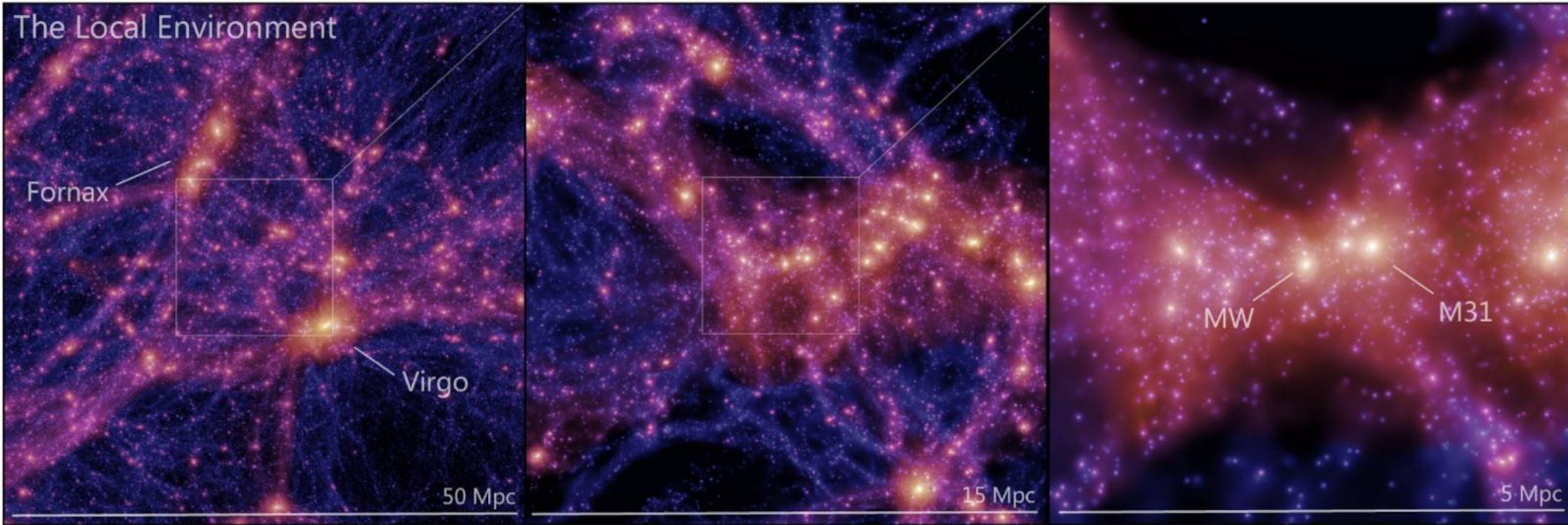


KN8005 Computer Lab #1

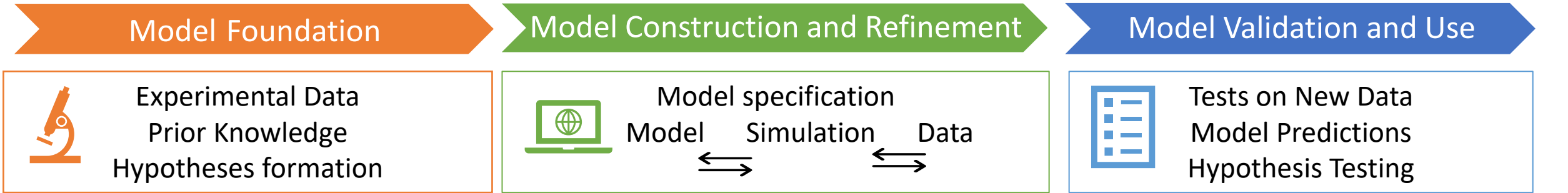
VT 2024

Computational Modelling of Neurons





McAlpine et al., 2022



A Simpler Model



vs



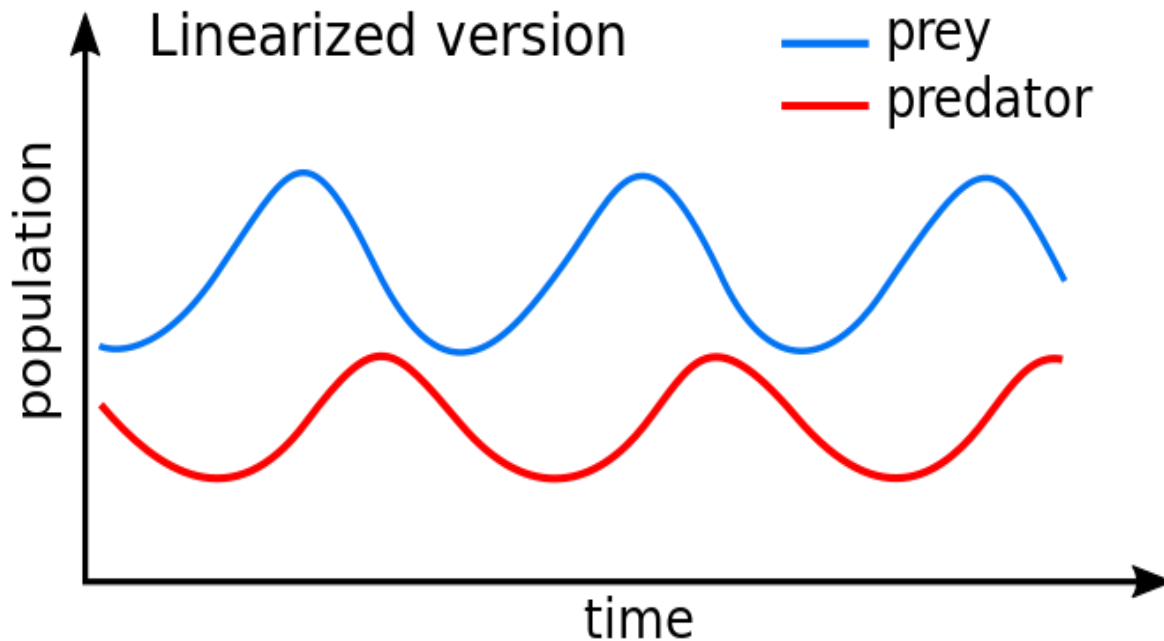
The Lotka-Volterra Equations (And Assumptions)

$$\frac{dP}{dt} = -Pm + bHP$$

$$\frac{dH}{dt} = Hr - aHP$$

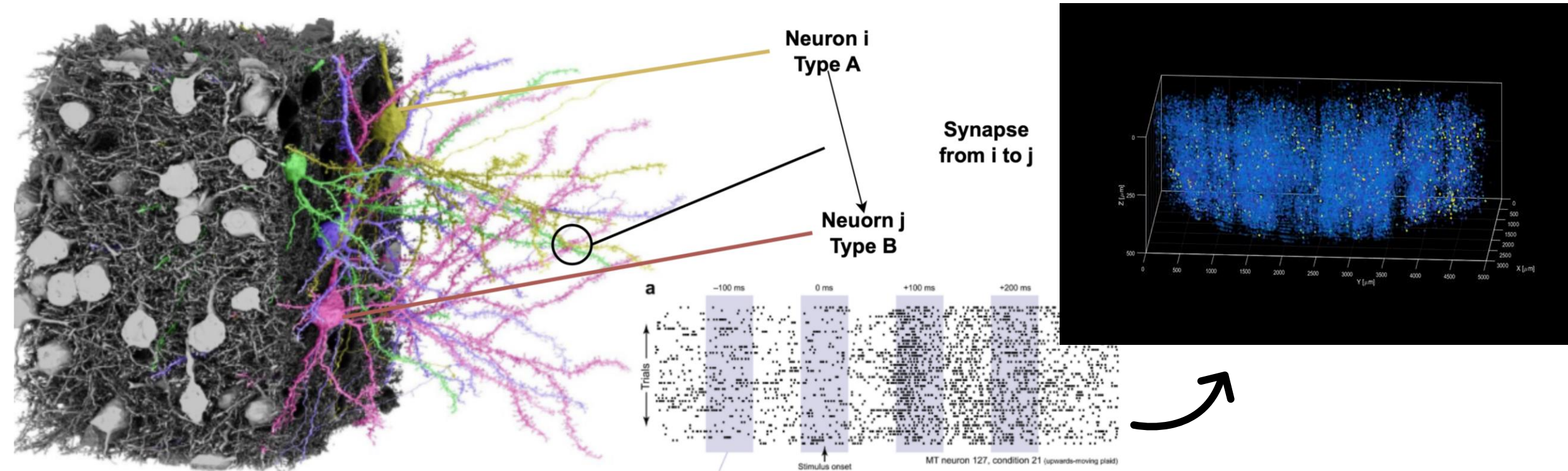
$$\begin{cases} P = P(t) & \text{Number of Predators} \\ H = H(t) & \text{Number of Prey} \end{cases}$$

$$\begin{cases} r > 0 & \text{Birth Rate of Prey} \\ m > 0 & \text{Death Rate of Predators} \\ a > 0 & \text{Death Rate of Prey/Predator} \\ b > 0 & \text{Birth Rate of Predators/Prey} \end{cases}$$



The Lotka-Volterra Model

Modelling Neuronal Activity



$250 \times 140 \times 90 \mu\text{m}$, layer 2/3, mouse visual cortex [Dorkenwald et al. 2019]

Designing Our Model

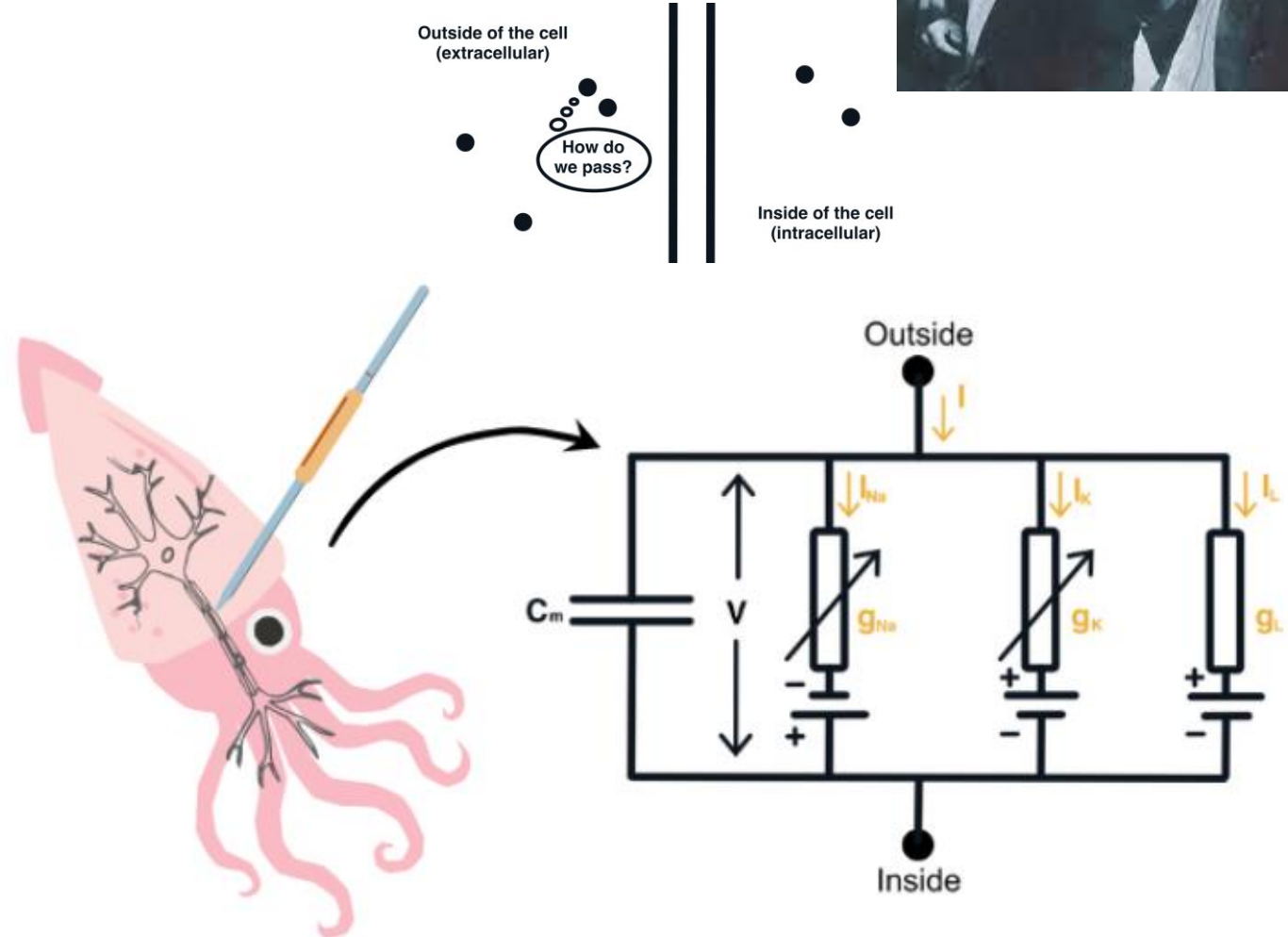
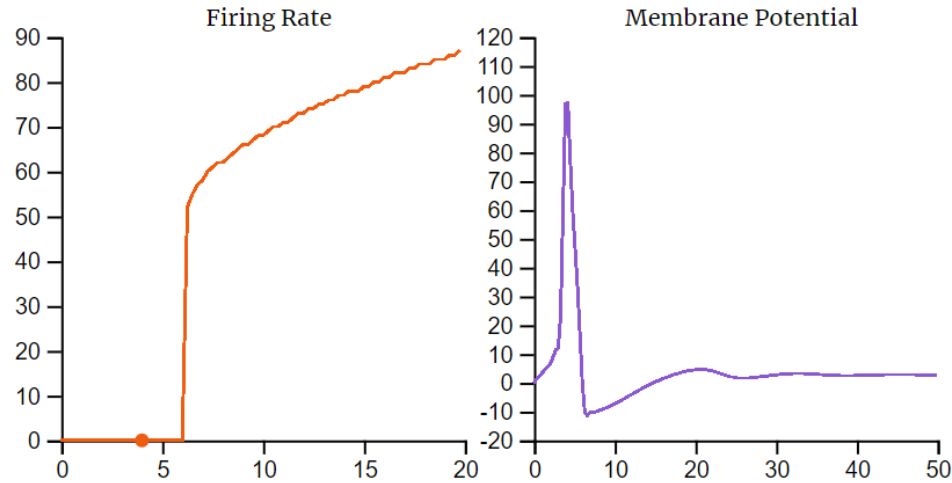
Identity (*What does the neuron look like?*)

Connectivity (*What type of synapses does the neuron have?*)

Activity (*What type of input does the neuron receive?*)

Modelling Neuronal Identity

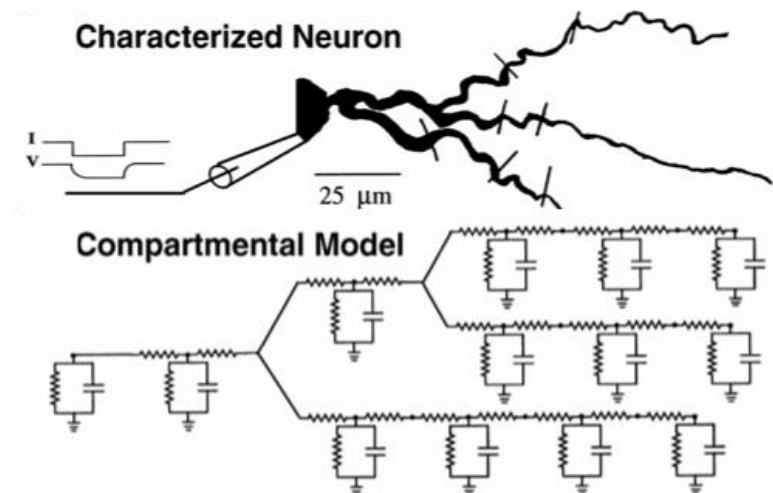
The Hodgkin-Huxley Model



Modelling Neuronal Identity

Compartmental Models and LIFs

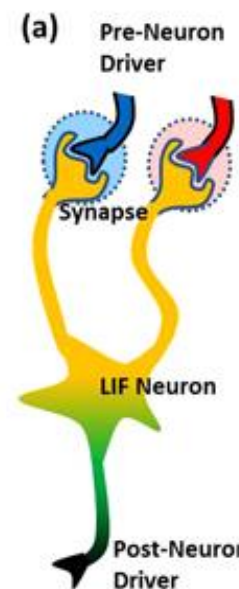
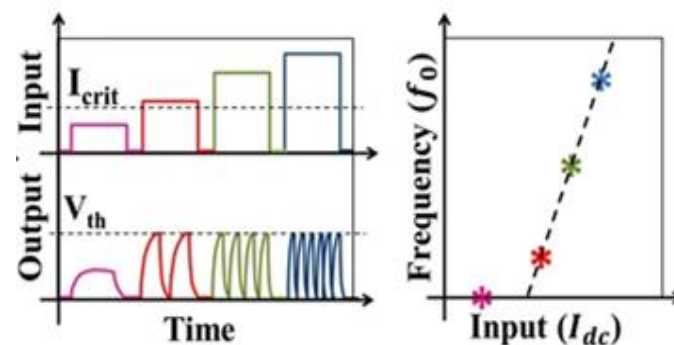
Compartmental models simulate parts of the neuron with separate properties, usually based on experimental observations



Point Neuron Models

Leaky Integrate and Fire (LIF) Neurons

- Spatiotemporal integration of synaptic inputs that will produce a spike at a certain threshold
- The 'leakiness' creates spontaneous change in potential (as in H-H)
- Only two states:
 - Subthreshold
 - Spike and reset



Step 1. Input Driver for V-spikes

$$V_j(t) = \sum_i \delta(t - t_i)$$

Step 2. Synaptic current response $I_j(t, t_i)$

$$= w_j \left(e^{-\frac{t-t_i}{\tau}} - e^{-\frac{t-t_i}{4\tau}} \right) \quad \text{if } t > t_i$$
$$= 0 \quad \text{if } t \leq t_i$$

Step 3. Network sums synaptic current

$$I(t) = \sum_j I_j(t)$$

Step 4. Output spike of LIF neuron

$$V_o(t) = LIF\{I(t)\}$$

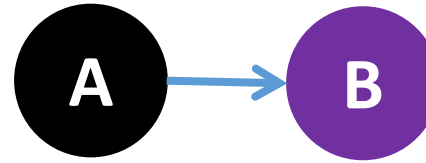
Step 5. Output Driver neuron issue spike

$$V_3(t) = LIF\{I(t)\}$$

Modelling Neuronal Connections

Types of Synapses

1. Static



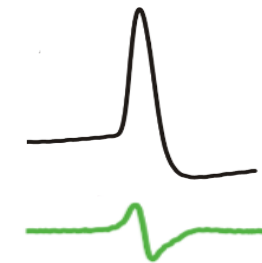
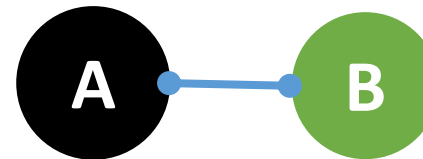
2. Facilitating or Depressing

- Synapse strength changes with consecutive spikes



3. Electrical Synapses

- Neurons are coupled with gap junctions

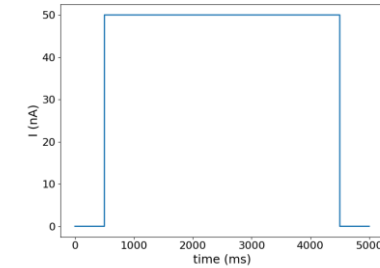


Modelling Neuronal Connections

Types of Input

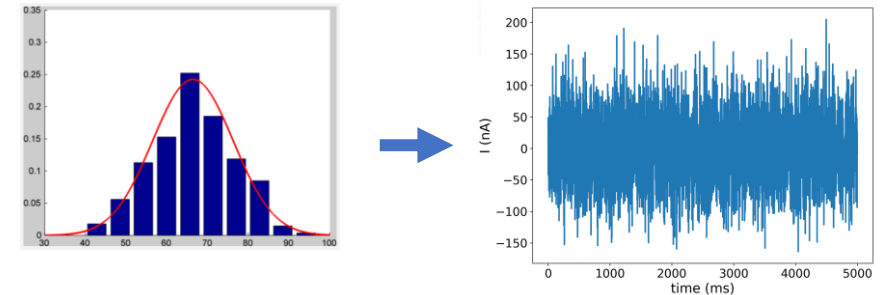
1. Current Injection

- Current of fixed amplitude is applied



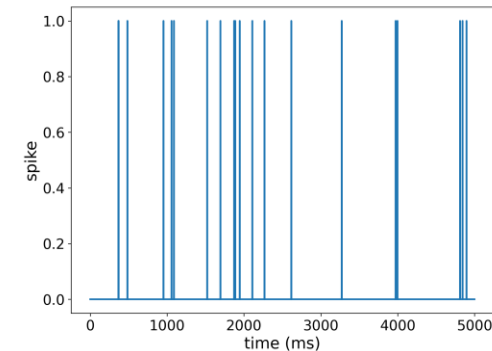
2. Gaussian

- Variable current. Captures the **randomness** of brain activity by introducing **noise** to the input



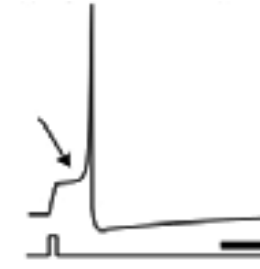
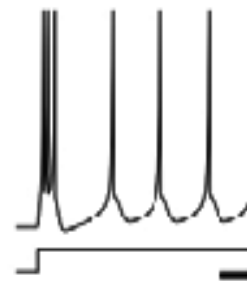
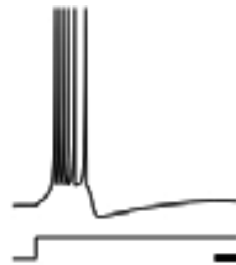
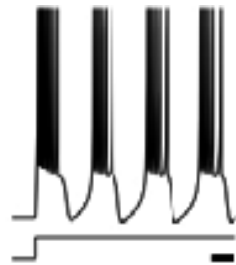
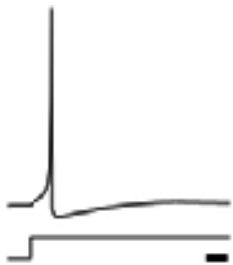
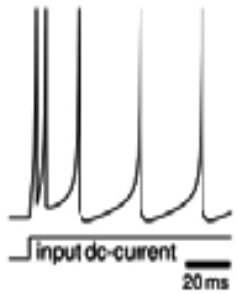
3. Poisson Process

- Events (spikes, arrivals, etc.) occur randomly and independently.
- The time between consecutive events follows an **exponential distribution**.

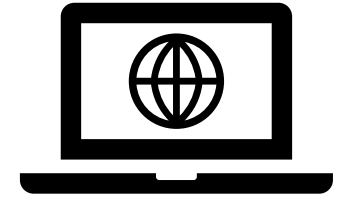


Your Task

To Model Different Firing Patterns using LIF model



Google colab



Neuronal Circuits > Resources> Labs> Simulation Labs> link to lab 1 in the manual