Chapter 3

**3.50**

Let *X* be the number of faxes, so *X* ~ Bin(25, .25).

* 1. *P*(*X* ≤ 6) = *B*(6;25,.25) = .561.
  2. *P*(*X* = 6) = *b*(6;25,.25) = .183.
  3. *P*(*X* ≥ 6) = 1 – *P*(*X* ≤ 5) = 1 – *B*(5;25,.25) = .622.
  4. *P*(*X* > 6) = 1 – *P*(*X* ≤ 6) = 1 – .561 = .439.

**3.81**

Let *X* ~ Poisson(*μ* = 20).

* 1. *P*(*X* ≤ 10) = *F*(10; 20) = .011.
  2. *P*(*X* > 20) = 1 – *F*(20; 20) = 1 – .559 = .441.
  3. *P*(10 ≤ *X* ≤ 20) = *F*(20; 20) – *F*(9; 20) = .559 – .005 = .554;

*P*(10 < *X* < 20) = *F*(19; 20) – *F*(10; 20) = .470 – .011 = .459.

* 1. *E*(*X*) = *μ =* 20, so *σ = =* 4.472. Therefore, *P*(*μ* – 2*σ* < *X* < *μ* + 2*σ*) =

*P*(20 – 8.944 < *X* < 20 + 8.944) = *P*(11.056 < *X* < 28.944) = *P*(*X* ≤ 28) – *P*(*X* ≤ 11) =

*F*(28; 20) – *F*(11; 20) = .966 – .021 = .945.

Chapter 4

**4.45**

With μ = .500 inches, the acceptable range for the diameter is between .496 and .504 inches, so unacceptable bearings will have diameters smaller than .496 or larger than .504.

The new distribution has μ = .499 and σ =.002.

P(X < .496 or X >.504) == P(Z < –1.5) + P(Z > 2.5) =

Φ(–1.5) + [1 – Φ(2.5)] = .073. 7.3% of the bearings will be unacceptable.

**4.47**

The stated condition implies that 99% of the area under the normal curve with μ = 12 and σ = 3.5 is to the left of *c* – 1, so *c* – 1 is the 99th percentile of the distribution. Since the 99th percentile of the standard normal distribution is *z* = 2.33, *c* – 1 = μ + 2.33σ = 20.155, and *c* = 21.155.

Chapter 5

**5.46**

* 1. The sampling distribution of  is centered at = *μ* = 12 cm, and the standard deviation of the distribution is= .01 cm.
  2. With *n* = 64, the sampling distribution of  is still centered at = *μ* = 12 cm, but the standard deviation of the distribution is= .005 cm.
  3. is more likely to be within .01 cm of the mean (12 cm) with the second, larger, sample. This is due to the decreased variability of that comes with a larger sample size.

**5.50**

* 1. *P*( 9,900 ≤  ≤ 10,200) ≈ 

= *P*(–1.26 ≤ *Z* ≤ 2.53) = Φ(2.53) – Φ(–1.26) = .9943 – .1038 = .8905.

* 1. According to the guideline given in Section 5.4, *n* should be greater than 30 in order to apply the CLT, thus using the same procedure for *n* = 15 as was used for *n* = 40 would not be appropriate.

**5.59**

* 1. *E*(*X*1 + *X*2 + *X*3) = 180, *V*(*X*1 + *X*2 + *X*3) = 45, *SD*(*X*1 + *X*2 + *X*3) == 6.708.

*P*(*X*1 + *X*2 + *X*3 ≤ 200) = .

*P*(150 ≤ *X*1 + *X*2 + *X*3 ≤ 200) = 

* 1. and , so

 and



* 1. *E*(*X*1 – .5*X*2 – .5*X*3) = *μ* – .5 *μ* – .5 *μ* = 0, while

*V*(*X*1 – .5*X*2 –.5*X*3) = ⇒ *SD*(*X*1 – .5*X*2 –.5*X*3) = 4.7434. Thus,

*P*(–10 ≤ *X*1 – .5*X*2 – .5*X*3 ≤ 5) = = .8531 – .0174 = .8357.

* 1. *E*(*X*1 + *X*2 + *X*3) = 150, *V*(*X*1 + *X*2 + *X*3) = 36 ⇒ *SD*(*X*1 + *X*2 + *X*3) = 6, so

*P*(*X*1 + *X*2 + *X*3 ≤ 200) = 

Next, we want *P*(*X*1 + *X*2 ≥ 2*X*3), or, written another way, *P*(*X*1 + *X*2 – 2*X*3 ≥ 0).

*E*(*X*1 + *X*2 – 2*X*3) = 40 + 50 – 2(60) = –30 and *V*(*X*1 + *X*2 – 2*X*3) = ⇒

*SD*(*X*1 + *X*2 – 2*X*3) = 8.832, so

*P*( *X*1 + *X*2 – 2*X*3 ≥ 0) = .

Chapter 6

**6.11**

* 1. .
  2. = and the standard error is the square root of this quantity.
  3. With , , , , the estimated standard error is .
  4. 
  5. 

**6.15**

* 1.  implies that . Consider . Then , implying that  is an unbiased estimator for *θ*.
  2. , so 

Chapter 7

**7.16**

* 1. The boxplot shows a high concentration in the middle half of the data (narrow box width). There is a single outlier at the upper end, but this value is actually a bit closer to the median (55 kV) than is the smallest sample observation.



* 1. From software, = 54.7 and *s* = 5.23. The 95% confidence interval is then

= (53.2, 56.2)

We are 95% confident that the true mean breakdown voltage under these conditions is between 53.2 kV and 56.2 kV. The interval is reasonably narrow, indicating that we have estimated *μ* fairly precisely.

* 1. A conservative estimate of standard deviation would be (70 – 40)/4 = 7.5. To achieve a margin of error of at most 1 kV with 95% confidence, we desire

= 216.09.

Therefore, a sample of size at least *n* = 217 would be required.

**7.20**

Because the sample size is so large, the simpler formula (7.11) for the confidence interval for *p* is sufficient:



**7.34a**

*n* = 14, , *s* = .79; 

A 95% lower confidence bound: . With 95% confidence, the value of the true mean proportional limit stress of all such joints is greater than 8.11 MPa. We must assume that the sample observations were taken from a normally distributed population.

Chapter 8

**8.58**

*μ =* the true average percentage of organic matter in this type of soil, and the hypotheses are *H*0: *μ* = 3 v. *H*a: *μ* ≠ 3. With *n* = 30, and assuming normality, we use the *t* test: . The *P-*value = 2[*P*( *t* > 1.759 )] = 2( .041 ) = .082. At significance level .10, since .082 ≤ .10, we would reject *H*0 and conclude that the true average percentage of organic matter in this type of soil is something other than 3. At significance level .05, we would not have rejected *H*0.

**8.75**

* 1. With *H*0: *p* = 1/75 v. *H*a: *p* ≠ 1/75, we reject *H*0 if either *z* ≥ 1.96 or *z* ≤ –1.96. With , , which is not in either rejection region. Thus, we fail to reject the null hypothesis. There is not evidence that the incidence rate among prisoners differs from that of the adult population. The possible error we could have made is a type II.
  2. *P*–value =. Yes, since .10 < .20, we could reject *H*0.