



這種做法的近似
在這個步驟產生

$$\text{at } P, \phi_+ = \frac{1}{4\pi\epsilon_0} \frac{q}{r} + \underbrace{\nabla\left(\frac{q}{4\pi\epsilon_0 r}\right) \cdot \left(-\hat{a}_z \frac{d}{2}\right)}$$

$$\phi_- = \frac{1}{4\pi\epsilon_0} \frac{-q}{r} + \underbrace{\nabla\left(\frac{-q}{4\pi\epsilon_0 r}\right) \cdot \left(\hat{a}_z \frac{d}{2}\right)}$$

$$\phi(P) = \phi_+ + \phi_-$$

$$= -\nabla\left(\frac{q}{4\pi\epsilon_0 r}\right) \cdot \left(\hat{a}_z \frac{d}{d}\right)$$

$$= \frac{-q}{4\pi\epsilon_0} \nabla\left(\frac{1}{r}\right) \cdot (\hat{a}_z d)$$

$$= \frac{-q}{4\pi\epsilon_0} \times \frac{-\hat{a}_r}{r^2} \cdot \hat{a}_z d$$

$$= \frac{q d \hat{a}_z \cdot \hat{a}_r}{4\pi\epsilon_0 r^2} = \frac{\vec{P} \cdot \hat{a}_r}{4\pi\epsilon_0 r^2} \quad \text{also or} \quad \frac{q d \cos\theta}{4\pi\epsilon_0 r^2}$$