Confidence Intervals for a Proportion

Colby Community College

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Note

We have no indication of how *good* of an estimate 0.43 is, just that it is the best of the available options.

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Round the confidence interval limits to three significant digits.

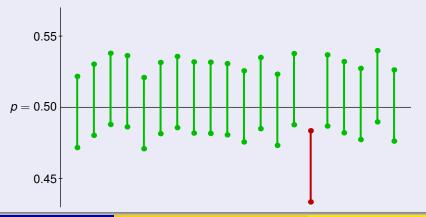
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If the true population proportion is p = 0.5, then we expect around 19 of 20 confidence intervals to contain the true value of p.



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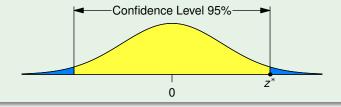


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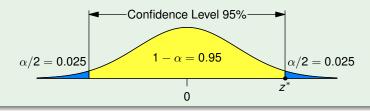
Definition

The value z^* is called a **critical value**.

Let us find the critical value corresponding to a 95% confidence level.



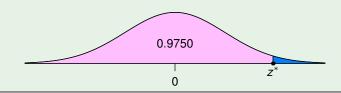
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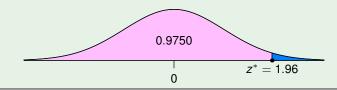
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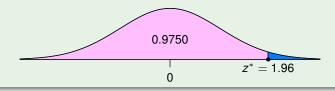
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Common Confidence Levels

Confidence Level	α	Critical Value
90%	0.10	1.645
95%	0.05	1.960
99%	0.01	2.575

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The margin of error for \hat{p} is:

$$z^* \cdot SE_{\hat{p}} = z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

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Round the confidence interval limits to four digits.

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(5) We are 90% confident that between 87.1% and 90.4% of American adults supported the expansion of solar power in 2018.

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Incorrect: "90% of sample proportions will fall between 0.8705 and 0.9035."

Reason: The values 0.8705 and 0.9035 result from one sample, they are not parameters describing the behavior of all samples.

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Caution

Never think that poll results are unreliable if the sample size if a small percentage of the population size.

Finding \hat{p} from a Confidence Interval

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If you know the confidence interval, (upper limit, lower limit), we can calculate the margin of error:

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Rounding

If the computed sample size n is not a whole number, round the value of n up to the next larger whole number.

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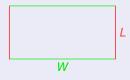
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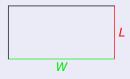


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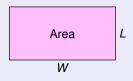


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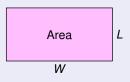
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Since this is a parabola that opens down, we know that the vertex, (0.5, 0.5), is the maximum value.

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- 3 Be sure to *round up to the next highest integer*, do not round using the usual rounding rules.