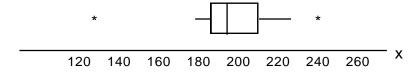
**a.** 
$$f_s = 216.8 - 196.0 = 20.8$$

inner fences: 196 - 1.5(20.8) = 164.6, 216.8 + 1.5(20.8) = 248

outer fences: 196 - 3(20.8) = 133.6, 216.8 + 3(20.8) = 279.2

Of the observations listed, 125.8 is an extreme low outlier and 250.2 is a mild high outlier.

**b.** A boxplot of this data appears below. There is a bit of positive skew to the data but, except for the two outliers identified in part (a), the variation in the data is relatively small.



1.78

- **a.** Since the constant  $\bar{x}$  is subtracted from each x value to obtain each y value, and addition or subtraction of a constant doesn't affect variability,  $s_y^2 = s_x^2$  and  $s_y = s_x$ .
- **b.** Let c = 1/s, where s is the sample standard deviation of the x's (and also, by part (a), of the y's). Then  $z_i = cy_i \Rightarrow s_z^2 = c^2s_y^2 = (1/s)^2s^2 = 1$  and  $s_z = 1$ . That is, the "standardized" quantities  $z_1$ , ...,  $z_n$  have a sample variance and standard deviation of 1.

2.42

- **a.** If Player X sits out, the number of possible teams is  $\binom{3}{1}\binom{4}{2}\binom{4}{2} = 108$ . If Player X plays guard, we need one <u>more</u> guard, and the number of possible teams is  $\binom{3}{1}\binom{4}{1}\binom{4}{2} = 72$ . Finally, if Player X plays forward, we need one <u>more</u> forward, and the number of possible teams is  $\binom{3}{1}\binom{4}{2}\binom{4}{1} = 72$ . So, the total possible number of teams from this group of 12 players is 108 + 72 + 72 = 252.
- **b.** Using the idea in **a**, consider all possible scenarios. If Players X and Y both sit out, the number of possible teams is  $\binom{3}{1}\binom{5}{2}\binom{5}{2}=300$ . If Player X plays while Player Y sits out, the number of possible teams is  $\binom{3}{1}\binom{5}{1}\binom{5}{2}+\binom{3}{1}\binom{5}{2}\binom{5}{1}=150+150=300$ . Similarly, there are 300 teams with Player X benched and Player Y in. Finally, there are three cases when X and Y both play: they're both guards, they're both forwards, or they split duties. The number of ways to select the rest of the team under these scenarios is  $\binom{3}{1}\binom{5}{0}\binom{5}{2}+\binom{3}{1}\binom{5}{2}\binom{5}{0}+\binom{3}{1}\binom{5}{1}\binom{5}{1}\binom{5}{1}=30+30+75=135$ .

Since there are  $\binom{15}{5}$  = 3003 ways to randomly select 5 players from a 15-person roster, the probability of randomly selecting a legitimate team is  $\frac{300+300+135}{3003} = \frac{735}{3003} = .245$ .

2.93

$$P(A \cup B) = P(A) + P(B) - P(A)P(B)$$
  
.626 =  $P(A) + P(B) - .144$ 

So P(A) + P(B) = .770 and P(A)P(B) = .144.

Let x = P(A) and y = P(B), then using the first equation, y = .77 - x, and substituting this into the second equation, we get x (.77 - x) = .144 or

$$x^2$$
 - .77x + .144 = 0. Use the quadratic formula to solve:  $\frac{.77 \pm \sqrt{.77^2 - (4)(.144)}}{2} = \frac{.77 \pm .13}{2} = .32$  or .45

So P(A) = .45 and P(B) = .32

2.100

a. 
$$P(both +) = P(carrier \cap both +) + P(not a carrier \cap both +)$$

$$= P(both + | carrier) \times P(carrier)$$

$$+ P(both + | not a carrier) \times P(not a carrier)$$

$$= (.90)^{2}(.01) + (.05)^{2}(.99) = .01058$$

$$P(both -) = (.10)^{2}(.01) + (.95)^{2}(.99) = .89358$$

$$P(tests agree) = .01058 + .89358 = .90416$$

b. P(carrier | both + ve) = 
$$\frac{P(carrier \cap both.positive)}{P(both.positive)} = \frac{(.90)^2(.01)}{.01058} = .7656$$

2.101

Let  $A = 1^{st}$  functions,  $B = 2^{nd}$  functions, so P(B) = .9,  $P(A \cup B) = .96$ ,  $P(A \cap B) = .75$ . Thus,  $P(A \cup B) = P(A) + P(B) - P(A \cap B) = P(A) + .9 - .75 = .96$ , implying P(A) = .81.

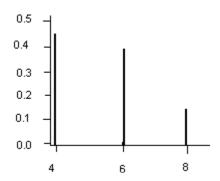
This gives P(B | A) = 
$$\frac{P(B \cap A)}{P(A)} = \frac{.75}{.81} = .926$$

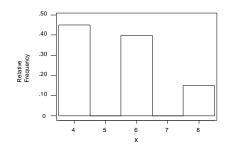
3.11

a.

X	4	6	8
P(x)	.45	.40	.15

b.





**c.** 
$$P(x \ge 6) = .40 + .15 = .55$$

$$P(x > 6) = .15$$