

\*Is this language regular?

a ... z

must be an equal number of a's and z's

such as: az, aazz, azaz

-No way to count/keep track in a regular language!

-Pumping Lemma for Regular Languages: (NOT ON EXAM)

Let L be a regular language, there exists some number  $P \geq 1$ , depending on L

such that for every word in the language where the length of  $w \geq P$ ,  $W = xyz$

with the length of y has to be at least 1, the length of x & y has to be  $\leq P$ , and for every  $i > 0$ ,  $(x&y)$  repeated i times followed by z has to be within L

-So assume a language is regular until it violates the Lemma, so come up with a W that is big enough that if you break it apart you are in trouble!

-What might I pick for W? :

$W = a(a)^P (z)^P$  z = a billion a's followed by a billion z's

= xyz

$x = aaa...aa$   $y = (aaa...)Z$

Violates the Lemma!

-Understand difference between regular language and context free language

-Can this be a rule in a context free grammar  $aS \rightarrow Sa$ ?

-NO! because of the left hand side

-Regular Grammar:  $N \rightarrow aN \mid \text{empty} \mid a \mid N$

-CFG:  $N \rightarrow \text{Anything Goes}$

-ML stuff up to patterns

Chs 1-(6 or 7)

-Lexing and parsing and stuff, show you one and tell me what it does

-Environments:

-Mapping of variables to values/types

-Interface:

-Create an empty environment w/o bindings (no pairs)  $\rightarrow$  empty-env

-Extend an environment (add a new binding to existing environment)  $\rightarrow$  extend-env

-Apply an environment (look up a value/type for a variable)  $\rightarrow$  apply-env

((x 5) (y 6) (a 10) empty-env)

-fair number of build a racket/ML function

-process a list, cons stuff

-No more than 10 lines of code

-Concept questions: ambiguity of a grammar, build me a parse tree, here is a language build me a grammar

-Whats a linker, lexer, parser

-Program:

-Text:

Executable

Lexical analysis → Parsing

(did you build program text that is syntactically correct?)

-Lexical Analysis outputs a list of tokens which is sent to the next step (Parsing)

-Are the individual words correct? Has nothing to do if they are put together in the right way → about individual words

-Parsing: about “phrase structure”, are the words in a correct syntax order? such as : did you say “if( bool expression) { }” correctly

-How does Cons work? :

-Cons as a function takes in two things (cons 'a '(b c)) → '(a b c) → List

-(cons 'a 'b) forms a pair → a.b → dotted pair/improper list (NOT A LIST!)

-The second thing that you gave it is not a list, so it cannot build a list from it!

-Cons Cell: In memory is two things paired together, a structure that has two elements.

-Removing ambiguities from Grammars:

<S> ::= <ifStatement> | S1 | S2

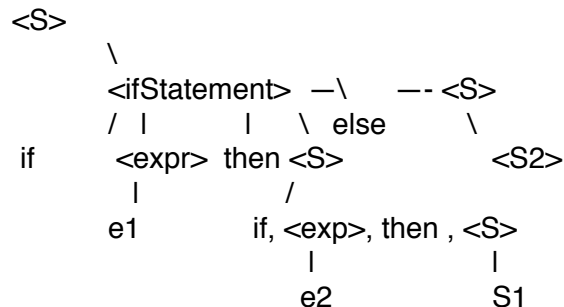
(S1 and S2 are Terminals)

<ifStatement> ::= if <expr> then <S> else <S> | if <expr> then <S>

<expr> ::= expr1 | expr2

Is this ambiguous or not?

if e1 then | if e2 then S1 else S2



So then: if, e1, then, if, e2, then ,s1,else, s2

-Associativity of the Uniary Operator:

not (not b) = (not (not b)) → right associativity

not b and c

can be: not (b and c)

or: (not b) and c

ML:

```
fun f n = n * n;  
val f = fn : int -> int
```

```
f 5;  
val it = 25 : int
```

```
fn n => n * n; (temporary function)  
val it = fn : int -> int
```

-Map: applies a function to everything in a list

```
map (fn n => n*n) [1,2,3,4];  
      (maps the function to everyone of the items in the list)  
val it = [1,4,9,16] : int list
```

```
map (fn n => if n > 4 then true else false) [1,4,9,16];  
val it = [false, false, true, true] : bool list
```

```
map (fn n => n +4) [1,4,9,16];  
val it = [5,9,13,20] : int list
```

-Fold: goes through a list and applies an operation to the list as you go  
give it a starting value and an operation and it will apply the operation as it goes

foldl - start at the left and work right  
foldr - start at the right and work left

```
foldl (op +) 0 [1,2,3,4];  
val it = 10 : int  
(0+1) + (0+2) + (0+3) + (0+4) = 10
```

```
foldr (op +) 0 [1,2,3,4,5,6];  
val it = 21 : int  
(0+6) + (0+5) + (0+4)....
```

-Map is a “curried” function, it takes multiple arguments one at a time. It takes in a function and gives you back a function, and then applies the function. You take two parameters but one at a time.

-Fold takes in an operator, returns a function that knows how to use a function. Takes in the base case, returns a function that knows how to apply the base case. Then finally returns a function that knows how to apply them to the list

-Given a list of ints, convert the list of ints to a list of real values: 1  $\rightarrow$  1.0

```
fun convert aList = map real aList;
```

```
convert[1,2,3,4]  $\rightarrow$  [1.0, 2.0, 3.0, 4.0]
```

-Square a List:

```
fun sqList aList = map (fn n => n*n) aList;
```

-Increment a List:

```
fun incList inc aList = map (fn n => inc +n) aList;
```

-Calculate Length: (answer will be an int, not a list. For this reason we use a fold instead of a map)

```
fun len aList = foldl (fn (a, b) => a + 1) 0 aList;
```

```
len [1,2,3] = 4
```