

Intensity Transforms

Introduction

Recap

- Spatial Operations
 - Geometric spatial transformations
- Image Interpolation
- Image Registration
- Image Domain Transforms

Lecture Objectives

- Spatial Domain Transformations – preview
- The Transformation Operator
- Intensity Transformations and examples
 - Contrast stretching
 - Image thresholding
- Basic Intensity Transformation Functions
 - Basic transforms
 - Piecewise-linear transformations

Key Stages in DIP

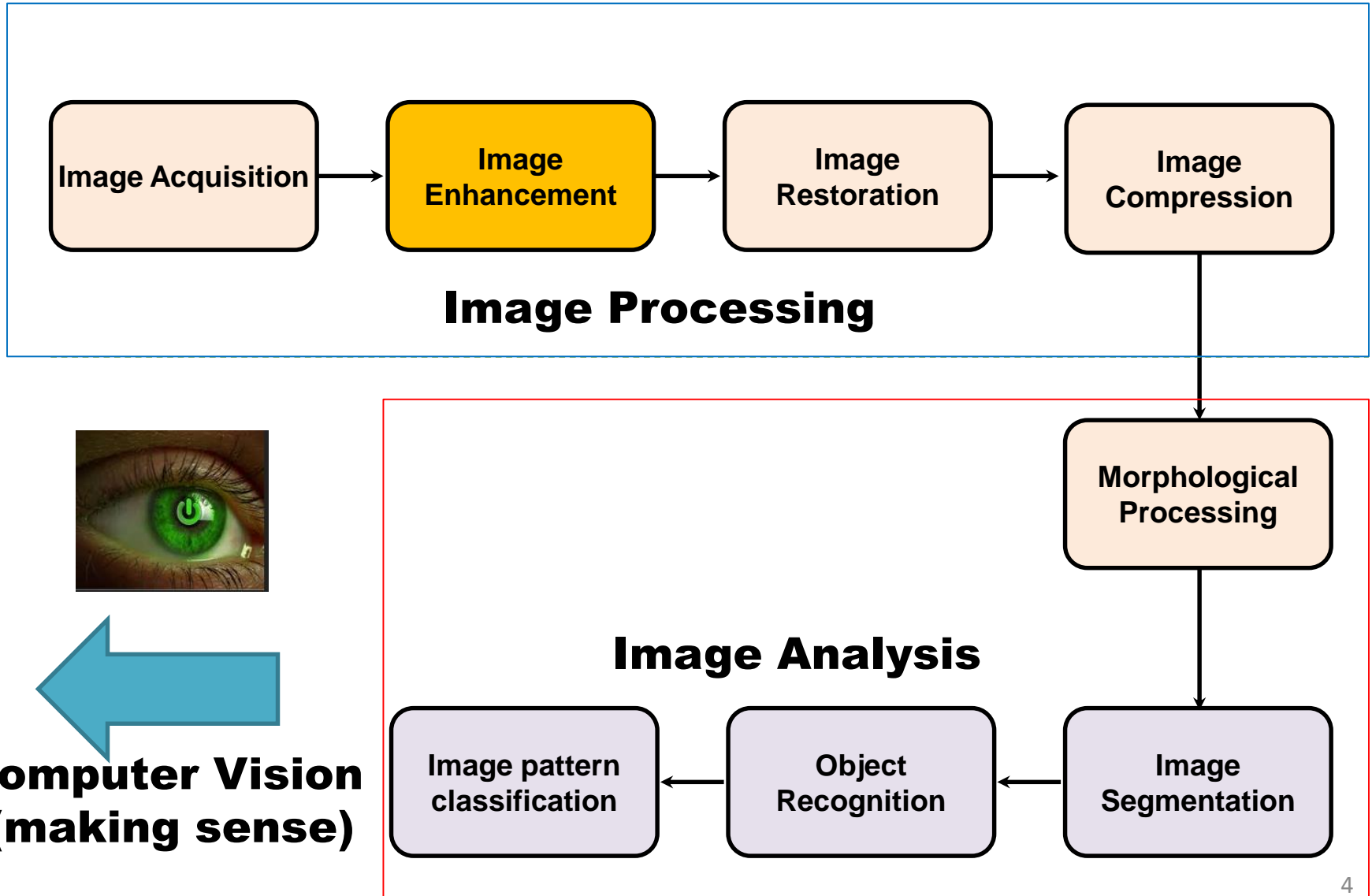


Image Enhancement

- Image Enhancement is:
 - The process of manipulating an image so that the result is **more suitable than the original** for a **specific** application. It's a subjective measure.
 - Visual interpretation
 - Decision made by the user of the system (**satisfaction**)
 - **Ex:** visibility of detailed features in the medical image
 - Machine perception
 - Quantified by the **system efficiency**
 - **Ex:** character recognition rate for number plate detection

Spatial Domain Transformations

Preview

Spatial Domain Transformations - Preview

- The term *spatial domain* refers to the **image plane** itself, and image processing methods in this category are based on *direct manipulation of pixels* in an image.
- In contrast, image processing in a *transform domain* involves:
 1. first transforming an image into the transform domain
 2. doing the processing in the transform domain, and
 3. obtaining the inverse transform to bring the results back into the spatial domain

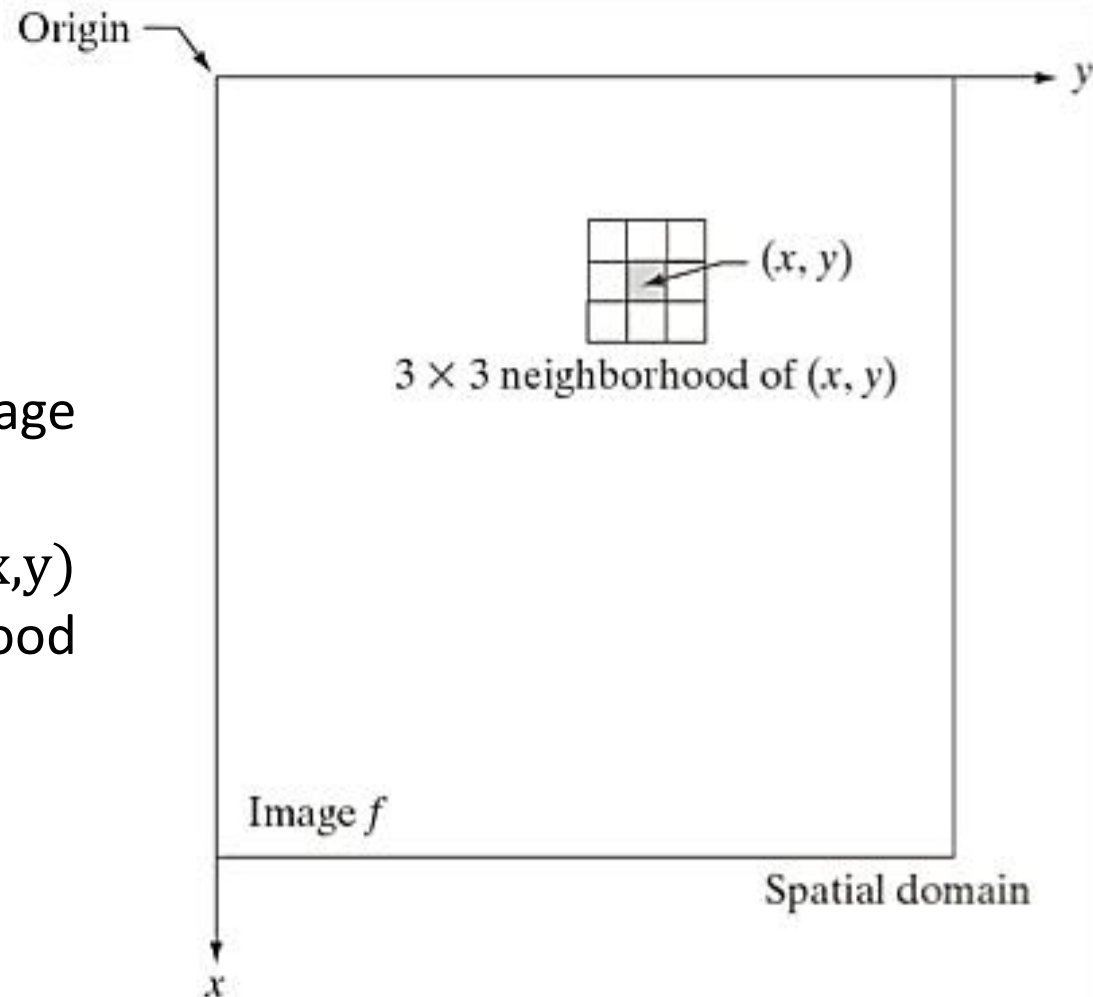
Spatial Domain Transformations - Preview

- Two principal categories of spatial domain processing are:
 1. Intensity transformations
 2. Spatial filtering
- *Intensity transformations* operate on **single pixels** of an image for tasks such as **contrast manipulation** and **image thresholding**.
- *Spatial filtering* performs operations on the **neighborhood of every pixel** in an image. Examples of spatial filtering include **image smoothing** and **image sharpening**.

Spatial Domain Transformations

Spatial filtering

- $g(x,y) = T[f(x,y)]$
 - $f(x,y)$ is the input image
 - $g(x,y)$ is the output image (transformed image)
 - T is an operator on $f(x,y)$ defined over a neighborhood of point (x,y)



The center of the neighborhood is moved from pixel to pixel, and then the operator T is applied to the pixels in the neighborhood to yield an output value at that location.

The Transformation Operator: **T**

The Transformation Operator: **T**

- **Intensity transformation**: neighborhood size is **1×1**
 - **T**: **intensity** (grey-level) **transformation function**
- **Spatial filtering**: neighborhood is usually an **odd sized window** of the size **a×b**, where $a=2k+1$ or $b=2k+1$ for $k \in \mathbb{Z}^+$
 - **T**: **spatial filter/spatial mask/kernel/template/window**

Intensity Transformation

Examples

Intensity Transformation - examples

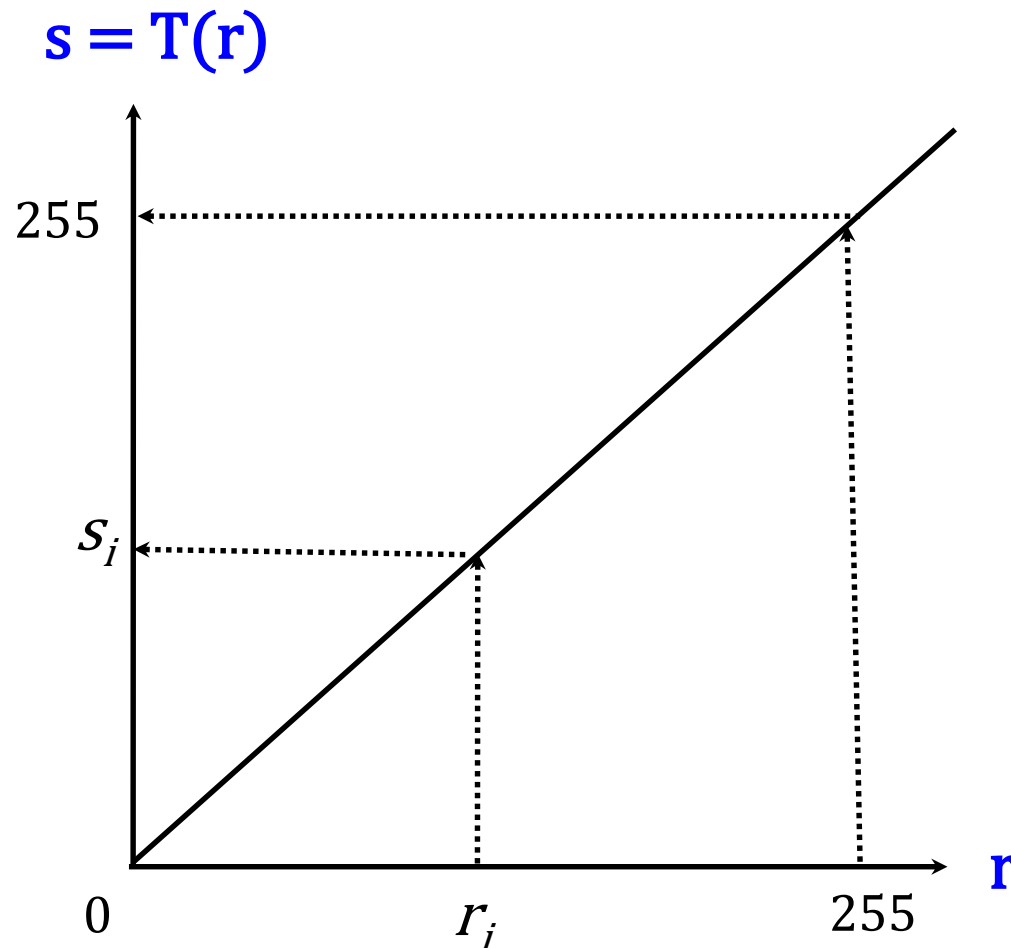
- The intensity transformation function operate on *neighborhood of size 1×1* for a pixel:

$$s = T(r)$$

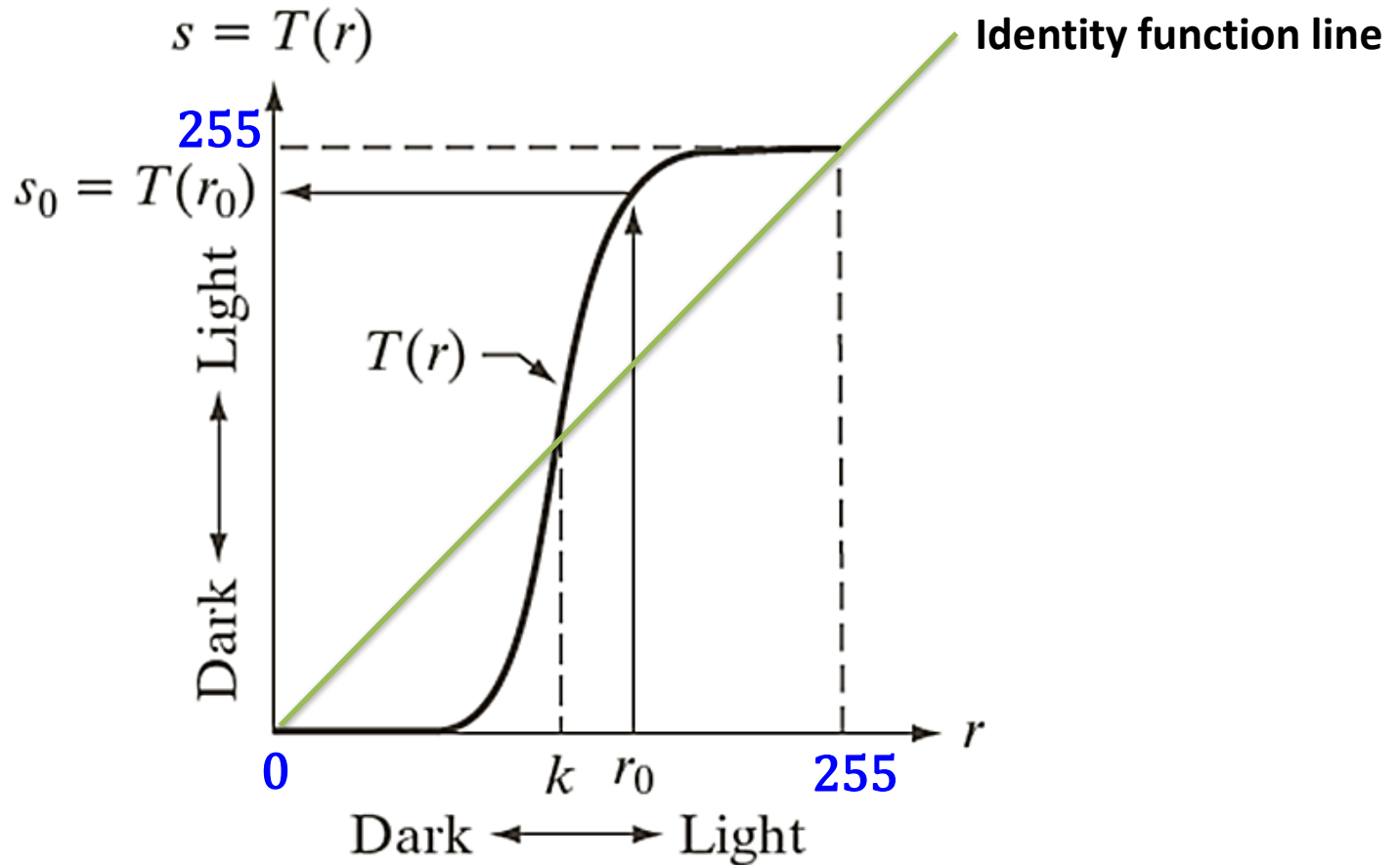
- Example:
 - Contrast stretching/Image stretching/Image normalization
 - Image thresholding
- The intensity transformation function whose results depend only on the **intensity at a point** sometimes are called *point processing techniques*, as opposed to the *neighborhood processing techniques*.

Identity Function

- The identity function is the trivial case in which the input and output intensities are *identical* (same).



Contrast stretching



- Values of r lower than k *reduce* (darken) the values of s , *toward black*.
- Values of r higher than k *increase* (lighten) the values of s , *toward white*.

Contrast stretching - formula

$$S = (r - f_{min}) \left[\frac{max - min}{f_{max} - f_{min}} \right] + min$$

S: color level of the output pixel

r : color level of the input pixel

f_{max} : maximum color level values in the input image

f_{min} : minimum color level values in the input image

max & min : desired maximum and minimum color levels that determines color range of the output image, respectively

Contrast stretching

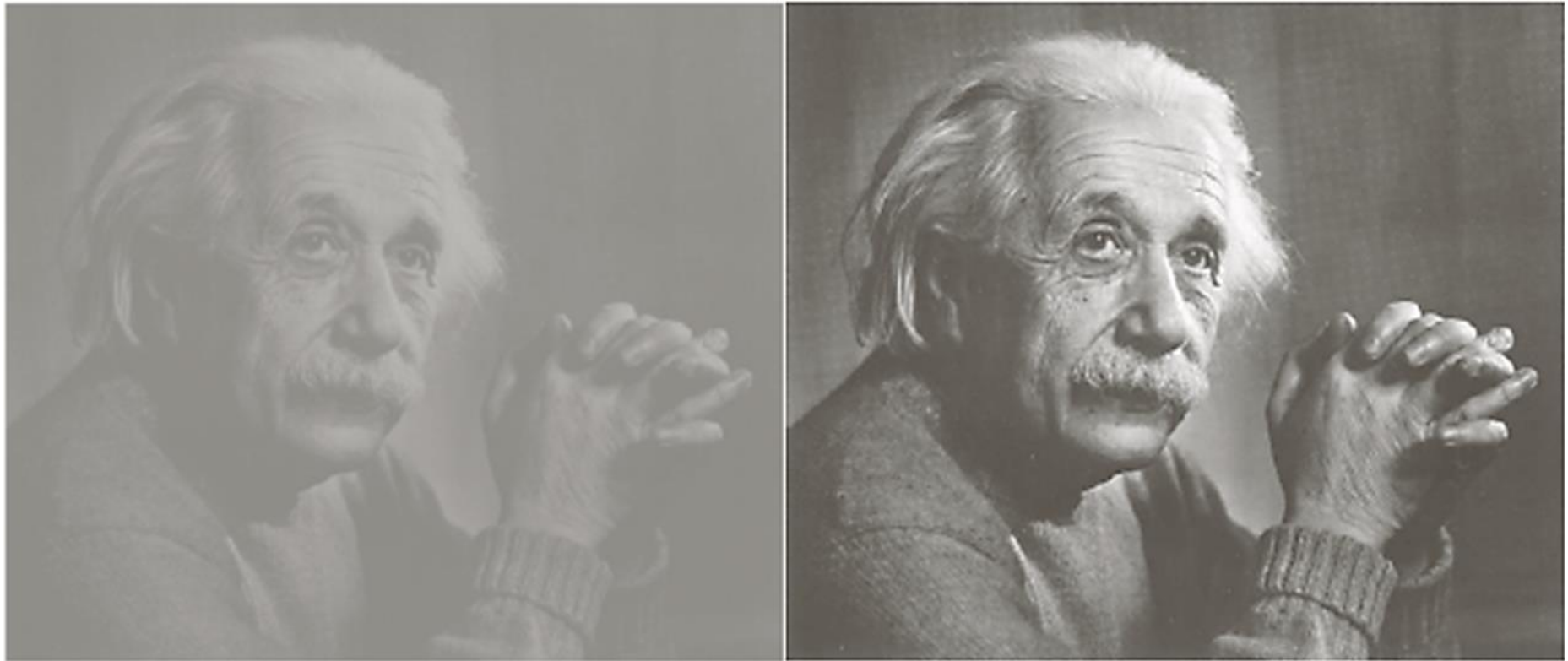


Image Thresholding

- **Limiting case** of the *contrast stretching*.
- Only two valid values
 - **0** for lower intensities
 - **1** for higher intensities

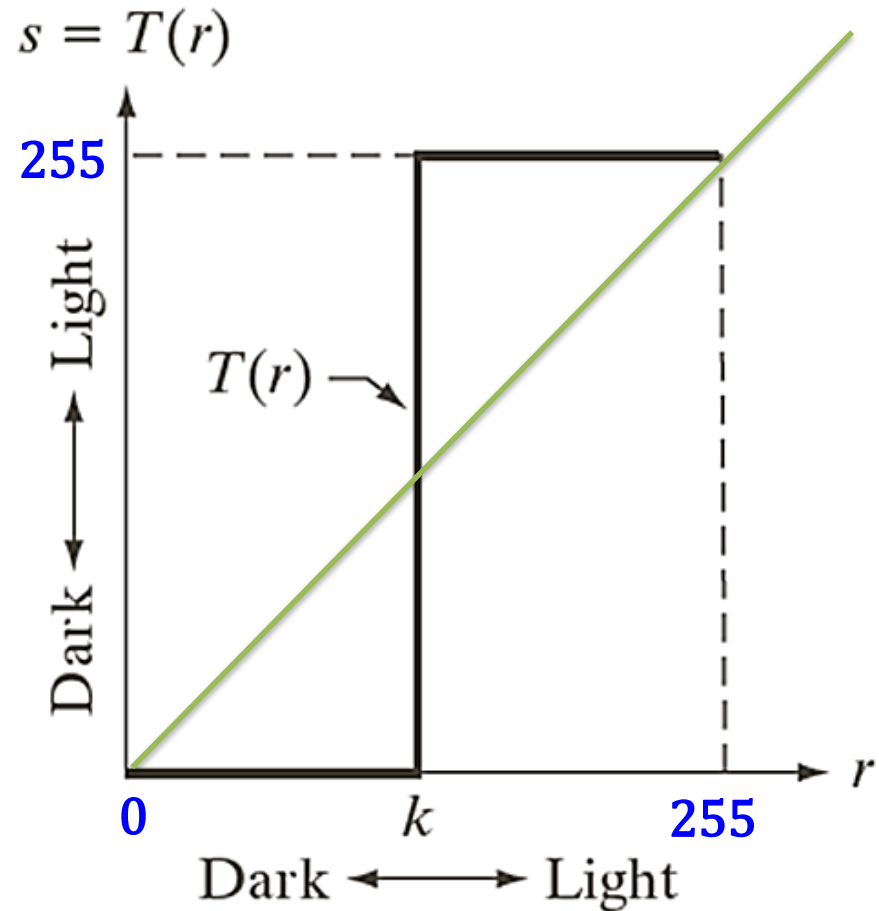


Image Thresholding



Basic Intensity Transformation Functions

Intensity Transformation Functions

- Basic transformations
 - Image negative
 - Log transformations
 - Power-Law (Gamma) transformations
- Piecewise-linear Transformations
 - Contrast stretching
 - Intensity-level slicing
 - Bit-plane slicing

Basic Transformation Functions

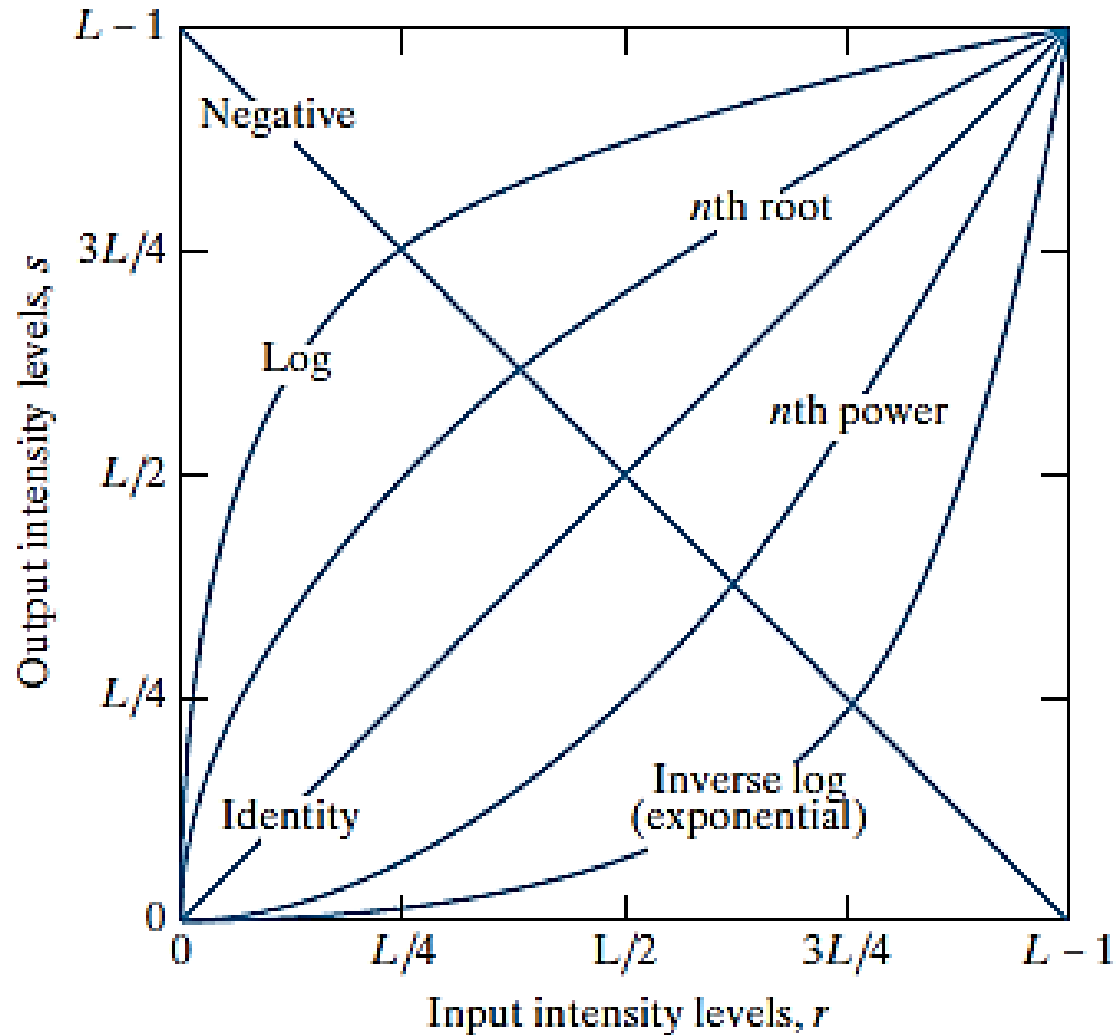


Image Negative

- Uses the transform:

$$s = (L - 1) - r$$

where L is the intensity in the range $[0, L-1]$.

- Similar to photographic negative function.
- Used for ***enhancing white or gray details*** embedded in dark regions of an image, especially when the black areas are dominant in size.

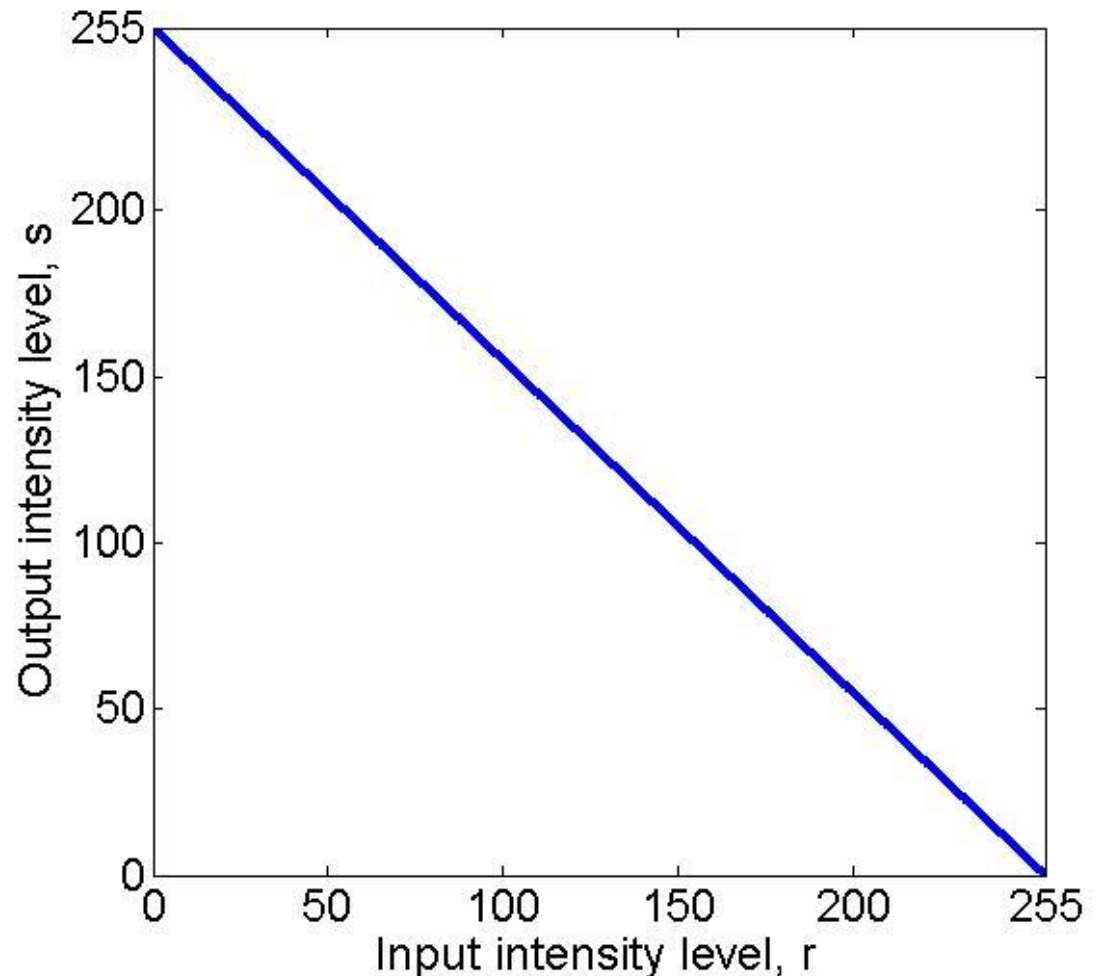
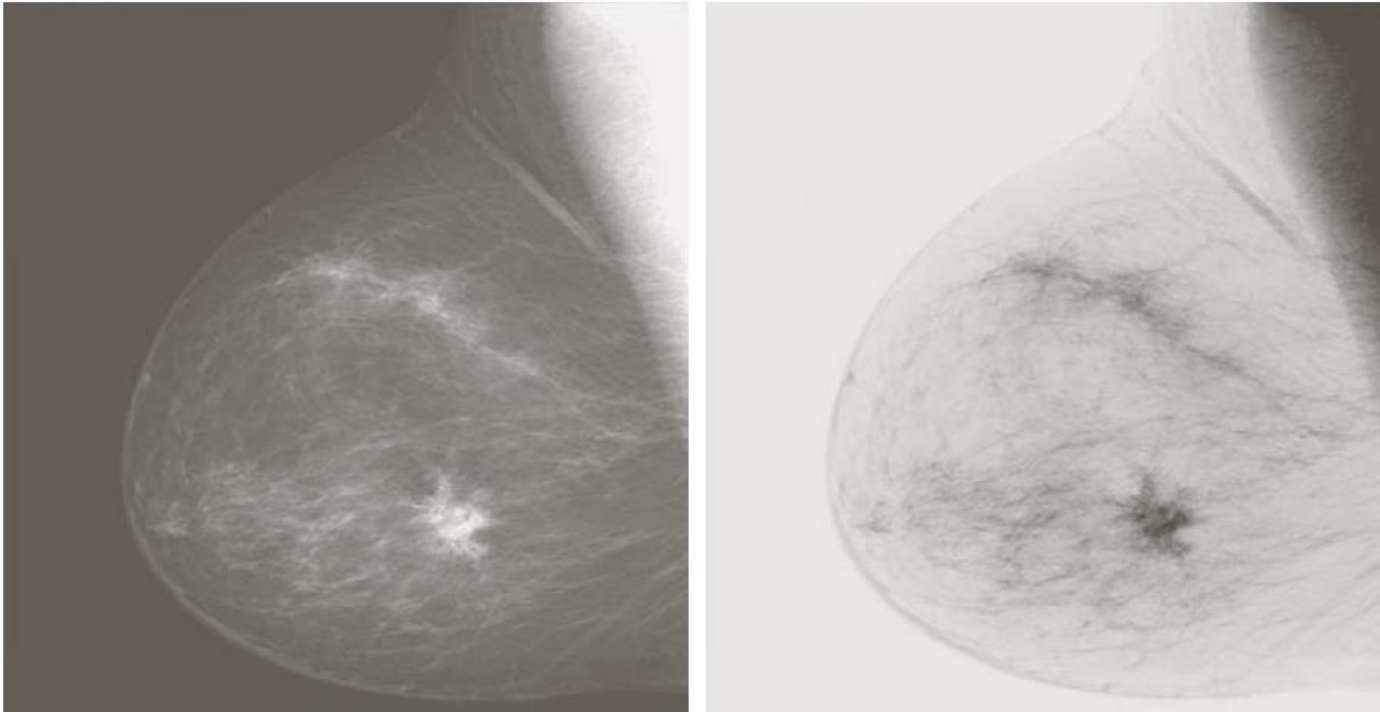


Image Negative



Digital mammogram showing a small lesion in breast which may lead to breast cancer

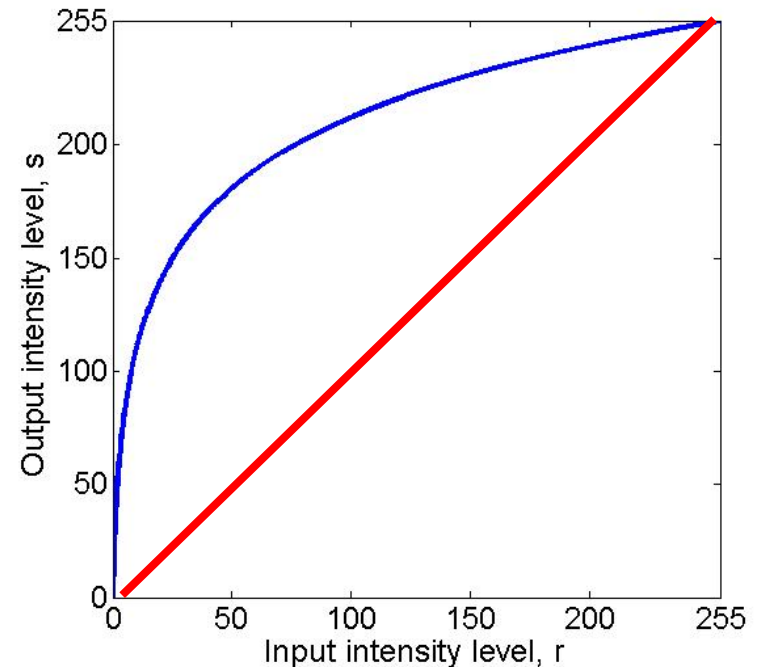
Log Transformation

- Uses the transform:

$$s = c \times \log_{10}(1+r)$$

where c is a constant and it is assumed that $r \geq 0$.

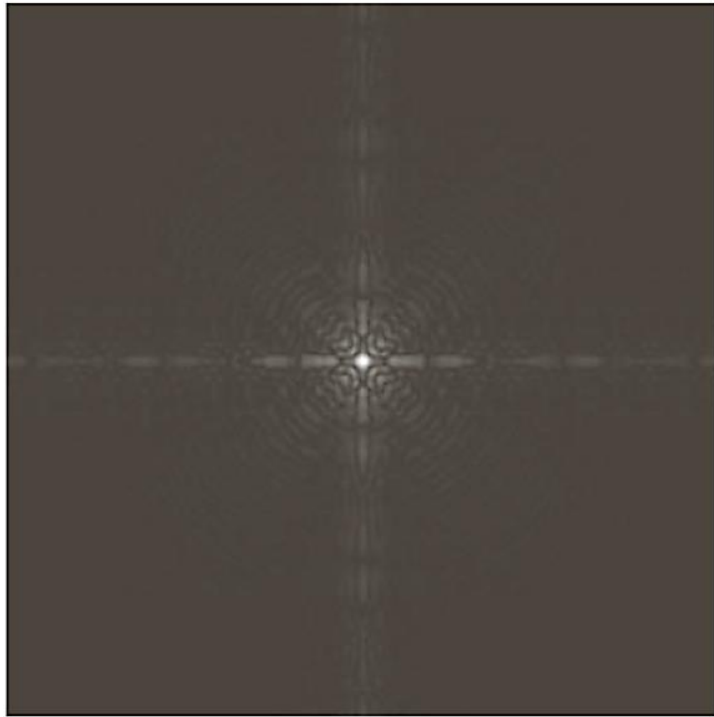
- Maps narrow input intensity ranges to wider output ranges for lower intensity values.
- Maps wider input intensity ranges to narrow output ranges for higher intensity values.



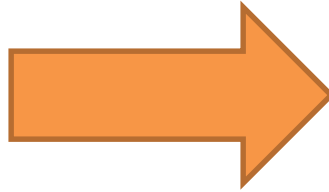
$$c=105.8865$$

- We use a transformation of this type to **expand** the values of **dark pixels** in an image, while **compressing** the **higher-level** values.

Log Transformation - example

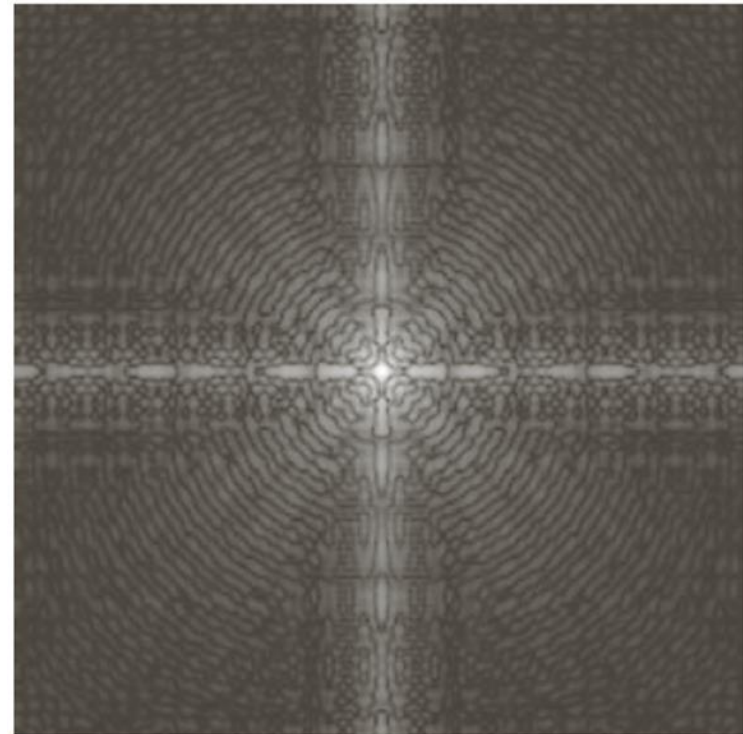


Log Transform



$$s = c \times \log(1 + r)$$

$$c = 1$$

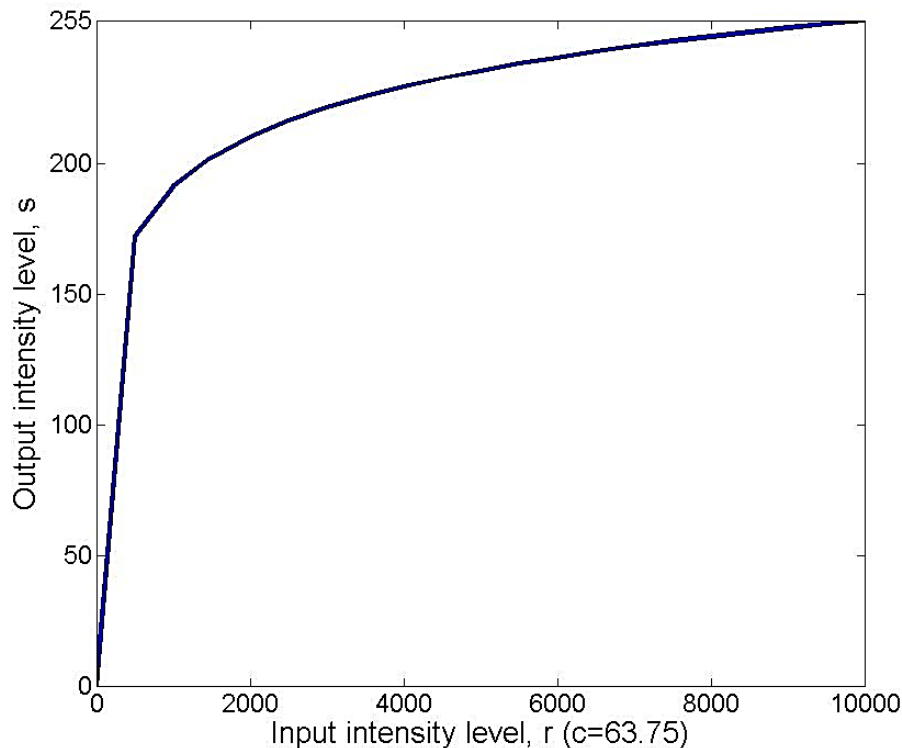


Input Fourier Spectrum, intensity range: $[0, 1.5 \times 10^6]$, scaled linearly to $[0, 255]$ for display

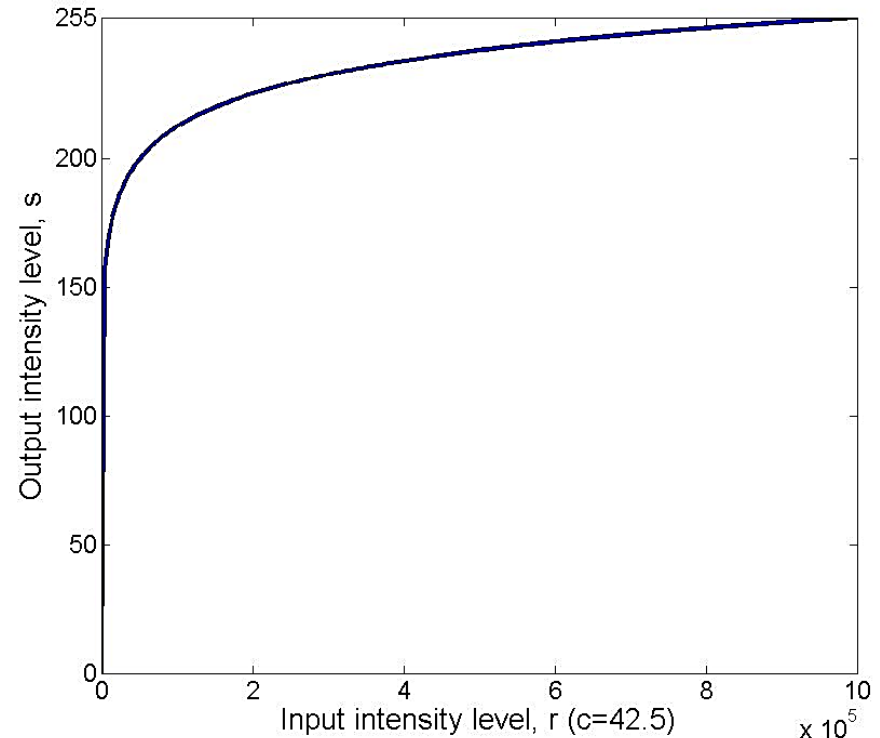
Output Fourier Spectrum

Log Transformation - **example**

$r \in [0, 9999]$, $c=63.75$



$r \in [0, 10^6 - 1]$, $c=42.5$



During image processing in ***transform domain***, it is ***not unusual*** to encounter spectrum values that range from 0 to 10^6 or higher.

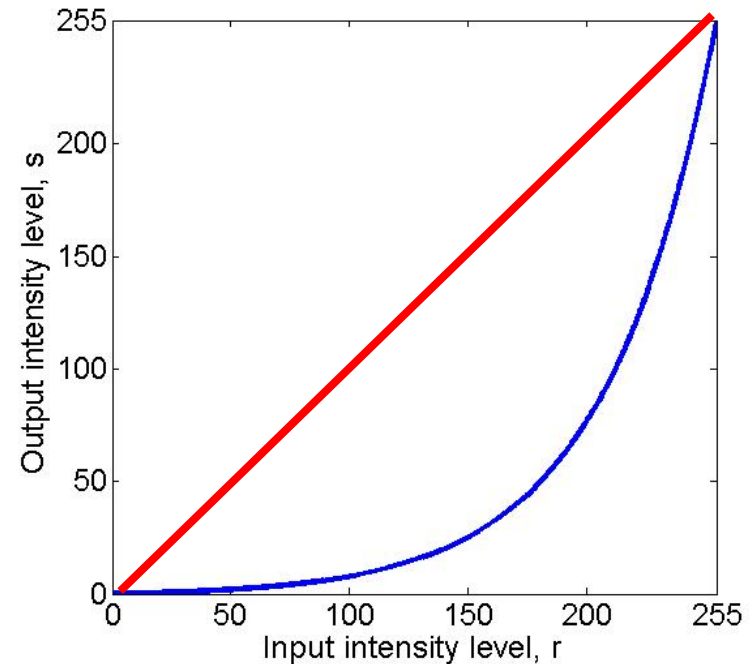
Inverse Log Transformation

- Uses the transform:

$$s = 10^{r/c} - 1$$

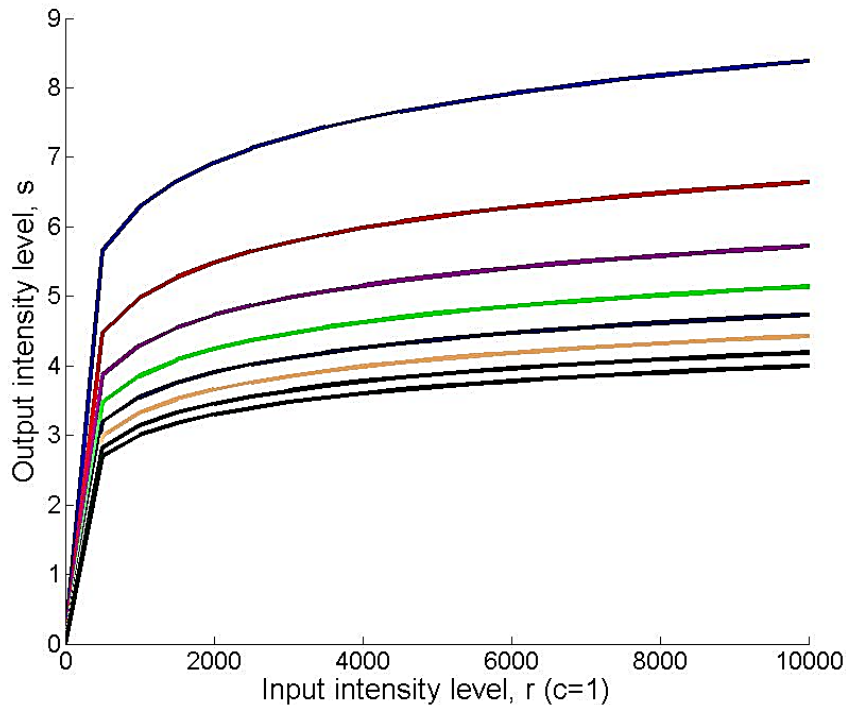
where c is a constant and it is assumed that $r \geq 0$.

- Maps wider input intensity ranges to narrow output ranges for lower intensity values.
- Maps narrow input intensity ranges to wider output ranges for higher intensity values.
- We use a transformation of this type to **expand** the **dynamic range** of images with very small variations in intensity values.



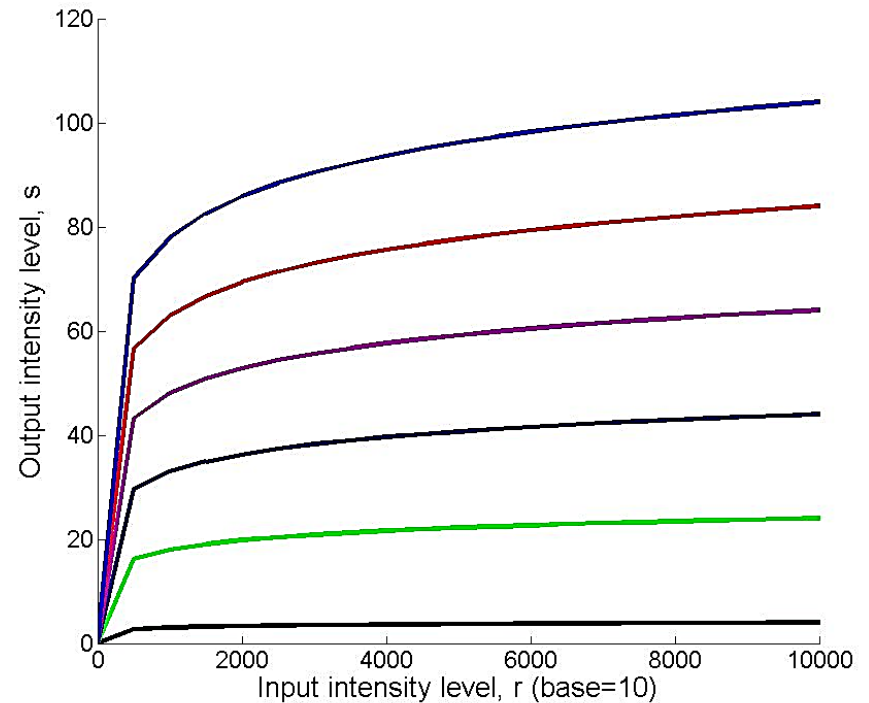
$$c = 105.8865$$

Log Transformations



Varying base

$$s = c \times \log_{10}(1+r)$$



Varying c

$$s = 10^{r/c} - 1$$

Power-Law (Gamma- γ) Transformation

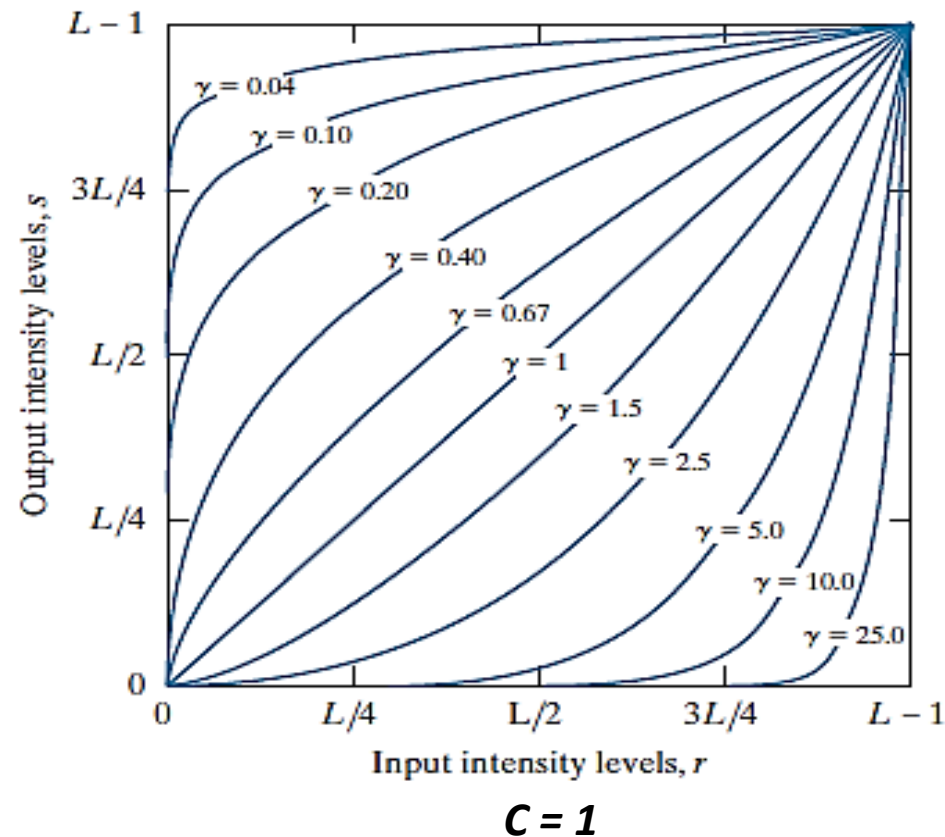
- Uses the transform:

$$s = c \times r^\gamma$$

OR

$s = c \times (r + \epsilon)^\gamma$ to account for output when **input is zero**.

where c and γ are positive constants.



- As with log transformations, power-law curves with fractional values of γ map a narrow range of dark input values into a wider range of output values, with the opposite being true for higher values of γ .

Power-Law (Gamma) Correction

- The response of many devices used for image capture, printing, and display obey a power law:

$$\text{voltage} = c \times \text{intensity}^\gamma$$

Example: ($\gamma \in [1.8, 2.5]$) for CRT devices

- The process used to correct these power-law response phenomena is called *gamma correction* or *gamma encoding*.

Gamma Correction

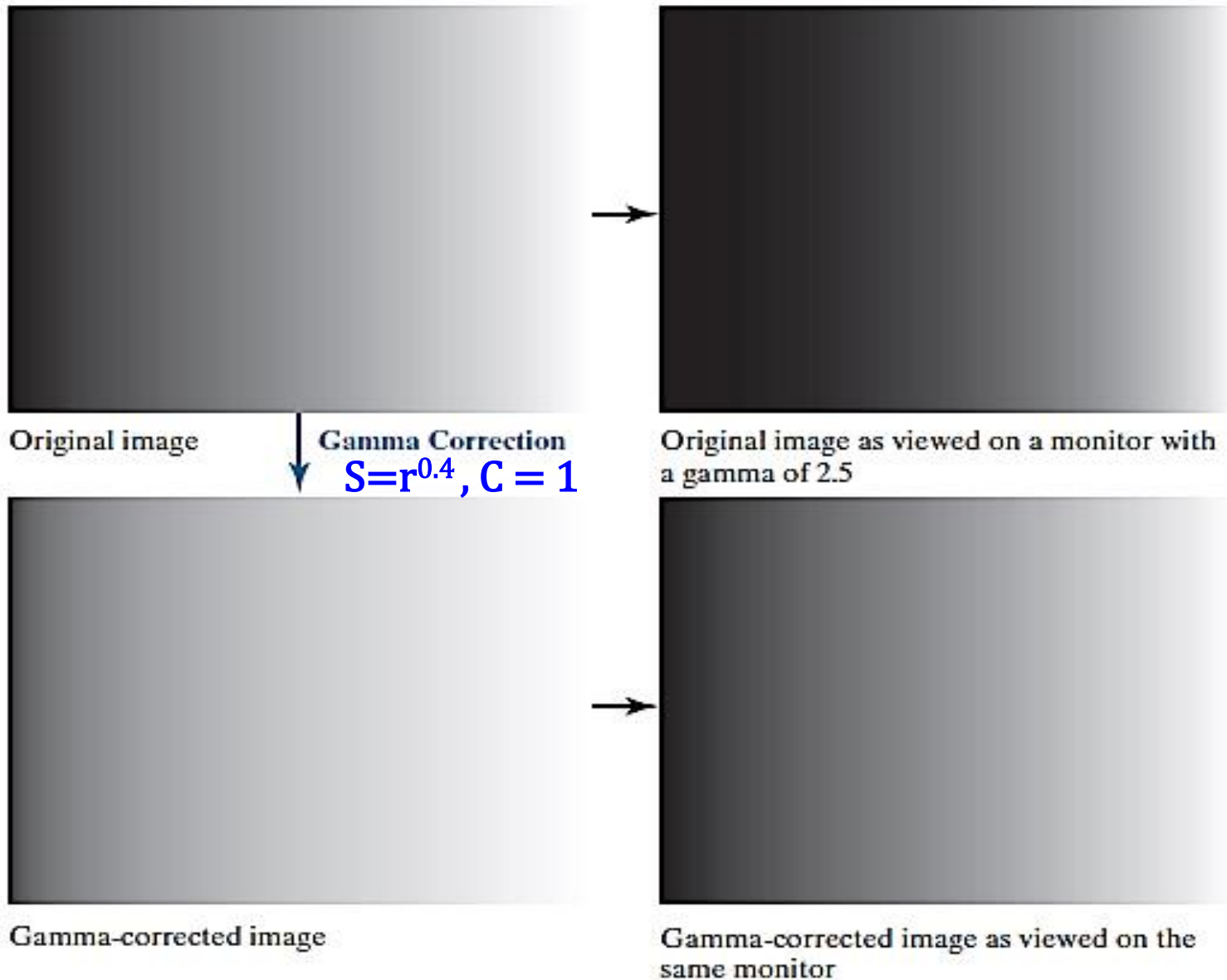


Original image



Original image as viewed on a monitor with a gamma (γ) = **2.5**

Gamma Correction



Power-Law (Gamma) Transformation

Contrast manipulation



MRI of an upper thoracic human spine with a fracture dislocation.

Power-Law (Gamma) Transformation

Contrast manipulation

Gamma Transformations



MRI of an upper thoracic human spine with a fracture dislocation and spinal cord impingement

$$s=r^{0.6}$$

$$s=r^{0.4}$$

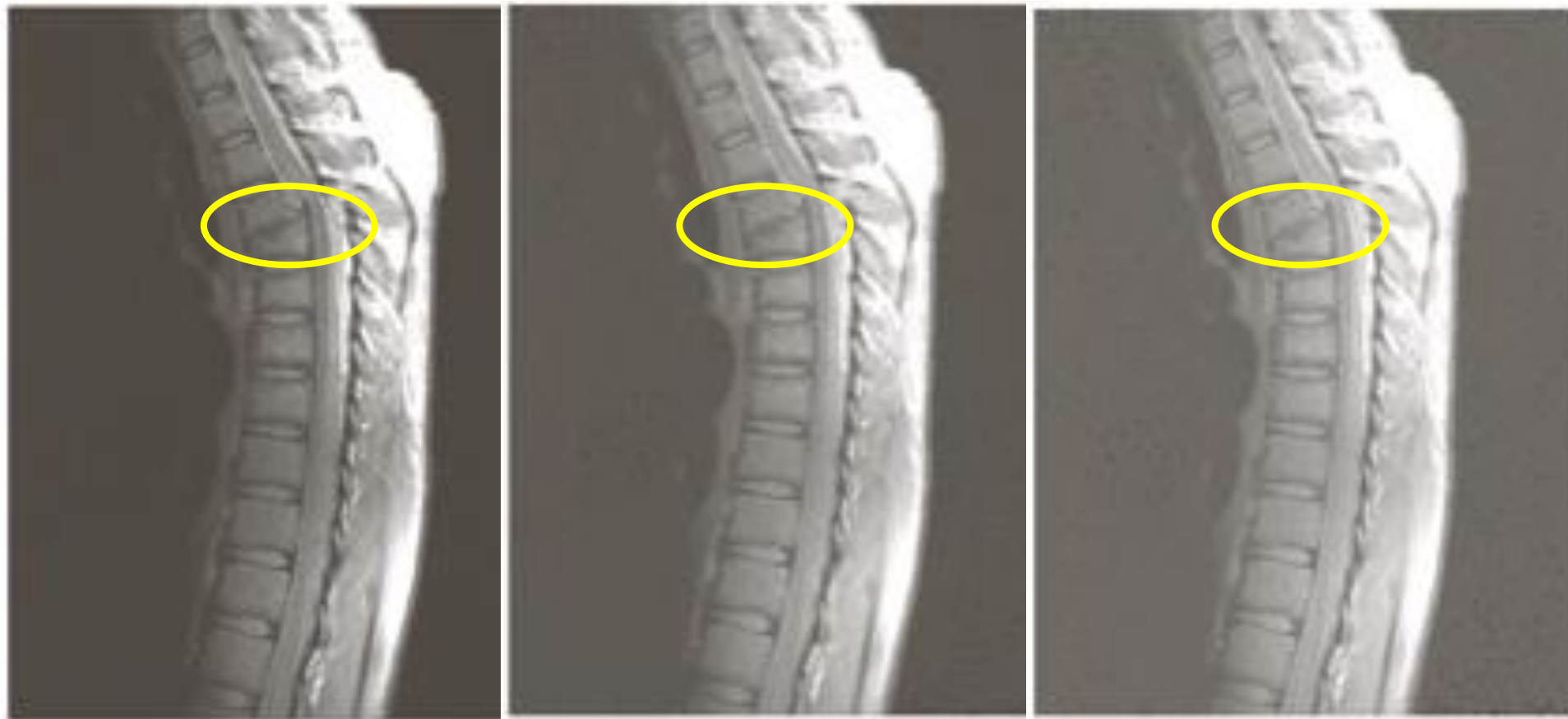
$$s=r^{0.3}$$

$C = 1$ in all the cases



Power-Law (Gamma) Transformation

Contrast manipulation



$\gamma=0.6$

$\gamma=0.4$

$\gamma=0.3$

Power-Law (Gamma) Transformation

Contrast manipulation



An aerial image with washed-out appearance

Power-Law (Gamma) Transformation

Contrast manipulation

Gamma Transformations



$$s=r^3$$



$$s=r^4$$



$$s=r^5$$



$C = 1$ in all the cases

Power-Law (Gamma) Transformation

Contrast manipulation



$\gamma=3$



$\gamma=4$



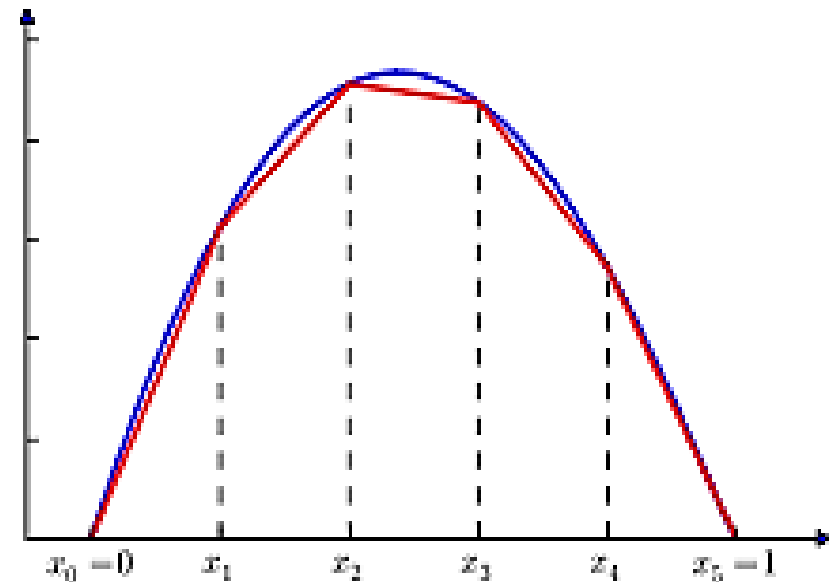
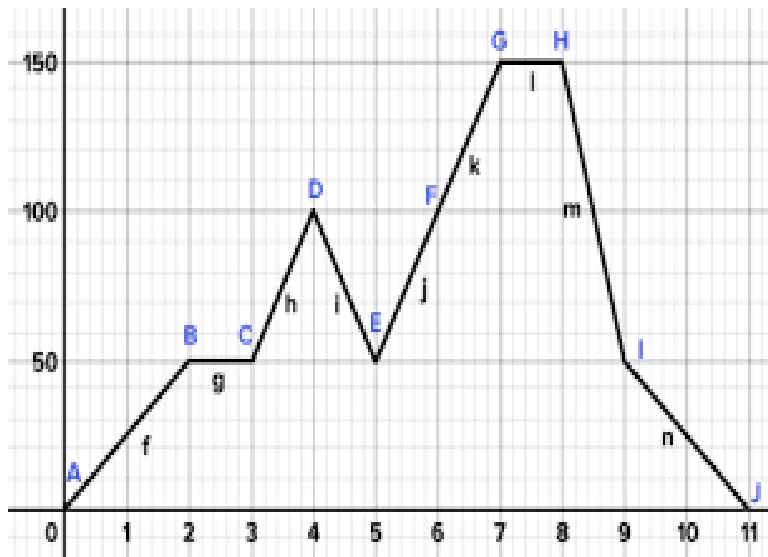
$\gamma=5$

Intensity Transformation Functions

- Basic transformations
 - Image negative
 - Log transformations
 - Power-Law (Gamma) transformations
- Piecewise-linear Transformations
 - Contrast stretching
 - Intensity-level slicing
 - Bit-plane slicing

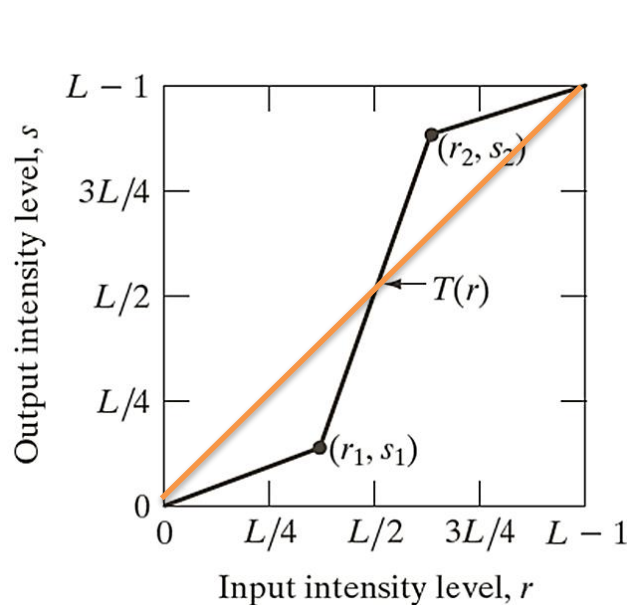
Piecewise-linear Transformations

- A *piecewise linear function* is a function composed of some number of **linear segments** defined over an equal number of intervals, usually of equal size.

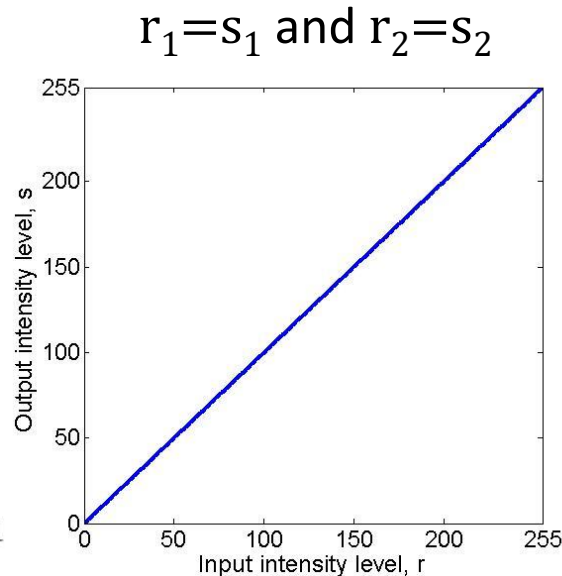


Contrast Stretching

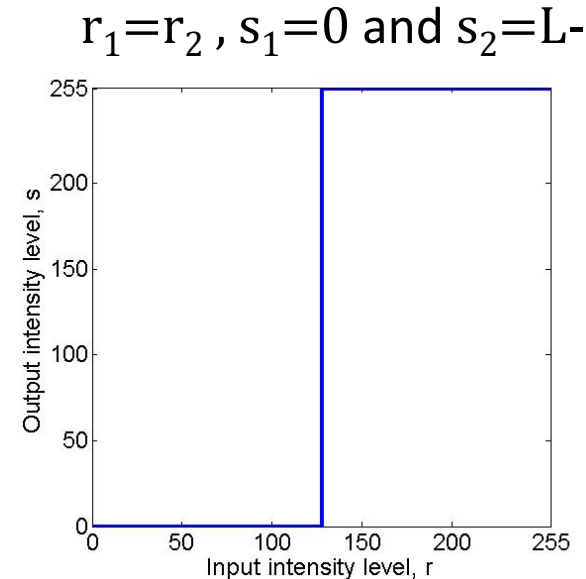
- *Contrast stretching* expands the range of intensity levels in an image so that it **spans the ideal full intensity range** of the recording medium or display device.
- The locations of points (r_1, s_1) and (r_2, s_2) control the shape of the transformation function.



Typical function for
contrast stretching
 $r_1 \leq r_2$ and $s_1 \leq s_2$



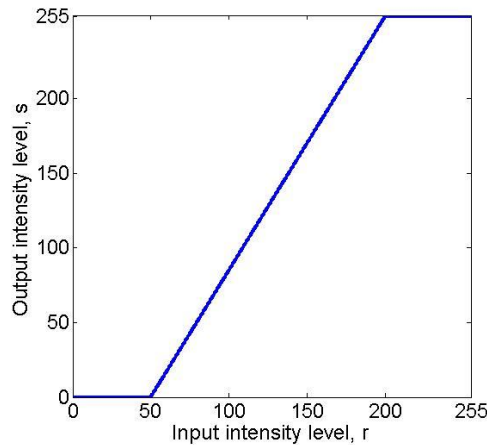
Identity function



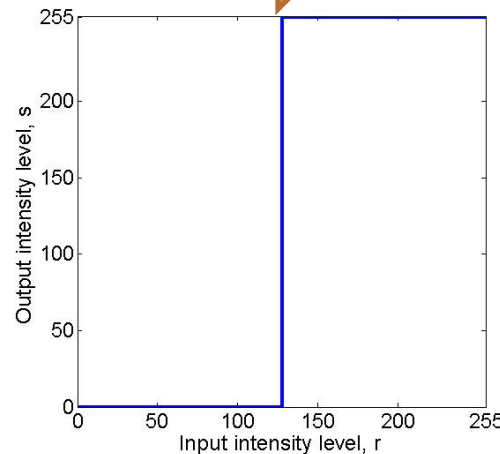
Thresholding function

$$S = (r - f_{min}) \left[\frac{max-min}{f_{max}-f_{min}} \right] + min$$

Contrast Stretching



$(r_1, s_1) = (r_{\min}, 0)$ and $(r_2, s_2) = (r_{\max}, L-1)$, where r_{\min} and r_{\max} denote the min & max intensity levels in the image



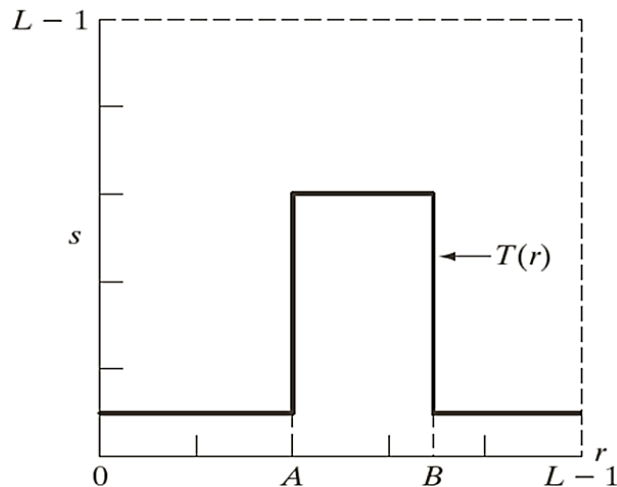
$(r_1, s_1) = (m, 0)$ and $(r_2, s_2) = (m, L-1)$, where m is the mean intensity level in the image.



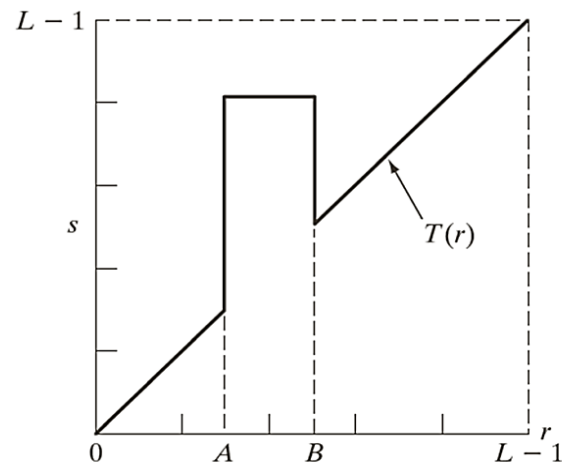
Scanning electron microscope image of pollen, magnified ≈ 700 times

Intensity-Level Slicing

- These functions highlight a specific range of intensities in an image.
- What about the **remaining intensities**?
 - Set to default (lower) level, **usually zero** (fig. 1)
 - **Preserve** original values (fig. 2)



(fig. 1)

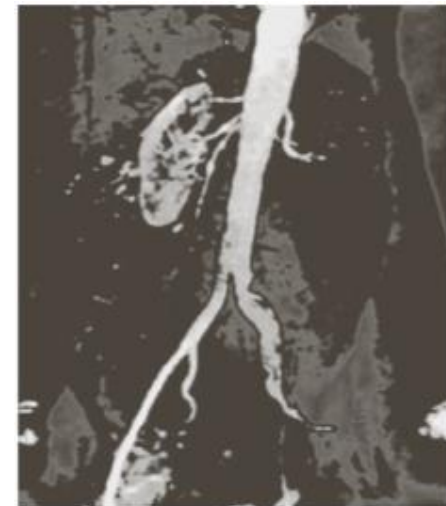
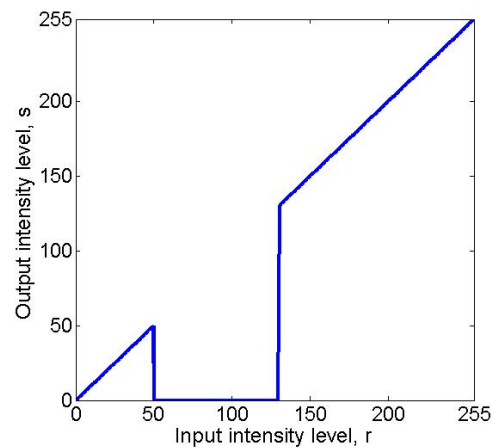
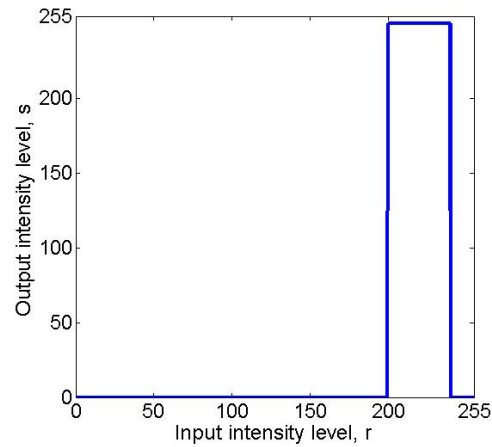


(fig. 2)

Intensity-Level Slicing

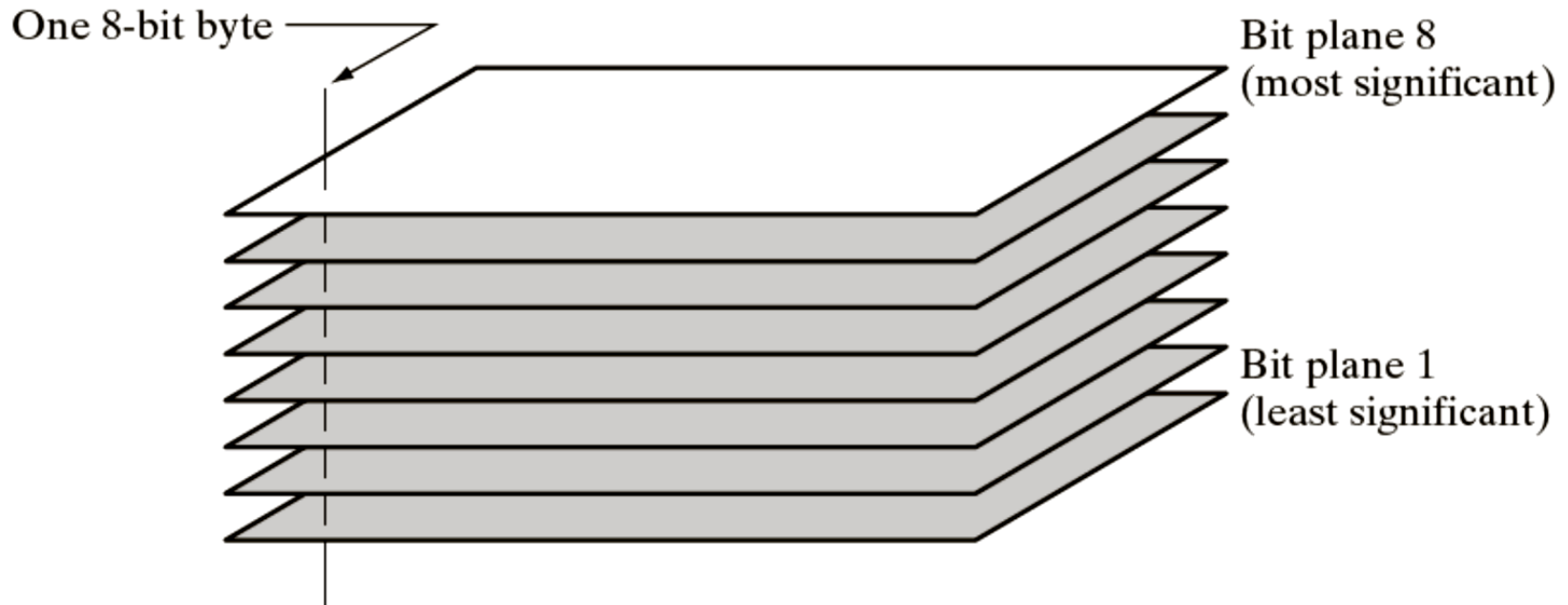


Aortic angiogram
near the kidney area



Bit-Plane Slicing

- Pixels intensities are stored as binary numbers.
- Each bit position represents a level-of-detail.



Bit-Plane Slicing

Different Bit planes



Given image



bit-8



bit-7



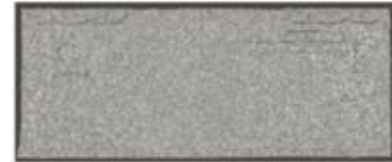
bit-6



bit-5



bit-4



bit-3



bit-2

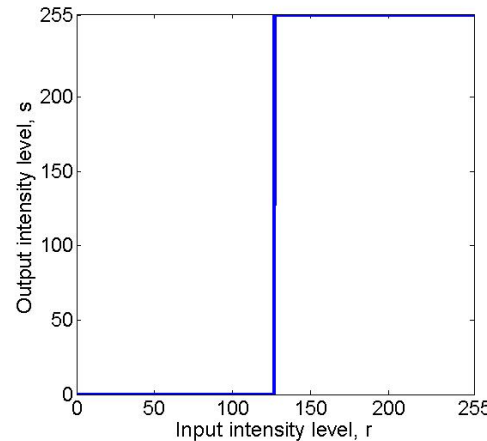


bit-1

The intensity of the boarder is 194_{10} , which is 11000010_2

How to obtain each bit plane from the original image?

Bit-Plane Slicing - example



maps to **0** intensity values between **0** and **127**, and maps to **1** values between **128** and **255**.

$$128_{10} = 10000000_2$$



bit-8

How about the rest?

$$64_{10} = 01000000_2$$

$$32_{10} = 00100000_2$$

$$16_{10} = 00010000_2$$

$$8_{10} = 00001000_2$$

$$4_{10} = 00000100_2$$

$$2_{10} = 00000010_2$$

$$1_{10} = 00000001_2$$

Bit-Plane Slicing – applications

- Analyze the **relative importance** of each bit in the image.
- Determine the **adequacy of the number of bits** used to quantize the image.
- Useful in modelling **image compression**, in which fewer number of planes are used in reconstructing an image.

Bit-plane Slicing – image decomposition



All bits



bit 8,7



bit 8,7,6,5



bit 8,7,6

Next Lecture

- What is a Histogram?
- Histogram Normalization
- What is Random variable
- Histogram Equalization