

2. (a) $\therefore 96\%$ confidence interval

$$\therefore \alpha = 1 - 0.96 = 0.04$$

$$1 - \frac{\alpha}{2} = 0.98$$

$$\therefore Z_{\frac{\alpha}{2}} = 2.05$$

$$\therefore E = Z_{\frac{\alpha}{2}} \cdot \frac{S}{\sqrt{N}} \quad \therefore 0.4 = 2.05 \cdot \frac{S}{\sqrt{40}}$$

$$S = 1.234$$

$$\therefore S \text{ should be } 1.234$$

(b) ~~$\therefore \alpha = 0.99$~~

$\therefore 99\%$ confidence interval

$$\therefore \alpha = 1 - 0.99$$

$$\therefore Z_{\frac{\alpha}{2}} = Z_{0.005} = 2.575$$

$$\therefore E = 2.575 \cdot \frac{1.234}{\sqrt{40}} \approx 0.502$$

$$\therefore 99\% \text{ confidence Interval is } [3 - 0.502, 3 + 0.502]$$

(c) $\therefore 96\%$ confidence interval

$$E = 0.1, \quad Z_{\frac{\alpha}{2}} = 2.053, \quad S = 1.234$$

\therefore

$$0.1 = 2.053 \cdot \frac{1.234}{\sqrt{N}}$$

$$N \rightarrow 641.8 \approx 642$$

$$N = 637.65 \approx 638$$

So we still need to make 598 more samples.