$$Out[\bullet] = -\frac{2(-2+n)}{pop}$$

Out[•]= 
$$\left\{\left\{n[t] \rightarrow \frac{1}{2} (4 + pop r) + e^{-\frac{2t}{pop}} c_1\right\}\right\}$$

$$In[*] := Solve \begin{bmatrix} \frac{1}{2} & (4 + pop r) + e^{-\frac{2t}{pop}} & const == 2, const \end{bmatrix}$$

$$Out[*] = \left\{ \left\{ const \rightarrow -\frac{1}{2} e^{\frac{2t}{pop}} pop r \right\} \right\}$$

$$ln[*]:=$$
 Simplify DSolve  $\left[-\begin{pmatrix} 1\\-\begin{pmatrix} 1\\-\begin{pmatrix} 4+\text{pop r}\end{pmatrix} - \frac{1}{-}&\text{pop r }e^{-\frac{2t}{\text{pop}}} - 1\end{pmatrix}\right]$   $pop*f[t] == f'[t], f[t], t$ 

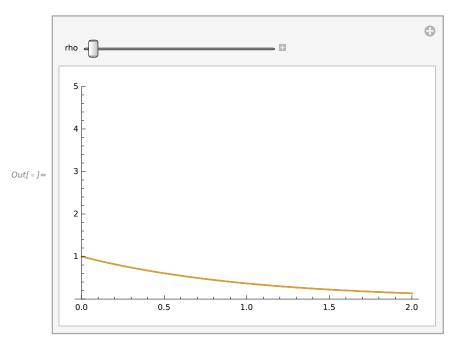
$$\textit{Out[*]} = \left\{ \left\{ f[t] \rightarrow e^{-\frac{1}{4}e^{\frac{-2t}{pop}}} pop \ r^{-\frac{t}{pop}} - \frac{rt}{2} \ c_1 \right\} \right\}$$

$$ln[*]:= \mathbf{e}^{-\frac{1}{4}} \mathbf{e}^{-2 \tan r} \operatorname{ho-tau} - \frac{\operatorname{rho+au}}{2} \mathbf{c}_1 /. \{ \tan \rightarrow 0 \}$$

Out[
$$\circ$$
]=  $e^{-\text{rho}/4}$   $\mathbb{C}_1$ 

$$Out[\, \circ \,] = \frac{1}{e^{4}} \left( \text{rho-}e^{-2 \, \text{tau}} \, \text{rho-} 12 \, \text{tau-} 2 \, \text{rho tau} \right) \left( - \, \text{rho} + e^{2 \, \text{tau}} \, \left( 2 + \, \text{rho} \right) \right)$$

-Exp[-tau-rho/2\*tau²](-1-rho tau)
$$\}$$
, {tau, 0, 2}, PlotRange → {0, 5}], {rho, 0, 50}]   
 [指數形式



## Define the function that convert numbers to the format in file names

```
In[*]:= number2Printed[number_] := Module[{returnedString = "e", foo, bar, idx, oom},
       If[number == 1, Return["1.0e+00"], If[number == 0, Return["0.0e+00"],
                                         如果
          If[number < 1,</pre>
         如果
            For[idx = 1, StringLength[returnedString] == 1, idx = idx + 1,
                        字串長度
              foo = Floor[number / 10^{-idx}];
                   弱取整
             If[foo == 0, ,
               bar = Round[(number - foo * 10^(-idx)) / 10^(-idx - 1)];
              If[StringLength[ToString[idx]] == 1,
              上… | 字串長度
                               轉換成字串
                returnedString = StringJoin[ToString[foo],
                                 字串結合
                                            轉換成字串
```

```
□1.4.1∨\\ 1 ⊥
      ".", ToString[bar], returnedString, "-0", ToString[idx]],
    returnedString = StringJoin[ToString[foo], ".", ToString[bar],
                    字串結合 轉換成字串
                                                 轉換成字串
      returnedString, "-", ToString[idx]]
                          轉換成字串
 Return[returnedString]
 oom = (StringLength[ToString[DecimalForm[Floor[number] * 1.]]] - 2);
                   轉換成字串【十進位形式 【弱取整
 foo = Floor[number / 10 ^ oom];
      弱取整
 bar = Round[(number - foo *10^{\circ} oom) / 10^{\circ} (oom - 1)];
 If[StringLength[ToString[oom]] == 1,
| … | 字串長度
               轉換成字串
  returnedString = StringJoin[ToString[foo],
                 字串結合 轉換成字串
    ".", ToString[bar], returnedString, "+0", ToString[oom]],
        轉換成字串
                                            轉換成字串
  returnedString = StringJoin[ToString[foo], ".", ToString[bar],
                  字串結合
                          轉換成字串
    returnedString, "+", ToString[oom]]
                        轉換成字串
];
 Return[returnedString]
];
```

Import parameters and data

```
ln[*]:= (* combinedParameters= Interpreter[DelimitedSequence["Number",{"[",", ","]"}]]]
                              解譯器
                                          分隔序列
        Import[StringJoin[NotebookDirectory[],"combined_parameters.txt"]]];
                          筆記本目錄
              字串結合
     sequenceLengths= Interpreter[DelimitedSequence["Number",{"[",", ","]"}]][
                                    分隔序列
       Import[StringJoin[NotebookDirectory[], "sequence_lengths.txt"]]];
                          筆記本目錄
     populationSizes= Interpreter[DelimitedSequence["Number",{"[",", ","]"}]]
                                    分隔序列
       Import[StringJoin[NotebookDirectory[],"population_sizes.txt"]]]; *)
              上字串結合
                          筆記本目錄
     combinedParameters = ToExpression[StringReplace[Import[
                           轉換成表示式
                                         字串替代
           StringJoin[NotebookDirectory[], "combined_parameters.txt"]], \{"[" \rightarrow "\{", "]" \rightarrow "\}"\}]];
           字串結合
                      筆記本目錄
     sequenceLengths = ToExpression[StringReplace[Import[
                        轉換成表示式
           StringJoin[NotebookDirectory[], "sequence\_lengths.txt"]], \{"[" \rightarrow "\{", "]" \rightarrow "\}"\}]];
                      上筆記本目錄
     populationSizes = ToExpression[StringReplace[Import[
                         轉換成表示式
                                      字串替代
           StringJoin[NotebookDirectory[], "population_sizes.txt"]], \{"[" \rightarrow "\{", "]" \rightarrow "\}"\}];
                       筆記本目錄
In[*]:= histograms = Table[Table[Table[Transpose[
                  表格 表格 表格 轉置
            ToExpression[StringReplace[Import[StringJoin[NotebookDirectory[], number2Printed]
                                              字串結合
                  combinedParameters[[idx1]]], "_", number2Printed[sequenceLengths[[idx2]]], "_",
                 number2Printed[populationSizes[[idx3]]], ".txt"]], \{"[" \rightarrow "\{", "]" \rightarrow "\}"\}]]
           ], {idx3, Length[populationSizes]}], {idx2, Length[sequenceLengths]}],
         {idx1, Length[combinedParameters]}];
               長度
  Fit scaling factors
In[*]:= predictionFree[tau_, gamma_, beta_, alpha_, combinedParameter_] :=
      (3 gamma * tau ^ 2 + beta * combinedParameter * tau + alpha) *
       Exp[-gamma * tau^3 - beta * combinedParameter * tau^2 / 2 - alpha * tau]
       指數形式
```

```
In[*]:= gammas = Table[0, {idx, Length[combinedParameters]]];
     betas = Table[0, {idx, Length[combinedParameters]}];
     alphas = Table[0, {idx, Length[combinedParameters]}];
     Module[{fit = Table[0, {idx0, Length[combinedParameters]}]}, Do[
        fit[[idx0]] = NonlinearModelFit[
                     非線性模型擬合
           Flatten[Table[Table[histograms[[idx0, idx1, idx2]], {idx2, Length[populationSizes]}],
             {idx1, Length[sequenceLengths]}], 2],
           predictionFree[tau, gamma, beta, alpha, combinedParameters[[idx0]]],
           {gamma, beta, alpha}, tau];
        gammas[[idx0]] = fit[[idx0]]["ParameterTable"][[1, 1, 2, 2]];
        betas[[idx0]] = fit[[idx0]]["ParameterTable"][[1, 1, 3, 2]];
        alphas[[idx0]] = fit[[idx0]]["ParameterTable"][[1, 1, 4, 2]],
        {idx0, Length[combinedParameters]}]]
               長度
      ... General: Exp[-6525.05] is too small to represent as a normalized machine number; precision may be lost.
      ... General: Exp[-6525.05] is too small to represent as a normalized machine number; precision may be lost.
      General: Exp[-6525.05] is too small to represent as a normalized machine number; precision may be lost.
      General: Further output of General::munfl will be suppressed during this calculation.
In[ • ]:= newPredictionFree[tau_, a_, b_, rho_] :=
                         \left(a+b-rho+\boldsymbol{e}^{-a + au} \left(-2 a-b+rho\right)\right)
```

```
In[*]:= zetas = Table[0, {idx, Length[combinedParameters]}];
     xis = Table[0, {idx, Length[combinedParameters]}];
| 表格 | 長度
     Module[{fit = Table[0, {idx0, Length[combinedParameters]}]}, Do[
        fit[[idx0]] = NonlinearModelFit[
                     非線性模型擬合
           Flatten[Table[Table[histograms[[idx0, idx1, idx2]], {idx2, Length[populationSizes]}],
                   表格表格
             {idx1, Length[sequenceLengths]}], 2],
           newPredictionFree[tau, zeta, xi, combinedParameters[[idx0]]], {zeta, xi}, tau];
        zetas[[idx0]] = fit[[idx0]]["ParameterTable"][[1, 1, 2, 2]];
        xis[[idx0]] = fit[[idx0]]["ParameterTable"][[1, 1, 3, 2]],
        {idx0, Length[combinedParameters]}]]
      ••• General: Exp[-1107.4] is too small to represent as a normalized machine number; precision may be lost.
      General: Exp[-976.056] is too small to represent as a normalized machine number; precision may be lost.
      — General: Exp[−1107.4] is too small to represent as a normalized machine number; precision may be lost.
      General: Further output of General::munfl will be suppressed during this calculation.
```

## Confirm two expressions are same

$$In[\circ] := \mathbf{Simplify} \Big[ \mathbf{newPredictionFree} \Big[ \mathbf{tau}, \, 2, \, -4, \, \mathbf{rho} \Big] \Big]$$

$$\mathbb{E} \Big[ \mathbf{Simplify} \Big[ \frac{1}{-} e^{\frac{1}{4}} \big( \mathbf{rho} - e^{-2 \, \mathsf{tau}} \, \mathbf{rho} - 12 \, \mathsf{tau} - 2 \, \mathsf{rho} \, \mathsf{tau} \big) \, \Big( - \, \mathsf{rho} + e^{2 \, \mathsf{tau}} \, (2 + \, \mathsf{rho}) \Big) \Big]$$

$$\mathbb{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big[ \mathbf{E} \Big] \mathbf{E} \Big[ \mathbf{E} \Big[$$

```
In[ • ]:= With[{idx0 = 6}, Show[
       同一起
          ListPlot[
          點集圖
            Flatten[Table[Table[histograms[[idx0, idx1, idx2]], {idx2, Length[populationSizes]}],
                      表格 表格
               {idx1, Length[sequenceLengths]}], 1],
            ImageSize → Full, PlotRange → All],
                          全範圍|繪製範圍
          Plot[newPredictionFree[tau, 2, -4, combinedParameters[[idx0]]],
            \label{eq:continuous_section} \begin{split} &\{\mathsf{tau},\, \mathsf{0},\, \mathsf{Transpose}[\mathsf{Max}[\mathsf{histograms}[[\mathsf{idx0},\, \mathsf{1},\, \mathsf{1}]]]][[\mathsf{1}]] \star \mathsf{3} \, / \, \mathsf{2}\}, \end{split}
                                    最大値
            PlotRange → Full, PlotStyle → Thick, AxesLabel → {"\tau(N×gen)", "P(\tau)(1/N/gen)"},
                          全範圍 繪製樣式
                                                    厚
                                                             座標軸標籤
                                                                                  數値化
                                                                                                       數值化
            PlotLegends → Placed[{"old", "bad", "new fit", "new"}, Below]]]]
       1.0
Out[ • ]=
       0.5
                         0.5
                                                                          2.0
                                                                                          2.5
                                                                                                           3.0
                                                                                                                           3.5
                                                                    old
```

```
In[ \circ ] := With[\{idx0 = 6\}, Show[
     同一起
        ListPlot[
        點集圖
         Flatten[Table[Table[histograms[[idx0, idx1, idx2]], {idx2, Length[populationSizes]}],
         壓平 表格 表格
           {idx1, Length[sequenceLengths]}], 1],
         ImageSize → Full, PlotRange → All],
                   全範圍圍製範圍
        Plot[{newPredictionFree[tau, 2, -4, combinedParameters[[idx0]]],
          newPredictionFree[tau, 2.5, -5, combinedParameters[[idx0]]]},
         {tau, 0, Transpose[Max[histograms[[idx0, 1, 1]]]][[1]] * 3/2},
         PlotRange → Full, PlotStyle → Thick, AxesLabel → {"\tau(N×gen)", "P(\tau)(1/N/gen)"},
         繪製範圍 全範圍 繪製樣式
                                       厚
                                             座標軸標籤
                                                              數値化
         PlotLegends → Placed[{"old", "bad", "new fit", "new"}, Below]]]]
         繪製圖例
     1.0
Out[ • ]=
     0.5
                               1.0
                                                                    2.5
                                                                                3.0
                                                                                            3.5
                                           — old — bad
```

```
In[\bullet]:= {With[{idx0 = 12}, Show[
         ListPlot[
        點集圖
          Flatten[Table[Table[histograms[[idx0, idx1, idx2]], {idx2, Length[populationSizes]}],
                 表格 表格
            {idx1, Length[sequenceLengths]}], 1],
          ImageSize → Large, PlotRange → All],
                    大
         影像尺寸
                             繪製範圍
         Plot[{predictionFree[tau, gammas[[idx0]],
            betas[[idx0]], alphas[[idx0]], combinedParameters[[idx0]]],
           predictionFree[tau, 0, 1, 1, combinedParameters[[idx0]]],
           newPredictionFree[tau, zetas[[idx0]], xis[[idx0]], combinedParameters[[idx0]]],
           newPredictionFree[tau, 2, -4, combinedParameters[[idx0]]]},
          {tau, 0, Transpose[Max[histograms[[idx0, 1, 1]]]][[1]] * 3 / 2},
          PlotRange → Full, PlotStyle → Thick, AxesLabel → {"\tau(N×gen)", "P(\tau)(1/N/gen)"},
         | 繪製範圍 | 全範圍 | 繪製樣式
                                       厚
                                               座標軸標籤
                                                                               數值化
          PlotLegends → Placed[{"old", "bad", "new fit", "new"}, Below]]]],
         繪製圖例
      With[\{idx0 = 7\},
       Plot[{predictionFree[tau, gammas[[idx0]],
           betas[[idx0]], alphas[[idx0]], combinedParameters[[idx0]]],
          predictionFree[tau, 0, 1, 1, combinedParameters[[idx0]]],
          newPredictionFree[tau, zetas[[idx0]], xis[[idx0]], combinedParameters[[idx0]]],
          newPredictionFree[tau, 2, -4, combinedParameters[[idx0]]]},
         {tau, 0, Transpose[Max[histograms[[idx0, 1, 1]]]][[1]]},
                 轉置
                           最大値
         PlotRange → Full, PlotStyle → Thick, AxesLabel → \{"\tau(N\times gen)", "P(\tau)(1/N/gen)"\},
                   全範圍 繪製樣式
                                       厚
                                              座標軸標籤
                                                               數値化
                                                                              數値化
         PlotLegends → Placed[{"old", "bad", "new fit", "new"}, Below], ImageSize → Large]]}
        繪製圖例
                       放置
                                                                 上下
                                                                        影像尺寸
```

