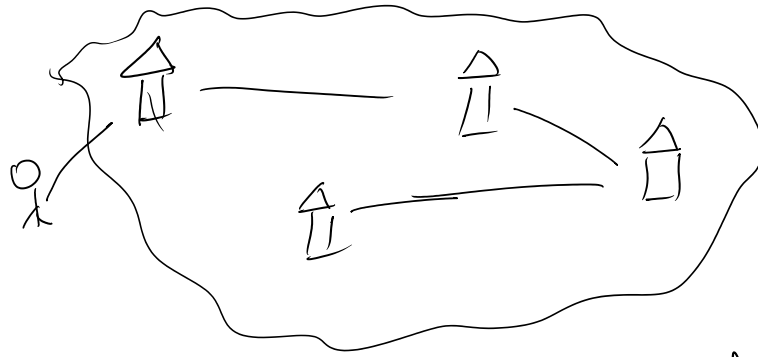


Task



Unique path

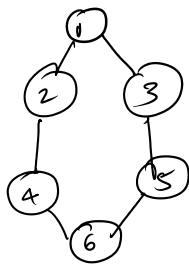
to connect all the houses without forming a loop/cycle



- Given an undirected graph $G = (V, E)$

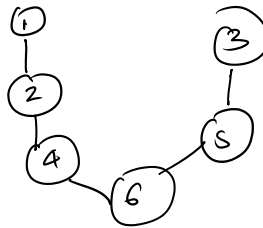
Spanning Tree $S \subseteq G$ $S = (\underline{V}, \underline{E'})$

#g



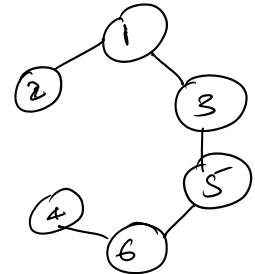
n nodes

ST



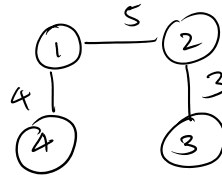
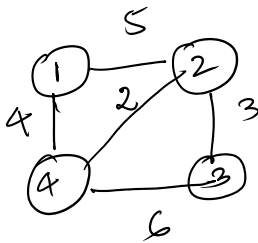
, (n-1) edges

ST

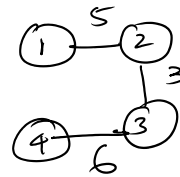


$S = (|V|, |V|-1)$

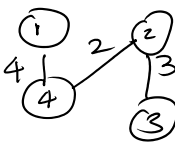
#g



Cost = 12



Cost = 14



Cost = 19

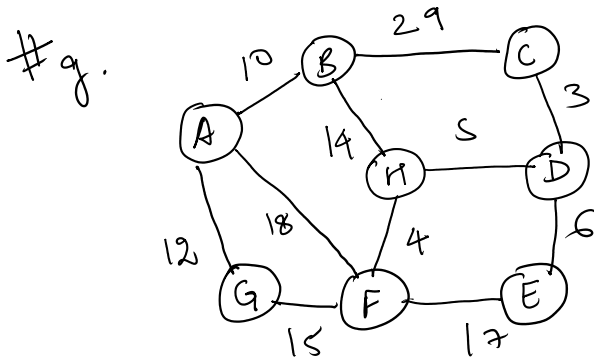


Minimum Spanning Tree - Spanning tree with min. cost

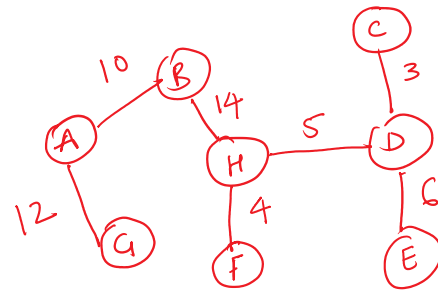
Prim's

Kruskal's

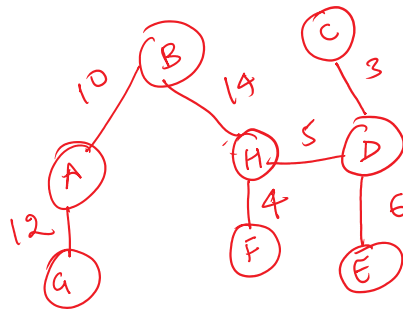
- ₁ Choose any vertex in G
 - ₂ Add it to empty tree
 - ₃ Until we have all vertices of G in the tree
- Choose the edge of the least cost that starts from any of the nodes in the tree
- Add that edge & that vertex in the tree



Start with A MST



Start with E



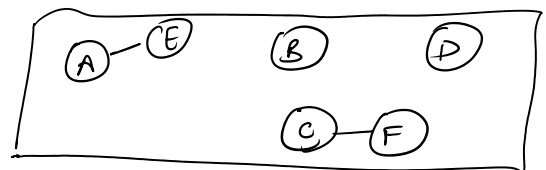
Cost = Total weight of edges in MST
= 54

Start at H?

Kruskal's Algo

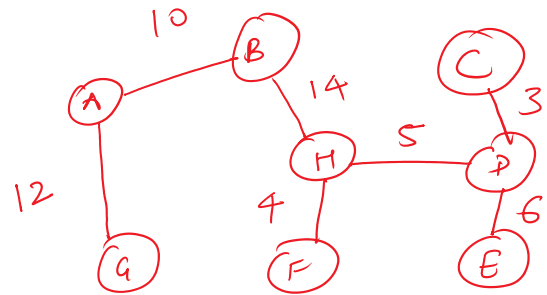
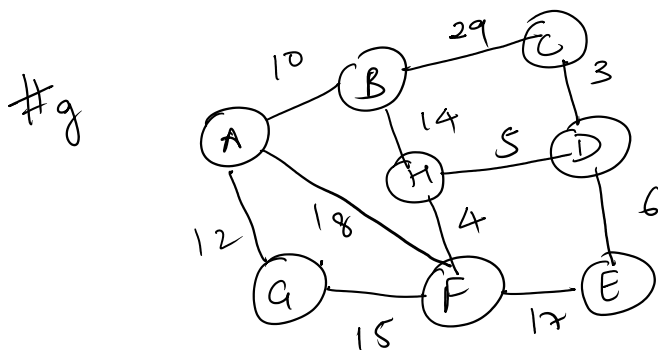
- ₁ Construct a forest with n vertices

FOREST

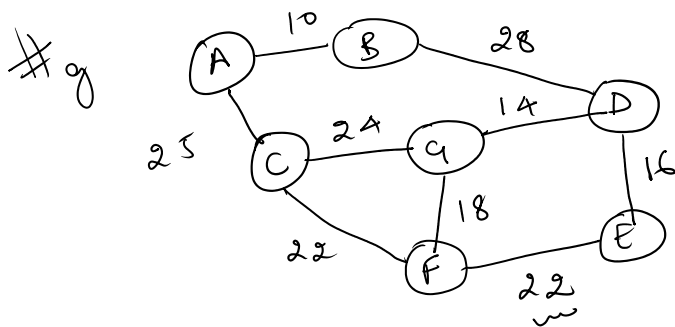


graph whose all connected sub-components are trees

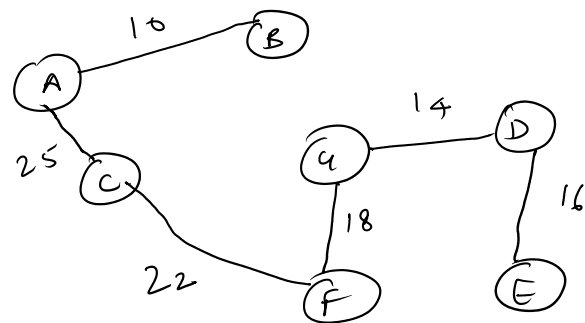
- ₂ Put the edges in a sorted form in a queue
- ₃ Until $(N-1)$ edges in the forest
 - i) Extract "min cost" edge from Queue
 - If it is forming a cycle, discard it
 - Else add it into the forest



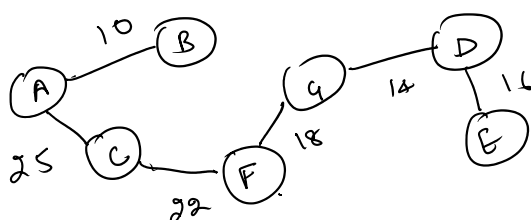
{ ~~(C,D)~~, ~~(H,F)~~, ~~(H,D)~~, ~~(D,E)~~, ~~(A,B)~~, ~~(A,G)~~, (B,H), (G,F), (F,E), (A,F), (B,C) }



Kruskal's



Prim's



Time complexity.

$$|E| = |V| - 1$$

Kruskal

$O(V \cdot \text{Extract min})$

Arrays

$O(E)$

$O(V^2)$

heaps $\log(E)$

$\log(|V| - 1)$

$O(V \log V)$