

So we are trying to sample from:

$$p(y_t | M, x; \hat{\theta}) \approx \frac{1}{M} \sum_m p_m(y_t | y_g^m)$$

↗ group

$$p(y_t | y_g^m) = \frac{p(y_t, y_g^m)}{p(y_g^m)}$$

$$= \frac{1}{Z_1(\alpha, \beta)} e^{-\alpha \sum_s \delta(y_{t,s} \neq y_g^m) - \beta \sum_{(r,s)} \delta(y_{t,r} \neq y_{t,s})}$$

$$\frac{1}{Z_2(\beta)} e^{-\beta \sum_{(r,s)} \delta(y_{g,r}^m \neq y_{g,s}^m)}$$

$$= \frac{Z_2}{Z_1} e^{-u}$$

u is the sum over all pairwise voxels in y_g , and we need to compute u for M times in order to evaluate y_t . There is no way to cancel u when sampling one voxel of y_t

for voxel s ,

$$p(y_{t,s} | y_{t,-s}, y_g) = \frac{1}{M} \sum_m p(y_{t,s} | y_{t,-s}, y_g^m)$$

Although the Z_2/Z_1 term is same for all m y_g samples and can be cancelled to compute the conditional probability at voxel s , the blue color u is a sum over all pairwise voxels in y_g , and is different for each sample of y_g . So, to sample one voxel of y_t , we need to compute u , thus having to go over all pair of voxels of y_g