Systems of Differential Equations: A First Look

Department of Mathematics

Salt Lake Community College

(Slides by Adam Wilson)

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Analytic Definition of a Solution of a DE System

A **solution** of a system of two differential equations is a pair of functions $x(t)$ and $y(t)$ that simultaneously satisfies both equations.