

# Systems of Differential Equations: A First Look

Colby Community College

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## Analytic Definition of a Solution of a DE System

A **solution** of a system of two differential equations is a pair of functions  $x(t)$  and  $y(t)$  that simultaneously satisfies both equations.