CZ4079 Final Year Project

A Machine Learning-Based Approach to Time-Dependent Shortest Path Queries

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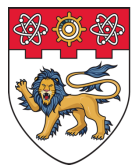

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Introduction: Problem

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- A **dynamic road network** $G = (V, E)$ with a time-dependent weight function $w : E, t \rightarrow \mathbb{R}$

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Introduction: Problem

- A **dynamic road network** $G = (V, E)$ with a time-dependent weight function $w : E, t \rightarrow \mathbb{R}$
- A **query** $Q(u, v, t)$ that asks for a shortest path from u to v departing at time moment t

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Introduction: General Approach

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- The new **machine learning-based approach** draws on collective wisdom of thousands of taxi drivers

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- **Unsupervised learning** is employed to figure out the time-dependent edge costs

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- The new **machine learning-based approach** draws on collective wisdom of thousands of taxi drivers
- **Unsupervised learning** is employed to figure out the time-dependent edge costs
- A modified Dijkstra's algorithm calculates a shortest path on the fly

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Introduction: Challenges

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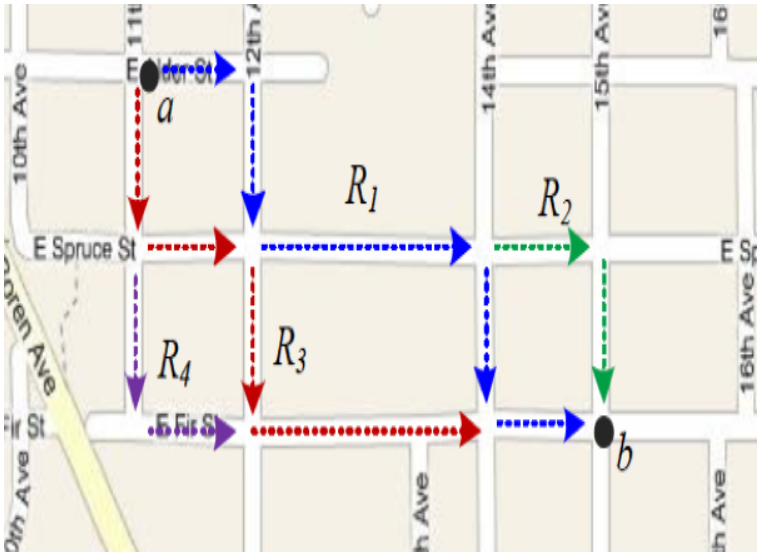
- Sparse sample points



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Introduction: Challenges

- Arbitrary u and v
- Sparse sample points
- Limited GPS accuracy

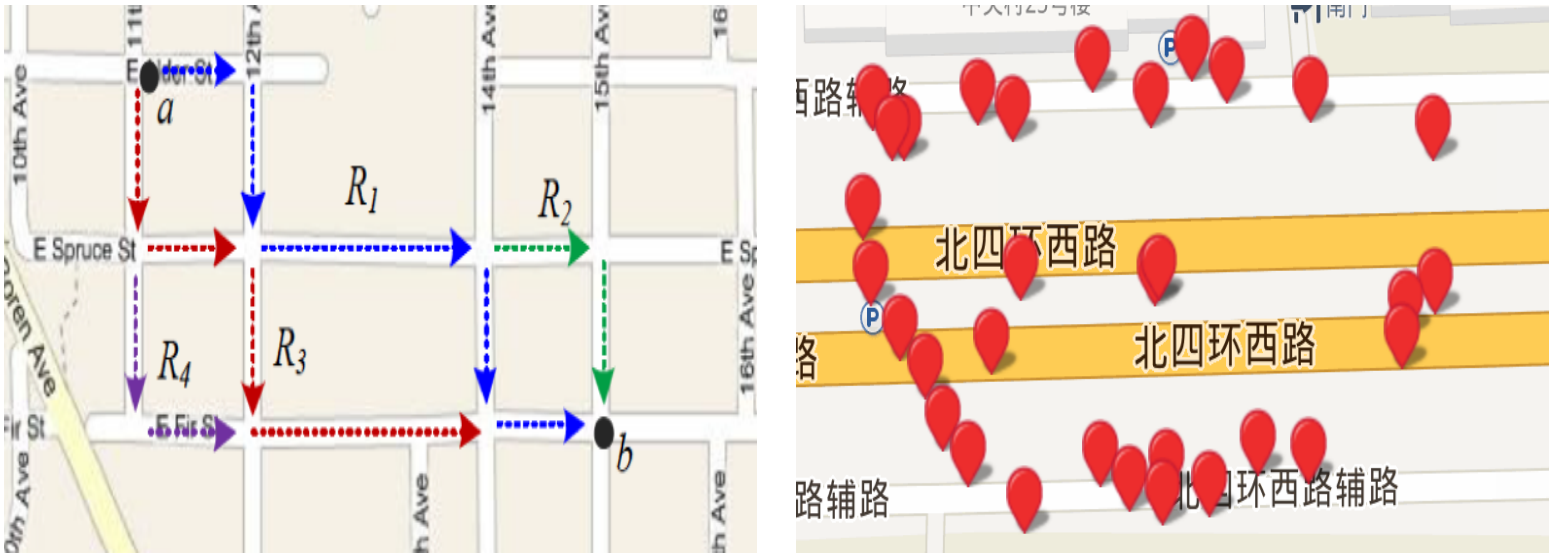

Figure 1: Examples of challenges

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Preliminary Processing: Data Description

- Is collected from Computational Sensing Lab at Tsinghua University
- Contains 83 million GPS records from 8,602 taxis in Beijing during May of 2009

Field	**Explanation**
CUID	ID for each taxi
UNIX_EPOCH	Unix timestamp
GPS_LONG	Longitude in WGS-84
GPS_LAT	Latitude in WGS-84
HEAD	Heading direction
SPEED	Instantaneous speed (m/s)
OCCUPIED	Hired (1) or not (0)

Table 1: A summary of the seven original fields

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Preliminary Processing: Reverse Geocoding

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Preliminary Processing: Reverse Geocoding

- GPS coordinate translation: 1.34°N, 103.68°E $\rightarrow$ SCSE, NTU

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Preliminary Processing: Reverse Geocoding

- GPS coordinate translation: 1.34°N, 103.68°E → SCSE, NTU
- China GPS shift problem: WGS84 v.s. BD09

Figure 2: An example of China GPS shift problem

Preliminary Processing: Reverse Geocoding

- GPS coordinate translation: 1.34°N, 103.68°E $\rightarrow$ SCSE, NTU
- China GPS shift problem: WGS84 v.s. BD09
- Solution: WGS84 $\xrightarrow{Baidu\ API}$ BD09 $\xrightarrow{Baidu\ API}$ Street

Figure 2: An example of China GPS shift problem

Preliminary Processing: Outlier Detection

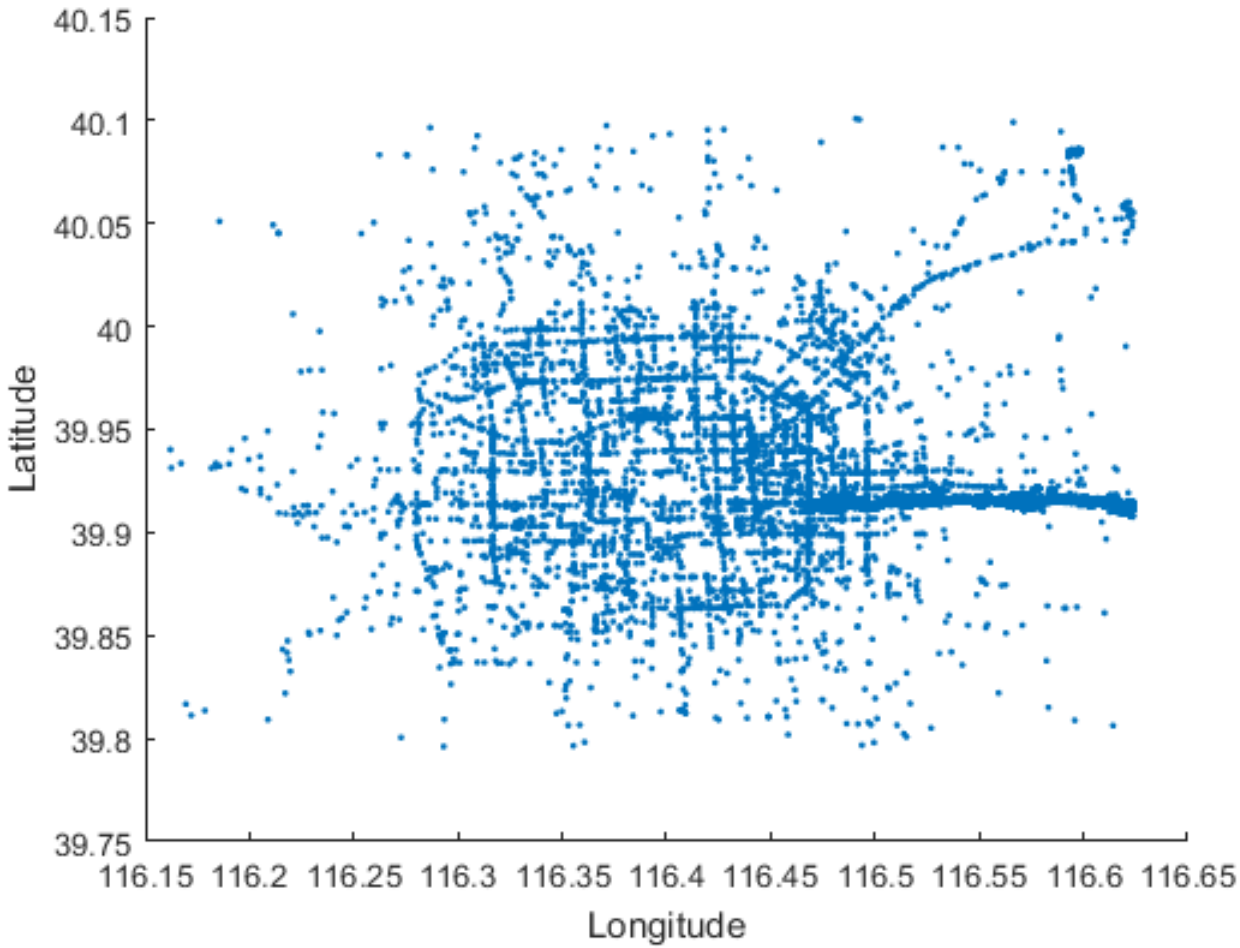

Figure 3: An example of outliers

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Preliminary Processing: Outlier Detection

Theorem (*Majority Clustering Theorem*)

If a **reasonable reverse geocoder** is used to reverse-geocode a set of GPS data points which are mapped to a particular street *in reality*, then, when plotted on a 2-D plane, majority (more than 50%) of the points must be clustered together to form a rough shape that is similar to the shape of the street that they are supposed to be mapped to.

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Two-step procedure:
Outlier Detection = Outlier Identification + Outlier Removal

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Preliminary Processing: Outlier Detection

Outlier Identification: Clustering

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Outlier Identification: Clustering

- Sample point concentration $\rightarrow$ cluster concentration

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Preliminary Processing: Outlier Detection

Outlier Identification: Clustering

- Sample point concentration $\rightarrow$ cluster concentration
- Top $k\%$ ($k = 50$) largest clusters as groups of correct sample points

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Preliminary Processing: Outlier Detection

Outlier Identification: Clustering

- Sample point concentration $\rightarrow$ cluster concentration
- Top $k\%$ ($k = 50$) largest clusters as groups of correct sample points
- 10×10 self-organising feature maps implementation

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Outlier Removal: Distance Threshold d_{max}

- Assign sample points to legal centroids no farther than d_{max}
- Remove all "orphan" sample points
- Use real physical distance on the Earth
- Set $d_{max} = 30$m or 50m

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Preliminary Processing: Outlier Detection

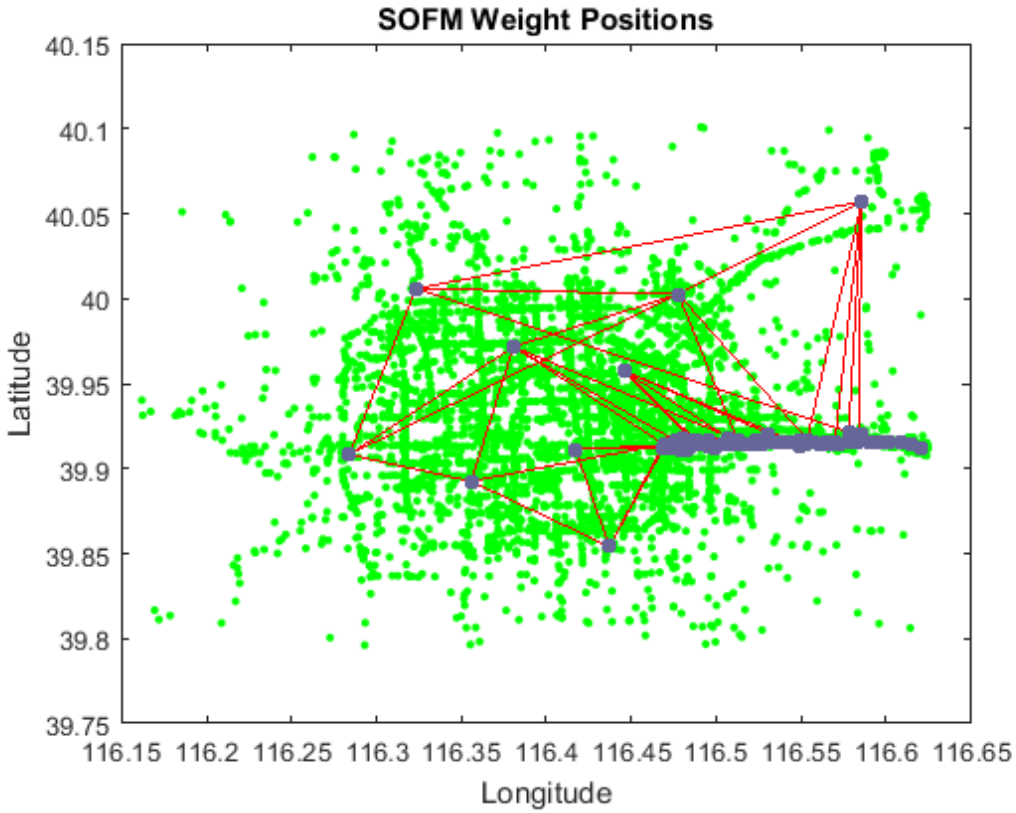

Figure 4: A plot of neuron positions after training

Preliminary Processing: Outlier Detection

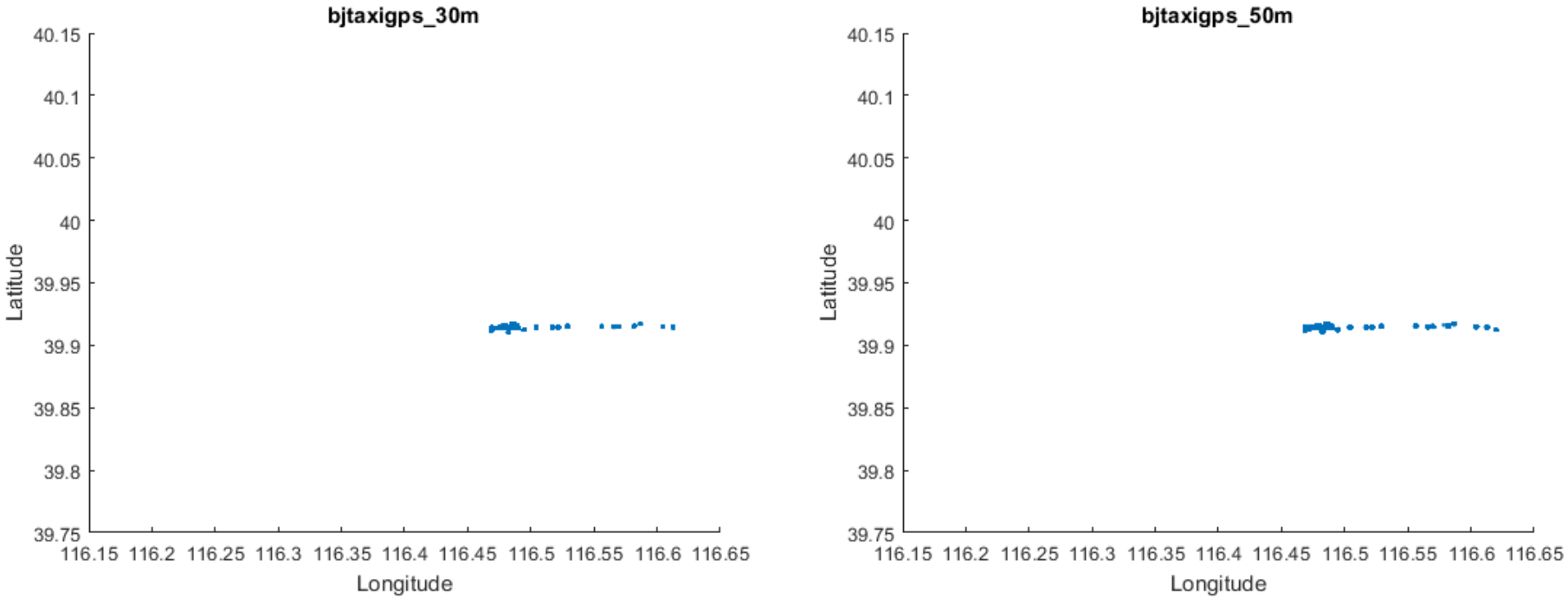

Figure 5: A plot of sample points after outlier removal

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Landmark Graph: Basic Ideas

Definition (*Landmark*)

A landmark is a road segment that is frequently traversed by taxi drivers according to the taxi GPS trajectory database.

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Rationale

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Step to build landmark graph

- Separate sample points into **trip**s

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Step to build landmark graph

- Separate sample points into **trip**s
- Count occurrences of each street
- Find connections between two landmarks

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Landmark Graph: Trip Identification

CUID	UTC	GPS_LONG	GPS_LAT	OCCUPIED	TRIP_ID
1	1/5/2009 0:02:00	116.39616	39.81294	0	4552265
1	1/5/2009 0:04:00	116.39575	39.82296	0	4552265
1	1/5/2009 0:07:00	116.39567	39.82774	0	4552265
1	1/5/2009 17:08:00	116.30142	39.98105	1	1
1	1/5/2009 17:10:00	116.29514	39.98419	1	1
1	1/5/2009 17:11:00	116.28959	39.98289	1	1
1	1/5/2009 17:12:00	116.28087	39.97552	1	1
1	1/5/2009 17:16:00	116.26813	39.93537	1	1
1	1/5/2009 18:11:00	116.36537	39.95019	0	4552271
1	1/5/2009 18:12:00	116.36546	39.94886	0	4552271
1	1/5/2009 18:13:00	116.35927	39.94528	0	4552271

Table 2: An example of trip identification

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Landmark Graph: Frequency Counting

CUID	UTC	GPS_LONG	GPS_LAT	Street	TRIP_ID
1	1/5/2009 0:02:00	116.39616	39.81294	A	4552265
1	1/5/2009 0:04:00	116.39575	39.82296	A	4552265
1	1/5/2009 0:07:00	116.39567	39.82774	B	4552265
1	1/5/2009 17:08:00	116.30142	39.98105	C	1
1	1/5/2009 17:10:00	116.29514	39.98419	C	1
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1	1/5/2009 18:12:00	116.36546	39.94886	C	4552271
1	1/5/2009 18:13:00	116.35927	39.94528	C	4552271

Table 3: An illustration of frequency counting

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Landmark Graph: Construction

For each trip

- Select a landmark j
- Record intermediate streets while searching for the next landmark k
- Repeat the process starting from k until all streets are examined

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Travel Time Estimation: Basic Ideas

Definition (*Significant Edge*)

A significant edge in a landmark graph $G = (V, E)$ is an edge $e \in E$ that has a support at least m, where m is a parameter specified in advance.

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Travel Time Estimation: Basic Ideas

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- Build a **predictive model** for travel time of each significant edge

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- Separate weekday's travel time from weekend's

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- Build a **predictive model** for travel time of each significant edge
- Separate weekday's travel time from weekend's
- Evaluate results against Baidu's estimates

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Travel Time Estimation: Underlying Distribution

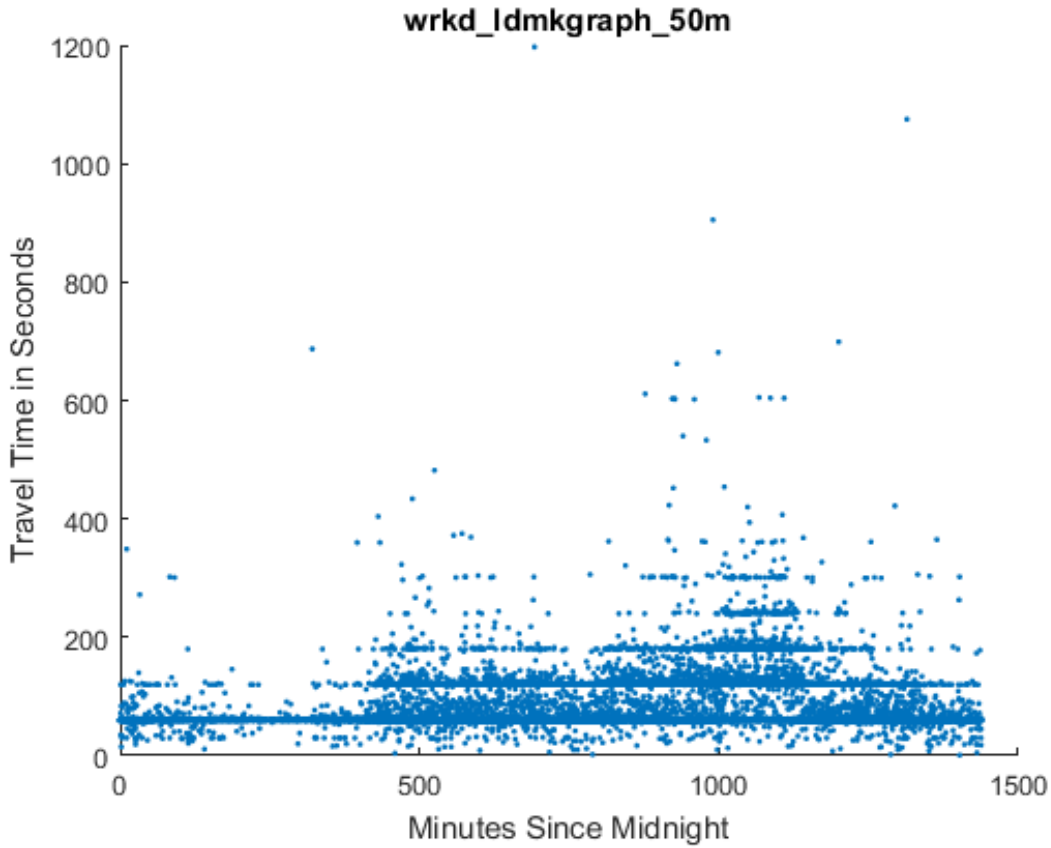

Figure 6: An example of travel time patterns

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Travel Time Estimation: Underlying Distribution

Possible Explanations

- Drivers choose different routes to travel between the two landmarks

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- Drivers choose different routes to travel between the two landmarks
- Drivers have different driving skills, preferences and behaviours

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Travel Time Estimation: Underlying Distribution

Possible Explanations

- Drivers choose different routes to travel between the two landmarks
- Drivers have different driving skills, preferences and behaviours
- The GPS devices report locations **periodically**, therefore, durations like 60 seconds or 120 seconds are very common

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Travel Time Estimation: Clustering

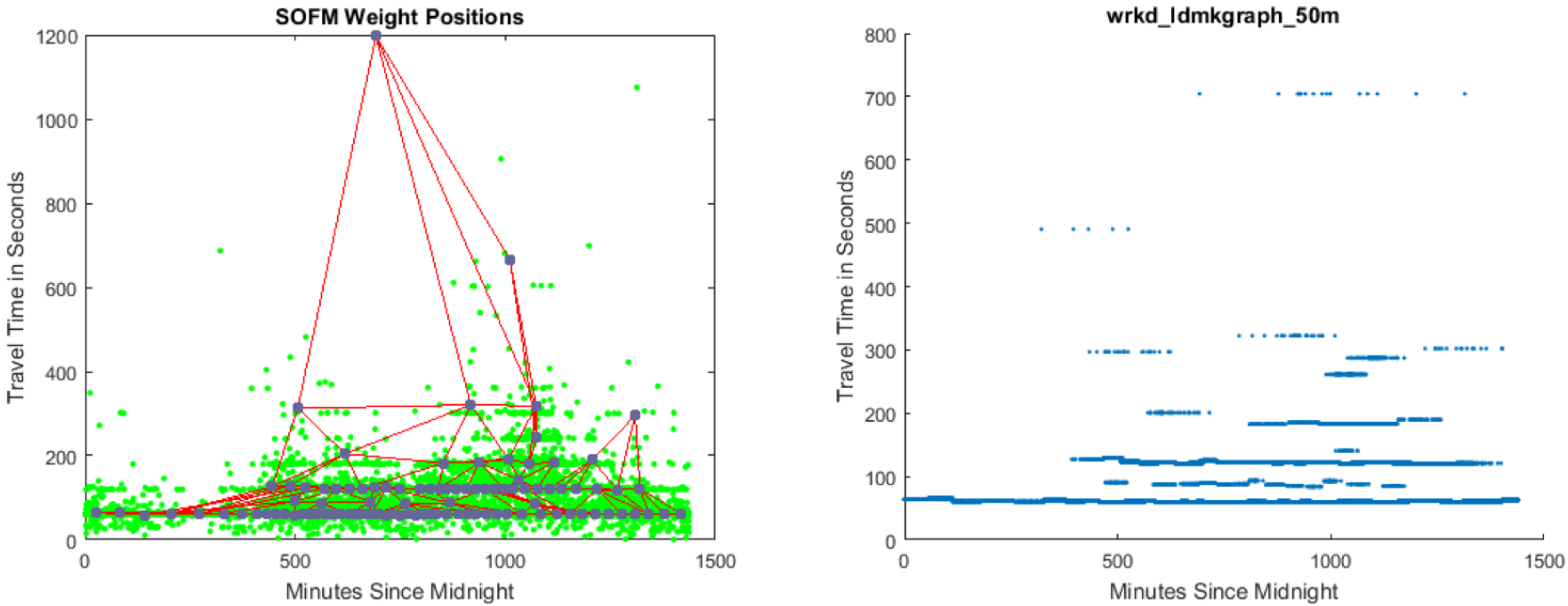

Figure 7: An illustration of travel time clustering

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Travel Time Estimation: Distribution Fit

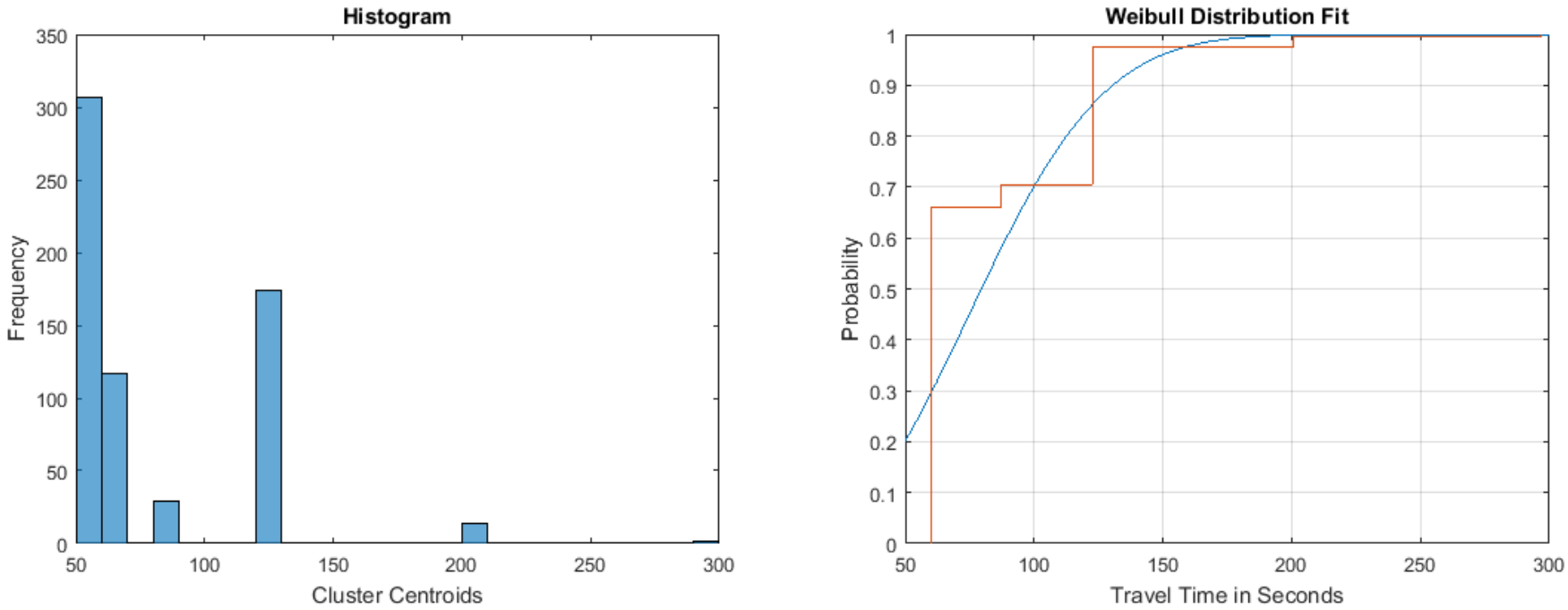

Figure 8: An illustration of fitting distribution

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Travel Time Estimation: Implementation

Definition (*Optimism Index*)

An optimism index indicates how optimistic a driver feels about his or her driving skills. A driver with an optimism index of $p\%$ usually drives faster than $(1-p)\%$ drivers under similar road conditions.

- Calculate and store α and β for each 30-minute window

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- Calculate and store α and β for each 30-minute window
- Use optimism index p to find out travel time

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Travel Time Estimation: Evaluation

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- Select the most significant 150 edges (pairs of landmarks)

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- Sample 20% of trips passing through each pair randomly

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Travel Time Estimation: Evaluation

- Select the most significant 150 edges (pairs of landmarks)
- Sample 20% of trips passing through each pair randomly
- Calculate travel time of each trip with optimism index $p = 0.5$

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Travel Time Estimation: Evaluation

- Select the most significant 150 edges (pairs of landmarks)
- Sample 20% of trips passing through each pair randomly
- Calculate travel time of each trip with optimism index $p = 0.5$
- Use Baidu Maps' API to give real-time estimates

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- Compare Baidu's estimates with the **median** travel time

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- Sample 20% of trips passing through each pair randomly
- Calculate travel time of each trip with optimism index $p = 0.5$
- Use Baidu Maps' API to give real-time estimates
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Landmark Graph	RMSE	Mean Error Ratio	Mean No. of Samples Per Edge
wrkd_ldmkgraph_50m	78.84	-0.009	1824.60
wrkd_ldmkgraph_30m	87.96	-0.065	1507.56
holi_ldmkgraph_50m	87.39	-0.16	832.96
holi_ldmkgraph_30m	76.41	-0.14	681.89

Table 4: A summary of evaluation results

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Travel Time Estimation: Evaluation

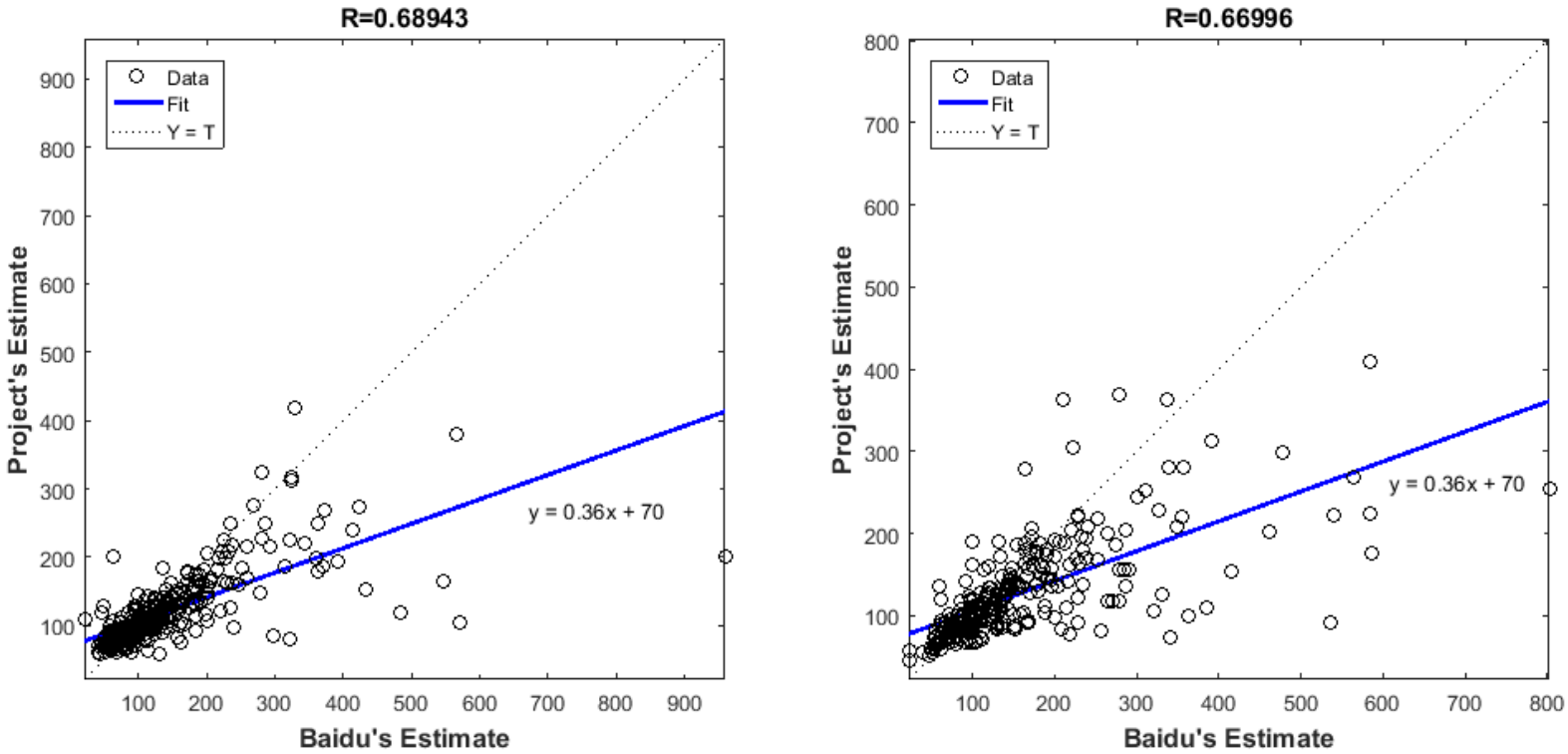

Figure 9: A plot of linear regression for weekday landmark graph

Travel Time Estimation: Evaluation

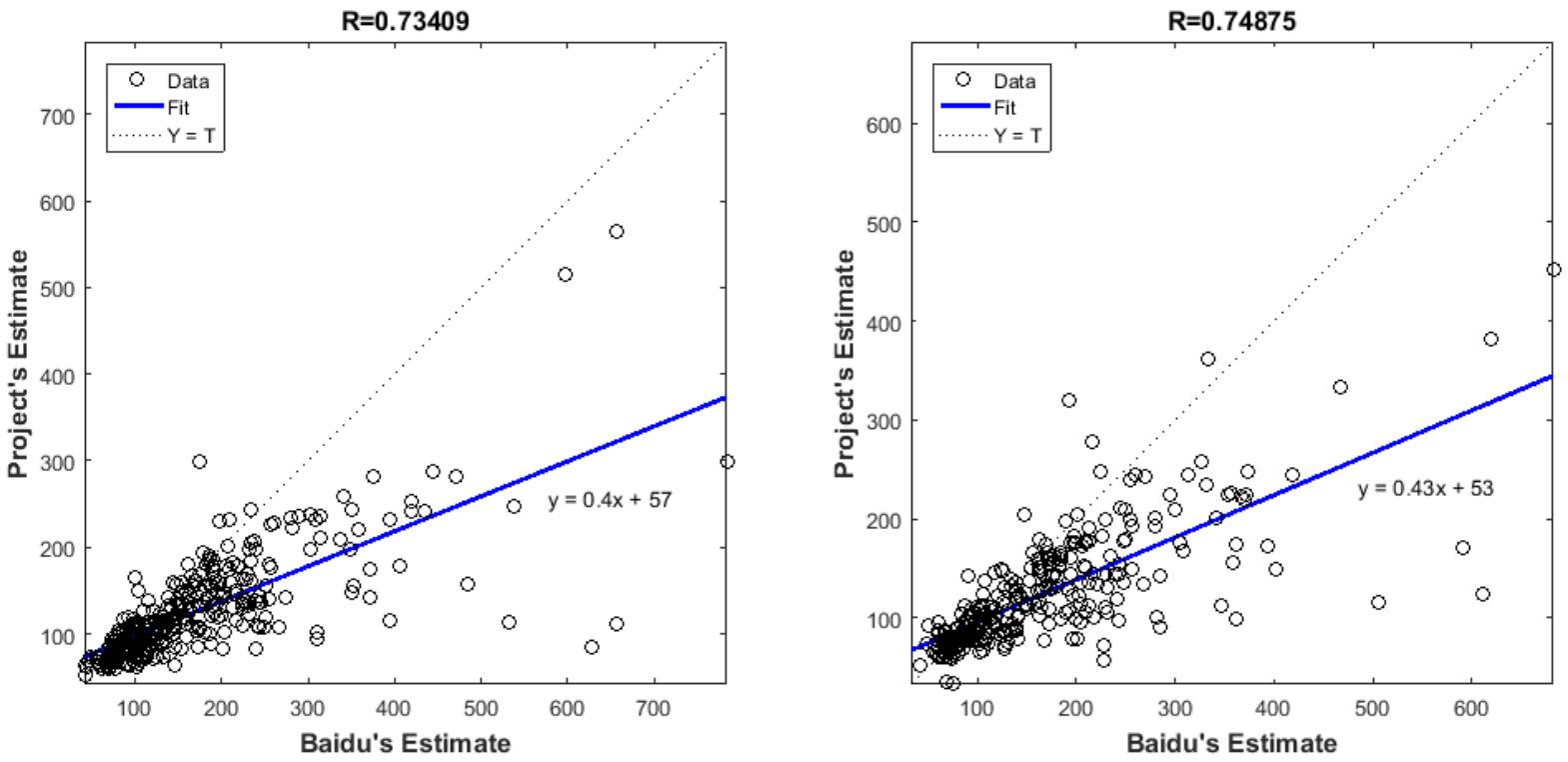

Figure 10: A plot of linear regression for weekend landmark graph

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Shortest Path Calculation: Basic Ideas

Definition (*FIFO Graph*)

A time-dependent graph $G = (V, E)$ with a dynamic weight function $w : E, t \to \mathbb{R}$ is a FIFO graph iff for every edge $(u, v) \in E$

$$\forall \Delta t \geq 0, \quad w(u, v, t_0) \leq \Delta t + w(u, v, t_0 + \Delta t) \tag{1}$$

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- Consider a landmark graph as a FIFO graph (usually true)

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- Consider a landmark graph as a FIFO graph (usually true)
- Modify Dijkstra's algorithm to calculate edge costs in an online fashion

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Shortest Path Calculation: Modified Dijkstra's Algorithm

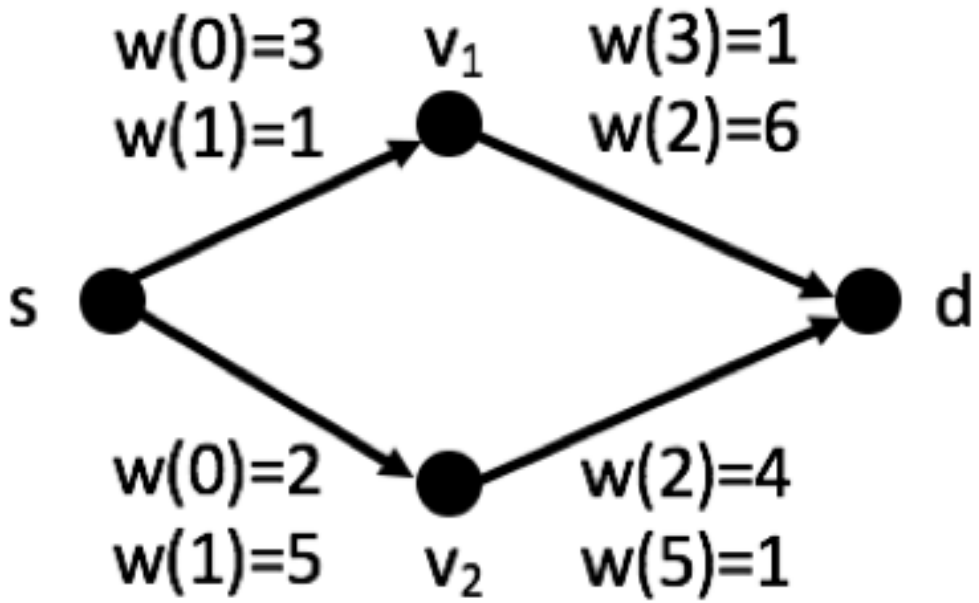

Figure 11: An example of modified Dijkstra's algorithm

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Conclusion and Q&A: Conclusion

- Framed the time-dependent shortest path problem

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- Framed the time-dependent shortest path problem
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- Proposed an innovative outlier detection approach
- Introduced algorithms for building landmark graphs

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Conclusion and Q&A: Conclusion

- Framed the time-dependent shortest path problem
- Identified challenges in solving the problem
- Proposed an innovative outlier detection approach
- Introduced algorithms for building landmark graphs
- Described procedures for estimating travel time

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Conclusion and Q&A: Conclusion

- Framed the time-dependent shortest path problem
- Identified challenges in solving the problem
- Proposed an innovative outlier detection approach
- Introduced algorithms for building landmark graphs
- Described procedures for estimating travel time
- Illustrated the modified Dijkstra's algorithm

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Conclusion and Q&A: Questions & Answers

Any questions?

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