

Exercise – Animated point vs static line segment

- We have a point **Bs(-2,2)** that is travelling in one frame time to another point **Be(3,-1)**.
- A bouncy wall is represented by a line segment and located at **L[(0,-3),(0,3)]**
- Find the final point position **Be'** after collision (if any?) and reflection of the point with the wall.

Solution – Following the notes printed and given in class

Step1 – Collision detection - Method 2

- Compute N.Bs, N.P0 and N.Be:
 - $N.Bs = (6,0).(-2,2) = -12$
 - $N.P0 = (6,0).(0,-3) = 0$
 - $N.Be = (6,0).(3,-1) = 18$

$$N.Bs < N.P0 \text{ and } N.Be > N.P0$$

a- Test passed – no rejection

b- Test Passed – no rejection

c- Compute **N.V**

a. If (**N.V == 0**) then no collision

$$N.V \text{ is } N(BsBe) = N.Be - N.Bs = 18 - (-12) = 30 \neq 0$$

$$N.V \text{ is } \neq 0 - \text{no rejection}$$

d- Compute **Ti**, the time of intersection where **Ti = (N.P0 - N.Bs) / (N.V)**

$$Ti = (0 - (-12)) / (30) = 2/5$$

e- If (**Ti < 0**) or (**Ti > 1**) then reject

$$Ti = (0 \leq 2/5 \leq 1)$$

$$Bi = Bs + Ti * V = (-2,2) + 2/5 * (5,-3) = (-2,2) + (2, -6/5) = (0, 4/5)$$

f- Test to check if **Bi** is within **P0** and **P1** area. We test if (**(Bi - P0).(Bi - P1) < 0**) then return collision at point **Bi**

$$(Bi - P0).(Bi - P1) = [(0,4/5) - (0,-3)].[(0,4/5) - (0,3)] = (0,19/5).(0,-11/5) = -209/25 < 0$$

If we followed **Method 3** steps, the first two steps would be to compute the **outward** normal of **BsBe** and do the **rejection test** as follow:

- a- \mathbf{M} = Outward normal of $\mathbf{V} = (\mathbf{V.y}, -\mathbf{V.x}) = (-3, -5)$
- b- $(\mathbf{BsP0.M}) * (\mathbf{BsP1.M}) = [(0 - (-2), (-3) - 2) \cdot (-3, -5)] * [(0 - (-2), 3 - 2) \cdot (-3, -5)]$
 $= [(2, -5) \cdot (-3, -5)] * [(2, 1) \cdot (-3, -5)]$
 $= (-6 + 25) * (-6 + (-5)) = 19 * (-11) = -209 < 0$

This means we can proceed and compute **Ti** and **Bi** as in **Method 2**

Step2 – Reflection

- a- Compute $\mathbf{Be'}$
 $\mathbf{Be'} = \mathbf{Bi} + \mathbf{I} - 2(\mathbf{I.n}) * \mathbf{n}$
 Where \mathbf{I} is the penetration vector and \mathbf{n} is \mathbf{N} normalized
 $\mathbf{I} = \mathbf{Be} - \mathbf{Bi} = (3, 1) - (0, 4/5) = (3, -9/5)$
 $\mathbf{n} = \mathbf{N} / \text{Length}(\mathbf{N}) = (6, 0) / 6 = (1, 0)$

 $\Rightarrow \mathbf{Be'} = (0, 4/5) + (3, -9/5) - 2 * [(3, -9/5) \cdot (1, 0)] * (1, 0)$
 $\Rightarrow \mathbf{Be'} = (0, 4/5) + (3, -9/5) - 2 * (3) * (1, 0)$
 $\Rightarrow \mathbf{Be'} = (-3, -1)$