

# Graph Attention Networks

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## 研究目的

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- 解決傳統方式 (spectral-based method) 在做 graph convolution 的問題
  - 利用 self-attention layers
  - 利用 stacking layers 來取得 node 的 neighborhoods features，此外，也不需要 costly matrix operation 以及 graph structure
- Node classification of graph-structured data via attention mechanism

## 研究方式

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- Previous literatures:
  - Recursive NN: (2 (<https://pdfs.semanticscholar.org/3edf/d97cf8657e02d2c796db9aa412ceb077b0eb.pdf>))
  - Graph NN (GNN): (3 ([https://www.researchgate.net/profile/Franco\\_Scarselli/publication/4202380\\_A\\_new\\_model\\_for\\_earning\\_in\\_graph\\_domains/links/0c9605188cd580504f000000/A-new-model-for-earning-in-graph-domains.pdf](https://www.researchgate.net/profile/Franco_Scarselli/publication/4202380_A_new_model_for_earning_in_graph_domains/links/0c9605188cd580504f000000/A-new-model-for-earning-in-graph-domains.pdf))) (4 (<https://persagen.com/files/misc/scarselli2009graph.pdf>))
  - Spectral based: requires graph structure data
  - Graph Convolution Network (GCN): (5 (<https://arxiv.org/abs/1509.09292>)) (MoNET (<https://arxiv.org/abs/1611.08402>))(GraphSAGE (<https://arxiv.org/abs/1706.02216>)) works with different sized neighborhoods and maintains the weight sharing property of CNNs., sampling a fixed-size neighborhood of each node, then aggregate through them
  - Attention based

- 資料結構: 一連串的 node，且每個 node ( $h_i$ ) 有  $F$  個 features，要輸出有另一組  $F'$  features 的 vector  $\mathbf{h} = \{h_1, h_2, \dots, h_N\}$
- Traditional attention mechanism** Construct weight matrix, then perform self-attention (將注意力分配到圖中其他節點)

$$e_{ij} = a(\vec{\mathbf{W}}h_i, \vec{\mathbf{W}}h_j)$$

where  $\mathbf{W} \in \mathbb{R}^{F' \times F}$  and  $a$  is a shared attentional mechanism  $a = \mathbb{R}^{F'} * \mathbb{R}^{F'} \rightarrow \mathbb{R}$

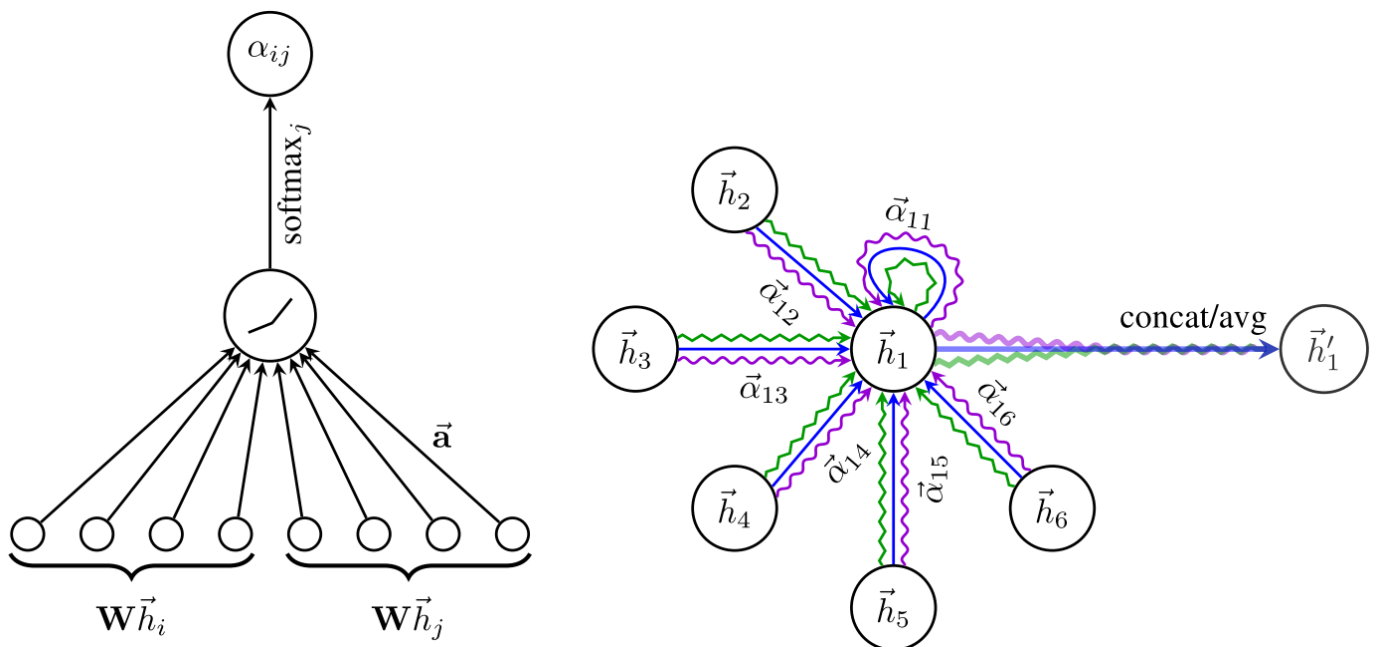
$$a_{ij} = \text{softmax}_j(e_{ij}) = \frac{\exp(e_{ij})}{\sum_{k \in N_i} \exp(e_{ik})}$$

- $e_{ij}$  代表 node  $j$  對 node  $i$  的重要程度
- $N_i$  是 node  $i$  的 neighbors 而  $j \in N_i$
- 本文中只用了 first-order neighbors of  $i$  (including  $i$ )

- Attention mechanism in this paper, GAT**

$$a_{ij} = \frac{\exp(\text{LeakyReLU}(\vec{a}^T [\vec{\mathbf{W}}h_i || \vec{\mathbf{W}}h_j]))}{\sum_{k \in N_i} \exp(\text{LeakyReLU}(\vec{a}^T [\vec{\mathbf{W}}h_i || \vec{\mathbf{W}}h_k]))}$$

where LeakyReLU use a negative input slope of  $\alpha = 0.2$



左圖是 attention mechnism 的示意圖，右圖為 multi-head attention 的示意圖

- Single-head attention: 最後根據 attention 的結果計算 linear combination of the featrues corresponding to them -> 每個 node 的 output features

$$\vec{h}'_i = \sigma(\sum_{j \in N_i} \alpha_{ij} \vec{\mathbf{W}}h_j)$$

- (Extended) Multi-head attention - concatenation

$$\vec{h}'_i = ||_{k=1}^K \sigma(\sum_{j \in N_i} \alpha_{ij} \mathbf{W} \vec{h}_j)$$

- (Extended) Multi-head attention - averaging

$$\vec{h}'_i = \sigma(\frac{1}{K} \sum_{k=1}^K \sum_{j \in N_i} \alpha_{ij}^k \mathbf{W}^k \vec{h}_j)$$

- Time complexity of a single GAT:  $O(|V|FF' + |E|F')$  where  $F$  is the number of input features, and  $|V|$  and  $|E|$  are the numbers of nodes and edges in the graph; multiply by  $K$  for  $K$ -head model
- 有另外實作針對 sparse matrix 的版本

## 評估方法

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- Transductive learning: 訓練中只知 testing data (unlabelled data), 調整 training node 的數量，衡量不同情境下的準確度
- Inductive learning: 訓練中不知道 testing data, 訓練好模型後去解決未知的 testing data

## 研究貢獻

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- Attention 機制是共享的，是一種局部模型