
|  |  | () |

1. [] https://en.wikipedia.org/wiki/Variance#Sample\_variance [↑](#endnote-ref-1)