

Lecture 16b | Normal Line Equation

- Time Based Collision
 - 1.1. Point-Line
 - 1.2. Intersection of a ray with a line segment

- CS230 2
- Game 2
- Implementation Techniques

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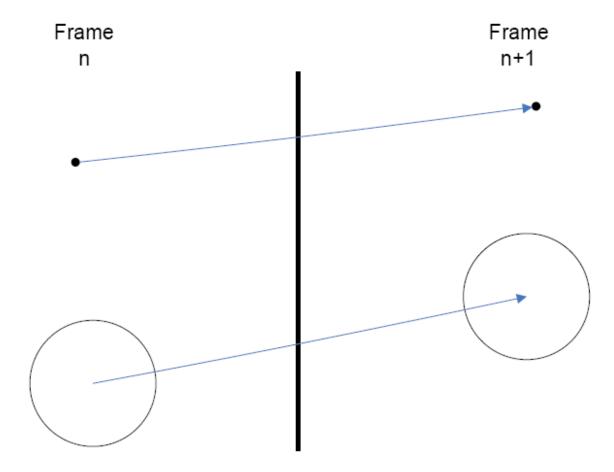
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1. Time Based Collision

1.1. Point-Line

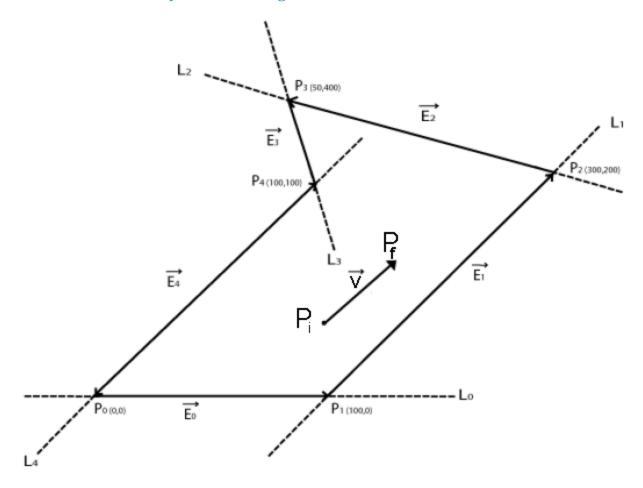
- The circle or point is moving and the line segment is static.
- Checking for collision at the previous and current positions is not enough.
- The circle (or the point) and the line can be not colliding with the line at frame n and frame n+1, but in reality they might have collided.



- As you can see in the figure above, the circle and the point aren't colliding with the line at frame n, and aren't colliding with it at frame n+1, but obviously, they are colliding with it sometime along the path.
- We need to interpolate along the path in order to find the exact time where the collision occurred.



1.2. Intersection of a ray with a line segment



Edge	Vector	Outward Normal
0	$\overrightarrow{E_0}$ = (100; 0)	$\overrightarrow{N_0}$ = (0; -100)
1	$\overrightarrow{E_1}$ = (200; 200)	$\overrightarrow{N_1}$ = (200; -200)
2	$\overrightarrow{E_2}$ = (-250; 200)	$\overrightarrow{N_2}$ = (200; 250)
3	$\overrightarrow{E_3}$ = (50; -300)	$\overrightarrow{N_3}$ = (-300; -50)
4	$\overrightarrow{E_4} = (-100; -100)$	$\overrightarrow{N_0}$ = (-100; 100)

Infinite Line	Equation
0	(0; -100).(x; y) = 0
1	(200 ; -200).(x ; y) = 20000
2	(200; 250).(x; y) = 110000
3	(-300 ; -50).(x ; y) = -350000
4	(-100 ; 100).(x ; y) = 0



- Consider a point to be located at P_i inside the chamber and moving with towards P_f
- This means that its velocity is $\overrightarrow{P_lP_f} = \overrightarrow{V}$
- Let \vec{P} be the position vector of point P (The moving point). Then the equation of the ray is: $\vec{P} = \overrightarrow{P_l P_f} *t + P_i = \vec{V} *t + P_i$
- At which time t_n , does the ray hit the line L given by: \vec{N} .P = D?
- Assume P_n is the spot where the ray intersects the line L
- This means that the ray intersects with the line at point P_n at time t_n
- This means that the point P_n belongs to both the ray and the line
- Thus, P_n in \vec{N} . $P_n = D$ is the same as $\vec{P}_n = \vec{V} * t_n + P_i$ (It's the same point, the point of intersection)
- By replacing the 2nd equation in the first one we get:

$$\vec{N}.(\vec{V}*t_n + P_i) = D$$

$$\vec{N}.\vec{V}*t_n + \vec{N}.P_i = D$$

$$\vec{N}.\vec{V}*t_n = D - \vec{N}.P_i$$

$$t_{n} = \frac{D - \vec{N}.P_{i}}{\vec{N}.\vec{V}}$$

- This means that \vec{N} . $\vec{V} \neq 0$ If \vec{N} . $\vec{V}=0$ the ray is parallel to the line and will never hit it.
- When there is a hit, we find the coordinates of $\vec{P}_n = \vec{V} * t_n + P_i$
- If t_n is less than 0 or greater than 1, than there is no collision.



Collision Exercise:

Given the following line segment L[P0(6; 0), P1(10; 7)], representing a wall in your game, we need to check if the following moving point objects cases may collide with L in the current frame? Each point object is moving from B_s to B_e .

To answer these questions, you need to apply the equations found in the "Lecture 16 - Normal Line Equation - Animated Point To Line.pdf" file, between slides 18 and 27.

Please follow these steps:

- We'll skip the first 3 non-collision tests: (1/5), (2/5) and (3/5)
- Compute ti
- If (0 <= ti <= 1), compute Bi
- Test for non-collision (4/5) and (5/5). Or you can combine both test into one.

Case 1:

$$B_s = (5; 2)$$
 , $B_e = (7; 3)$

Case 2:

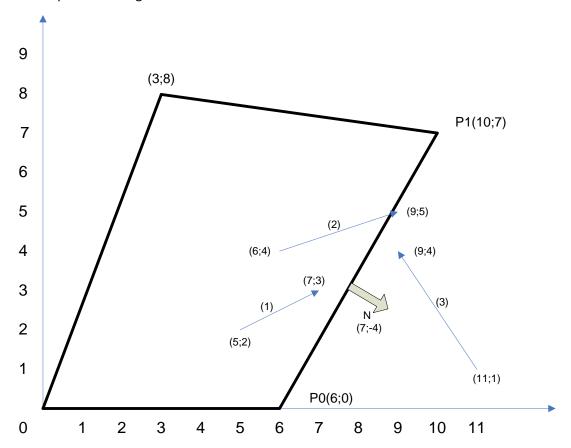
$$B_s = (6; 4)$$
 , $B_e = (9; 5)$

Case 3:

$$B_s = (11; 1)$$
 , $B_e = (9; 4)$



• Examples: Checking for collision with line POP1



• We need to find normal line equation of POP1

$$\circ$$
 $\overrightarrow{P_0P_1} = P_1 - P_0 = (10 - 6; 7 - 0) = (4; 7)$

$$\bigcirc \overrightarrow{N} = (\overrightarrow{P_0 P_1}.y; -\overrightarrow{P_0 P_1}.x) = (7; -4)$$

o Finding the constant D of the equation:

$$\vec{N}$$
.P₁ = (7; -4).(10; 7) = 70 - 28 = 42 = D

(Any point of the line works. We could have used P_0):

$$\vec{N}$$
.P₀ = (7; -4).(6; 0) = 42 - 0 = 42 = D

- Normal line equation:
 - P(x;y) is any point on POP1
 - $\vec{N}.P = D$
 - (7; -4).(x; y) = 42



• Case (1):

$$OB_{s} = (5; 2)$$

o
$$B_e = (7;3)$$

$$\vec{V} = B_e - B_s = (7; 3) - (5; 2) = (2; 1)$$

• We should find the collision time t_i using the equation $t_i = \frac{D - \vec{N}.B_S}{\vec{N}.\vec{V}}$

$$\circ \quad t_i = \frac{42 - (7 \ ; -4).(5 \ ; 2)}{(7 \ ; -4).(2 \ ; 1)} = \frac{42 - 35 + 8}{14 - 4} = \frac{15}{10} = 1.5$$

- o t_i is greater than $1 \rightarrow No$ collision
- Case (2):

o
$$B_s = (6; 4)$$

o
$$B_e = (9; 5)$$

$$\vec{V} = B_e - B_s = (9; 5) - (6; 4) = (3; 1)$$

• We should find the collision time t_i using the equation $t_i = \frac{D - \vec{N}.B_S}{\vec{N}.\vec{V}}$

$$\circ \quad t_i = \frac{42 - (7; -4).(6; 4)}{(7; -4).(3; 1)} = \frac{42 - 42 + 16}{21 - 4} = \frac{16}{17} = 0.94$$

- $0 \le t_i \le 1 \rightarrow$ then the ray collides with the line L at time $t_i = 0.94$
- \circ To get the exact point of intersection, we should replace t_i in the ray equation.

$$\vec{B}_i = \vec{V} * t_i + B_S = (3; 1)*0.94 + (6; 4) = (2.82; 0.94) + (6; 4) = (8.82; 4.94)$$

To verify that this point belongs to the line L, its coordinates should satisfy the normal line equation of L:

$$\vec{N}$$
.P = D

$$(7; -4).(8.82; 4.94) = 42$$

 $61.74 - 19.76 \cong 42$ (The lost precision is due to the fact that we're using 2 decimal digits)

Check if outside boundaries (Non-Collision tests 4 and 5 combined):

$$(B_i - P_0) \cdot (B_i - P_1) =$$

$$[(8.82; 4.94) - (6; 4)] \cdot [(8.82; 4.94) - (9; 5)] = [2.82; 0.94] \cdot [-0.18; -0.06] < 0$$

 \Rightarrow B_i is inside

Case (3)

$$\circ$$
 $B_{S} = (11; 1)$

o
$$B_e = (9; 4)$$

$$\circ \quad \vec{V} = B_e - B_s = (9; 4) - (11; 1) = (-2; 3)$$

• We should find the collision time t_i using the equation $t_i = \frac{D - \vec{N}.B_S}{\vec{N}.\vec{V}}$

$$\circ \quad t_i = \frac{42 - (7\;;-4).(11\;;1)}{(7\;;-4).(-2\;;3)} = \frac{42 - 77 + 4}{-14 - 12} = \frac{-31}{-26} = 1.19$$

o t_i is greater than $1 \rightarrow No$ collision

